

# Lecture Notes in Computer Science

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## From Logic Design to Logic Programming

Theorem Proving Techniques and P-Functions

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