# Lecture Notes in Computer Science

4136

Commenced Publication in 1973
Founding and Former Series Editors:
Gerhard Goos, Juris Hartmanis, and Jan van Leeuwen

#### **Editorial Board**

David Hutchison

Lancaster University, UK

Takeo Kanade

Carnegie Mellon University, Pittsburgh, PA, USA

Josef Kittler

University of Surrey, Guildford, UK

Jon M. Kleinberg

Cornell University, Ithaca, NY, USA

Friedemann Mattern

ETH Zurich, Switzerland

John C. Mitchell

Stanford University, CA, USA

Moni Naor

Weizmann Institute of Science, Rehovot, Israel

Oscar Nierstrasz

University of Bern, Switzerland

C. Pandu Rangan

Indian Institute of Technology, Madras, India

Bernhard Steffen

University of Dortmund, Germany

Madhu Sudan

Massachusetts Institute of Technology, MA, USA

Demetri Terzopoulos

University of California, Los Angeles, CA, USA

Doug Tygar

University of California, Berkeley, CA, USA

Moshe Y. Vardi

Rice University, Houston, TX, USA

Gerhard Weikum

Max-Planck Institute of Computer Science, Saarbruecken, Germany

# Renate A. Schmidt (Ed.)

# Relations and Kleene Algebra in Computer Science

9th International Conference on Relational Methods in Computer Science and 4th International Workshop on Applications of Kleene Algebra, RelMiCS/AKA 2006 Manchester, UK, August/September, 2006 Proceedings



#### Volume Editor

Renate A. Schmidt University of Manchester School of Computer Science Oxford Rd, Manchester M13 9PL, UK E-mail: Renate.Schmidt@manchester.ac.uk

Library of Congress Control Number: 2006931478

CR Subject Classification (1998): F.4, I.1, I.2.3, D.2.4

LNCS Sublibrary: SL 1 – Theoretical Computer Science and General Issues

ISSN 0302-9743

ISBN-10 3-540-37873-1 Springer Berlin Heidelberg New York ISBN-13 978-3-540-37873-0 Springer Berlin Heidelberg New York

This work is subject to copyright. All rights are reserved, whether the whole or part of the material is concerned, specifically the rights of translation, reprinting, re-use of illustrations, recitation, broadcasting, reproduction on microfilms or in any other way, and storage in data banks. Duplication of this publication or parts thereof is permitted only under the provisions of the German Copyright Law of September 9, 1965, in its current version, and permission for use must always be obtained from Springer. Violations are liable to prosecution under the German Copyright Law.

Springer is a part of Springer Science+Business Media

springer.com

© Springer-Verlag Berlin Heidelberg 2006 Printed in Germany

Typesetting: Camera-ready by author, data conversion by Scientific Publishing Services, Chennai, India Printed on acid-free paper SPIN: 11828563 06/3142 5 4 3 2 1 0

### **Preface**

This volume contains the joint proceedings of the 9th International Conference on Relational Methods in Computer Science (RelMiCS-9) and the 4th International Workshop on Applications of Kleene Algebra (AKA 2006). The joint event was hosted by the School of Computer Science at the University of Manchester, UK, from August 29 to September 2, 2006. RelMiCS/AKA is the main forum for the relational calculus as a conceptual and methodological tool and for topics related to Kleene algebras. Within this general theme, the conference series is devoted to the theory of relation algebras, Kleene algebras and related formalisms as well as to their diverse applications in software engineering, databases and artificial intelligence. This year, special focus was on formal methods, logics of programs and links with neighboring disciplines. This diversity is reflected by the contributions to this volume.

The Programme Committee selected 25 technical contributions out of 44 initial submissions from 14 countries. Each paper was referred by at least three reviewers on its originality, technical soundness, quality of presentation and relevance to the conference. The programme included three invited lectures by distinguished experts in the area: "Weak Kleene Algebra and Computation Trees" by Ernie Cohen (Microsoft, USA), "Finite Symmetric Integral Relation Algebras with no 3-Cycles" by Roger Maddux (Iowa State University, USA), and "Computations and Relational Bundles" by Jeff Sanders (Oxford, UK). In addition, for the first time, a PhD programme was co-organized by Georg Struth. It included the invited tutorials "Foundations of Relation Algebra and Kleene Algebra" by Peter Jipsen (Chapman University, USA), and "Relational Methods for Program Refinement" by John Derrick (Sheffield University, UK).

As in previous years, the RelMiCS Conference and the AKA Workshop were co-organized because of their considerable overlap. Previous RelMiCS meetings were held in 1994 at Dagstuhl, Germany, in 1995 at Parati, Brazil, in 1997 at Hammamet, Tunisia, in 1998 at Warsaw, Poland, in 1999 at Québec, Canada, in 2001 at Oisterwijk, The Netherlands, in 2003 at Malente, Germany and in 2005 at St.Catharines, Canada. The AKA Workshop has been held jointly with RelMiCS since 2003, after an initial Dagstuhl Seminar in 2001.

I would like to thank the many people without whom the meeting would not have been possible. First, I would like to thank all authors who submitted papers, all participants of the conference as well as the invited keynote speakers and the invited tutorial speakers for their contributions. I am very grateful to the members of the Programme Committee and the external referees for carefully reviewing and selecting the papers. I thank my colleagues on the Steering Committee for their advice and the support for the changes introduced for this year's event. Special thanks go to the members of the local organization team in the School of Computer Science at the University of Manchester for all their

#### VI Preface

help: the staff in the ACSO office, especially Bryony Quick and Iain Hart, the staff of the finance office, and the technical staff, as well as Zhen Li and David Robinson. Moreover, I am extremely grateful to Georg Struth for his tremendous amount of effort—as Programme Chair he helped with every aspect of the planning and organization of RelMiCS/AKA 2006 and the PhD Programme. Finally, it is my pleasure to acknowledge the generous support by: the UK Engineering and Physical Sciences Research Council (grant EP/D079926/1), the London Mathematical Society, the British Logic Colloquium, the University of Manchester (President's Fund), and the School of Computer Science, University of Manchester.

Manchester, June 2006

Renate Schmidt General Chair RelMiCS/AKA 2006

# Organization

#### **Conference Chairs**

Renate Schmidt (UK, General Chair) Georg Struth (UK, Program Chair)

## Steering Committee

Rudolf Berghammer (Germany, Chair)

Jules Desharnais (Canada)

Ali Jaoua (Qatar)

Bernhard Möller (Germany)

Ewa Orlowska (Poland)

Gunther Schmidt (Germany)

Renate Schmidt (UK)

Harrie de Swart (Netherlands) Michael Winter (Canada)

#### **Program Committee**

Roland Backhouse (UK)

Rudolf Berghammer (Germany)

Stéphane Demri (France)

Jules Desharnais (Canada)

Zoltán Ésik (Hungary, Spain)

Marcelo Frías (Argentina)

Hitoshi Furusawa (Japan)

Stéphane Gaubert (France)

Steven Givant (USA)

Valentin Goranko (South Africa)

Martin Henson (UK)

Ali Jaoua (Qatar)

Peter Jipsen (USA)

Wolfram Kahl (Canada)

Yasuo Kawahara (Japan)

Zhiming Liu (China)

Bernhard Möller (Germany)

Damian Niwinski (Poland)

Ewa Orlowska (Poland)

Alban Ponse (Netherlands)

Ingrid Rewitzky (South Africa)

Ildikó Sain (Hungary)

Holger Schlingloff (Germany)

Gunther Schmidt (Germany)

Renate Schmidt (UK)

Giuseppe Scollo (Italy)

Georg Struth (UK)

Michael Winter (Canada)

Harrie de Swart (Netherlands)

#### External Referees

Balder ten Cate Wim Hesselink Zhao Liang
Alexander Fronk Peter Höfner Kamal Lodaya
Marian Gheorghe Britta Kehden Maarten Marx

#### VIII Organization

Sun Meng Andrea Schalk Thomas Triebsees Szabolcs Mikulas Nikolay V. Shilov Jeff Sanders Venkat Murali Kim Solin Liang Zhao Ian Pratt-Hartmann Dmitry Tishkovsky

## Local Organization

Renate Schmidt (Local Organization Chair) Bryony Cook, Iain Hart (Registration, Secretarial Support) Zhen Li (Webpages) David Robinson (Local Organization)

## **Sponsoring Institutions**

British Logic Colloquium Engineering and Physical Sciences Research Council London Mathematical Society University of Manchester

# **Table of Contents**

Weak Kleene Algebra and Computation Trees	1
Finite Symmetric Integral Relation Algebras with No 3-Cycles	2
Computations and Relational Bundles	30
An Axiomatization of Arrays for Kleene Algebra with Tests	63
Local Variable Scoping and Kleene Algebra with Tests	78
Computing and Visualizing Lattices of Subgroups Using Relation Algebra and RelView	91
On the Complexity of the Equational Theory of Relational Action Algebras	106
Demonic Algebra with Domain	120
Topological Representation of Contact Lattices	135
Betweenness and Comparability Obtained from Binary Relations  Ivo Düntsch, Alasdair Urquhart	148
Relational Representation Theorems for General Lattices with Negations	162
Monotonicity Analysis Can Speed Up Verification	177

## X Table of Contents

Max-Plus Convex Geometry	192
Lazy Semiring Neighbours and Some Applications  Peter Höfner, Bernhard Möller	207
Omega Algebra, Demonic Refinement Algebra and Commands  Peter Höfner, Bernhard Möller, Kim Solin	222
Semigroupoid Interfaces for Relation-Algebraic Programming in Haskell	235
On the Cardinality of Relations	251
Evaluating Sets of Search Points Using Relational Algebra	266
Algebraization of Hybrid Logic with Binders	281
Using Probabilistic Kleene Algebra for Protocol Verification	296
Monotone Predicate Transformers as Up-Closed Multirelations	311
Homomorphism and Isomorphism Theorems Generalized from a Relational Perspective	328
Relational Measures and Integration	343
A Relational View of Recurrence and Attractors in State Transition  Dynamics	358
On Two Dually Nondeterministic Refinement Algebras	373
On the Fixpoint Theory of Equality and Its Applications	388

	Table of Contents	XI
Monodic Tree Kleene Algebra		402
Weak Relational Products		417
Author Index		433