## Studies in Systems, Decision and Control

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## Deyan Radev

# Measuring Systemic Risk

A Probabilistic Perspective



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