

## Editors

Professor Dr.-Ing. Manfred Thoma

Institut fuer Regelungstechnik, Universität Hannover, Appelstr. 11, 30167 Hannover,  
Germany

E-mail: thoma@irt.uni-hannover.de

Professor Dr. Frank Allgöwer

Institute for Systems Theory and Automatic Control, University of Stuttgart,  
Pfaffenwaldring 9, 70550 Stuttgart, Germany  
E-mail: allgower@ist.uni-stuttgart.de

Professor Dr. Manfred Morari

ETH/ETL I 29, Physikstr. 3, 8092 Zürich, Switzerland

E-mail: morari@aut.ee.ethz.ch

## Series Advisory Board

P. Fleming

University of Sheffield, UK

P. Kokotovic

University of California, Santa Barbara, CA, USA

A.B. Kurzhanski

Moscow State University, Russia

H. Kwakernaak

University of Twente, Enschede, The Netherlands

A. Rantzer

Lund Institute of Technology, Sweden

J.N. Tsitsiklis

MIT, Cambridge, MA, USA

For further volumes:

<http://www.springer.com/series/642>

Carla Seatzu, Manuel Silva,  
and Jan H. van Schuppen (Eds.)

---

# Control of Discrete-Event Systems

Automata and Petri Net Perspectives



*Editors*

Carla Seatzu  
Department of Electrical  
and Electronic Engineering  
University of Cagliari  
Cagliari  
Italy

Jan H. van Schuppen  
Centrum Wiskunde & Informatica  
Amsterdam  
The Netherlands

Manuel Silva  
Department of Computer Science  
and Systems Engineering  
University of Zaragoza  
Zaragoza  
Spain

ISSN 0170-8643  
ISBN 978-1-4471-4275-1  
DOI 10.1007/978-1-4471-4276-8  
Springer London Heidelberg New York Dordrecht

e-ISSN 1610-7411  
e-ISBN 978-1-4471-4276-8

Library of Congress Control Number: 2012941741

© Springer-Verlag London 2013

This work is subject to copyright. All rights are reserved by the Publisher, whether the whole or part of the material is concerned, specifically the rights of translation, reprinting, reuse of illustrations, recitation, broadcasting, reproduction on microfilms or in any other physical way, and transmission or information storage and retrieval, electronic adaptation, computer software, or by similar or dissimilar methodology now known or hereafter developed. Exempted from this legal reservation are brief excerpts in connection with reviews or scholarly analysis or material supplied specifically for the purpose of being entered and executed on a computer system, for exclusive use by the purchaser of the work. Duplication of this publication or parts thereof is permitted only under the provisions of the Copyright Law of the Publisher's location, in its current version, and permission for use must always be obtained from Springer. Permissions for use may be obtained through RightsLink at the Copyright Clearance Center. Violations are liable to prosecution under the respective Copyright Law.

The use of general descriptive names, registered names, trademarks, service marks, etc. in this publication does not imply, even in the absence of a specific statement, that such names are exempt from the relevant protective laws and regulations and therefore free for general use.

While the advice and information in this book are believed to be true and accurate at the date of publication, neither the authors nor the editors nor the publisher can accept any legal responsibility for any errors or omissions that may be made. The publisher makes no warranty, express or implied, with respect to the material contained herein.

Printed on acid-free paper

Springer is part of Springer Science+Business Media ([www.springer.com](http://www.springer.com))

# Preface

Control of discrete-event dynamic systems is the topic of this book. The aim is to provide an introduction to the field, starting at an elementary level and going to close to the current research front. The reader will find concepts, theorems, algorithms, and examples. Particularly addressed to Ph.D. students and junior researchers working on control of discrete-event dynamic systems (DEDS) and, more generally, on control theory, this monograph only presumes a little background of elementary topics of control theory. The chapters are almost all based on lectures of a summer school for Ph.D. students held in June 2011 in Cagliari, Sardinia, Italy.

Three related modeling formalisms of DEDS are covered: *automata*, *Petri nets*, and *systems in dioids*. The first focus of the book is on control of *decentralized* and of *distributed* DEDS, informally speaking composed by the interconnection of two or more subsystems. Most engineering systems are currently of this type. The second focus of the book deals with heavily loaded or populated DEDS, eventually distributed, for which the so called *state explosion* problem becomes particularly acute. Therefore it becomes important to consider ‘coarse views’ obtained through fluidization of the discrete event model. Those fluid or continuous over-approximated views of DEDS lead to special classes of hybrid systems.

Control theory for DEDS is motivated by the ordering of events or actions. Problems of control of DEDS arise in control engineering, computer engineering, and sciences. Areas in which DEDS control problems arise include manufacturing systems, automated guided vehicles, logistics, aerial vehicles, underwater vehicles, communication networks, mobile phones or chemical engineering systems, but also software systems on computers, laptops, and readers. The research into control of DEDS, heavily loaded or not, is thus well motivated by engineering but also theoretically quite deep.

A brief description of the book by parts and by chapters follows. The first part (nine chapters) concerns control of *automata*. After a chapter on modeling of engineering systems by automata (Chapter 1) there follows one with the concepts of automata, decidability, and complexity (Chapter 2). Supervisory control of automata is summarized first with respect to complete observations and subsequently with respect to partial observations (Chapters 3 and 4, respectively). Observers and

diagnosers for automata, in particular distributed observers, are covered in Chapter 5. Supervisory control of distributed DEDS is introduced by three special cases in Chapter 6. That chapter is followed by one on distributed control with communication (Chapter 7) and one on coordination control (Chapter 8). Finally, Chapter 9 deals with timed automata.

The second part of the book addresses the control of *Petri nets*. It includes eleven chapters and can be seen as structured into two main parts: the first one, including eight chapters, dealing with discrete Petri nets; the second part, including three chapters, dealing with fluid relaxations. The former eight chapters can be divided into two blocks: the first six are devoted to *untimed* models, while the remaining two are related to *timed* models. In particular, Chapters 10 and 11 introduce basic concepts and structural analysis techniques. Chapters 12 and 13 are related to control. After considering supervisory control with languages specifications (Chapter 12), structural methods tailored for resource allocation problems are studied in the following one. Chapters 14 and 15 deals with diagnosis problems, the second one using net unfolding. Petri nets enriched with different temporal metrics and semantics are introduced in Chapter 16 and used in Chapter 17 for fault diagnosis, now on-line over timed models.

Chapters 18, 19 and 20 are based on fluid relaxation of DEDS. In particular, the fluid or continuous views of Petri nets are introduced in Chapter 18 on both untimed and timed models, dealing even with improvements of the relaxation with respect to the underlying discrete case. Finally, Chapters 19 and 20 are devoted to observability and diagnosis, and controllability and control, respectively.

The third and last part deals with the modeling and control of DEDS in dioids. A *dioid* is a mathematical structure with two operations, usually referred to as addition and multiplication, where the former, unlike in standard algebra, is idempotent. The most well known example for a dioid is the so-called max-plus algebra. Restricted classes of timed DEDS, in particular timed event graphs, become linear in a suitable dioid framework. For such systems, control does not involve logical decisions, only choices regarding the timing of events. They frequently appear in the context of manufacturing systems, but also arise in other engineering areas. Chapter 21 shows how to model timed event graphs in dioid frameworks and provides a detailed example from the area of high-throughput screening. Chapter 22 summarizes and illustrates control synthesis for systems in dioids.

Cagliari, Italy  
Zaragoza, Spain  
Amsterdam, Netherlands  
April 2012

Carla Seatzu  
Manuel Silva  
Jan H. van Schuppen  
Editors

# Acknowledgements

The editors thank the authors of the chapters of this book for their dedicated efforts to produce well readable chapters for the intended audience. They also thank the reviewers of the book for their efforts to provide comments to the authors on the chapters. A list of the reviewers is provided elsewhere in the book. They thank the Guest Editor Christoforos N. Hadjicostis for handling the review process of several chapters co-authored by one of the editors.

The European Commission is thanked for its financial support in part by the European Community's Seventh Framework Programme for the DISC Project under Grant Agreement number INFSO-ICT-224498. They also thank Alessandro Giua as the coordinator of the DISC project for his stimulation of the editors for this book.

The authors of Chapters 2, 3, 4, 6, and 8 acknowledge the financial support by the GAČR grants P103/11/0517 and P202/11/P028, and by RVO: 67985840.

The authors of Chapters 13, 18, 19 and 20 acknowledge the financial support by the Spanish CICYT under grant: DPI2010-20413.

# Contents

## Part I: Automata

<b>1</b>	<b>Modelling of Engineering Phenomena by Finite Automata . . . . .</b>	<b>3</b>
Jörg Raisch		
1.1	Introduction . . . . .	3
1.2	State Models with Inputs and Outputs . . . . .	5
1.2.1	Mealy Automata . . . . .	5
1.2.2	Moore Automata . . . . .	10
1.3	Automata with Controllable and Uncontrollable Events . . . . .	10
1.4	Finite Automata as Approximations of Systems with Infinite State Sets . . . . .	12
1.4.1	$\ell$ -Complete Approximations . . . . .	14
1.4.2	A Special Case: Strictly Non-anticipating Systems . . . . .	16
1.5	Further Reading . . . . .	21
References . . . . .		21
<b>2</b>	<b>Languages, Decidability, and Complexity . . . . .</b>	<b>23</b>
Stefan Haar and Tomáš Masopust		
2.1	Introduction . . . . .	23
2.2	Regular Languages and Automata . . . . .	24
2.2.1	Words and Languages . . . . .	24
2.2.2	Regular Languages . . . . .	25
2.2.3	Automata . . . . .	25
2.2.4	Closure Properties of Regular Languages . . . . .	28
2.2.5	Regularity and Recognizability . . . . .	29
2.2.6	Criteria for Regularity . . . . .	29
2.2.7	Minimality . . . . .	30
2.3	Chomsky Grammars . . . . .	31
2.3.1	Type 0 Grammars and Languages . . . . .	31
2.3.2	Type 1: Context-Sensitive . . . . .	32

2.3.3	Type 2: Context-Free Languages and Pushdown Automata .....	32
2.3.4	Type 3 Languages .....	35
2.3.5	The Chomsky Hierarchy .....	35
2.4	Turing Machines and Decidability .....	35
2.4.1	Universal Turing Machine .....	37
2.4.2	Decidable and Undecidable Problems .....	38
2.5	Complexity Classes .....	39
2.5.1	Reduction .....	40
2.6	Further Reading .....	42
	References .....	42
<b>3</b>	<b>Supervisory Control with Complete Observations .....</b>	<b>45</b>
	Tomáš Masopust and Jan H. van Schuppen	
3.1	Introduction .....	45
3.2	Motivation of Supervisory Control .....	45
3.3	Concepts of Automata and of Languages .....	47
3.4	Concepts of Control of Discrete-Event Systems .....	49
3.5	Problem of Existence of a Supervisory Control .....	51
3.6	Existence of a Supervisory Control .....	52
3.7	Implementation of a Supervisory Control by a Supervisor .....	55
3.8	Computation of a Supervisor .....	56
3.9	Partially-Ordered Sets .....	57
3.10	Supremal Controllable Sublanguages .....	58
3.11	Supremal Supervision .....	61
3.12	Further Reading .....	62
	References .....	63
<b>4</b>	<b>Supervisory Control with Partial Observations .....</b>	<b>65</b>
	Jan Komenda	
4.1	Introduction .....	65
4.2	Concepts of Supervisory Control with Partial Observations .....	66
4.2.1	Observer Automaton .....	67
4.2.2	Supervisor with Partial Observations .....	71
4.3	Existence of Supervisors .....	71
4.4	Algorithm for Verification of Observability and Automata Implementation of Supervisors .....	75
4.5	General Case of Unobservable Specifications .....	77
4.6	Algorithms .....	80
4.7	Extensions .....	83
4.8	Further Reading .....	83
	References .....	83

<b>5 Diagnosis and Automata . . . . .</b>	85
Eric Fabre	
5.1 Diagnosis vs. State Estimation . . . . .	85
5.2 Observer and Diagnoser . . . . .	87
5.3 Probabilistic Observer . . . . .	89
5.4 Diagnosability . . . . .	94
5.5 Modular Observers . . . . .	97
5.6 Distributed State Estimation . . . . .	101
5.7 Conclusion and Further Reading . . . . .	104
References . . . . .	105
<b>6 Supervisory Control of Distributed Discrete-Event Systems . . . . .</b>	107
Jan Komenda, Tomáš Masopust, and Jan H. van Schuppen	
6.1 Introduction . . . . .	107
6.2 Motivation . . . . .	108
6.3 Systems . . . . .	109
6.4 Problem Formulation . . . . .	112
6.5 Decentralized Control – Existence and Construction of a Tuple of Supervisors . . . . .	113
6.6 Decentralized Control – Undecidability . . . . .	116
6.7 Decentralized Control – Maximal Languages . . . . .	117
6.8 Distributed Control of Distributed DESs . . . . .	119
6.9 Research Issues . . . . .	122
6.10 Further Reading . . . . .	123
References . . . . .	123
<b>7 An Overview of Synchronous Communication for Control of Decentralized Discrete-Event Systems . . . . .</b>	127
Laurie Ricker	
7.1 Introduction . . . . .	127
7.2 Notation and Definitions . . . . .	128
7.3 State-Based Communication Protocols . . . . .	132
7.4 Event-Based Communication Protocols . . . . .	142
7.5 Further Reading . . . . .	145
References . . . . .	146
<b>8 Coordination Control of Distributed Discrete-Event Systems . . . . .</b>	147
Jan Komenda, Tomáš Masopust, and Jan H. van Schuppen	
8.1 Introduction . . . . .	147
8.2 Definitions . . . . .	148
8.3 Problem Statement . . . . .	151
8.4 Coordination Control with Complete Observations: Existence . . .	152
8.5 Coordination Control with Complete Observations: Supremal Supervision . . . . .	155
8.6 Coordination Control with Partial Observations: Existence . . .	160

8.7	Coordination Control with Partial Observations: Supremal Supervision . . . . .	163
8.8	Further Reading . . . . .	165
	References . . . . .	165
<b>9</b>	<b>An Introduction to Timed Automata . . . . .</b>	<b>169</b>
	Béatrice Bérard	
9.1	Motivation and Example . . . . .	169
9.2	Definition and Timed Semantics . . . . .	170
9.2.1	Timed Transition Systems . . . . .	170
9.2.2	The Model of Timed Automata . . . . .	172
9.2.3	Semantics of Timed Automata . . . . .	172
9.2.4	Languages of Timed Automata . . . . .	173
9.3	Networks of Timed Automata . . . . .	174
9.4	Zone Graph of a Timed Automaton . . . . .	177
9.5	Region Graph of a Timed Automaton . . . . .	179
9.6	Language Properties . . . . .	182
9.6.1	Closure Properties . . . . .	183
9.6.2	Undecidability Results . . . . .	185
9.7	Further Reading . . . . .	185
	References . . . . .	186

## Part II: Petri Nets

<b>10</b>	<b>Introduction to Petri Nets . . . . .</b>	<b>191</b>
	Maria Paola Cabasino, Alessandro Giua, and Carla Seatzu	
10.1	Introduction . . . . .	191
10.2	Petri Nets and Net Systems . . . . .	192
10.2.1	Place/Transition Net Structure . . . . .	192
10.2.2	Marking and Net System . . . . .	194
10.2.3	Enabling and Firing . . . . .	194
10.3	Modeling with Petri Nets . . . . .	197
10.4	Analysis by Enumeration . . . . .	199
10.4.1	Reachability Graph . . . . .	200
10.4.2	Coverability Graph . . . . .	201
10.4.3	Behavioral Properties . . . . .	204
10.5	Further Reading . . . . .	210
	References . . . . .	211
<b>11</b>	<b>Structural Analysis of Petri Nets . . . . .</b>	<b>213</b>
	Maria Paola Cabasino, Alessandro Giua, and Carla Seatzu	
11.1	Introduction . . . . .	213
11.2	Analysis via State Equation . . . . .	214
11.3	Analysis Based on the Incidence Matrix . . . . .	216
11.3.1	Invariant Vectors . . . . .	216
11.3.2	P-Invariants Computation . . . . .	218
11.3.3	Reachability Analysis Using P-Invariants . . . . .	221

11.4	Structural Properties . . . . .	222
11.4.1	Structural Boundedness . . . . .	222
11.4.2	Structural Conservativeness . . . . .	223
11.4.3	Structural Repetitiveness and Consistency . . . . .	224
11.4.4	Structural Liveness . . . . .	224
11.5	Implicit Places . . . . .	224
11.6	Siphons and Traps . . . . .	226
11.7	Classes of P/T Nets . . . . .	227
11.7.1	Ordinary and Pure Nets . . . . .	228
11.7.2	Acyclic Nets . . . . .	229
11.7.3	State Machines . . . . .	229
11.7.4	Marked Graphs . . . . .	230
11.7.5	Choice-Free Nets . . . . .	231
11.8	Further Reading . . . . .	232
	References . . . . .	232
<b>12</b>	<b>Supervisory Control of Petri Nets with Language Specifications . . . . .</b>	<b>235</b>
	Alessandro Giua	
12.1	Introduction . . . . .	235
12.2	Petri Nets and Formal Languages . . . . .	236
12.2.1	Petri Net Generators . . . . .	236
12.2.2	Deterministic Generators . . . . .	238
12.2.3	Classes of Petri Net Languages . . . . .	239
12.2.4	Other Classes of Petri Net Languages . . . . .	241
12.3	Concurrent Composition and System Structure . . . . .	241
12.4	Supervisory Design Using Petri Nets . . . . .	242
12.4.1	Plant, Specification and Supervisor . . . . .	243
12.4.2	Monolithic Supervisor Design . . . . .	243
12.4.3	Trimming . . . . .	246
12.5	Supervisory Control of Unbounded PN Generators . . . . .	248
12.5.1	Checking Nonblockingness . . . . .	249
12.5.2	Checking Controllability . . . . .	249
12.5.3	Trimming a Blocking Generator . . . . .	251
12.5.4	Trimming an Uncontrollable Generator . . . . .	253
12.5.5	Final Remarks . . . . .	254
12.6	Further Reading . . . . .	254
	References . . . . .	254
<b>13</b>	<b>Structural Methods for the Control of Discrete Event Dynamic Systems – The Case of the Resource Allocation Problem . . . . .</b>	<b>257</b>
	Juan-Pablo López-Grao and José-Manuel Colom	
13.1	Introduction . . . . .	257
13.2	Abstraction and Modelling: Class Definitions and Relations . . . . .	259
13.3	Liveness Analysis and Related Properties . . . . .	265
13.4	Structure-Based Synthesis Methods: An Iterative Control Policy . . . . .	272

13.5	Further Reading .....	276
	References .....	277
<b>14</b>	<b>Diagnosis of Petri Nets .....</b>	<b>279</b>
	Maria Paola Cabasino, Alessandro Giua, and Carla Seatzu	
14.1	Introduction .....	279
14.2	Basic Definitions and Notations .....	280
14.3	Characterization of the Set of Consistent Markings .....	282
14.3.1	Minimal Explanations and Minimal e-Vectors .....	282
14.3.2	Basis Markings and j-Vectors .....	283
14.4	Diagnosis Using Petri Nets .....	286
14.5	Basis Reachability Graph .....	289
14.6	Some Important Problems Strictly Related to Online Diagnosis ..	293
14.6.1	Online Diagnosis via Fluidification .....	293
14.6.2	Diagnosability Analysis .....	294
14.6.3	Decentralized Diagnosis .....	295
14.7	Further Reading .....	296
	References .....	298
<b>15</b>	<b>Diagnosis with Petri Net Unfoldings .....</b>	<b>301</b>
	Stefan Haar and Eric Fabre	
15.1	Motivation .....	301
15.2	Asynchronous Diagnosis with Petri Net Unfoldings .....	304
15.3	Asynchronous Diagnosis .....	308
15.4	Taking the Methodology Further .....	311
15.5	Asynchronous Diagnosability: Weak versus Strong .....	313
15.6	Conclusion and Outlook .....	315
15.7	Further Reading .....	316
	References .....	316
<b>16</b>	<b>Petri Nets with Time .....</b>	<b>319</b>
	Béatrice Bérard, Maria Paola Cabasino, Angela Di Febbraro, Alessandro Giua, and Carla Seatzu	
16.1	Introduction and Motivation .....	319
16.2	Timing Structure and Basic Concepts .....	320
16.2.1	Timed Elements .....	320
16.2.2	Timed Petri Nets and Time Petri Nets .....	321
16.2.3	Deterministic and Stochastic Nets .....	321
16.3	T-Timed Petri Nets and Firing Rules .....	323
16.3.1	Atomic vs. Non Atomic Firing .....	323
16.3.2	Enabling Semantics .....	323
16.3.3	Server Semantics .....	324
16.3.4	Memory Policy .....	325
16.4	Deterministic Timed Petri Nets .....	326
16.4.1	Dynamical Evolution .....	326
16.4.2	Timed Marked Graphs .....	329

16.5	Stochastic Timed Petri Nets . . . . .	332
16.5.1	Construction of the Markov Chain Equivalent to the STdPN . . . . .	334
16.5.2	Performance Analysis . . . . .	336
16.6	Time Petri Nets . . . . .	338
16.7	Further Reading . . . . .	340
	References . . . . .	340
<b>17</b>	<b>The On-Line Diagnosis of Time Petri Nets . . . . .</b>	<b>343</b>
	René K. Boel and George Jiroveanu	
17.1	Introduction . . . . .	343
17.2	Time Petri Nets . . . . .	345
17.3	The Diagnosis of TPNs – The Setting and the Problem Description . . . . .	347
17.4	The Analysis of TPNs . . . . .	349
17.4.1	Analysis of TPNs Based on State Classes . . . . .	349
17.4.2	Analysis of TPNs Based on Time Processes . . . . .	354
17.5	The On-Line Implementation . . . . .	359
17.6	Further Reading . . . . .	362
	References . . . . .	363
<b>18</b>	<b>Introduction to Fluid Petri Nets . . . . .</b>	<b>365</b>
	C. Renato Vázquez, Cristian Mahulea, Jorge Júlvez, and Manuel Silva	
18.1	Introduction and Motivation . . . . .	365
18.2	Fluidization of Untimed Net Models . . . . .	368
18.2.1	The Continuous PN Model . . . . .	368
18.2.2	Reachability . . . . .	369
18.2.3	Some Advantages . . . . .	370
18.3	Fluidization of Timed Net Models . . . . .	372
18.3.1	Server Semantics . . . . .	372
18.3.2	Qualitative Properties under ISS . . . . .	374
18.3.3	On the Quantitative Approximation under ISS . . . . .	376
18.4	Improving the Approximation: Removing Spurious Solutions, Addition of Noise . . . . .	379
18.4.1	Removing Spurious Solutions . . . . .	379
18.4.2	Adding Noise: Stochastic T-Timed Continuous PN . . . . .	382
18.5	Steady State: Performance Bounds and Optimization . . . . .	383
18.6	Further Reading . . . . .	384
	References . . . . .	385
<b>19</b>	<b>Continuous Petri Nets: Observability and Diagnosis . . . . .</b>	<b>387</b>
	Cristian Mahulea, Jorge Júlvez, C. Renato Vázquez, and Manuel Silva	
19.1	Introduction and Motivation . . . . .	387
19.2	A Previous Technicality: Redundant Configurations . . . . .	388
19.3	Observability Criteria . . . . .	390
19.4	Reducing Complexity . . . . .	395

19.5	Structural and Generic Observability . . . . .	396
19.6	Observers Design . . . . .	399
19.7	Diagnosis Using Untimed CPNs . . . . .	402
19.8	Further Reading . . . . .	404
	References . . . . .	405
<b>20</b>	<b>Continuous Petri Nets: Controllability and Control . . . . .</b>	<b>407</b>
	Jorge Júlvez, C. Renato Vázquez, Cristian Mahulea, and Manuel Silva	
20.1	Introduction and Motivation . . . . .	407
20.2	Control Actions under Infinite Server Semantics . . . . .	409
20.3	Controllability . . . . .	409
20.3.1	Controllability When All the Transitions Are Controllable . . . . .	410
20.3.2	Controllability When Some Transitions Are Uncontrollable . . . . .	412
20.4	Control Techniques under Infinite Server Semantics . . . . .	414
20.4.1	Control for a Piecewise-Straight Marking Trajectory . . . . .	414
20.4.2	Model Predictive Control . . . . .	415
20.4.3	ON-OFF Control . . . . .	418
20.4.4	Comparison of Control Methods . . . . .	419
20.4.5	Control with Uncontrollable Transitions . . . . .	420
20.5	Towards Distributed Control . . . . .	422
20.5.1	Distributed Continuous Petri Nets . . . . .	423
20.5.2	A Control Strategy for DcontPNs . . . . .	424
20.6	Further Reading . . . . .	426
	References . . . . .	427

### Part III: Systems in Doids

<b>21</b>	<b>Discrete-Event Systems in a Doid Framework: Modeling and Analysis . . . . .</b>	<b>431</b>
	Thomas Brunsch, Jörg Raisch, Laurent Hardouin, and Olivier Boutin	
21.1	Timed Event Graphs . . . . .	431
21.2	Motivational Example . . . . .	434
21.3	Doid Algebraic Structures . . . . .	437
21.4	Linear Dynamical Systems in Max-Plus Algebra . . . . .	438
21.5	The 2-Dimensional Doid $\mathcal{M}_{in}^{ax}[\gamma, \delta]$ . . . . .	440
21.6	High-Throughput Screening Systems . . . . .	445
21.7	Further Reading . . . . .	448
	References . . . . .	449
<b>22</b>	<b>Discrete-Event Systems in a Doid Framework: Control Theory . . . . .</b>	<b>451</b>
	Laurent Hardouin, Olivier Boutin, Bertrand Cottenceau, Thomas Brunsch, and Jörg Raisch	
22.1	Motivation . . . . .	451
22.2	Theory and Concepts . . . . .	452

22.2.1	Mapping Inversion over a Dioid	453
22.2.2	Implicit Equations Over Dioids	455
22.2.3	Dioid $\mathcal{M}_{in}^{ax}[\gamma, \delta]$	457
22.3	Control	459
22.3.1	Optimal Open-Loop Control	459
22.3.2	Optimal Input Filtering in Dioids	462
22.3.3	Closed-Loop Control in Dioids	464
22.4	Further Reading	467
	References	468
<b>Index</b>		471

# List of Contributors

Béatrice Bérard

LIP6, Université Pierre & Marie Curie and CNRS UMR 7606  
BC 169, 4 place Jussieu, 75005 Paris, France  
e-mail: Beatrice.Berard@lip6.fr

René K. Boel

EESA SYSTeMS Research Group, Ghent University  
Technologiepark 914, Zwijnaarde 9052, Belgium  
e-mail: rene.boel@ugent.be

Olivier Boutin

Calle Santiago 2 – 4ºC, 11005 Cadiz, Spain  
e-mail: olivier.research@gmail.com

Thomas Brunsch

Fachgebiet Regelungssysteme, TU Berlin, Sekr. EN11, Einsteinufer 17, 10587  
Berlin, Germany.  
Also: Laboratoire d'Ingénierie des Systèmes Automatisés, Université d'Angers, 62  
Avenue Notre-Dame du Lac, 49000 Angers, France  
e-mail: brunsch@control.tu-berlin.de

Maria Paola Cabasino

Department of Electrical and Electronic Engineering, University of Cagliari  
Piazza D'Armi, 09123 Cagliari, Italy  
e-mail: cabasino@diee.unica.it

José-Manuel Colom

Instituto de Investigación en Ingeniería de Aragón (I3A), University of Zaragoza  
María de Luna 1, E-50018, Zaragoza, Spain  
e-mail: jm@unizar.es

Bertrand Cottenceau  
LUNAM, University of Angers, LISA, ISTIA  
62 Av. Notre-Dame du Lac, 49000 Angers, France  
e-mail: bertrand.cottenceau@univ-angers.fr

Angela Di Febbraro  
Department of Mechanical Engineering, Energetics, Production, Transportation  
and Mathematical Models, University of Genova  
Via Montallegro 1, 16145 Genova, Italy  
e-mail: angela.difebbraro@unige.it

Eric Fabre  
INRIA Rennes Bretagne Atlantique  
Campus de Beaulieu, 35042 Rennes Cedex, France  
e-mail: eric.fabre@inria.fr

Alessandro Giua  
Department of Electrical and Electronic Engineering, University of Cagliari  
Piazza D'Armi, 09123 Cagliari, Italy  
e-mail: giua@diee.unica.it

Stefan Haar  
INRIA/LSV, CNRS & ENS de Cachan  
61, avenue du Président Wilson, 94235 CACHAN Cedex, France  
e-mail: Stefan.Haar@inria.fr

Laurent Hardouin  
Laboratoire d'Ingénierie des Systèmes Automatisés, Université d'Angers  
62 Avenue Notre-Dame du Lac, 49000 Angers, France  
e-mail: laurent.hardouin@istia.univ-angers.fr

George Jiroveanu  
Transelectrica SA - Romanian National Power Grid Company  
Brestei 5, 200581, Craiova, Romania  
e-mail: george.jiroveanu@transelectrica.ro

Jorge Júlvez  
Instituto de Investigación en Ingeniería de Aragón (I3A), University of Zaragoza  
María de Luna 1, E-50018, Zaragoza, Spain  
e-mail: julvez@unizar.es

Juan-Pablo López-Grao  
Department of Computer Science and Systems Engineering, University of Zaragoza  
María de Luna 1, E-50018, Zaragoza, Spain  
e-mail: jpablo@unizar.es

Jan Komenda  
Institute of Mathematics, Academy of Sciences of the Czech Republic  
Žižkova 22, 616 62 Brno, Czech Republic  
e-mail: komenda@math.cas.cz

**Cristian Mahulea**

Instituto de Investigación en Ingeniería de Aragón (I3A), University of Zaragoza  
María de Luna 1, E-50018, Zaragoza, Spain  
e-mail: cmahulea@unizar.es

**Tomáš Masopust**

Institute of Mathematics, Academy of Sciences of the Czech Republic  
Žižkova 22, 616 62 Brno, Czech Republic  
e-mail: masopust@math.cas.cz

**Jörg Raisch**

Fachgebiet Regelungssysteme, TU Berlin, Sekr. EN11, Einsteinufer 17, 10587  
Berlin, Germany.  
Also: Fachgruppe System-und Regelungstheorie, Max-Planck-Institut für Dynamik  
komplexer technischer Systeme, Magdeburg  
e-mail: raisch@control.tu-berlin.de

**S. Laurie Ricker**

Department of Mathematics & Computer Science, Mount Allison University  
67 York St. Sackville, NB Canada E4L 1E6  
e-mail: lricker@mta.ca

**Carla Seatzu**

Department of Electrical and Electronic Engineering, University of Cagliari  
Piazza D'Armi, 09123 Cagliari, Italy  
e-mail: seatzu@diee.unica.it

**Manuel Silva**

Instituto de Investigación en Ingeniería de Aragón (I3A), University of Zaragoza  
María de Luna 1, E-50018, Zaragoza, Spain  
e-mail: silva@unizar.es

**Jan H. van Schuppen**

CWI, P.O. Box 94079, 1090 GB Amsterdam, Netherlands  
e-mail: J.H.van.Schuppen@cwi.nl

**C. Renato Vázquez**

Instituto de Investigación en Ingeniería de Aragón (I3A), University of Zaragoza  
María de Luna 1, E-50018, Zaragoza, Spain  
e-mail: cvazquez@unizar.es

## Reviewers

René K. Boel	Ghent University, Belgium
José Manuel Colom	University of Zaragoza, Spain
Isabel Demngodin	University Aix-Marseille, France
Mariagrazia Dotoli	Polytechnique of Bari, Italy
Maria Pia Fanti	Polytechnique of Bari, Italy
Anne-Kathrin Hess	Technical University of Berlin, Germany
Richard Hill	University of Detroit Mercy, Michigan, USA
Jorge Júlvez	University of Zaragoza, Spain
Pia L. Kempker	VU University Amsterdam, Amsterdam, Netherlands
Jan Komenda	Academy of Sciences, Brno, Czech Republic
Xenofon Koutsoukos	Vanderbilt University, Nashville, Tennessee, USA
Dimitri Lefebvre	University Le Havre, Strasbourg, France
Feng Lin	Wayne State University, Detroit, Michigan, USA
Jan Lunze	University of Bochum, Germany
Kristian Lyngbaek	Palo Alto Research Center, Palo Alto, California, USA
Cristian Mahulea	University of Zaragoza, Spain
Tomáš Masopust	Academy of Sciences, Brno, Czech Republic
José Merseguer	University of Zaragoza, Spain
Behrang Monajemi Nejad	Technical University of Berlin, Germany
Geert Jan Olsder	Delft University of Technology, Delft, Netherlands
Laurie Ricker	Mount Allison University, Sackville, NB Canada
Karen Rudie	Queen's University, Kingston, Canada
Carla Seatzu	University of Cagliari, Italy
Manuel Silva	University of Zaragoza, Spain
Rong Su	Nanyang Technological University, Singapore
John Thistle	University of Waterloo, Ontario, Canada
Ton van den Boom	Delft University of Technology, Delft, Netherlands
Jan H. van Schuppen	CWI, Amsterdam, Netherlands
Renato Vázquez	University of Zaragoza, Spain
Tiziano Villa	University of Verona, Italy
Tae-Sic Yoo	Idaho National Laboratory, Idaho, USA
Liewei Wang	University of Zaragoza, Spain
Xu Wang	University of Zaragoza, Spain
Yorai Wardi	Georgia Institute of Technology, Atlanta, Georgia, USA
Thomas Wittmann	University of Erlangen, Germany

# Acronyms

AGV	Automated Guided Vehicle
BIC	Bounded Input Controllable
BRG	Basis Reachability Graph
CDFG	Controlled Deterministic Finite Generator
CPN	Continuous Petri Net
CS	Controllability Space
CSS	Cooperating Sequential System
CTMC	Continuous Time Markov Chain
DcontPN	Distributed Continuous Petri Net
DEDS	Discrete Event Dynamic Systems
DES	Discrete Event System
DFA	Deterministic Finite Automaton
DFG	Deterministic Finite Generator
DFMeA	Deterministic Finite Mealy Automaton
DFMoA	Deterministic Finite Moore Automaton
DTPN	Deterministic Timed Petri Net
DuSCOP	Dual Supervisory Control and Observation
ELCP	Extended Linear Complementarity Problem
EQ	Equal Conflict
FMS	Flexible Manufacturing System
FSM	Finite State Machine
FSS	Finite Server Semantics
GTS	Graph Transformation System
HC	Hamiltonian Circuit
HTS	High-Throughput Screening
ILP	Integer Linear Programming
ILPP	Integer Linear Programming Problem
ISS	Infinite Server Semantics
JF	Join Free
LPP	Linear Programming Problem
L-S <sup>3</sup> PR	Linear System of Simple Sequential Processes with Resources

MPC	Model Predictive Control
MPN	Markovian Petri Net
MRI	Magnetic Resonance Imaging
MTS	Mono-T-Semiflow
MVN	Modified Verifier Net
NDFG	Nondeterministic Finite Generator
NDFMeA	Nondeterministic Finite Mealy Automaton
NDFMoA	Nondeterministic Finite Moore Automaton
NFA	Nondeterministic Finite Automaton
NS-RAS	Non-Sequential Resource Allocation System
OCC	Output Control Consistent
PC <sup>2</sup> R	Processes Competing for Conservative Resources
PDA	PushDown Automaton
PLC	Programmable Logic Controller
PN	Petri Net
QPP	Quadratic Programming Problem
RAP	Resource Allocation Problem
RAS	Resource Allocation System
SAT	Satisfiability
SB	Structurally Bounded
SCTdMG	Strongly Connected Timed Marked Graph
SL	Structurally Live
SPQR	System of Processes Quarrelling over Resources
S <sup>3</sup> PR	System of Simple Sequential Processes with Resources
S-RAS	Sequential Resource Allocation System
STdPN	Stochastic Timed Petri Net
TCPN	Timed Continuous Petri Net
TdPN	Timed Petri Net
TEG	Timed Event Graph
TM	Turing Machines
TMG	Timed Marked Graph
TPN	Time Petri Net
VN	Verifier Net
WP	Weighted Path