# Procedure-Level Verification of Real-time Concurrent Systems\*

Farn Wang Chia-Tien Lo

Institute of Information Science, Academia Sinica, Taipei, Taiwan 115, Republic of China +886-2-7883799 ext. 2420; FAX +886-2-7824814; farn@iis.sinica.edu.tw

Abstract. We want to develop verification techniques for real-time concurrent system specifications with high-level behavior structures. Nowadays, there is a big gap in between the classical verification theories and the engineering practice in real-world projects. This work identifies two common engineering guidelines respected in the development of realworld software projects, structured programming and local autonomy in concurrent systems, and experiments with special verification algorithm based on those engineering wisdoms. The algorithm we have adopted respects the integrity of program structures, treats each procedure as an entity instead of as a group of statements, allows local state space search to exploit the local autonomy in concurrent systems without calculating the Cartesian products of local state spaces, and derives from each procedure declaration characteristic information which can be utilized in the verification process anywhere the procedure is invoked. We have endeavored to implement our idea, test it against an abstract version of a real-world protocol in a mobile communication environment, and report the data.

### 1 Introduction

There is a great disparity between the engineering practice and the classical theories in verifying sophisticated computer systems. It is the goal of this work to investigate this disparity and experiment with verification techniques which combine the engineering wisdom with the classical verification theories.

Facing each nontrivial industrial problem human has encountered, there are in general two types of approaches used to surpass it and push the technology frontier forward. The first is engineering and the second is scientific. With the engineering approach, people strive to solve the problem using common wisdoms derived from their experiences in the field. With the scientific approach, people emphasize understanding the nature of the problem, by building mathematical models which simulate the problem, and design solution techniques based on

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the models. In the evolution of industry, these two approaches usually benefit from each other. On one hand, engineering wisdom reveals the true nature of the problem and inspires people to build better models. On the other hand, better understanding of the problem nature corroborates the engineering wisdom and may eventually lead to better solution.

As the computer systems we would like to build become more and more sophisticated, nowadays these two types of approaches are also employed in the task of system verification. On the engineering side, people have developed various engineering guidelines from their experience in the field and have been successful in constructing some really big real-world systems with complex highlevel behavior [28, 18, 30]. Examples of those successes include network layer communication protocols, software systems with abstract data types, parallel databases. On the theoretical side, basic mathematical models have been proposed to help people better understanding the intrinsic nature, e.g. complexities, of the problem [1, 4, 9, 10, 12, 14, 15, 25, 31]. Indeed, it has been reported that the advancement in the classical theory has led to the successful verification of several small real-world products, including physical layer communication protocols[7] and integrated circuit design[4, 23].

But ironically, if we look at the common guidelines respected by computer system engineers, we find that they are very hard to mechanize and really do not fit into the classical verification theories. For example, in building sophisticated system, people adopt the guideline of *structured programming* to structurally divide the design into smaller functional parts like procedures and loops and to refrain themselves from using arbitrary connection among the parts. But in the classical theories, basic models are usually assumed to be equivalent to random graphs. If there is a procedure, the standard treatment is just to use it as a macro expansion regardless of its functional integrity.

Another example of the disparity regards the practice in using clocks. For engineers, clocks sometimes serve as convenient devices in simplifying interaction among different threads in concurrent systems. Here is a hypothetical example. A gentleman named Mike drives his friend Frank to a shopping mall and tells Frank that he will come back to pick him up at 5pm. In this case the interaction gets simplified to a number, i.e. the deadline to meet. Both of them do not care what the other party plans to do before 5pm as long as the deadline is met. But from the viewpoint of the verification theory, clock is really not so pleasant a device because it always blows up the worst case complexities by an exponential factor. Also interestingly enough, even clock readings are intuitively numbers, the most, if not the only, used property of clock readings in real-time system verification theories is that if you increment a clock reading by noninfinitesimal amount for enough number of times, it will eventually be bigger than any given finite constant.

The third example of the disparity concerns with the way people use concurrency. In the design of sophisticated systems involving the interaction of several parties, it is the common engineering wisdom to localize the design consideration so that the reliability and safety of the whole systems can be derived from the verification of local properties of each party. But in the classical verification theory, calculation of Cartesian products of the local state spaces is usually adopted as the safe and complete technique. One exception is the composition and hiding operation proposed in process algebra [15, 25]. But still successful application to a real-world project with high-level behavior structure is yet to be observed.

This work integrates the two engineering guidelines cited in the above, i.e. structured programming and local autonomy in concurrent systems, into the design of verification algorithm which can be efficient in verifying well-designed computer systems. We target our research on real-time concurrent systems with timed atomic actions, synchronization primitives, procedures, loops, nondeterminism, and concurrency. A real-time system performs by giving out correct response at the correct moment. A concurrent system may allow several threads[11] (basic autonomous sequential executions) running concurrently. Recently, a theoretical framework for this purpose was proposed in [33] in which the verification complexities for both recursive and nonrecursive real-time concurrent systems are discussed and an algorithm is developed for the nonrecursive ones. One desirable feature of the algorithm is that it respects the procedure and loop structures of the systems by treating a rendezvousless execution of a procedure (loop) as a numerical entities, i.e. its execution time, which once analyzed, can be used in the verification process anywhere the procedure (loop) is invoked. Local autonomy of concurrent systems is utilized by a technique called timing coincidence analysis which determines the coincidibility of two states by telling if there are two synchronization-less local state sequences with the same execution time leading to the two states respectively. Such a technique enables us to construct global analysis from local state space search outcomes and is supposed to work well in systems with long autonomous executions and procedure invocations in between synchronization among the concurrent threads.

In this paper, we report the implementation of the algorithm proposed in [33]. However, we shall redesign the specification language to make it look like a traditional programming language. Several techniques to improve the averagecase performance of the algorithm are incorporated which make the analysis of an abstract version of a general session setting control protocol (GSSC) in a wireless communication environment feasible. First, some related work will be discussed in section 2. We then formally introduce our new specification language and review the complexity issues in section 3. The reachability analysis algorithm proposed in [33] is then rewritten to fit our specification language in section 4. The important techniques we employed in the implementation are discussed in section 5. GSSC is discussed in section 6 with the performance on the reachability analysis of two states, one consistent and one inconsistent, reported. Section 7 discusses some extension to the implementation on the way and some future work.

We shall adopt the following notations. Given a set or sequence K, |K| is the number of elements in K. We let  $\mathcal{N}$  be the set of nonnegative integers,  $\mathcal{Z}$  the set of integers,  $\mathcal{N}^{\{\infty\}} = \mathcal{N} \cup \{\infty\}$ , and  $\mathcal{N}^{\{*\}} = \mathcal{N} \cup \{*\}$ .

### 2 Related work

With the theoretical development of real-time and hybrid automata[1, 14, 21, 26, 27, 32] and the successful engineering of automated verification tools[2, 8, 4, 23], the research of computer-aided verification has received much attention. At this moment, various state-based [1, 4, 9, 10, 12, 14, 31] or event-based[20] model description languages are available, to which the standard verification technique of global space reachability analysis is usually applied. So far, several small real-world examples have been verified using this approach [4, 7, 23]. However such abstractions, although very elegant, may be at too low a level to make automatic verifiers efficiently uncover the behavior structures hidden in big system model descriptions.

Process algebra [15, 25] takes advantage of hiding and composition operators to construct complex systems from submodules. Since the verification algorithms for process algebra take care of general specifications without special program structure in mind, it may not be able to exploit the regularity of high-level behavior structure resulted from the observance of engineers to those guidelines.

People also use first-order logic or even higher-order logics to verify system designs. In those cases, very high-level behavior structures can be specified and verified[6, 13, 29]. For example, in [19], it was proposed to use positive cycles as intuitive refutation units in verifying real-time systems. The drawback is that the verification software can only do as much as proof checking and the engineers are pretty much left to their own. Still several remarkable benchmarks have been passed because of the industrious ingenuity of researchers in the community[6].

A good integration of engineering wisdom and scientific principles is formal methods in the line of VDM[18] and Z[30]. In that approach, a set of guidelines for system construction and a set of rules for verification are proposed and have been successfully applied in several real-world projects with benefits recorded. For example, in 1992, a Queen's Award of Britain was given to Oxford University Computing Laboratory and IBM UK Laboratories at Hursley Park for the development of IBM CICS using Z notation.

### 3 Real-time concurrent systems

#### 3.1 Syntax

The underlying concept of our approach is  $DAG_1^1$  procedure, defined in [33], which is a single-source single-destination directed acyclic graph in which each node represents a compound statement of procedure-call and atomic operation. Here we shall redefine  $DAG_1^1$  procedure in the concept of traditional programming languages. As in the traditional imperative languages, a  $DAG_1^1$  procedure is constructed from three types of statements, timed atomic, rendezvous, procedurecalling, and two types of statement structures, switch, concatenation. A timed atomic statement is executed with a prespecified earliest starting time and deadline. Unlike in Ada, here rendezvous is fulfilled by having all the participating parties executing the same rendezvous type at the same time. A procedure-call represents either a fixed or a nondeterministic number of sequential execution of a  $DAG_1^1$  procedure. A switch statement structure represents a nondeterministic choice, while a concatenation statement structure represents a successive execution of two statement structures. We use the following example to give intuition to the readers before the formal definition.

Example 1. In Figure 1, we illustrate three procedures, P, Q, R. P may loop nondeterministically many times to invoke R. Q invokes R also as the body of a 2-iteration loop.  $\sigma$  is a rendezvous type. An interval, like [4,9], represents a

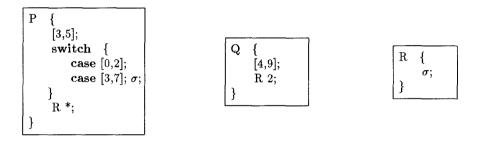


Fig. 1. Several simple procedures

timed atomic statement with the earliest starting times and deadlines.

**Definition 1 :**  $\mathbf{DAG}_1^1$  procedure. A  $\mathbf{DAG}_1^1$  procedure P is constructed from finite application of the following rules.

$$P ::= w\{B\}$$
  
$$B ::= [i, j]; \mid \sigma; \mid w_1n; \mid w_1*; \mid B_1B_2 \mid \mathbf{switch}\{\mathbf{case}B_1\mathbf{case}B_2 \dots \mathbf{case}B_n\}$$

Here  $w, w_1$  are procedure names (character strings) and  $B, B_1, B_2, B_n$  are statement structures.  $i \in \mathcal{N}, j \in \mathcal{N} \cup \{\infty\}$ , and n is a nonnegative integer.  $\sigma$  is a rendezvous type. Given  $P = w\{B\}$ , we shall use  $\overline{P}$  as the notation for the name w of P.

Given a set  $\Pi$  of DAG<sup>1</sup><sub>1</sub> procedures, we treat each statement position as the true identity of the corresponding statement. That is given two statement positions which both execute a syntactically identically statement (say a rendezvous " $\sigma_{;,}$ " or a procedure-calling " $\bar{P}n_{;}$ " or a timed atomic statement " $[i, j]_{;}$ "), we shall still treat these two positions as two different statements. Given a DAG<sup>1</sup><sub>1</sub> procedure P, we let  $S(\bar{P})$  be the set of statements used in P. We also define  $S_0(\bar{P})$  and  $S_f(\bar{P})$  to be the set of first and final statements in P respectively in the following.

- If  $\overline{P}{B}$  is defined, then  $S_0(\overline{P}) = S_0(B)$
- If B is a statement, then  $S_0(B) = \{B\}$ .
- $S_0(B_1B_2) = S_0(B_1).$

•  $S_0($ switch {case  $B_1 \dots$  case  $B_n$ }) =  $S_0(B_1) \cup \dots \cup S_0(B_n)$ Similarly, we have the following definition for  $S_f(\bar{P})$ .

- If  $\overline{P}{B}$  is defined, then  $S_f(\overline{P}) = S_f(B)$
- If B is a statement, then  $S_f(B) = \{B\}$ .
- $S_f(B_1B_2) = S_f(B_2).$

•  $S_f$ (switch {case  $B_1 \dots case B_n$ }) =  $S_f(B_1) \cup \dots \cup S_f(B_n)$ 

Given a concatenation statement structure  $B_1B_2$  in a DAG<sup>1</sup><sub>1</sub> procedure P, for each  $s_1 \in S_f(B_1)$  and  $s_2 \in S_0(B_2)$ , we call  $s_2$  a successor of  $s_1$ .

Notice that the looping in  $DAG_1^1$  procedures are restrained as a special type of procedure calls. Conceptually, a real-time concurrent system allows many threads running concurrently. By giving additional information on the starting statement of each thread and the participating parties of each rendezvous type, a set of procedure definitions can be grouped to define a real-time concurrent system.

**Definition 2 :** Real-time concurrent system. Given a set  $\Pi$  of DAG<sup>1</sup><sub>1</sub> procedures, we let  $\Sigma^{\Pi}$  be the set of rendezvous types used in procedures in  $\Pi$ . A real-time concurrent system is a tuple  $\langle \Pi, \Omega, \tau \rangle$  satisfying the following properties.

- $\Pi$  is a set of  $DAG_1^1$  procedure definitions such that for every procedure P defined in  $\Pi$ , any procedure referenced in P is also defined in  $\Pi$ .
- $\Omega$  is a sequence  $\langle \overline{P_1}, \ldots, \overline{P_m} \rangle$  of procedure names in  $\overline{\Pi}$  and declares the *m* threads in the system. For each  $1 \leq i \leq m$ , thread *i* starts by invoking  $P_i$ .
- $\tau : \Sigma^{\Pi} \mapsto 2^{\{1,\ldots,|\Omega|\}}$  defines the set of parties participating in each rendezvous. For each  $i \in \tau(\sigma)$ , thread *i* is expected to participate in each instance of rendezvous  $\sigma$ .

A real-time concurrent system is *recursive* iff its procedure-calls are recursive.

Example 2. Assume we have the four procedure definitions in example 1. Then  $R = \langle \{P, Q, R\}, \langle \bar{P}, \bar{Q} \rangle, \{\alpha \rightarrow \{1, 2\}\} \rangle$  is a legitimate nonrecursive and unambiguous real-time concurrent system.

### 3.2 An operational semantics for systems with single discrete clock

Given a real-time concurrent system with m threads, the *states* of the system can be described by an array of *local states* of the m threads. The procedure-calling scheme for the threads in our real-time concurrent systems resembles the pushpop operation of stacks[17] which have often been used as theoretical abstraction of nested procedure-callings. The *local state* of a thread can be conceptually recorded in a structure like the *control stack* (the name we shall adopt henceforth) in [3] and the *activation record* in [16, 34]. All possible executions of a thread from a moment can be deduced from the contents of the corresponding control stack.

Given a real-time concurrent system R, we let  $S^{\langle R \rangle}$  be the set of statements used in procedures defined in R. Given a thread local state (control stack)  $\Gamma$ represented as the following sequence bottom top  $(s_0, t_0)$   $(s_1, t_1)$   $(s_2, t_2)$  .....  $(s_{m-1}, t_{m-1})$   $(s_m, t_m)$ 

we let  $(s_0, t_0)$  and  $(s_m, t_m)$  be the *bottom* and *top* respectively of  $\Gamma$ . A control stack, say the above-mentioned  $\Gamma$ , must satisfy the following conditions.

- For each  $0 \leq i < m$ , either
  - for some P and n,  $s_i$  is a procedure-calling statement "Pn;" with  $0 \le t_i < n$ ; or
  - for some P,  $s_i$  is a procedure-calling statement " $\bar{P}*$ ," with  $t_i = 0$ .
- One of the following must be true for the top  $(s_m, t_m)$  of  $\Gamma$ .
  - $-s_m$  is a procedure-calling statement "Pn;" and  $0 \le t_m \le n$ .
  - $-s_m$  is a procedure-calling statement " $\bar{P}*$ ;" and  $t_m = 0$ .
  - $s_m$  is a timed atomic statement "[i, j];" and either  $0 \le t_m \le j \ne \infty$  or  $0 \le t_m \le i \lor t_m = j = \infty$ .
  - $-s_m$  is a rendezvous statement " $\sigma$ ;" and either  $t_m = 0$  or  $t_m = \sigma$ .

Given a control stack  $\Gamma$ , we let  $top(\Gamma)$  symbolically denote the top of  $\Gamma$ .  $\Gamma\gamma$  is a new control stack obtained by pushing  $\gamma$  into  $\Gamma$ .  $pop(\Gamma)$  is a new control stack obtained by popping the top element from  $\Gamma$ . Given  $top(\Gamma) = (s, t)$  with  $t, c \in \mathbb{Z}$ , we let  $\Gamma^{+c}$  be an abbreviation of  $pop(\Gamma)(s, t+c)$ , i.e. the local state obtained by incrementing the top counter value by c.

Suppose we are given a local state  $\Gamma = (s_0, t_0)(s_1, t_1) \dots (s_m, t_m)$ . For each  $0 \leq i \leq m$ , when  $s_i$  is a procedure-calling statement "Pn;," it means the thread is now in the middle of executing procedure P and is going to invoke P consecutively for  $|n - t_i|$  more times.

Similar to [17], we can define the succession of local states which follows the intuition of control stack evolution during procedure-calling and strongly matches the relation among paths in activation trees as discussed in [3]. However, for the convenience of our algorithm design, we shall present the following concept of local state successions.

**Definition 3 :** <u>Succession of thread local states</u>. The succession relation,  $\vdash$ , between local states are defined in the following way. Suppose we are given a local state  $\Gamma$  whose top is (s, t).

- Fixed-loop procedure-call : Suppose s is a procedure-calling statement " $\bar{P}n$ ;." If t < n, then for each  $s_0 \in S_0(\bar{P})$ ,  $\Gamma \vdash \Gamma^{+1}(s_0, 0)$ . If t = n, then for each successor statement s' of s,  $\Gamma \vdash \text{pop}(\Gamma)(s', 0)$ .
- \*-loop procedure-call : If s is a procedure-calling statement " $\bar{P}*;$ ," then for each  $s_0 \in S_0(\bar{P})$ ,  $\Gamma \vdash \Gamma(s_0, 0)$  and for each successor statement s' of s,  $\Gamma \vdash \text{pop}(\Gamma)(s', 0)$ .
- Return from procedure-call : When  $s \in S_f(\bar{P})$ , if one of the following three condition is true,
  - s is a timed statement "[i, j]" and  $i \le t \le j$ .
  - $-t = \sigma$  form some rendezvous type  $\sigma$ .
  - s is a procedure-calling statement " $\bar{Q}n$ ;" and t = n.
  - -s is a procedure-calling statement " $\bar{Q}*;$ ."
  - $\Gamma \vdash \operatorname{pop}(\Gamma)$

- Timed statement : Suppose s is a timed atomic statement "[i, j];."
  - If t < i, then  $\Gamma \vdash \Gamma^{+1}$ .
  - If  $i < t < j \neq \infty$ , then  $\Gamma \vdash \Gamma^{+1}$ .
  - If  $i < t < j = \infty$ , then  $\Gamma \vdash \text{pop}(\Gamma)(s, \infty)$ .
  - If i < t < j, then for each successor statement s' of s,  $\Gamma \vdash \text{pop}(\Gamma)(s', 0)$ .
  - Rendezvous statement : If s is a rendezvous statement and t = 0, then for each successor statement s' of s,  $\Gamma \vdash \text{pop}(\Gamma)(s, \sigma) \vdash \text{pop}(\Gamma)(s', 0)$ .

Based on the concept of local state succession, we are now ready to define the computation in multi-thread real-time concurrent systems.

**Definition4 : States and runs.** Suppose we are given a real-time concurrent system  $R = \langle \Pi, \Omega, \tau \rangle$ . A state of R is a sequence of  $|\Omega|$  local states. A finite sequence  $(\Delta_0, g_0)(\Delta_1, g_1) \dots (\Delta_m, g_m)$  is called a  $\Delta_0$ -run of R, where for each  $0 \leq k \leq m, \Delta_k$  is a state and  $g_k \in \{0,1\}$  indicates the presence of a global clock tick. Assume, for each  $0 \le k \le m$ ,  $\Delta_k = \langle \Gamma_k^{(1)}, \ldots, \Gamma_k^{(n)} \rangle$ . The following requirements are imposed on a  $\Delta_0$ -run.

- For each  $0 \le k < m$  and  $1 \le i \le n$ , either  $\Gamma_k^{(i)} \to \Gamma_{k+1}^{(i)}$  or  $\Gamma_k^{(i)} = \Gamma_{k+1}^{(i)}$ . Enforcement of synchrony to global clock : For each  $0 \le k < m, g_k =$ 1 iff every thread increments its time reading by 1, that is for each  $1 \le i \le n$ such that  $\operatorname{top}(\Gamma_k^{(i)}) = (s,t)$  and  $\operatorname{top}(\Gamma_{k+1}^{(i)}) = (s',t')$ , s = s' and either t+1 = t' or  $t = t' = \infty$ .
- Enforcement of rendezvous : For each  $\sigma \in \Sigma^{\Pi}$  and each  $0 \leq k \leq m$ , if  $\operatorname{top}(\Gamma_k^{(i)}) = (s, \sigma)$  for some s and  $i \in \tau(\sigma)$ , then for each  $\overline{j} \in \tau(\sigma)$ ,  $top(\Gamma_k^{(j)}) = (s', \sigma)$  for some s'.

Given a state  $\Delta$  and a  $\Delta$ -run  $\Psi = (\Delta_0, g_0)(\Delta_1, g_1) \dots (\Delta_m, g_m)$ , for each  $0 \leq k \leq$ m, the time of the k-th state in  $\Psi$ , in symbols  $time_{\Psi}(k)$ , is defined inductively by two cases : (1)  $time_{\Psi}(0) = 0$ . (2) For each  $0 \le k < m$ ,  $time_{\Psi}(k+1) =$  $time_{\Psi}(k) + g_k$ . 

Example 3. Assume that we have the real-time concurrent system in example 2. It can be seen that while thread 1 may loop nondeterministically many times, thread 2 terminates after executing two instances of rendezvous  $\alpha$ . Thus the whole system only has runs with two rendezvous instances.

#### 3.3Complexities of reachability analysis

We shall introduce a basic version of the reachability problem here. Such a version is instrumental in constructing other interesting versions.

**Definition 5** : State reachability. Given a real-time concurrent system R = $\langle \Pi, \Omega, \tau \rangle$ , a state  $\Delta'$  is said reachable from another state  $\Delta$  in R iff there is a  $\Delta$ -run  $(\Delta_0, g_0)(\Delta_1, g_1) \dots (\Delta_m, g_m)$  such that  $\Delta' = \Delta_m$ .

The reachability problem in our real-time concurrent systems can then be formulated in the following way. Given a real-time concurrent system R and two of its states  $\Delta, \Delta'$ , the corresponding state reachability problem instance asks if  $\Delta'$  is reachable from  $\Delta$  in R. We cite the following theorem and lemmas from [33] to show the complexities of the problem for recursive and nonrecursive systems.

**Theorem 6.** Two-counter machine halting problem[22] is reducible to the reachability problem of real-time concurrent systems.

**Lemma 7.** QBF[17] is reducible in PTIME to the state reachability problem for nonrecursive real-time concurrent systems.

**Lemma 8.** The state reachability problem of nonrecursive real-time concurrent systems is in PSPACE.

### 4 Reachability analysis for nonrecursive systems

Our algorithm will be presented in two steps. First, we shall give a skeleton view of the algorithm in subsection 4.1 in which the implementation of one particular code line is not detailed. The skeleton describes how we exploit the autonomy of each thread in between hitting rendezvous to reduce the size of state space. Second, details about that one code line will be supplemented in subsection 4.2 and 4.3.

### 4.1 Skeleton view of the algorithm

We formalize the concept of thread autonomy in between hitting rendezvous with the following definition.

**Definition 9 :** Successor through rendezvous-less run. Given a real-time concurrent system R, and two states  $\Delta$  and  $\Delta'$ , we say  $\Delta'$  is a successor through rendezvous-less run (or  $\neg r$ -successor) of  $\Delta$  iff there is a finite  $\Delta$ -run  $\Psi = (\Delta_0, g_0) \dots (\Delta_m, g_m)$  of R such that

- $\Psi$  ends at  $\Delta'$ , i.e.  $\Delta' = \Delta_m$ ; and
- for each 0 < k < m,  $\Delta_k$  does not mark the completion of a rendezvous, that is, assuming  $\Delta_k = \langle \Gamma_k^{(1)}, \ldots, \Gamma_k^{(n)} \rangle$ , for each  $1 \le i \le n$ , there is no  $\sigma \in \Sigma^{\Pi}$ s.t.  $\operatorname{top}(\Gamma_k^{(i)}) = (s, \sigma)$  for some s.

In between hitting rendezvous, each thread executes in an independent way. We say a state  $\langle \Gamma^{(1)}, \ldots, \Gamma^{(n)} \rangle$  is at the stage of completion of rendezvous  $\sigma$  iff for some  $1 \leq i \leq n, s$ ,  $\operatorname{top}(\Gamma^{(i)}) = (s, \sigma)$ . A major source of efficiency of our algorithm comes from the fact that we only work with states which are at the completion stage of rendezvous. The algorithm in table 1 takes this characteristic of real-time concurrent systems into consideration to answer instances of state reachability problem. Succession relation among such states is figured out by manipulation of arithmetic set expressions as defined in subsection 4.2 The correctness of procedure Reachable() has been proven in [33] and restated in the following lemma.

**Lemma 10.** Given two states  $\Delta$ ,  $\Delta'$  of a nonrecursive real-time systems R, with the oracle for  $\neg r$ -successorship,  $\Delta'$  is reachable from  $\Delta$  in R iff Reachable( $R, \Delta, \Delta'$ ) is TRUE.

Reachable(R, Δ, Δ')
/\* R = ⟨II, Ω, τ⟩, is a nonrecursive real-time concurrent system. \*/ {

(1) Generate the set X of all states in which a rendezvous is at the stage of completion.
(2) Determine the pairwise ¬r-successor relation in X ∪ {Δ, Δ'} and call it Y.
(3) If Δ' is reachable from Δ in (X ∪ {Δ, Δ'}, Y), answer TRUE; else answer FALSE.

Table 1. Algorithm for state reachability problem

All but the second code line in table 1 are obvious. In subsection 4.2, we shall introduce arithmetic set expressions, as the abstraction tool used to construct a solution for the second code line. In subsection 4.3, we shall use the technique of timing coincidibility analysis to determine the  $\neg r$ -successor relation between two states.

#### 4.2 Arithmetic set expressions and their operations

The transitions in our system models are carried out within intervals bounded by earliest starting times and deadlines. Since earliest starting times, and deadlines alike, of a sequence of consecutive transitions can be accumulated during the analysis of thread behavior, it is natural to define the addition and integer multiplication of integer intervals. And indeed our reachability analysis algorithm is presented based on this kind of arithmetic set operations.

Our arithmetic set expression is constructed by the following rules.

$$H ::= \{c\} \mid H_1 \cup H_2 \mid H_1 \cap H_2 \mid H_1 + H_2 \mid H_1k \mid H_1*$$

c, k are natural numbers.  $\{c_1, \ldots, c_n\}$  is a shorthand for  $\{c_1\} \cup \ldots \cup \{c_n\}$ . Conceptually, we treat an integer interval [a, b) as a shorthand for the set  $\{a, a + 1, \ldots, b - 1\}$ . Especially,  $[a, \infty)$  is a shorthand for  $\{a\} + \{1\}^*$ . The meaning of these set expression is inductively given in the following.

- Case  $H = \{c\}$ , H is the set of integer c.
- Case  $H = H_1 \cup H_2$   $(H = H_1 \cap H_2)$ , H is the union (intersection) of  $H_1$  and  $H_2$ .
- Case  $H = H_1 + H_2$ ,  $H = \{a + b \mid a \in H_1; b \in H_2\}$ .
- Case  $H = H_1 k$ , (1) when k = 0, then  $H = \{0\}$ ; (2) otherwise  $H = H_1(k 1) + H_1$ .
- Case  $H = H_1 *$ ,  $H = \bigcup_{k>0} H_1 k$ .

Note  $\emptyset$  acts as a nullifier in arithmetic set addition, i.e. for all integer set expression H,  $H + \emptyset = \emptyset$ . Also, we allow distribution of addition against union and intersection.

An arithmetic set expression H is said to be in *periodical normal form (PNF)* iff  $H = \bigcup_{1 \le i \le m} (\{a_i\} + \{c_i\}*)$ . In the following, we give a set of rewriting rules to transform arithmetic set expressions into PNF arithmetic set expressions. 1)  $\left(\bigcup_{1 \le i \le m} (\{a_i\} + \{c_i\}*)\right) \cap \left(\bigcup_{1 \le j \le n} (\{b_j\} + \{d_j\}*)\right)$ 

$$= \bigcup_{1 \le i \le m; 1 \le j \le n} K_{\cap}(\{a_i\} + \{c_i\} *, \{b_j\} + \{d_j\} *)$$
where  $K_{\cap}(\{a\} + \{c\} *, \{b\} + \{d\} *)$  is defined by the following two cases.  
- If there is no integer solution  $i, j$  to  $a + ci = b + dj$ ,  
then  $K_{\cap}(\{a\} + \{c\} *, \{b\} + \{d\}) = \emptyset$   
- Otherwise, let  $\overline{i}, \overline{j}$  be the minimum integer solution.  
 $K_{\cap}(\{a\} + \{c\} *, \{b\} + \{d\} *) = \{a + c\overline{i}\} + \{\operatorname{lcm}(c, d)\} *$   
2)  $\left(\bigcup_{1 \le i \le m} (\{a_i\} + \{c_i\} *)\right) + \left(\bigcup_{1 \le j \le n} (\{b_j\} + \{d_j\} *)\right)$   
 $= \bigcup_{1 \le i \le m; 1 \le j \le n} \left( \{a_i + b_j + \operatorname{lcm}(c_i, d_j)\} + \{\operatorname{gcd}(c_i, d_j)\} *)$   
 $= \bigcup_{1 \le i \le m; 1 \le j \le n} \left( \bigcup_{\{a_i + b_j + c_ih + d_jk \mid h, k \in \mathcal{N}; c_ih + d_jk < \operatorname{lcm}(c_i, d_j)\}} \right)$   
3)  $\left(\bigcup_{1 \le i \le m} (\{a_i\} + \{c_i\} *)\right) k$   
 $= \begin{cases} \{0\} & \text{if } k = 0 \\ \left(\bigcup_{1 \le i \le m} (\{a_i\} + \{c_i\} *)\right) (k - 1) + \bigcup_{1 \le i \le m} (\{a_i\} + \{c_i\} *) \text{ if } k > 0 \end{cases}$   
After application of the rule, rule 2 should be used immediately.

4) 
$$\left(\bigcup_{1 \le i \le m} \{\{a_i\} + \{c_i\}\}\right) * = \sum_{1 \le i \le m} (\{a_i\} * + \{c_i\}*)$$
  
After application of the rule, rule 2 and distribution of addition against  
unions should be used iteratively to transform the formula to its PNF.

#### 4.3 Timing coincidibility analysis

The technique of timing coincidibility analysis is based on the following observation. Given two concurrent threads starting their execution simultaneously, after running without interaction (rendezvous) for t time units according to the global clock, they may get to local states  $\Gamma, \Gamma'$  respectively. Then due to the strong synchrony in global clock systems, we can conclude that  $\Gamma, \Gamma'$  may happen at the same time during the two threads rendezvous-less executions respectively. This implies that we can separately work with the subtasks of searching in the local state space of each thread while analyzing the reachability between states. By figuring out the general time patterns between pairs of local states in the local state spaces, we can tell the  $\neg r$ -successor relations by intersecting those time representations. In this approach, time representations are often very concise since it tends to ignore the difference among different state sequences as long as they have the same time values.

The following definition formalizes the concept of local state space search.

**Definition 11 :** Local state sequence. Given a real-time concurrent system  $R = \langle \Pi, \Omega, \tau \rangle$ , a finite local state sequence  $\Phi = \Gamma_0 \Gamma_1 \dots \Gamma_m$ , with  $\Gamma_k \vdash \Gamma_{k+1}$  for each  $0 \leq k < m$ , defines a legitimate thread execution in R from  $\Gamma_0$  and is called a  $\Gamma_0$ -sequence.  $\Phi$  is rendezvous-less iff for every 0 < k < m,  $\Gamma_k$  is not at the completion stage of a rendezvous, i.e.  $\forall \sigma \in \Sigma^H \forall s(\operatorname{top}(\Gamma_k) \neq (s, \sigma))$ .

**Definition 12 :** <u>Rendezvous-less time expressions</u>. Given a DAG<sub>1</sub><sup>1</sup> procedure  $\bar{P}\{B\}$ , the *rendezvous-less time expression* of  $\bar{P}$ ,  $texp_{\neg r}(\bar{P})$ , is defined inductively as follows.

- then  $texp_{\neg r}(\bar{P}) = texp_{\neg r}(B)$ .
- $texp_{\neg r}([i, j];) = [i, j]$
- $texp_{\neg r}(\sigma) = \emptyset$
- $texp_{\neg r}(\bar{P_1}n;) = (texp_{\neg r}(\bar{P_1}))n$
- $texp_{\neg r}(\bar{P}_{1}*;) = (texp_{\neg r}(\bar{P}_{1}))*$
- $texp_{\neg r}(B_1B_2) = texp_{\neg r}(B_1) + texp_{\neg r}(B_2)$
- $texp_{\neg r}(switch\{caseB_1...caseB_n\}) = texp_{\neg r}(B_1) \cup ... \cup texp_{\neg r}(B_n)$

Suppose we are given a finite rendezvous-less local state sequence  $\Phi = \Gamma_0 \dots \Gamma_m$ with  $top(\Gamma_i) = (s_i, t_i)$  for each  $0 \leq i \leq m$ . We conveniently let  $terp_{\neg r}(\Phi)$  equal to

$$\sum_{0 \le i < m; s_i = [i, j]; 0 \le t_i \neq \infty; 0 \le t_{i+1} \neq \infty} (t_{i+1} - t_i) + \delta_{\varPhi} * + \sum_{0 \le i < m; s_i = "} (\bar{Q}_{*;"}((texp_{\neg r}(\bar{Q})))) * )$$

be our notation for the time expression for rendezvous-less local state sequence  $\Phi$ . Here  $\delta_{\Phi}$  is  $\{1\}$  when  $\exists 0 \leq i \leq m(t_i = \infty)$ ;  $\{0\}$  otherwise. Also we let

$$texp_{\neg r}(\Gamma, \Gamma') =$$

 $\bigcup_{(\Phi \text{ is a finite simple rendezvous-less } \Gamma \text{-sequence of } R \text{ ends at } \Gamma')} texp_{\neg r}(\Phi)$ 

where "simple" means no two local states are the same.

The execution times of all rendezvous-less execution sequences between two local states can be figured out by doing some arithmetic on time expressions. The meaning of the time expression is given by the following lemma proven in [33].

**Lemma 13.** Given two local states  $\Gamma, \Gamma'$  of a nonrecursive real-time concurrent system, there is a rendezvous-less execution sequence of time t from  $\Gamma$  to  $\Gamma'$  iff  $t \in \operatorname{texp}_{\neg r}(\Gamma, \Gamma')$  which is computable.

With definition 11, 12, and lemma 13, we have made the concept of autonomous execution of a single thread precise and proven our derivation of rendezvous-less thread execution time expression correct. Now all these can be readily combined to prove the correctness of the technique of timing coincidibility analysis.

**Lemma 14.** Given  $t \in \mathcal{N}$  and two states of a nonrecursive real-time concurrent system  $R, \Delta = \langle \Gamma^{(1)}, \ldots, \Gamma^{(n)} \rangle$  and  $\Delta' = \langle \Gamma'^{(1)}, \ldots, \Gamma'^{(n)} \rangle$ ,  $\Delta'$  is a successor of  $\Delta$  through rendezvous-less run of t time units in R iff  $t \in \bigcap_{1 \leq i < n} \operatorname{texp}_{\neg r}(\Gamma^{(i)}, \Gamma'^{(i)})$ 

Proof. According to definition 9, 11, 12, and lemma 13.

### 5 Implementation techniques

We have employed several techniques to take advantage of the behavior structure of procedure-callings and local autonomy to make the reachability analysis more efficient. As we have observed, such techniques are valuable and often result in orders of magnitude in verification performance improvement.

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#### 5.1 Nonpeak execution path

Given a stack  $\Gamma$ , remember that we use  $|\Gamma|$  to denote the height of  $\Gamma$ . A local state sequence  $\Gamma_0\Gamma_1\ldots\Gamma_m$  is called a peak local state sequence iff there are integers i, j, k with  $0 \le i < j < k \le m$  such that  $|\Gamma_i| < |\Gamma_j|$  and  $|\Gamma_j| > |\Gamma_k|$ .

In an interval of the rendezvous-less execution of a thread, a peak in its execution sequence represents a procedure-call which does not incur any rendezvous. The effect of the rendezvous-less procedure-call can be treated as purely numerical values, i.e. its rendezvous-less time expressions. Thus we introduce the following new concept of local state succession involving encapsulated procedurecalls.

**Definition 15** Successors of local states with encapsulated procedure-call. If s is a procedure-calling statement " $\overline{P}n$ ," with t < n, then for each  $1 \le c \le n-t$ ,  $\Gamma \vdash \Gamma^{+c}$ .

We have observed that while calculating the rendezvous-less time expressions between two local states, we only have to consider nonpeak path. While calculating the time expression of a rendezvousless local state sequence  $\Phi$  between two local states, if we find out that two consecutive local states along  $\Phi$  are connected by the above-defined successor relations, we shall include  $(texp_{\neg r}(\bar{P}))c$  in  $texp_{\neg r}(\Phi)$ .

#### 5.2 Starting timed atomic local states

While computing the time expression of rendezvousless local state sequence, we ignore those local states which mark the execution in the middle of timed atomic statements. That is we can ignore all local states  $\Gamma$  with  $top(\Gamma) = (s, t)$ , s = [i, j]; and  $t \neq 0$  by introducing the following new local state successor relationship.

#### Definition 16 Successors from starting timed atomic local states.

If  $top(\Gamma) = (\overline{s, 0})$  and s is a timed statement [i, j]; then for each successor statement s' of  $s, \Gamma \vdash pop(\Gamma)(s', 0)$ .

Suppose we are given a rendezvousless local state sequence  $\Phi = \Gamma_0 \dots \Gamma_m$ , if  $\operatorname{top}(\Gamma_0) = (s,t)$  and  $\operatorname{top}(\Gamma_m) = (s',t')$  with  $s = [i,j];, s' = [i',j'];, t \neq 0$ , and  $t' \neq 0$ . Let  $\overline{\Phi}$  be the local state sequence identical to  $\Phi$  except that

- $\overline{\Phi}$  starts t time units earlier than  $\Phi$  in s; and
- $\overline{\Phi}$  ends t' time units earlier than  $\Phi$  in s'.

Then we can compute  $texp_{\neg r}(\Phi)$  to be  $texp_{\neg r}(\bar{\Phi}) - [t,t] + [t',t']$ . Note however that our original time expression definition does not deal with subtraction. But since we always reduce time expression to PNF, a time expression like [a, b] + [c, c] \* -[t, t] is equivalent to [a + cg - t, b + cg - t] + [c, c] \* where g is the smallest integer solution for x to  $a + cx \geq t$ .

#### 5.3 Local state space segmentation

Given a real-time concurrent system with m threads, a naive approach in calculating states is to calculate all the Cartesian products of m local states. This usually results in huge number of pseudo states most of which can never be reached from the system initial state. The trick we use in the implementation is to segment the local state space of each thread by rendezvous local states. Thus given a state  $\Delta = \langle \Gamma_1, \ldots, \Gamma_m \rangle$ , while calculating the states reachable from  $\Delta$ through rendezvous-less runs, we only compute the Cartesian product of the local state subspaces  $K_1, \ldots, K_m$  defined in the following way. For each  $1 \leq i \leq m$ , if  $\Gamma_i$  is a rendezvous local state, then  $K_i$  is the next segment reachable from local states in the segment where  $\Gamma_i$  is in. Otherwise it is the present segment where  $\Gamma_i$  is in.

### 6 General Session Setup Control protocol

We have tested our implementation against an abstract version of a real-world project which deals with the communication link setup in a mobile phone environment. The test example GSSC comes from the Wireless Communication Department, Computer & Communication Research Laboratories, Industrial Technology Research Institute, Taiwan, ROC. It deals with setting up and later releasing a communication channel between a client and a server. Five threads are involved in the system, the client, the system service for client (SS\_C), the line control unit (LCU), the system service form server (SS\_S), and the server. The protocol must take care of communication failure incurred by, e.g. timeout, server busy, .....

In our experiment, we test two cases, one for the reachability of an inconsistent states and one for that of a consistent one. We thus give a brief description to all these five threads. After this, we shall then present part of the protocol in our description language.

- Reaction sequence from the client's viewpoint :
  - 1) The client starts the whole session by sending an SS\_SETUP\_req message to SS\_C.
  - 2) If an SS\_RELEASE\_ind message is received from SS\_C, quit the session. If an SS\_FACILITY\_ind message is received, send an SS\_FACILITY\_req message to SS\_C to request for the facility and wait for further response from SS\_C.
  - 3) If an SS\_RELEASE\_ind message is received from SS\_C, quit the session. If an SS\_FACILITY\_ind message is received, then send an SS\_RELEASE\_req message to release the resources and quit.
- Reaction sequence from SS\_C's viewpoint :
  - 1) When an SS\_SETUP\_req message is received from the client, send an LCU\_DATA\_req message with identifier 4 to LCU and starts a timer which timeouts at 10 time units later.

2) If an LCU\_RELEASE\_ind message is received from LCU within 10 time units, send an SS\_RELEASE\_ind message to the client and quit the session.

If a timeout occurs, send an SS\_RELEASE\_ind message to the client and an LCU\_RELEASE\_req message with identifier 4 to LCU to quit the session.

If an LCU\_DATA\_ind message is received from LCU within 10 time units, send an SS\_FACILITY\_ind message back to the client and wait for its further response.

3) If an SS\_RELEASE\_req message is received from the client, send an LCU\_RELEASE\_req message with identifier 4 to LCU to quit.

If an SS\_FACILITY\_req message is received from the client, send an LCU\_DATA\_req message with identifier 4 to LCU and starts a timer which timeouts at 10 time units later.

4) If an LCU\_RELEASE\_ind message is received from LCU within 10 time units, send an SS\_RELEASE\_ind message to the client and quit.

If a timeout occurs, send an SS\_RELEASE\_ind message to the client and an LCU\_RELEASE\_req message with identifier 4 to LCU to quit the session.

If an LCU\_DATA ind message is received from LCU within 10 time units, send an SS\_FACILITY ind message back to the client and wait for its further response.

- 5) Upon the reception of an SS\_RELEASE\_req message from the client, send an LCU\_RELEASE\_req message with identifier 4 to LCU to quit the session.
- Reaction sequence from LCU's viewpoint :
  - 1) If an LCU\_DATA\_req message is received with identifier 4, send an LCU\_DATA\_ind message to SS\_S. Go back to initial state.
  - 2) If an LCU\_DATA\_req message is received with identifier 132, send an LCU\_DATA\_ind message to SS\_C. Go back to initial state.
  - 3) If an LCU\_RELEASE\_req message is received with identifier 4, send an LCU\_RELEASE\_ind message to SS\_S. Go back to initial state.
  - 4) If an LCU\_RELEASE\_req message is received with identifier 132, send an LCU\_RELEASE\_ind message to SS\_C. Go back to initial state.
- Reaction sequence from SS\_S's viewpoint :
  - 1) When an LCU\_DATA\_ind message is received from LCU, if it is an SS\_START message, then send an SS\_SETUP\_ind message to the server and wait its response; otherwise quit.
  - 2) If an SS\_RELEASE\_req message is received from the server, send an LCU\_RELEASE\_req message with identifier 132 to LCU to quit. If an SS\_FACILITY\_req message is received from the server, send an LCU\_DATA\_req message with identifier 132 to LCU and starts a timer which timeouts at 10 time units later.
  - 3) If an LCU\_RELEASE\_ind message is received from LCU within 10 time units, send an SS\_RELEASE\_ind message back to the server and quit.

If a timeout occurs, send an SS\_RELEASE\_ind message to the server and an LCU\_RELEASE\_req message with identifier 132 to LCU to quit. If an LCU\_DATA\_ind message is received from the LCU within 10 time units, send an SS\_FACILITY\_ind message to the server and wait for its further response.

- 4) If an SS\_RELEASE\_req message is received from the server, then send an LCU\_RELEASE\_req message with identifier 132 to LCU to quit. If an SS\_FACILITY\_req message is received from the server, send an LCU\_DATA\_req message with identifier 132 to LCU and starts a timer which timeouts at 10 time units later.
- 5) If an LCU\_RELEASE\_ind message is received from LCU within 10 time units, send an SS\_RELEASE\_ind message back to the client and quit the session.
- 6) If a timeout happens, send an SS\_RELEASE\_ind message to the server and an LCU\_RELEASE\_req message with identifier 132 to LCU to quit.
- Reaction sequence from the server's viewpoint :
  - 1) Upon receipt of an SS\_SETUP\_ind message from SS\_S, the server either sends an SS\_RELEASE\_req message back to SS\_S if the service is not available and goes back to the initial state, or sends an SS\_FACILITY\_req message to SS\_S to notify that the service is available and waits for further response from SS\_S.
  - 2) Upon receipt of the an SS\_RELEASE message, the server knows that the the service is no longer needed and go back to the initial state. On the other hand, if an SS\_FACILITY\_ind message is received from SS\_S, the server may either send an SS\_RELEASE\_req message to SS\_S in case the server has to abort the service, or an SS\_FACILITY\_req message to provide the service and wait for further response from SS\_S.
  - 3) Upon receipt of the an SS\_RELEASE message, the server knows that the the service has completed and goes back to the initial state.

In our specification, we treat each message as a rendezvous. Message to and from LCU with different identifiers are also treated as of different message types for convenience. Messages between the client and SS\_C all begin with prefix SS\_C\_. Messages between the server and SS\_S all begin with prefix SS\_S\_. In table 2 and 3. we list our specifications for thread LCU, and SS\_C. Because of page limit, we shall not present the specification for the client, SS\_S, and the server. Also in table 4, we list the thread and rendezvous type declaration.

We have performed two reachability analyses. One is for an unreachable state which says that the server has aborted the service while the client is still using the service. The total number of states generated is 3675 and the CPU time is 5075 seconds on a Sparc 10 clone.

The second is for a reachable state which says that the client is using the service provided by the server. The total number of states generated is 3676 and the CPU time is 6649 seconds on a Spare 10 clone.

```
/* Line Control Unit */
LCU {
    LCU_body *;
ł
LCU_body {
    [0,\infty]; /* NULL */
    switch {
        case LCU_DATA_reg_132;
                                  /* LCU_DATA_req */
             LCU_DATA_ind_132;
        case LCU_DATA_req_4; /* LCU_DATA_req */
             LCU_DATA_ind_4:
        case LCU_RELEASE_req_4;
             LCU_RELEASE_ind_4; /* LCU_RELEASE_ind */
        case LCU_RELEASE_req_132;
             LCU_RELEASE_ind_132; /* LCU_RELEASE_ind */
    }
}
```

Table 2. Thread LCU, Line Control Unit

### 7 The challenge ahead

It is easy to see that given an unstructured real-time system specification, its timing behavior structure can be horribly difficult to analyze. But this kind of input assumption usually contradicts the common practice of structured programming in software engineering, the high-level semantics of programming languages, and the design rules in real-time systems. We advocate procedure-level model descriptions and verifications for real-time concurrent systems for their potentially better average-case performance in automated verification. At the current stage, we have implemented an verification system which respects and utilizes the highlevel behavior structures demonstrated in the program structures and local autonomy of real-time concurrent system specifications. An abstract version of a real-world protocol is tested with performance reported. However, we are still looking for test examples which exhibit more program structures like nested procedure-calling.

The concept of statements with earliest starting times and deadlines was also adopted in formal frameworks like [20, 24]. Special techniques for reachability analysis has also been reported under this kind of framework[20, 5]. However, we do not know if there is any previous formal framework for real-time concurrent systems aimed at taking advantage of local autonomy and program structures to improve the verification performance.

```
/* Supplementary Service A */
/* Any service request to LCU is with identifier 4 */
SS_C {
    SS_C_body *;
ł
SS_C_body {
    [0,\infty]; /* NULL */
    SS_C_SETUP_req:
    [0,0]; /* PD_TI := 4 */
    LCU_DATA_req_4:
    [0,0]; /* set timer = 10; Initiated */
    switch {
          [0,10]; LCU_RELEASE_ind_132; SS_C_RELEASE_ind;
    case
    case [0,10]; LCU_DATA_ind_132; SS_C_FACILITY_ind; [0,\infty];
          switch {
          case SS_C_RELEASE_req;
                [0,0]; /* PD_TI := 4 */
                LCU_RELEASE_req_4;
          case SS_C_FACILITY_req;
                [0,0]; /* PD_TI := 4 */
                LCU_DATA_req_4;
                [0,0]; /* set timer = 10 */
                switch
                       ſ
                case
                      [0,10]; LCU_RELEASE_ind_132; SS_C_RELEASE_ind;
                case
                      [0,10]; LCU_DATA_ind_132; SS_C_FACILITY_ind;
                      [0,\infty]; SS_C_RELEASE_req;
                      [0,0]; /* PD_TI := 4 */
                      LCU_RELEASE_reg_4;
                      [10,10]; SS_C_RELEASE_ind; LCU_RELEASE_req_4;
                case
                }
          3
    case [10,10]; [0,0]; SS_C_RELEASE_ind; LCU_RELEASE_reg_4;
    }
}
```

```
Table 3. Thread SS_C, System Service for the Client
```

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We thanks Professor Clarke and his crew at CMU for offering SMV[4, 23], which were used in our reachability analysis part of our implementation, and the associated technical advice. SMV is used as a routine for calculating the transitive closure in the rendezvous state graph in table 1.

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/\*=Thread description== <C, SS\_C, LCU, SS\_S, S> /\*=Rendezvous description=== /\* Between SS\_C and LCU \*/  $LCU_DATA_req_4 : 1,2;$ LCU\_RELEASE\_reg\_4 : 1,2; LCU\_DATA\_ind\_132 : 1,2; LCU\_RELEASE\_ind\_132 : 1,2; /\* Between Client and SS\_C \*/ SS\_A\_SETUP\_req : 0,1; SS\_A\_RELEASE\_ind : 0,1; SS\_A\_FACILITY\_ind : 0,1; SS\_A\_RELEASE reg : 0.1: SS\_A\_FACILITY\_req : 0,1; /\* Between SS\_S and LCU \*/ LCU\_RELEASE\_reg\_132 : 2,3; LCU\_DATA\_reg\_132 : 2.3: LCU\_RELEASE\_ind\_4 : 2,3;  $LCU_DATA_ind_4 : 2,3;$ /\* Between Server and SS\_S \*/ SS\_B\_SETUP\_ind : 3,4; SS\_B\_RELEASE\_req : 3,4; SS\_B\_FACILITY\_req : 3,4; SS\_B\_RELEASE\_ind : 3,4; SS\_B\_FACILITY\_ind: 3,4;

Table 4. Thread and rendezvous type declaration

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