Complex Data Analytics with Formal Concept Analysis

Rokia Missaoui • Léonard Kwuida Talel Abdessalem Editors

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In memory of Vincent Duquenne 27.06.1950–26.02.2020.

Foreword

It was in 1970s that Galois connections and respective lattices of closed sets (studied before in Mathematics by Garrett Birkhoff and Oystein Ore) were found useful for modeling information structures and processes [3,26]. After several decades of research in formal concept analysis (FCA) no one can say now that FCA proposes hardly scalable techniques for the analysis of binary data. Highly efficient FCA algorithms with various options for approximation strategies are now widely used for the analysis of complex voluminous heterogeneous data.

In spite of intrinsic complexity of computational problems related to unrestricted generation of both formal concepts and implication bases [15,16], several efficient FCA algorithms were found already around year 2000 [10,19] and new efficient implementations show excellent scalability [1]. Numerous approaches to partial generation of concepts and implications were proposed, based on interestingness constraints [17] and probabilistic considerations [2,5].

Models for treating complex data with FCA-based approaches are manifold. Several approaches were proposed and developed for relational data, first considered through the prism of conceptual scaling, which reduces complex data to binary (or unary, in terms of Rudolf Wille). Most popular approaches to treating complex data in FCA "directly", i.e., without binarizing (scaling, in FCA terms) them, are logical concept analysis [7], pattern structures [9], fuzzy concept analysis [4], relational concept analysis [11], triadic concept analysis [13,20,22,23], polyadic CA [25], and probabilistic FCA [14]. Recent interest in natural language processing, knowledge graphs, and social network analysis inspired development of new FCA-based approaches [6,8,12,21].

The recent wave of interest in deep neural networks is tempered by the problems of explainability and robustness of proposed solutions. For some applied domains, like medicine, law, and finance, these issues are crucial: experts would not accept efficient accurate solutions that do not provide acceptable explanations. FCA can propose a broad scope of tools for finding interpretable solutions, since explainability is in the core of FCA. Several attempts were made already to combine neural network efficiency with explainability provided by FCA-based approaches [18,24].

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This volume presents an important step in all the above-mentioned directions: meeting the challenge of big and complex data, combining FCA-based approaches with methods based on neural networks to guarantee explainability of results.

Moscow, Russia August 2020 Sergei O. Kuznetsov

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Preface

With the advent of complex and big data and the increasing number of studies towards their management and analysis, it becomes important to get a better insight into existing studies, trends, and challenges and rely on promising theories such as formal concept analysis (FCA) together with recently developed technologies to design new, accurate, and scalable solutions for big data analytics facilities.

FCA is an important formalism that is associated with a variety of research areas such as lattice theory, knowledge representation, data mining, machine learning, and semantic Web, to name a few. It is successfully exploited in an increasing number of application domains such as software engineering, information retrieval, social network analysis, and bioinformatics. The mathematical power of FCA comes from its concept lattice formalization in which each element captures a formal concept while the whole structure represents a hierarchy that offers conceptual clustering, browsing, and association rule mining.

Although there are significant theoretical and practical contributions within the FCA community, including the design and implementation of efficient algorithms and tools for concept lattice computation and exploitation, this book examines a set of important and relevant research directions in complex data management and updates the contribution of the FCA community for analyzing complex and large data. For example, formal concept analysis and some of its extensions are exploited, revisited, and coupled with recent processing paradigms to maximize the benefits in analyzing large data. This book is a follow-up project of the workshop BigFCA'2019—Formal Concept Analysis in the Big Data Era—which was jointly organized with the ICFCA'2019 Conference in Frankfurt (see https://icfca2019.frankfurt-university.de/bigfca.html).

This volume of eleven chapters is meant to cover the state of the art of the research on the intersection of FCA and complex data analysis in a more systematic and detailed manner than it was done in the workshop proceedings mentioned above.

Gatineau, QC, Canada Bern, Switzerland Palaiseau, France September 2020 Rokia Missaoui Léonard Kwuida Talel Abdessalem

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Acronyms

ACN Abstract Conceptual Navigation

FCA Formal Concept AnalysisFD Functional DependencyIR Information RetrievalKG Knowledge Graph

NLP Natural Language Processing

OA Object-Attribute

OAC Object-Attribute-Condition
PAC Probably Approximately Correct

PGP Projected Graph Pattern RCA Relational Concept Analysis TCA Triadic Concept Analysis