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Optical Flow and Trajectory Estimation Methods



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To Andrea

—Joel Gibson

To Ingrid

—Oge Marques

Preface

Optical flow can be thought of as the projection of 3-D motion onto a 2-D image plane. We are generally given the 2-D projections of the objects at different points in time, i.e., the images, and asked to ascertain the motion between these projections. While points of a physical object, considered at different points in time, should indeed have some dense motion vector in 3-D space, the projection of these points onto a 2-D image sacrifices this one-to-one characteristic. Indeed, it is ordinary that the projection of a point on an object is hidden or *occluded* from view or moved outside of the domain of the image. This inverse process is akin to trying to deduce objects from shadows cast on the ground.

Yet understanding the motion within a scene is the key to solving many problems. Within film and video, high-quality motion estimation is fundamental to the restoration of archival footage. Optical flow is used to help interpolate frames for speed changes. Robots use real-time motion approximations to navigate their environment. Combined with stereo depth estimation, optical flow is an intrinsic part of scene flow.

Perhaps the most fundamental concept in optical flow is *color constancy*. It claims that the projection of a given point on any image will produce the same color value. For all but synthetically generated images this will not hold exactly. As the amount or angle of light changes between the captured images, color intensity can vary dramatically. A closely related property which attempts to mitigate this variability is *gradient constancy* or edge matching.

For all but the most simplistic case, matching the color of a pixel between two images yields a one-to-many map. The process might be improved by comparing the neighborhoods around a pixel in order to find a best match. This too fails along the edge of an object where the neighborhoods all look the same in what is called *aperture effect*.

We must add some knowledge about how flow behaves in order to choose which of the many possible color constancy matches is best. In this role, the most successful regularizer has been Total Variation (TV). Roughly speaking, total variation in optical flow sums the total amount of change in the flow field. Then, given

ambiguous flows with similar color constancy, it will choose the flow with the least total change.

Since the beginning of modern optical flow estimation methods, multiple frames have been used in an effort to improve the computation of motion. More recently, researchers have stitched together sequences of optical flow fields to create *trajectories*. These trajectories are temporally coherent, a necessary property for virtually every real-world application of optical flow. New methods compute these trajectories directly using variational methods and low-rank constraints.

Optical flow and trajectories are ill-posed, under-constrained, inverse problems. Sparse regularization has enjoyed some success with other problems in computer vision but there has been little application in optical flow. In part this is because of the difficulty of dictionary learning in the absence of an exemplar. Applying sparsity to trajectories as a low-rank constraint has been stifled by the computational complexity.

This book focuses on two main problems in the domain of optical flow and trajectory estimation: (i) The problem of finding convex optimization methods to apply sparsity to optical flow; and (ii) The problem of how to extend sparsity to improve trajectories in a computationally tractable way.

It is targeted at researchers and practitioners in the fields of engineering and computer science. It caters particularly to new researchers looking for cutting-edge topics in optical flow as well as veterans of optical flow wishing to learn of the latest advances in multi-frame methods.

We expect that the book will fulfill its goal of serving as a preliminary reference on the subject. Readers who want to deepen their understanding of specific topics will find more than eighty references to additional sources of related information spread throughout the book.

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Colorado Springs, CO, USA
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June 2016

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Contents

1 Optical Flow Fundamentals	1
1.1 Color Constancy	1
1.2 Aperture Problem	3
1.3 Small Versus Large Motion	3
1.3.1 Linearization	3
1.3.2 Nonconvexity	4
1.4 Occlusions	4
1.5 Total Variation	4
1.6 From Optical Flow to Trajectory	5
1.7 Sparsity	5
1.8 Dictionary	5
1.9 Low Rank	6
References	6
2 Optical Flow and Trajectory Methods in Context	9
2.1 Introduction	9
2.2 Algorithms	11
2.2.1 Spatio-Temporal Smoothing	11
2.2.2 Parameterizations	12
2.2.3 Optical Flow Fusion	13
2.2.4 Sparse Tracking to Dense Flow	15
2.2.5 Low Rank Constraints	16
2.3 Data Sets and Performance Measurement	18
2.3.1 Existing Data Sets	18
2.3.2 Individual Measurement Efforts	19
2.4 Trajectory Versus Flow	20
2.5 Conclusions	21
References	21

3 Sparse Regularization of TV-L¹ Optical Flow	25
3.1 Introduction	25
3.2 Previous Work	26
3.3 Our Work	27
3.3.1 Partially-Overlapping Patches	27
3.3.2 Dictionary Learning	30
3.3.3 Sparse Total Variation	30
3.3.4 Nesterov's Method	32
3.4 Experimental Results	34
3.4.1 Dictionaries	34
3.4.2 Implementations Details	35
3.4.3 Discussion	36
3.5 Conclusions	39
References	39
4 Robust Low Rank Trajectories	41
4.1 Introduction	41
4.2 Previous Work	42
4.3 Our Work	44
4.4 Experimental Results	45
4.5 Concluding Remarks	47
References	48