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# Sparse Representations and Compressive Sensing for Imaging and Vision



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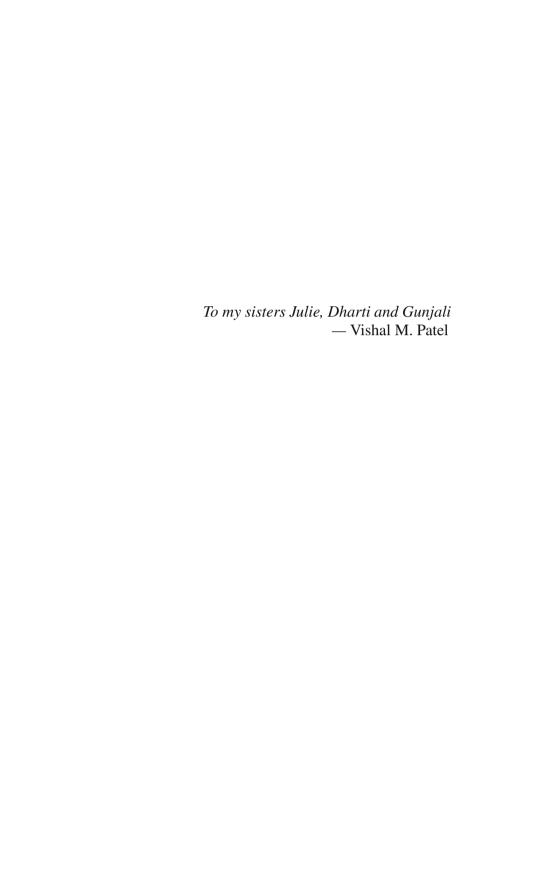
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