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# Collaborative state estimation of lithium-ion battery based on multi-time scale low-pass filter forgetting factor recursive least squares - double extended Kalman filtering algorithm

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Abstract: For the lithium battery management system and real-time safety monitoring, two issues are of great significance, namely the ability to accurately update the model parameters in real time and to accurately estimate the state of charge and health. In this context, this thesis adopts the second-order RC equivalent circuit model and the forgetting factor recursive least squares - double extended Kalman filtering (FFRLS-DEKF) algorithm with multi-time scales and low-pass filter. forgetting factor recursive least squares is applied to conduct online parameter identification, and the traditional double extended Kalman filtering algorithm is optimized to evaluate the state of charge and model parameters in the micro-scale and macro-scale. In this way, the error caused by two different characteristics is reduced, and a low-pass filter is added to optimize the fluctuation problem of the estimated value of the model parameters. According to the experiment results, the maximum error between the model simulation value and the actual value of the terminal voltage is 0.0459 V. If the initial value of the state of charge deviates from the actual value, the maximum errors under BBDST and HPPC conditions record 0.0235 and 0.0048, respectively, the forgetting factor recursive least squares - double extended Kalman filtering algorithm with multi-time scales and low-pass filter is able to track the true value within 40 seconds. Furthermore, the lithium-ion battery state of health both reaches 98% under the two conditions. In summary, the experimental analysis shows that the algorithm helps reduce the influence of initial values on the results, thereby reducing error accumulation and improving the robustness.

Key words: Low pass filter; Second-order RC model; forgetting factor recursive least squares; Collaborative state estimation; double extended Kalman; multi-time scale

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# 1. Introduction

At present, new energy vehicles, aerospace, and many other emerging energy strategies are developing rapidly [1, 2]. Lithium-ion battery management systems (BMS) and real-time reliable detection systems have been regarded as the core technology of new energy systems [3, 4]. Lithium-ion batteries' number of cycles, cost, reliability, and safety problems are becoming increasingly prominent. The demand for technological breakthrough and theoretical innovation of high-quality lithium-ion battery is rapidly expanding [5]. The requirement of accurately updating the model parameters in real-time and accurately estimating the state of charge and health are increasing. There are many applications around us. For example, EV wireless charging and Wireless sensor Networks field[6, 7]. Electric Vehicle Charging Study[8]. The research and development of a new generation of high-end lithium-ion battery energy and intelligent real-time detection system is the key breakthrough of the national new energy research and development industry [9]. The in-depth research on lithium-ion batteries' state of charge and health by many industry personnel will be introduced in detail below [10].

In the initial estimation of the state of charge of the lithium-ion battery, the discharge experiment method is adopted to carry out a constant discharge of the lithium-ion battery and stop it when it reaches the cut-off voltage. This method is relatively simple and the obtained results are relatively accurate [11]. Still, it takes a long time and can not calculate the lithium-ion battery under the working state in real time. In order to make up for the deficiency of discharge experiment method, the ampere hour method is proposed to estimate state of charge [12]. Its principle is to calculate the total amount of charge and discharge charge in a period of time by giving state of charge value at a particular time. The estimated value can be obtained by superimposing the given value and calculated value [13]. There are some problems with ampere hour method, for example, its estimation error will accumulate over time and estimation accuracy depends on the initial value [14]. In order to solve the error accumulation problem of the ampere-hour method, Kalman Filter algorithm was proposed based on the ampere-hour [15]. This algorithm

is mainly composed of prediction and update. It continuously iterates estimating state of charge, quickly tracks the real state of charge value and calculates the optimal estimate value [16]. However, Kalman Filter algorithm can only solve linear problems, and the estimation of state of charge is usually a nonlinear process, so it needs to linearize the nonlinear system [17]. When Kalman Filter can not solve the nonlinear problem, Extended Kalman Filter algorithm based on Kalman filter algorithm to solve the nonlinear system [18], by linearizing the nonlinear state space equation, Kalman filter algorithm to achieve state of charge estimation [19]. The authors propose a cubic Kalman filtering algorithm combining fuzzy adaptive and singular value decomposition in order to solve the problem of slow convergence time of cubic Kalman algorithm[20].

Four kind of algorithms based on Kalman filter extension are introduced in detail (extended Kalman filter, unscented Kalman filter, cubature Kalman filter and ensemble Kalman filter), the advantages and disadvantages, estimation accuracy and anti-interference ability of these four algorithms were compared in detail [21]. The author proposed a novel Adaptive Square root Extended Kalman filter based on extended Kalman filter algorithm, which solved the filtering divergence problem and ensured non-negative deterministic in [22]. In addition to the author proposed a correntropy - weighted least squares - extended Kalman filter algorithm to estimate state of charge, and the error can be effectively reduced under the condition of non-Gaussian noise in [23]. Aiming at the problem of battery parameter marginalization and ageing, the authors estimate state of charge accurately by volume Kalman filter combined with recursive least squares in [24]. The author focuses on the fractal-order adaptive extended Kalman filter, which can quickly track the unknown variance in [25]. An estimation method with an adaptive feedback compensator is proposed, which can improve state of charge estimation performance and fast convergence in [26].

With the rapid development of society, the use frequency of lithium-ion battery products is increasing [27], and the aging problem of lithium-ion battery is becoming increasingly apparent. In order to know the aging degree of battery in real time and accurately [28], we introduce the battery State of Health (SOH). The battery health status is defined as the ratio of the capacity released by the power battery from the full charge state to the cut-off voltage at a certain rate to the standard capacity under standard conditions [29]. This ratio is a manifestation of the battery health status and conforms to most current lithium-ion batteries [30]. At present, there are several methods to estimate the health status of lithium-ion batteries: neural network algorithm. The abandon the traditional equivalent circuit method and independent of model, a method of state of health estimation based on incremental capacity and fusion of wavelet neural network and genetic algorithm is proposed in [31]. The authors developed a neural network that used more than 110,000 measurements to train and validate the model in [32]. The author proposes a new multi-scale state of health model to solve the capacity degradation problem, and finally constructs a prediction framework based on wavelet neural network and integrated learning network in [33]. Model estimation method, a model-based voltage construction method is proposed to eliminate unfavorable numerical conditions and reshape incremental capacity (IC) curves in [34]. The author proposes a novel state of health estimator based on fusion, which has a high estimate of intensive reading in [35]. The author proposed a battery health assessment framework based on fuzzy comprehensive evaluation (FCE) and improved multiple grey model (IMGM) to optimize multiple health indicators (MHIs) system to reduce the influence of Health indicator (HI) error on the overall prediction results in [36]. Data driven and Support vector machine [37-39]. The author proposes an improved sine-cosine algorithm based on the two-order RC model [40]. The author takes machine learning as the starting point, analyzes and compares five popular intelligent algorithms, and provides some enlightenment for maximum likelihood method to estimate state of health [41].

With the increasing accuracy requirements of the algorithm, this paper proposes a multi-time scale low-pass filter forgetting factor recursive least squares method - double extended Kalman filter (FFRLS-DEKF) coestimation algorithm for state of charge and state of health. Based on extended Kalman filter algorithm, a double extended Kalman filter is used. One Kalman filter is used to estimate the slow time-varying characteristics of parameters and the other Kalman filter is used to estimate the fast time-varying characteristics of system states,

which can effectively solve the problem of different time scales of system parameters and system states. In the parameter estimation, a low pass filter is introduced to optimize the parameter estimation result, which improves the accuracy of state of health estimation value. The advantage of the whole algorithm in terms of computational efforts is that it calculates two kinds of variables at different time scales, which meets the different requirements of system parameters and system states and improves the accuracy of estimation. However, the disadvantage is that it requires a large amount of calculation and has certain requirements for equipment performance.

2. Mathematical analysis

# 2.1 2-RC equivalent modeling

The equivalent circuit model is inseparable from the charge-discharge experiment, and the performance parameters of lithium-ion battery are studied by Hybrid Pulse Power Characterization Test (HPPC) [42]. In order to accurately estimate state of charge, state of health and other model parameters under lithium-ion battery operation, the second-order RC equivalent circuit model is selected in this paper [43]. Compared with the Thevenin equivalent circuit model [44], the second-order RC circuit model has an additional RC loop representing dynamic response, as shown in Fig. 1.

# [Insert Figure 1]

### Fig. 1 Second order RC equivalent circuit model

In this model,  $U_b$  represents the voltage source of the lithium-ion battery, which varies with state of charge,  $R_i$  represents the ohmic internal resistance of the battery [45],  $R_1$  and  $R_2$  both represent the polarization resistance of the battery, U represents the measured terminal voltage, and in the equivalent circuit, RC circuit composed of  $R_1$  and  $C_1$  represents the process of rapid voltage change in the electrochemical reaction inside the battery [46]. The RC circuit composed of  $R_2$  and  $C_2$  represents the process in which the voltage of the electrochemical reaction inside the battery changes slowly, and I is the direction of the current circuit [47]. According to Kirchhoff's voltage

law, the KVL equation of the circuit can be obtained as shown in Equation (1).

In order to estimate the charged state, it is necessary to establish the system's state equation, observation equation

and parameter estimation parameter equation, and equation (2) can be obtained by discretization Equation (1).

$$\begin{cases} x_{k,l+1} = f(x_{k,l},\theta_k,u_{k,l}) + w_{k,l} \\ Y_{k,l} = g(x_{k,l},\theta_k,u_{k,l}) + v_{k,l} \\ \theta_{k+1} = \theta_k + \rho_k \end{cases}$$
(2)

According to the second order RC equivalent circuit model,  $[SOC U_1 U_2]$  was selected as the state variable, and combined with equation (2) and state of charge definition discretization, the equation (3) was obtained as follows

follows.

$$\begin{bmatrix} SOC_{k+1} \\ U_{1,k+1} \\ U_{2,k+1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 - T/\tau_1 & 0 \\ 0 & 0 & 1 - T/\tau_2 \end{bmatrix} \# \#$$

$$U_{b,k+1} = U(SOC,k+1) + U_i + U_1 + U_2$$

$$(3)$$

In equation (3), *T* is sampling time,  $\tau_1$  and  $\tau_2$  equal to  $R_1C_1$  and  $R_2C_2$  respectively, the relation of SOC - OCV can be obtained by polynomial fitting. Forgetting Factor Recursive Least Square method is used for polynomial fitting of data, the variation of parameters is not obvious, the order of polynomial is increasing, the more likely produce oscillations. In polynomial fitting of experimental data, it is found that the effect of polynomial fitting with sixth order is equivalent to that of polynomial fitting with seventh order due to the existence of oscillation phenomenon. Therefore, sixth-order polynomial is chosen as the fitting target. U(SOC, k + 1) can be expressed as shown in Equation (4).

$$U(SOC, k+1) = K_0 + K_1 SOC + K_2 SOC^2 + K_3 SOC^3 + K_4 SOC^4 + K_5 SOC^5 + K_6 SOC^6$$
(4)

Where k and l represent the macroscopic system parameters and the microscopic system state indicators respectively, where  $x_{k,l}$  is the state equation of the system,  $U_{k,l}$  is the input matrix,  $Y_{k,l}$  is the observation equation at this moment, where  $w_{k,l}$  and  $\rho_k$  are the process noise of the observation equation and parameter equation,  $v_{k,l}$  is

the observation noise. Both system noise and observation noise are gaussian white noise, and their variances are expressed as Q and R. Where K is an undetermined coefficient, which can be obtained by fitting open circuit voltage (OCV) and state of charge.

#### 2.2 FFRLS Parameter identification

Choosing 4.2V/70Ah term-power lithium-ion battery, which has the advantages of high energy density[48], good cycle performance and long battery life. In the lithium-ion battery management system (BMS), the Hybrid Pulse Power Characterization Test (HPPC) is carried out with ternary lithium-ion battery as the experimental object [49]. The principle is to discharge the battery every SOC=0.1 to get the variation rule of each parameter [50]. The voltage transformation curve is shown in Figure 2 (a), and the current curve is shown in Figure 2(b).

[Insert Figure 2 (a)]

[Insert Figure 2 (b)]

(a) HPPC voltage curve

(b) HPPC current curve

Fig. 2 Voltage and current curve under HPPC test

The variation curves of various parameters are obtained by Hybrid Pulse Power Characterization experiment and the parameters of the second-order RC model are identified by using the Forgetting Factor Recursive Least Square (FFRLS) [51]. In the identification process, the function of the forcing factor is to give a small weight to the data with a long running time, while the latest observation data occupy a large weight. The identification process is as follows:

The second-order RC equivalent circuit model is transformed into the mathematical form of the least square method, as shown in Equation (5).

$$U_b = \left(\frac{R_1}{R_1 C_1 s + 1} + \frac{R_2}{R_2 C_2 s + 1} + R_i\right) \mathbf{I} + U$$
(5)

As in equation (5), let  $\tau_1 = R_1C_1$  and  $\tau_2 = R_2C_2$ , Substitute it into Equation (5) to obtain:

$$\tau_{1}\tau_{2}U_{b}s^{2} + (\tau_{1} + \tau_{2})U_{b}s + U_{b} = s^{2}\tau_{1}\tau_{2}R_{i}I + s[R_{1}\tau_{2} + R_{2}\tau_{1} + R_{i}(\tau_{1} + \tau_{2})]I + (R_{1} + R_{2} + R_{i})I + s^{2}\tau_{1}\tau_{2}U + s(\tau_{1} + \tau_{2})U + U$$
(6)

As in equation (6), let  $a = \tau_1 \tau_2$ ,  $b = \tau_1 + \tau_2$ ,  $c = R_1 + R_i + R_2$ ,  $d = R_1 \tau_2 + R_2 \tau_1 + R_i (\tau_1 + \tau_2)$ , Then the above

equation can be simplified to equation (7).

$$aU_{b}s^{2} + bU_{b}s + U_{b} = as^{2}R_{i}I + dsI + cI + as^{2}U + bsU + U$$
(7)

Substitute  $s = \frac{[x(k) - x(k-1)]}{T}$ ,  $s^2 = [x(k) - 2x(k-1) + x(k-2)]/T$  into equation (7) for discretization, where

T is the sampling time, as shown below:

$$U_{b}(k) - U(k) = \frac{-bT - 2a}{T^{2} + bT + a} [U(k - 1) - U_{b}(k - 1)] + \frac{a}{T^{2} + bT + a} [U(k - 2) - U_{b}(k - 2)] +$$

$$\frac{cT^{2} + dT + aR_{i}}{T^{2} + bT + a} I(k) + \frac{-dT - 2aR_{i}}{T^{2} + bT + a} I(k - 1) + \frac{aR_{i}}{T^{2} + bT + a} I(k - 2)$$
(8)

Simplify (8), we can get Eq.(9) as follow.

$$U_{b}(k) - U(k) = k_{1}[U(k-1) - U_{b}(k-1)] + k_{2}[U(k-2) - U_{b}(k-2)] + k_{3}I(k) + k_{4}I(k-1) + k_{5}I(k-2)$$
(9)

Each coefficient in equation (9) can be expressed as follows:

$$k_{1} = \frac{-bT - 2a}{T^{2} + bT + a}$$

$$k_{2} = \frac{a}{T^{2} + bT + a}$$

$$k_{3} = \frac{cT^{2} + dT + aR_{i}}{T^{2} + bT + a}$$

$$k_{4} = \frac{-dT - 2aR_{i}}{T^{2} + bT + a}$$

$$k_{5} = \frac{aR_{i}}{T^{2} + bT + a}$$
(10)

As in equation (10), let  $\theta = [k_1, k_2, k_3, k_4, k_5]^T$ , bring it into the forgetting factor recursive least squares algorithm, and solve the parameter values of the second-order RC equivalent circuit from the identification results. The

forgetting factor recursive least squares recurrence equation is as follows:

.

$$\begin{cases} \hat{\theta}(k+1) = \hat{\theta}(k) + K(k+1)[y(k+1) - \phi^{T}(k+1)\hat{\theta}(k)] \\ K(k+1) = P(k+1)\phi(k+1)[\phi^{T}(k+1)P(k)\phi(k+1) + \lambda]^{-1} \\ P(k+1) = \lambda^{-1}[I - K(k+1)\phi^{T}(k+1)]P(k) \end{cases}$$
(11)

Where P(k) is the covariance matrix,  $\phi(k) = [v_{k-1} v_{k-1} I_k I_{k-1} I_{k-2}]$ , *K* is the gain,  $\lambda$  It is a genetic factor, generally  $0 < \lambda < 1$ , when the  $\lambda$  gets smaller value, the better the tracking effect of the algorithm, but it will cause

the fluctuation of the algorithm  $\lambda$ , When *l* is taken, it is the standard least squares recursive method. Through continuous iterative calculation, the results of each time can be obtained  $\theta$ . The value of  $R_i$ ,  $R_1$ ,  $R_2$ ,  $C_1$  and  $C_2$  are calculated from equation (12).

$$R_{i} = \frac{k_{3} - k_{4} + k_{5}}{1 + k_{1} - k_{2}}$$

$$\tau_{1}\tau_{2} = \frac{T^{2}(1 + k_{1} - k_{2})}{4(1 - k_{1} - k_{2})}$$

$$\tau_{1} + \tau_{2} = \frac{T(1 + k_{2})}{1 - k_{1} - k_{2}}$$

$$R_{i}\tau_{1} + R_{i}\tau_{2} + R_{1}\tau_{2} + R_{2}\tau_{1} = \frac{T(k_{3} - k_{5})}{1 - k_{1} - k_{2}}$$

$$R_{i} + R_{1} + R_{2} = \frac{k_{3} + k_{4} + k_{5}}{1 - k_{1} - k_{2}}$$
(12)

#### 2.3 Multi time scale double extended Kalman filter algorithm

The traditional dual extended Kalman filter (DEKF) is used to estimate the battery system parameters and system state at the same time [52]. In each iterative calculation, the state filter of extended Kalman filter uses parameter estimation  $\hat{\theta}_k^-$  The parameter filter of extended Kalman filter uses the current state estimation value  $x_k$  estimate the system model parameters. Since the traditional double extended Kalman filter can only estimate parameters and states at the same time, a multi time scale double extended Kalman filter is proposed in this paper. From equation (2), it can predict the state value of the system at the micro scale, predict the parameter value of the model at the macro scale, and provide stable system parameters and state estimation. The recursive process of dual extended Kalman filter is as follows:

Step 1: initialize system status value and parameter value

$$\hat{\theta}_0 = E[\theta], \ P_{\theta_0} = E[(\theta_0 - \hat{\theta}_0)(\theta_0 - \hat{\theta}_0)^T], \ \hat{x}_0 = E[x], \ P_{x0} = E[(x_0 - \hat{x}_0)(x_0 - \hat{x}_0)^T$$
(13)

Step 2: parameter filter time update equation

$$\hat{\theta}_{l}^{-} = \hat{\theta}_{l-1}, P_{1}^{-} = P_{1} + Q^{\theta}$$
(14)

Step 3: parameter filter measurement update equation

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$$\begin{cases} K_{1} = P_{l}C_{l}^{T}[C_{l}P_{l}C_{l}^{T} + R_{1}]^{-} \\ \hat{\theta}_{1} = \hat{\theta}_{1}^{-} + K_{1}Y_{l} - K_{1}g(x_{k},\hat{\theta}_{l}^{-},u_{k}) \\ P_{\theta_{l}} = (I - K_{1}C_{l})P_{1}^{-} \end{cases}$$
(15)

Step 4: state filter time update equation

$$\hat{x}_{k}^{-} = f(\hat{x}_{k-1}, \hat{\theta}_{k-1}, u_{k}), P_{k}^{-} = A\hat{P}_{k-1}A^{T} + Q_{k-1}$$
(16)

Step 5: state filter measurement update equation

$$\begin{aligned} \mathbf{K}_{k} &= P_{k} C_{k}^{T} [C_{k} P_{k}^{-} C_{k}^{T} + \mathbf{R}_{k}]^{-} \\ \hat{x}_{k} &= \hat{x}_{k}^{-} + \mathbf{K}_{k} Y_{k} - \mathbf{K}_{k} g \left( x_{k}, \hat{\theta}_{l}^{-}, u_{k} \right) \\ P_{k} &= (I - \mathbf{K}_{k} C_{k}) P_{k}^{-} \end{aligned}$$
(17)

The calculation method of A,  $C_k$  and  $C_l$  is as follows

$$A \triangleq \frac{\partial f(x_{k,l},\theta_k,u_{k,l})}{\partial x}, \ C_k \triangleq \frac{\partial g(x_{k,l},\theta_k,u_{k,l})}{\partial x}, \ C_l \triangleq \frac{\partial g(x_{k,l},\theta_k,u_{k,l})}{\partial \theta}$$
(18)

Where:  $\hat{\theta}_0$  is the initial value of the parameter value, which can be calculated according to the model,  $P_{\theta_0}$  is the parameter value of the parameter error covariance matrix,  $\hat{x}_0$  is the initial value of state quantity,  $P_{x_0}$  the initial value of the state error covariance matrix, all of which are the initial values in the algorithm,  $\hat{\theta}_1$  is the estimated value of the minimum variance of the parameter at time l,  $\hat{x}_k$  is the minimum variance estimate of the parameter at time k,  $K_k$  and  $K_1$  is Kalman gain,  $C_k$  is the state transition matrix at time k. it should be noted that  $C_k$  in parameter filtering refers to the total derivative of the measurement equation with respect to the parameters. We need to decompose the total derivative into partial derivatives and the process is as follows:

$$C_{l} \triangleq \frac{\partial g(x_{k,l},\theta_{k},u_{k,l})}{\partial \theta} = \frac{\partial g(x_{k,l},\hat{\theta}_{l}^{-},u_{k,l})}{\partial \hat{\theta}_{l}^{-}} + \frac{\partial g(x_{k,l},\hat{\theta}_{l}^{-},u_{k,l})}{\partial \hat{x}_{k}} \times \frac{\mathrm{d}\hat{x}_{k}}{d\hat{\theta}_{l}^{-}}$$
(19)

$$\frac{\mathrm{d}\hat{x}_{k}}{d\hat{\theta}_{l}^{-}} = \frac{df\left(x_{k-1,l}\hat{\theta}_{l}^{-}, u_{k-1,l}\right)}{d\hat{\theta}_{l}^{-}} = \left(\frac{\partial f\left(x_{k-1,l}\hat{\theta}_{l}^{-}, u_{k-1,l}\right)}{\partial\hat{\theta}_{k}^{-}} + \frac{\partial f\left(x_{k-1,l}\hat{\theta}_{l}^{-}, u_{k-1,l}\right)}{\partial\hat{x}_{k-1}} \times \frac{d\hat{x}_{k-1}}{d\hat{\theta}_{l}^{-}}\right) \quad (20)$$

$$\frac{d\hat{x}_{k-1}}{d\hat{\theta}_{l}^{-}} = \frac{d\hat{x}_{k-1}^{-}}{d\hat{\theta}_{l}^{-}} - k_{k-1}^{x} \frac{dg(x_{k-1,l}\hat{\theta}_{l}^{-}, u_{k-1,l})}{d\hat{\theta}_{l}^{-}}$$
(21)

The flowchart of the multi time scale double extended Kalman filter algorithm is shown in Fig.3 and the specific steps are as follows.

[Insert Figure 3]

Fig.3 The flowchart of the multi time scale double extended Kalman filter

Step 1 : Initialize the multi time scale dual extended Kalman filter algorithm and select the appropriate values of  $\hat{\theta}_0$ ,  $P_{\theta_0}$ ,  $\hat{x}_0$  and  $P_{x_0}$  using Eq.(13).

Step 2: Under macro scale, according to the slow time characteristic of the parameter, the parameter filter starts to update,  $\hat{\theta}_l^-$  and  $P_l^-$  are calculated from Eq.(14).

Step 3: The obtained parameter value  $\hat{\theta}_l^-$  and  $P_l^-$  is brought into Eq. (15) for parameter filter measurement update to complete a parameter filtering process. After *l* return to the second step to continue the parameter iterative calculation.

Step 4: Under micro scale, From the obtained  $\hat{\theta}_k^-$ ,  $\hat{x}_0$  and  $P_{x0}$ , calculate  $\hat{x}_k^-$  and  $P_k^-$  according to Eq.(16). Step 5: Based on the obtained status update value  $\hat{x}_k^-$  and  $P_k^-$ , calculate the status measurement update value by Eq.(17). After k return to step four to start a new round of system status update.

The whole process of multi-time scale dual extended Kalman filter algorithm can be realized through the fivestep iterative calculation process.

# 2.4 Low pass filtering combined iterative calculation

The loss of lithium-ion will lead to the attenuation of lithium-ion battery capacity and the further aging of lithium-ion battery state. In order to capture this attenuation, the state of health (SOH) is introduced, SOH of lithium-ion battery represents the capacity of the current battery to store electric energy relative to the new battery, and usually represents the state of the battery from the beginning to the end of its life in the form of percentage, which is used to quantitatively describe the performance state of the current battery. When the battery is produced, the state of health is 100%, which means 1. In this part, which is defined as the ratio of the actual maximum available capacity  $Q_{max}$  to the rated capacity  $Q_N$ . In this paper, the multi-time scale dual extended Kalman filter algorithm is used to continuously estimate the battery capacity parameters in real time in view of the time-varying

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characteristics of lithium-ion battery parameters at the macro scale, so as to reduce the estimation error of SOH. The calculation equation of SOH is shown in Eq.(22).

$$SOH = \frac{Q_{max}}{Q_N} \times 100\%$$
 (22)

During the estimation of the parameter filter, the estimated capacity occasionally fluctuates greatly. In order to obtain the accurate state of health estimation value, a low-pass filter is added to the parameter estimation part of the algorithm. The low-pass filtering method uses the sampling value and the output value of the last filtering to get the effective filtering value, so that the output has a feedback effect on the input, reducing the amplitude of the result fluctuation, and its frequency value will not change, nor will it change its real value. As shown in Eq. (23).

$$Y(n) = \alpha X(n) + (1 - \alpha)Y(n - 1)$$
(23)

In Eq.(23), Y(n) is the filter output value, Y(n-1) is Last filter output value, X(n) is sample value,  $\alpha$  is Filter coefficients.

In order to better demonstrate the running process of the multi-time scale low-pass filter forgetting factor recursive least squares - double extended Kalman filtering algorithm, the flow chart of the multi-time scale low-pass filter forgetting factor recursive least squares - double extended Kalman filtering algorithm is shown in Fig.4.

#### [Insert Figure 4]

Fig.4 Flow chart of the multi-time scale low-pass filter FFRLS - DEKF algorithm

The algorithm starts with initialization of the program. In the first step the data obtained through experiments are imported into the forgetting factor recursive least squares algorithm for online parameter identification. In the second step, the obtained data for each parameter are applied to the multi-time scale double extended Kalman filtering algorithm for continuous iterative computation. Final output state of charge estimate, before outputting state of health, low-pass filtering optimizes the output for the estimated value.

# 

# 3. Experimental analysis

# 3.1 System platform design

In this study, a ternary lithium-ion battery with a standard capacity of 70Ah was used as the research object. To verify the accuracy of the proposed algorithm, a small-scale test platform was built through the existing conditions in the laboratory. Fig.5 depicts the structure of the experimental platform and Tab.1 describes the specifications of the BMS and lithium-ion battery.

# [Insert Figure 5]

#### Fig.5 Experimental lithium-ion battery test platform

As shown in Fig.5, the structure of test platform includes: (a) Programable constant temperature test box, it is used to control the ambient temperature and prevent changes in ambient temperature from affecting the results of the experiment. (b) Ternary lithium-ion battery. (c) High-rate power battery charge-discharge tester (CT-4016-5 V100A-NTFA), it is used for charge and discharge experiments. (d) BMS performance control systems. (e) PC serves as the control hub.

#### Tab.1 Lithium-ion battery and BMS specifications

[Insert Table 1]

# 3.2 FFRLS algorithm verification

Through the above theoretical analysis, the experimental data obtained from HPPC test was brought into the forgetting factor recursive least square method (FFRLS) to obtain the real-time data of each parameter. Each result was plotted by Origin, and the estimated voltage value was compared with the real voltage value to verify the accuracy of the algorithm.

	[Insert Figure 6 (a)]	[Insert Figure 6 (b)]
(a)	R <sub>i</sub> identification result curve	(b) $R_1$ identification result curve

[Insert Figure 6 (c)]

[Insert Figure 6 (d)]

(c)  $R_2$  identification result curve

(d)  $C_1$  identification result curve

Fig. 6 Estimated values of FFRLS parameters under Second RC model

Fig.6 shows the four parameter results of forgetting factor recursive least squares algorithm edge identification,

(a) - (c) are the identification results of ohmic internal resistance and two polarization resistances of the battery

respectively, (d) is the identification result of polarization capacitance. At the initial stage of battery discharge,

the parameters fluctuate greatly. With the continuous decrease of SOC, the parameters gradually tend to be stable

under the estimation of forgetting factor recursive least squares algorithm.

[Insert Figure 7 (a)]

[Insert Figure 7 (b)]

(b) FFRLS simulation voltage error result curve

(a) Comparison between simulated voltage and the actual voltage

Fig. 7 Second order RC model voltage validation and error curve

Fig. 7 (a) shows the comparison between the simulated voltage and the actual voltage obtained by the forgetting factor recursive least squares algorithm. It can be seen from the figure that the results obtained by the forgetting factor recursive least squares algorithm are basically consistent with the real results. At the end, the error is largely due to the large voltage fluctuation of the lithium-ion battery. It can be seen from (b) that the maximum voltage error of forgetting factor recursive least squares algorithm in verifying the model is 0.0459V, and the error is within the allowable range. Through the result analysis, forgetting factor recursive least squares has good accuracy in the process of parameter identification.

#### 3.2 HPPC condition verification

Through the above theoretical analysis, this section will verify whether the multi time scale forgetting factor recursive least squares - double extended Kalman filtering algorithm based on low-pass filter is accurate when the initial SOC value is equal to 0.6, the fast time scale l is equal to 1s and the slow time scale k is equal to 80s under (Hybrid Pulse Power Characteristic) HPPC working conditions, and whether the capacity value estimated by parameter filter is stable and reliable through low-pass filter. In order to intuitively see the accuracy of the algorithm, extended Kalman filter (EKF) and double extended Kalman filter (DEKF) will be verified under the same conditions to compare whether the three algorithms are better than the other two algorithms at 25 degrees ambient temperature.

[Insert Figure 8 (b)]

(b) SOC error curve under HPPC condition

[Insert Figure 8 (d)]

(d) SOH curve under HPPC working condition

[Insert Figure 8 (a)]

(a) Estimated SOC and true SOC curve under HPPC condition

[Insert Figure 8 (c)]

(c) Estimated capacity and low-pass filter capacity under HPPC condition

Fig. 8 Three different algorithms SOC estimation, low pass filtering and SOH results under HPPC

When the initial value is equal to 0.6, by verifying the extended Kalman filter (ekf), double extended Kalman filter (ekf), and comparing the multi time scale forgetting factor recursive least squares - double extended Kalman filtering algorithm based on the low-pass filter (The algorithm is represented in the legend as r-dekf) with the real SOC, it can be seen from Fig. 8 (b) that the maximum error of forgetting factor recursive least squares - double extended Kalman filtering algorithm is 0.0048, the maximum error of double extended Kalman filtering algorithm is 0.0225, and the maximum error of extended Kalman filtering algorithm is 0.0867 under Hybrid Pulse Power Characteristic working condition. In addition, forgetting factor recursive least squares - double extended Kalman filtering algorithm can quickly converge to the accurate value in 40 seconds. On the contrary, the

convergence speed of the other two algorithms is slower than that forgetting factor recursive least squares - double extended Kalman filtering algorithm. In Fig.8 (c) f - C denotes the curve after estimation by low-pass filtering. It can be seen from Fig.8 (c) that the capacity estimated by forgetting factor recursive least squares - double extended Kalman filtering algorithm fluctuates greatly, but after the low-pass filtering algorithm, the capacity estimation tends to be stable, and the battery state of health (SOH) is determined by the estimated filter value Fig.8 (d) shows that the state of health lithium-ion battery is at 98%. In order to further verify the multi time scale reliability of the algorithm, it will be verified when the slow time scale *k* becomes 20s.

[Insert Figure 9 (a)]

#### [Insert Figure 9 (b)]

(b) SOC error curve under HPPC condition

(a) Estimated SOC and true SOC curve under HPPC condition

Fig. 9 Comparison diagram of real SOC and estimated SOC, estimation error diagram.

It can be seen from Fig. 9 (a) and (b) that the convergence of the algorithm is worse than that when the slow time scale is 80s. Before SOC = 0.4, the algorithm error under Hybrid Pulse Power Characteristic working condition has reached 0.0068, the maximum error when the full scale is 80s is 0.0048, and the error continues to accumulate. The analysis shows that when the time k of the slow time scale is small, the algorithm will also produce large errors. Therefore, it shows that a reasonable time is particularly important when selecting the slow time scale.

To further verify the stability and accuracy of the multi-time scale low-pass filter forgetting factor recursive least squares - double extended Kalman filtering algorithm under different temperature environments, the battery was placed in an environment of 35 degrees celsius for the same Hybrid Pulse Power Characteristic experiments. The obtained results are shown below.

[Insert Figure 10 (a)]

(a) Estimated SOC and true SOC curve under HPPC

[Insert Figure 10 (b)]

(b) SOC error curve under HPPC condition

condition

[Insert Figure 10 (c)]	[Insert Figure 10 (d)]

(c) SOH curve under HPPC working condition

Fig.10 SOC and SOH curves output by the algorithm at 35 degrees ambient temperature

(d) Low-pass filtering effect

The data obtained from the Hybrid Pulse Power Characteristic test at an ambient temperature of 35 degrees and the results obtained after the algorithm can be seen that the multi time scale low-pass filter forgetting factor recursive least squares - double extended Kalman filtering algorithm has a maximum error of 0.0172 in estimating the SOC, which is within the allowable error range. the difference between the SOH output curve in the SOH output curve in the SOH output curve and the SOH curve in Figure 8 is within 0.01. The stability of the algorithm under different temperature environments is demonstrated. Since zero SOC is a nonexistent quantity in reality, the experimental SOC less than 0.2 is used here only as a reference.

# 3.3 BBDST condition verification

In order to verify the accuracy of multi time scale forgetting factor recursive least squares - double extended Kalman filtering algorithm based on low-pass filter under different working conditions, this section verifies the algorithm under Beijing bus dynamic stress test (BBDST) at 25 degrees ambient temperature. When the initial SOC value is equal to 0.6, the slow time scale k is equal to 80s, and the fast time scale l is equal to 1s, calculate the system state value, estimate the capacity value through the parameter filter, and optimize through the low-pass filter, then estimate the SOH value. The results are shown in the figure below.

[Insert Figure 11 (a)]	[Insert Figure 11 (b)]
(a) Estimated SOC and true SOC curve	(b) SOC error curve
[Insert Figure 11 (c)]	[Insert Figure 11 (d)]
(c) Estimated capacity and low-pass filter capacity	(d) SOH curve

diagram

Fig. 11 Three different algorithms SOC estimation, low pass filtering and SOH results under BBDST

It can be seen from Fig.11 that under Beijing bus dynamic stress test working condition, the multi time scale forgetting factor recursive least squares - double extended Kalman filtering algorithm based on low-pass filter (The algorithm is represented in the legend as r-dekf) is the closest to the real value, and its maximum error of 0.0235, the maximum error of double extended Kalman filtering algorithm is 0.0335, and the maximum error of extended Kalman filtering algorithm is 0.0335, and the maximum error of extended Kalman filtering algorithm is 0.0762. It can be seen that forgetting factor recursive least squares - double extended Kalman filtering algorithm filtering algorithm has the best effect in estimating state of charge. As can be seen from Fig.11 (c), the estimation of the algorithm fluctuates greatly before the low-pass filter algorithm is added, and the estimation capacity is more gentle and less fluctuated after the low-pass filter algorithm is added. Its health state is about 98%, which is consistent with the estimated state of health under Hybrid Pulse Power Characteristic working conditions. It also shows the new reliability of the algorithm in jointly estimating state of charge estimation value when state of charge slow time scale k = 20s is also verified under Beijing bus dynamic stress test working conditions.

[Insert Figure 12 (a)]	[Insert Figure 12 (b)]

(a) Estimated SOC and true SOC curve

Fig. 12 Result of FFRLS-DEKF method deviating from the correct initial SOC. Result of battery health status

(b) SOC error curve

As can be seen from Fig. 12, when the slow time scale is 20 seconds, the algorithm will accumulate and increase the error when SOC = 0.6, and the error has reached 0.03 when SOC = 0.2. Therefore, through the analysis of two working conditions, the multi time scale forgetting factor recursive least squares - double extended Kalman filtering algorithm based on low-pass filter can reflect a good state of charge estimation accuracy.

Similarly to verify the accuracy and stability of the multi-time scale low-pass filter forgetting factor recursive least squares - double extended Kalman filtering algorithm estimation under Beijing bus dynamic stress test

(BBDST )working condition. Two ambient temperature experiments were conducted on the battery again, one at		
35 degrees ambient temperature and the other at 15 degree	es ambient temperature. The algorithm will estimate	
the SOC and SOH under the obtained experimental data, the estimated results are as follows.		
[Insert Figure 13 (a)]	[Insert Figure 13 (b)]	
(a) Estimated SOC and true SOC curve	(b) SOC error curve	

[Insert Figure 13 (c)] [Insert Figure 13 (d)]

(c) SOH estimation curve (d) Estimated capacity and low-pass filter capacity diagram

Fig.13 Algorithm SOC and SOH results for different ambient temperature BBDST conditions

In Figure 13, r-dekf-15, SOH-15 and f-C-15 denotes the estimated curve of the algorithm at 15 degrees. r-dekf-35, SOH-35 and f-C-15 denotes the estimated curve of the algorithm at 35 degrees. The algorithm has a maximum error of 0.0355 at an ambient temperature of 15 deg. with a maximum error of 0.0115 at an ambient temperature of 35 deg. In the SOH estimation, both ambient temperature estimates result in values with an error no greater than 0.02 compared to the error at 25 deg. The results show that the algorithm is able to have good stability at different ambient temperatures. Since zero SOC is a nonexistent quantity in reality, the experimental SOC less than 0.2 is used here only as a reference.

4. Conclusions

Considering the continuous improvement of the requirements for real-time condition monitoring and reliability of lithium-ion batteries. In this paper, HPPC and BBDST experimental data are obtained through experiments. An innovative multi-time scale low-pass filter forgetting factor recursive least squares - double extended Kalman filtering algorithm is proposed to solve the multi-time scale and parameter identification problem, which cannot be solved by traditional double extended Kalman filtering and extended Kalman filtering algorithm. forgetting factor recursive least squares algorithm is used to online identify the parameters of the second-order RC equivalent circuit model, which effectively solves the problem of real-time parameter updating, it is verified by MATLAB simulation. The multi-time scale double extended Kalman filtering algorithm performs state estimation and parameter estimation at macro and micro scales respectively, it effectively solves the multi-time scale problem. The low pass filter solves the problem of capacitance fluctuation in parameter estimation and is used as a representation of the state of health. Experimental results show that the low-pass filter multi-time scale forgetting factor recursive least squares - double extended Kalman filtering algorithm has good performance in joint estimation of SOC and SOH.

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# DATA AVAILABILITY STATEMENT

Data available on request from the authors	The data that support the findings of this study are available		
	from the corresponding author upon reasonable request.		

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#### International Journal of Circuit Theory and Application

Battery type	Ternary lithium-ion battery	BMS type	BMS-HIL-1005
Size	149mm*98mm*40mm	Size	1800mm*700mm*1500mm
Standard capacity	70Ah	Input voltage	220V
Nominal voltage	3.7V	Max power	1500W
Internal resistance	5Ωm		
Maximum continuous discharge	3C		
Charging upper voltage	4.2V		
Discharge lower limit voltage	2.75V		

# Tab.1 Lithium-ion battery and BMS specifications

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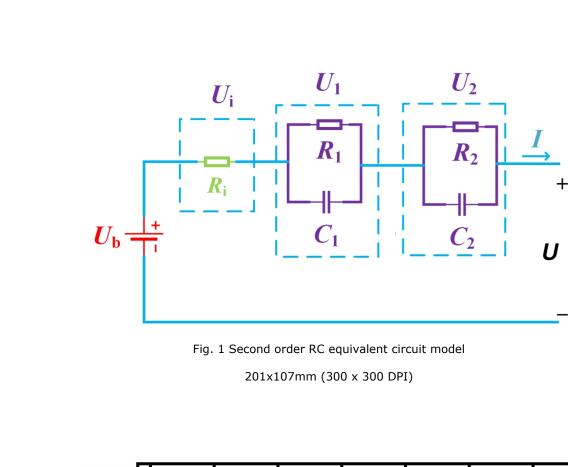
- Fig. 2 Second order RC equivalent circuit model
- Fig. 2 Second order KC equiva
  Fig. 2 (a) HPPC voltage curve

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- Fig. 2 (b) HPPC current curve
- <sup>6</sup> Fig.3 The flowchart of the multi time scale double extended Kalman filter
- Fig.4 Flow chart of the multi-time scale low-pass filter FFRLS DEKF algorithm
- 9 Fig.5 Experimental lithium-ion battery test platform
- Fig. 6 (a) Ri identification result curve
- Fig. 6 (b) R1 identification result curve
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- Fig.13 (c) SOH estimation curve
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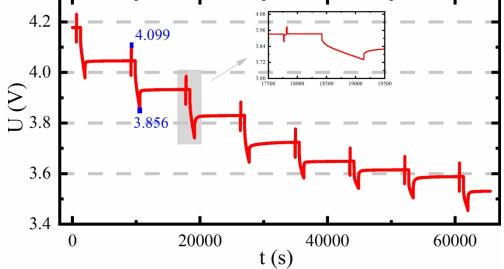
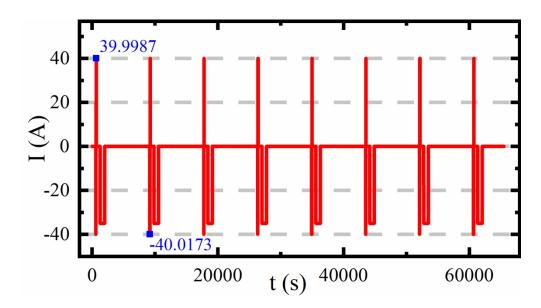
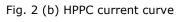
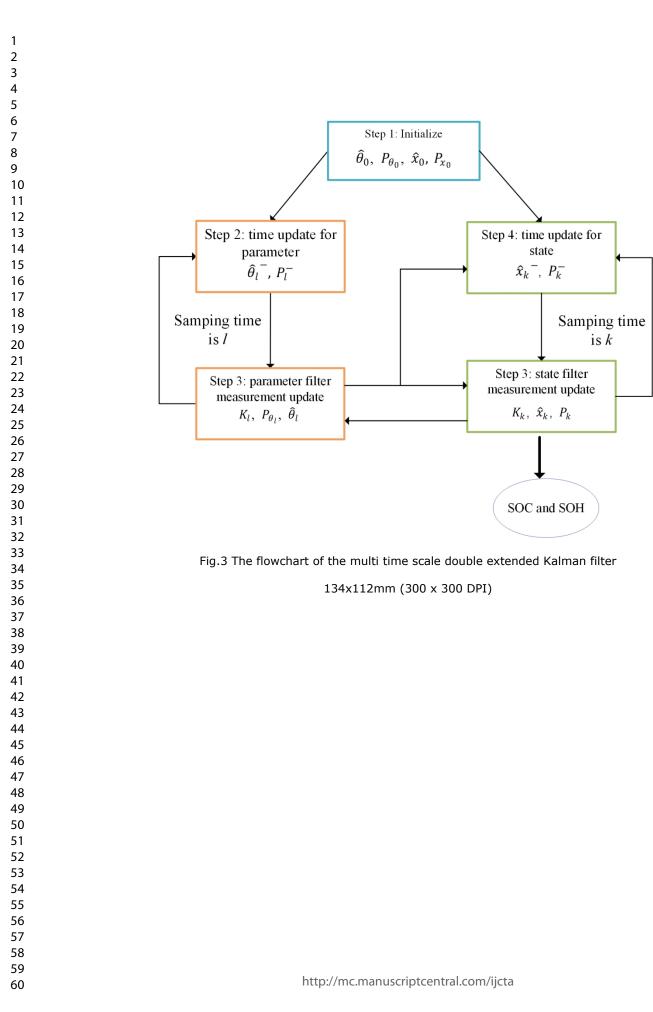


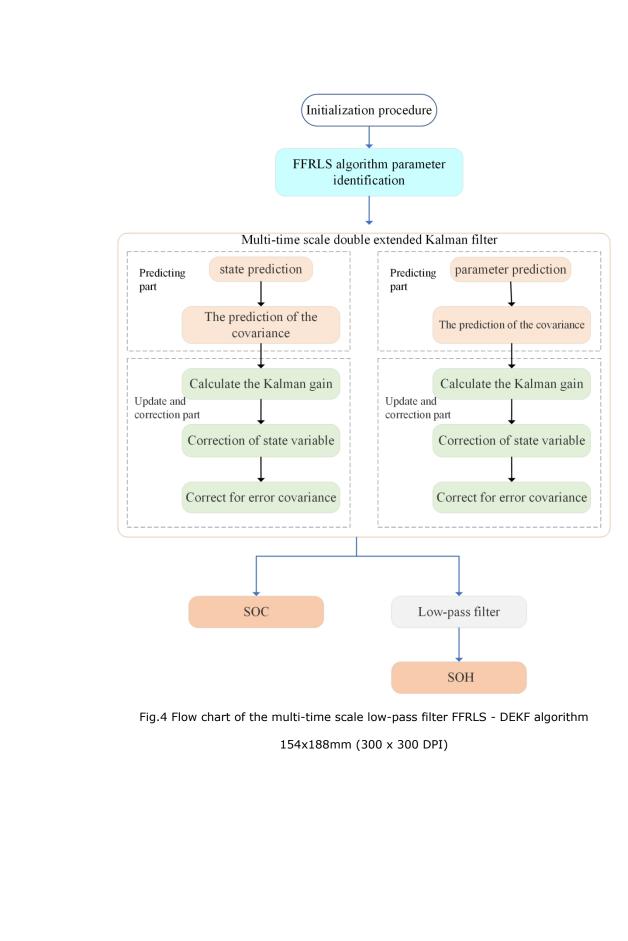
Fig. 2 (a) HPPC voltage curve 181x99mm (300 x 300 DPI)





178x98mm (300 x 300 DPI)





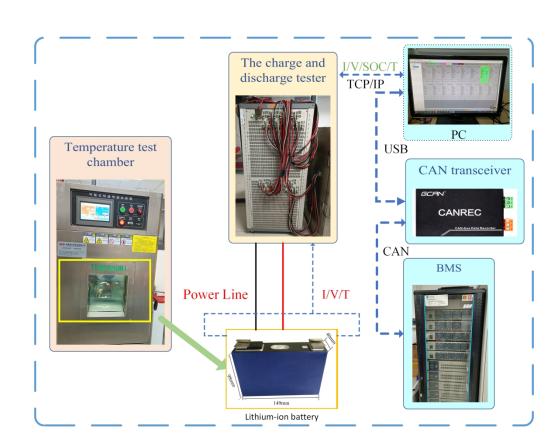
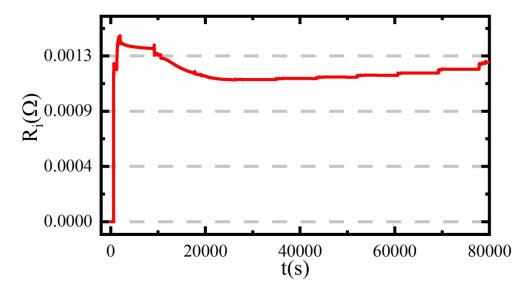


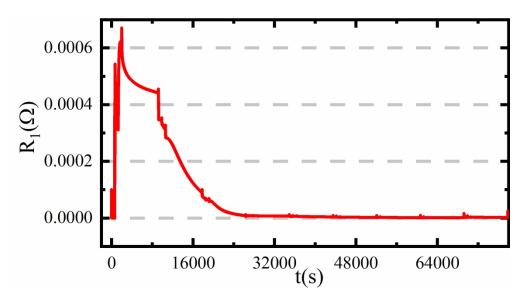
Fig.5 Experimental lithium-ion battery test platform

225x176mm (300 x 300 DPI)



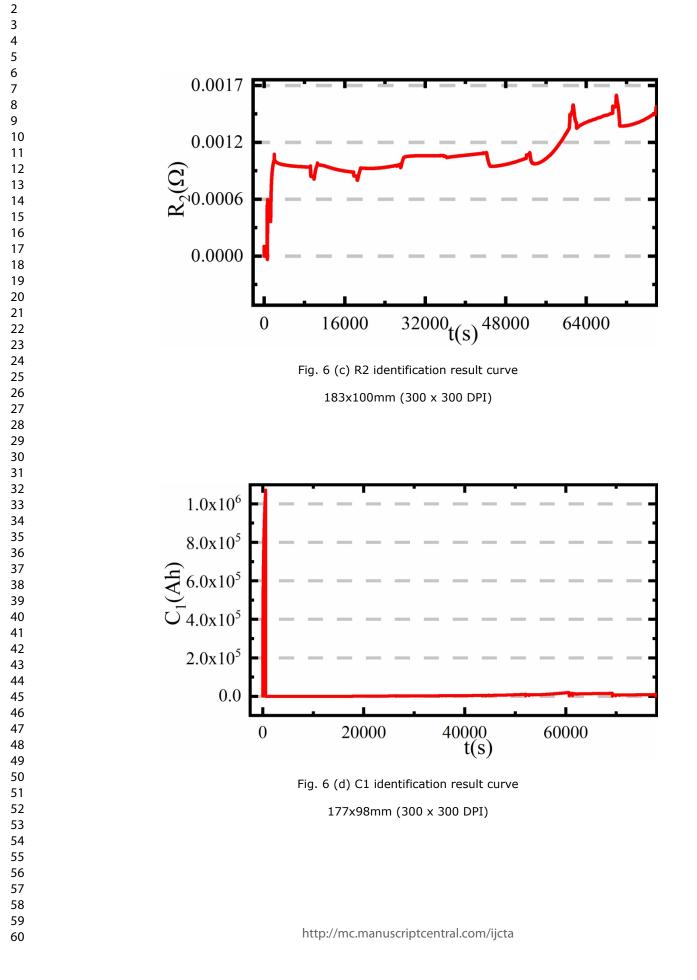


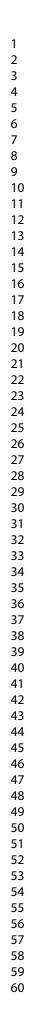
180x96mm (300 x 300 DPI)





179x97mm (300 x 300 DPI)





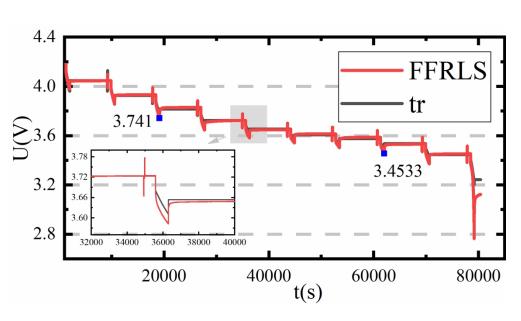


Fig. 7 (a) Comparison between simulated voltage and the actual voltage  $177 \times 99$ mm (300 x 300 DPI)

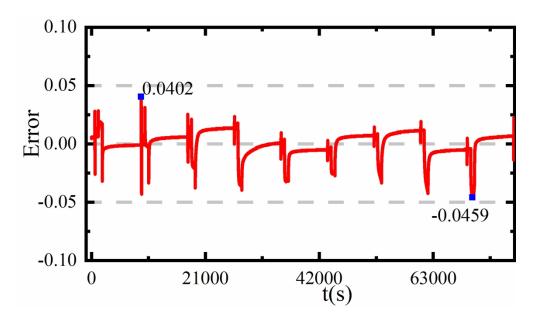


Fig. 7 (b) FFRLS simulation voltage error result curve

169x99mm (300 x 300 DPI)

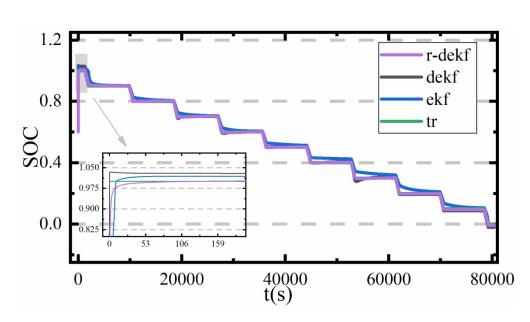


Fig. 8 (a) Estimated SOC and true SOC curve under HPPC condition

178x99mm (300 x 300 DPI)

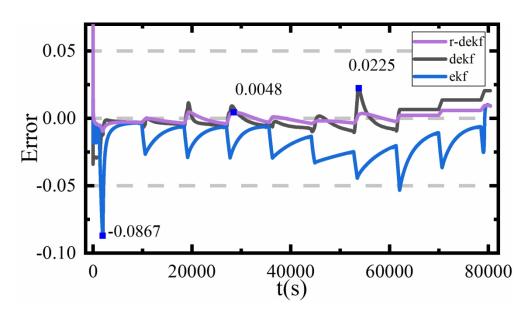
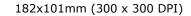


Fig. 8 (b) SOC error curve under HPPC condition



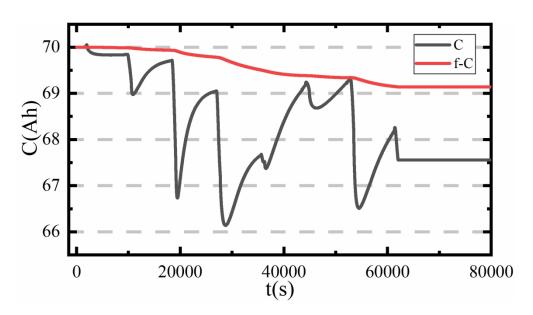
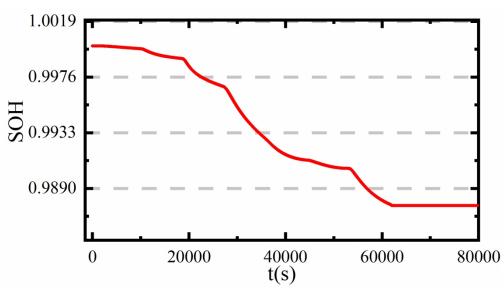
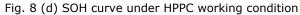
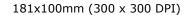


Fig. 8 (c) Estimated capacity and low-pass filter capacity under HPPC condition  $178 \times 99 \text{mm}$  (300 x 300 DPI)







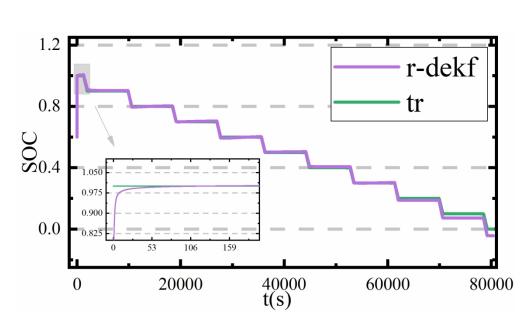
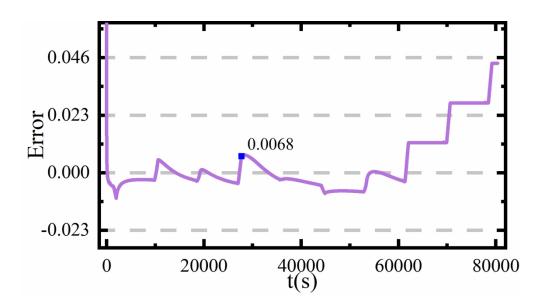
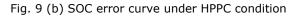


Fig. 9 (a) Estimated SOC and true SOC curve under HPPC condition

179x100mm (300 x 300 DPI)





185x101mm (300 x 300 DPI)

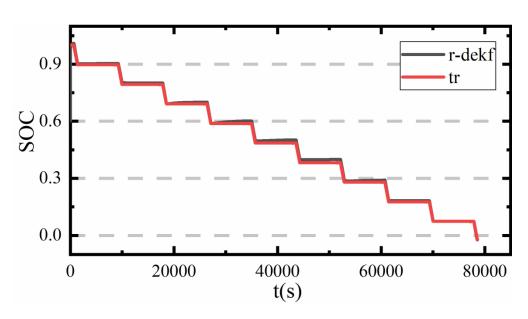


Fig.10 (a) Estimated SOC and true SOC curve under HPPC condition

178x99mm (300 x 300 DPI)

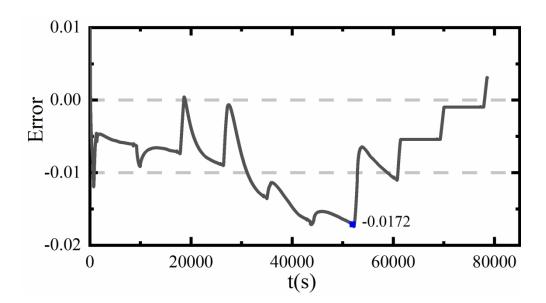
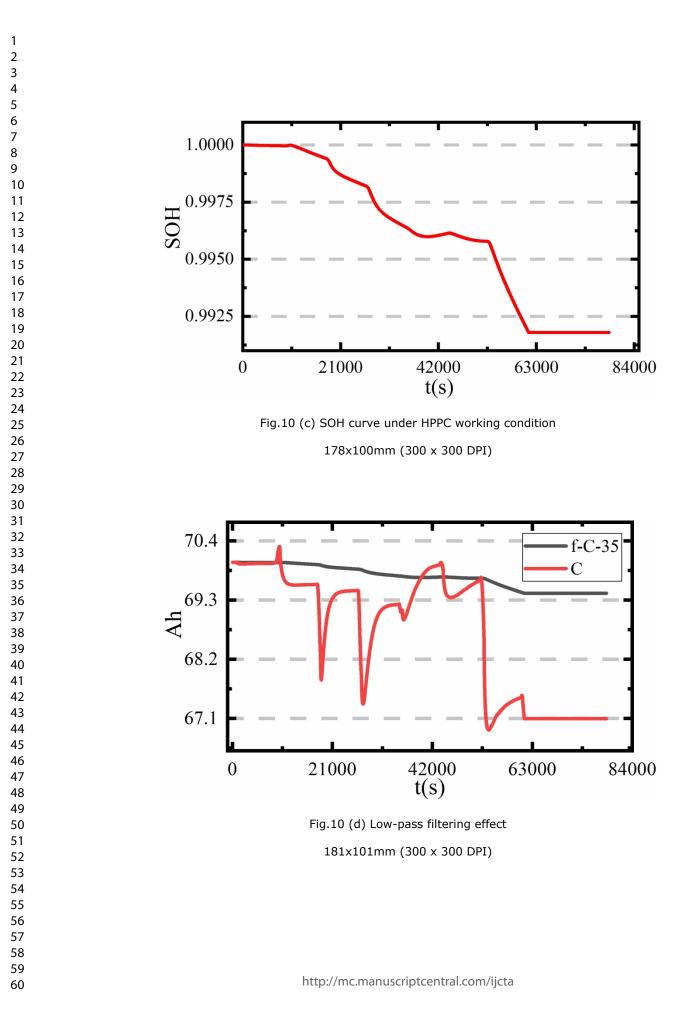


Fig.10 (b) SOC error curve under HPPC condition

179x100mm (300 x 300 DPI)



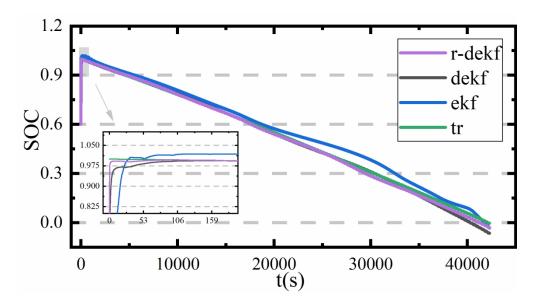
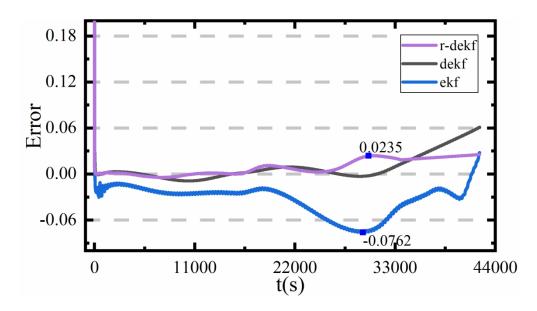
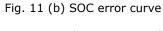


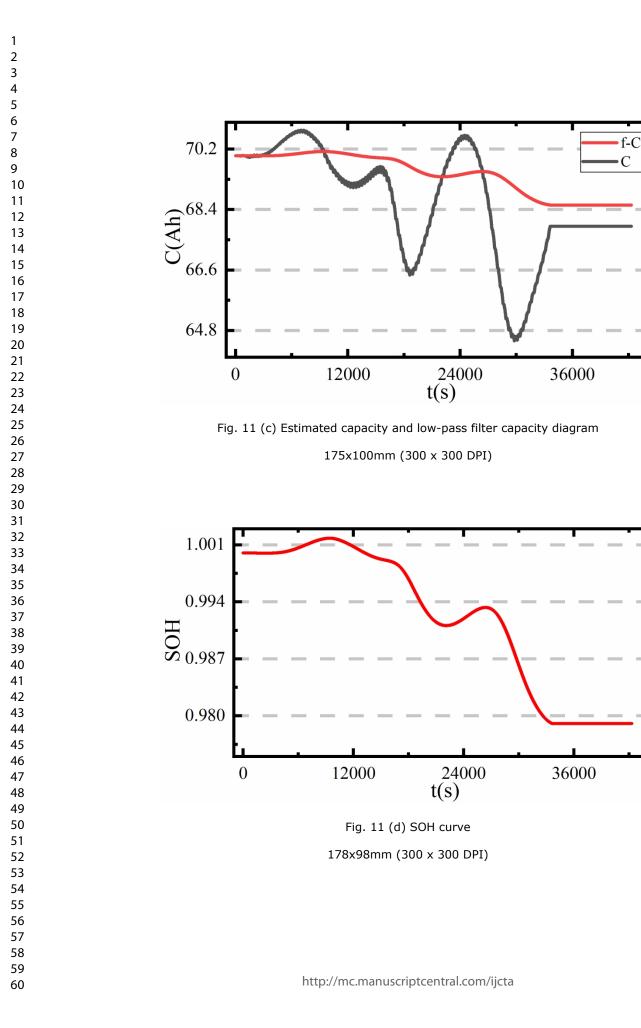
Fig. 11 (a) Estimated SOC and true SOC curve

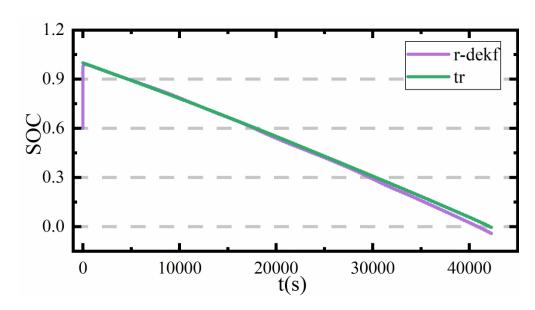
179x100mm (300 x 300 DPI)

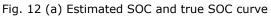


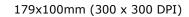


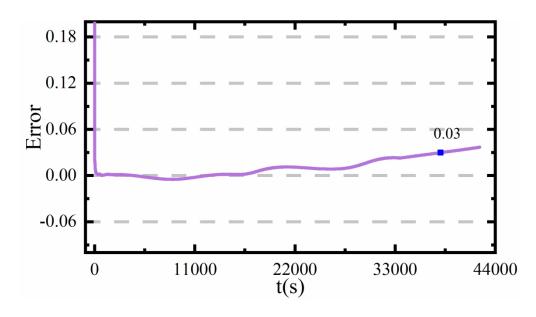
179x99mm (300 x 300 DPI)

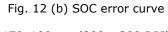




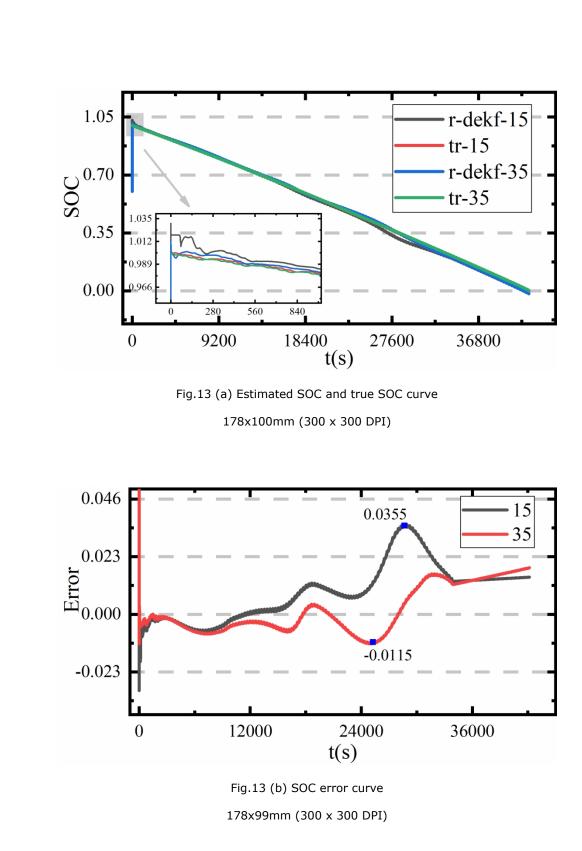


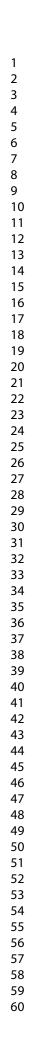


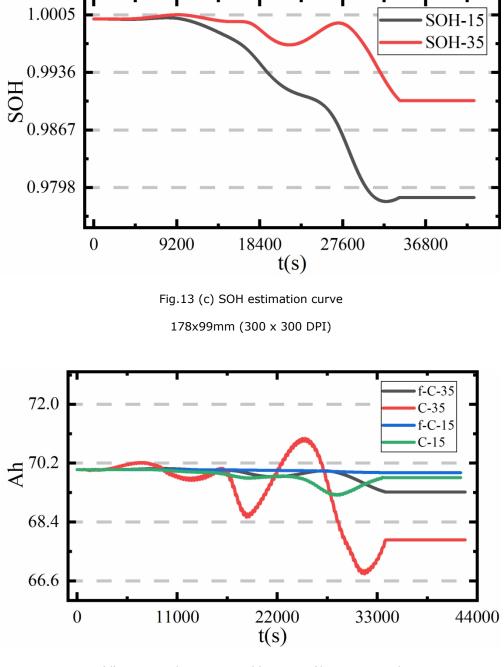




179x100mm (300 x 300 DPI)









178x99mm (300 x 300 DPI)