The Layered Games Framework for Specifications and Analysis of Security Protocols

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Abstract. The layered games framework provides a solid foundation to the accepted methodology of building complex distributed systems, as a 'stack' of independently-developed protocols. Each protocol in the stack, realizes a corresponding 'layer' model, over the 'lower layer'. We define layers, protocols and related concepts. We then prove the *fundamental lemma of layering*. The lemma shows that given a stack of protocols $\{\pi_i\}_{i=1}^u$, s.t. for every $i \in \{1, \ldots u\}$, protocol π_i realizes layer L_i over layer L_{i-1} , then the entire stack can be composed to a single protocol $\pi_{u||\ldots||1}$, which realizes layer L_u over layer L_0 .

The fundamental lemma of layering allows precise specification, design and analysis of each layer independently, and combining the results to ensure properties of the complete system. This is especially useful when considering (computationally-bounded) adversarial environments, as for security and cryptographic protocols.

Our specifications are based on *games*, following many works in applied cryptography. This differs from existing frameworks allowing compositions of cryptographic protocols, which are based on *simulatability* of ideal functionality.

1 Introduction

The design and analysis of complex distributed systems, such as the Internet and applications using it, is an important and challenging goal. Such systems are designed in modular fashion, typically by decomposing the system into multiple layers (or modules-). Some of the well known layered network architectures include the 'OSI 7-layers reference model' and the 'IETF 5-layers reference model' (also referred to as the Internet or TCP/IP model); see e.g. [30]. The present work is part of an effort, described in [25], to extend such layered networking architectures, to support secure e-commerce applications. Figure 1 shows the five IETF layers, together with two optional security sub-layers, and the four secure e-commerce layers of [25].

Layered (or modular) architectures allow to specify, design, analyze, implement and test protocols for each layer, independently of protocols for other layers. This is based on the paradigm of *lower layers abstraction*: when discussing and

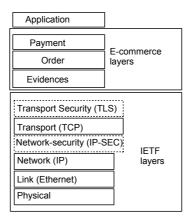


Fig. 1. IETF and e-commerce layers; (optional) security sub-layers marked with dotted contour

analyzing a protocol π_i for layer i, running in multiple nodes, we abstract the satisfactory behaviors of the lower layers by a single abstract $layer \ model \ \mathsf{L}_{i-1}$, and the satisfactory behaviors of layer i into abstract layer model L_i . Protocol π_i realizes $layer \ model \ \mathsf{L}_i$ over $layer \ model \ \mathsf{L}_{i-1}$, if the behavior of (multiple instances of) π_i running over layer model L_{i-1} , satisfies layer model L_i (except with negligible probability). We write this as: $\mathsf{L}_i \vdash \left[\mathsf{L}_{i-1}^{\pi_i}\right]$.

A pair of protocols π_i and π_{i-1} , of layers i, i+1, can be composed into a single protocol, which we denote as $\pi_{i||i-1}$. Our main result is the fundamental lemma of layering, showing that by composing protocols of multiple layers, we can implement a high-layer model directly over a low-layer model. Given layer models $\{\mathsf{L}_i\}_{i=0}^l$, and protocols π_1, \ldots, π_l , where $\mathsf{L}_i \vdash \begin{bmatrix} \pi_i \\ \mathsf{L}_{i-1} \end{bmatrix}$ for $i=1,\ldots,l$, their layered composition $\pi_{1||\ldots||l}$ implements L_l over L_0 , i.e. $\mathsf{L}_l \vdash \begin{bmatrix} \pi_{1||\ldots||l} \\ \mathsf{L}_0 \end{bmatrix}$. This provides firm foundations to the security of modular and layered architectures, as in Figure 1.

For example, in [27] we define the delivery evidences layer model $L_{\rm DE}$, and the lower communication layer model $L_{\rm Comm}$; and we show a protocol $\pi_{\rm DE}$ s.t. $L_{\rm DE} \vdash \begin{bmatrix} \pi_{\rm DE} \\ L_{\rm Comm} \end{bmatrix}$. Similarly, in [26] we define the orders layer model $L_{\rm Orders}$, and show protocol $\pi_{\rm Order}$ s.t. $L_{\rm Orders} \vdash \begin{bmatrix} \pi_{\rm Order} \\ L_{\rm DE} \end{bmatrix}$. Using the fundamental lemma of layering, the composite protocol $\pi_{\rm DE||O}$ realizes the orders layer directly over the communication layer, i.e. $L_{\rm Orders} \vdash \begin{bmatrix} \pi_{\rm DE||O} \\ L_{\rm Comm} \end{bmatrix}$. This is illustrated in Figure 2, where we outline the games each of the protocols $(\pi_{\rm DE}, \pi_{\rm Order}$ and their composition

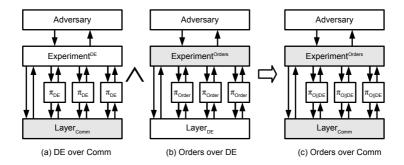


Fig. 2. Layering of realizations of the Order and Delivery Evidences (DE) layers

 $\pi_{\text{DE}||O}$, the two lower layers (Comm and DE), the two experiments protocols (DE and Orders), and the adversary protocol.

The layered games framework provides solid foundations to the accepted methodology, of using layered architectures (also called reference models), to specify, design, analyze, implement and test each layer independently. In spite of the extensive use of layered architectures, such foundations did exist prior to this work. For example, the IP (Internet Protocol) layer is essentially only required to provide a vaguely-described 'best effort' service. Existing proposals and standard of specifications of layers are only stated informally, often by partial-specification for the *operation* of the protocols, rather than to the *service* the higher layer can rely on. Composition of protocols is also used without formal definition or proof.

A possible explanation for the fact that layering was not yet based on formal foundations, in spite of its wide use, is the fact that similar compositions work as expected for many models, often trivially. For example, the composition of two polynomial time algorithms is trivially also a polynomial time algorithm. However, as [2] argue, composition properties require proof, and may not hold for all (natural) models. For example, the composition of two polynomial time interactive Turing machines (ITM), or of an (infinite) state machine with polynomial-time transition function, may not be polynomial-time, in the natural setting where the outputs of each machine is considered part of the inputs of the other. Indeed, in developing the layered games framework, we found that some definitional choices could have subtle but critical impact on composability. Details within.

Precise specifications of models for network layers can be hard to write and analyze, since they depend on many implementation and environment aspects. However, such rigorous specifications, and analysis, are critical, at least for security and cryptographic protocols, which must resist adversarial attacks. The layered games framework allows meaningful models, and analysis of implementations (protocols), using standard reduction techniques and composition of protocols (layers).

Compositions and reductions are standard techniques in design and analysis of cryptographic functions and protocols. As noted above, polynomial-time algorithms trivially compose well. However, composition of cryptographic protocols is more challenging. Several frameworks were shown to ensure secure composition, including universal composability (UC) by [14], reactive simulatability by [5, 34], observational equivalence by [32], and more. These frameworks all follow the ideal functionality paradiqm.

The ideal functionality paradigm is elegant and powerful, and resulted in many significant results, including proofs that arbitrary functions and functionalities can be computed securely, e.g. [21, 12, 14]. Grossly simplifying, an 'ideal functionality' for layer i is a single program or ITM F_i , which has multiple copies of the interfaces to layer i+1. Protocol π_i is considered secure, if executions of multiple copies of it over F_{i-1} , are indistinguishable from executions of F_i .

However, it may not always be feasible to define an ideal functionality capturing the possible behaviors of a realistic network layer. In fact, even defining the behaviors of each layer is challenging; transforming this into a program, would be impractical or impossible, and may result in over-specification. Note that over-specification of layers (or protocols) is usually considered harmful by practitioners, see e.g. [9].

This inability to use ideal functionalities as specifications for networking and e-commerce layer models, is our motivation in developing the layered games framework. The layered games framework allows protocol compositions with realistic specifications for network and e-commerce layer models, and with emphasis on simplicity and usability, even at some reduction in scope and generality.

As the name implies, the layered games framework is based on the *game playing paradigm*, instead of following the ideal functionality paradigm. The game playing paradigm is central to the theory of cryptography, see e.g. [21, 20]. Game playing supports strong analytical tools, e.g. [8], and may facilitate the use of (semi) automated proof-checking tools, see e.g. [24].

In the game-playing paradigm, one specifies an interactive game between a component and an adversary, where security is defined by the probability of the adversary winning in the game. With information-theoretic games the adversarial entity is allowed unbounded computational resources, while *concrete* and *probabilistic polynomial time* games assume certain limitations on adversarial resources, e.g. available time. Game-based specifications are widely used, and available for many cryptographic primitives such as digital signature and encryption schemes, pseudo-random functions, and much more, e.g., [22, 23, 20].

Some primitives have secure implementations for game-based specifications, where the corresponding ideal functionalities are not realizable, see [17, 11, 13]. This provides another motivation for investigating compositions of protocols satisfying game-playing specifications. However, our focus is different: allowing realistic models for network layers, without trying to define them as 'ideal functionality'.

Further related works. Our execution model is closely related to the execution models of I/O Automata of [33], especially the Probabilistic I/O Automata model of Canetti et al. [15], and to the Reactive Simulatability framework [5, 6, 35]. In an especially related work, Backes et al. [4] define a relaxed notion of conditional reactive simulatability, where simulation is required only if the environment fulfills some constraints; however, there are significant differences between the works, most notably their constraints are on the environment and not on the lower layers.

The layered games framework follows the *computational* approach to cryptography, which treats protocols and cryptographic schemes as programs/machines, operating on arbitrary stings (bits). This is in contrast to the *symbolic* approach, where cryptographic operations are seen as functions on a space of symbolic (formal) expressions, and security properties are stated as symbolic expressions; see [18, 10]. Several works investigate compositions of cryptographic protocols with the symbolic approach, e.g. Datta et al. [16] and Backes at al. [3]. We believe that it may be possible and beneficial, to extend the layered games framework to support symbolic/formal analysis, possibly building on recent results on the relationships between the two approaches, such as [1]. This may facilitate the use of verification tools; notice also that we use state machines as the basic computational model, which can also be helpful in applying verification tools.

Organization. In Section 2 we define protocols, configurations (of protocols), and executions (of configurations). In Section 3 we define layer games, models and realizations. In Section 4 we present and prove the fundamental lemma of layering. We conclude and discuss future work in Section 5.

For space limitations, the proof and detailed examples of applications of the framework are deferred to the full version of this paper [28]; see also [27, 26].

2 Protocols, Configurations and Executions

2.1 Protocols

Our basic element of computation is a *protocol*. We use protocols to model all the entities compromising the systems we investigate, including even adversarial entities ('the adversary'). Protocols are state machines¹ that accept input on one of few *input interfaces*, and produce output on one or more *output interfaces*. The transition function δ maps the input (interface and value), current state and random bits, to a new state and to outputs on the different output interfaces. We use \bot to denote a special value which is not a binary string ($\bot \not\in \{0,1\}^*$); a protocol outputs \bot on some output interface to signal 'no output'.

¹ We use state machines, rather than e.g. ITM as in Universal Composability [14], since we found it simpler, and easier to ensure that an execution involving multiple protocols, some of which are adversarial, will have well-defined scheduling and distribution of events. Also, in many cases protocols may be represented by *finite* state machines, which may have advantages including possible use of automated verification tools.

The transition function δ can depend on two additional inputs: random bits and a security parameter. The random bits may be ignored to define deterministic protocols, including analysis of protocols using pseudo-random bits. The (unary) security parameter, allows to define computational properties of the protocol and of specifications, such as security against computationally-bounded adversary. Specifically, we use the security parameter to define a *polynomial* protocol.

Definition 1 (Protocol). A protocol π is a tuple $\langle S, I_{IN}, I_{OUT}, \delta \rangle$ where:

- 1. S is a set of states, where $\bot \in S$ is the initial state,
- 2. I_{IN} is a set of input interface identifiers,
- 3. I_{OUT} is a set of output interface identifiers,
- 4. $\delta: IN \to OUT$ is a transition function, with:
 - Domain $IN = 1^* \times S \times I_{IN} \times \{0, 1\}^* \times \{0, 1\}^*$ (security parameter, current state, input interface, input value, random bits).
 - Range OUT = $S \times \prod_{i \in I_{OUT}} (\{0,1\}^* \cup \{\bot\})$. The outputs consist of a new state, denoted $\delta.S \in S$, and output values $\delta.ov[\iota] \in \{0,1\}^* \cup \{\bot\}$ for each interface $\iota \in I_{OUT}$.

The protocol is polynomial if δ is polynomial-time computable, and if the length of the outputs is the same as the length of the inputs², plus a polynomial in the security parameter, i.e. $\exists c \in \mathbb{N} \text{ s.t. } \forall (1^k, s, \iota_i, x, r) \in IN, \iota_o \in I_{OUT} : |\delta.ov[\iota_o](k, s, \iota_i, x, r)| \leq |x| + |k|^c$.

Notations

 Π , Π_{poly} : Let Π denote the set of all protocols, and Π_{poly} denote the set of polynomial protocols.

Dot notation: the range of δ is a set of pairs $(s, ov[\iota])$, where $s \in S$ is the new state and $ov[\iota] \in \{0,1\}^* \cup \{\bot\}$ is the output on each output interface $\iota \in I_{OUT}$. To refer directly to the state or the outputs, we use dot notation as in $\delta.s(\cdot)$ and $\delta.ov[\iota](\cdot)$ respectively. We similarly use dot notation in other places, i.e. $\alpha.\beta$ refers to element β of a record or tuple α .

We can connect protocols, via their interfaces, in different *configurations*, as we define next. We can also connect from an output interface of a protocol, to an input interface of the same protocol; this makes it trivial to compose several protocols into a single protocol, which is useful (see Section 4). Note that if we

This restriction of the output length to be the same as input length, plus some 'overhead' which depends only on the security parameter, is a simple method to prevent exponential blow-up in input and output lengths, as outputs of one protocol become inputs to another protocol during execution. This restriction is reasonable in practice, and sufficient for our needs; for example, it allows a protocol to 'duplicate' input from one interface, to multiple output interfaces, but maintains a polynomial bound on the length of the inputs and outputs on each interface during the execution. More elaborate ways to to prevent exponential blow-up were presented by [31] describing a general model for systems which satisfy certain acyclic conditions, [14] and [29] for UC, and [6] for reactive simulatability.

compose several polynomial protocols in this manner, then the resulting protocol is also polynomial.

2.2 Configuration

We study interactions of multiple protocols, connected via their interfaces; we call the set of interconnected protocols a configuration. Configuration are a directed graph, whose nodes P are identifiers for protocols, and whose edges are defined by mappings $p' = \mathsf{nP}(p,\iota)$ (for 'next protocol') and $\iota' = \mathsf{nI}(p,\iota)$ (for 'next interface'), mapping output interface $\iota \in \mathsf{oI}(p)$ of node p, to input interface $\iota' \in \mathsf{iI}(p)$ of node p'. Identification of the input and output interfaces, corresponds to the awareness of the network-layer, e.g. of router or firewall, to the identification of the network interface card on which a packet was received. For example, Figure 2, shows three (homomorphic) configurations. The definition follows.

Definition 2 (Configuration). A configuration is a tuple $C = \langle P, il, ol, nP, nl \rangle$, where:

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P is a set of protocol instance identifiers,
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il, ol map identifiers in P to input and output interfaces, respectively,

nP maps from instance identifier $p \in P$ and an output interface $\iota \in \mathsf{ol}(p)$, to $p' = \mathsf{nP}(p, \iota)$, where either $p' = \bot$ or $p' \in P$ (another instance),

nl maps from instance identifier $p \in P$ and an output interface $\iota \in ol(p)$, to input interface ι' , where if $nP(p,\iota) \in P$ then $\iota' \in il(nP(p,\iota))$,

Above, we defined configurations without any 'size' parameter, as required e.g. to analyze protocols and distributed algorithms designed for networks with a variable number of parties (and where complexities may depend on the number of parties). This is for simplicity and to avoid clutter; the extensions to (uniform or non-uniform) 'configuration families' seem quite obvious. Notice that for many applications, e.g. in [27, 26], it may be sufficient to consider a small fixed set of parties.

Still, configurations as defined above, are quite general. In particular, we intentionally avoided assuming any specific communication or synchronization mechanisms. This allows use of the framework in diverse scenarios, e.g. with or without assumptions on synchronization, communication and failures.

2.3 Executions

An execution is a sequence of events, each event corresponding to one transition of a protocol π running in one node $p \in \mathsf{P}$ inside a configuration $C = \langle \mathsf{P}, \mathsf{il}, \mathsf{ol}, \mathsf{nP}, \mathsf{nI} \rangle$; to define the execution, we use a mapping $\pi = \Gamma(p)$ from the protocol identifiers P to the protocols realizing each node.

An important design goal, is that the set of executions of a given configuration C, with a specific mapping to protocols Γ , would be a well-defined random variable. This makes it easier to use an execution as a 'subroutine', to facilitate reduction-based reasoning and proofs. To further simplify such reductions, we require that executions be a deterministic function of explicit random-tape inputs. Specifically, the i^{th} event in the execution, denoted ξ_i , is defined by the (deterministic) transition function of the protocol $\Gamma(p_i)$ invoked at this event (where p_i is the identifier of that node). We allow the protocol to make random choices, but only using uniformly-selected random bits $R_i \in_R \{0,1\}^*$, provided as input to the transition function. Let $\mathbb{R} = \{R_i \equiv \{0,1\}^*\}_{i=1,2,\dots}$ be the sequence whose elements are the sets of all binary strings $\{0,1\}^*$; each execution is a deterministic function of the specific sequence $R \in \mathbb{R}$ used in that execution (i.e. $R = \{R_i\}_{i=1,2,\dots}$ s.t. $(\forall i)R_i = \{0,1\}^*$).

Each protocol instance has its own state, and in each round may decide to invoke interfaces of multiple other protocol instances; see for example the configurations in Figure 2. Therefore, some scheduling mechanism for events is required. To ensure well-defined executions, without any non-deterministic choice (except for the explicit use of the random input strings $R \in \mathbb{R}$), we use a deterministic schedule \mathcal{S} (cf. [15]).

A schedule S of configuration $C = \langle \mathsf{P}, \mathsf{il}, \mathsf{ol}, \mathsf{nP}, \mathsf{nI} \rangle$, is a sequence of pairs $S = \{\langle p_i, \iota_i \rangle\}_{i \in \mathbb{N}}$ where $p_i \in \mathsf{P}$. We (later) require protocols to perform correctly for any schedule, therefore, the schedule can be considered as adversarial (and not even limited by computational assumptions). On the other hand, the schedule, is defined in advance and cannot depend on the execution (or on the random bits $R \in \mathbb{R}$); in a sense, we separated the adversarial mechanisms into a non-adaptive, computationally-unlimited element (the schedule), and an adaptive, usually computationally-limited element (modeled as a protocol, or multiple protocols, in the configuration, and aware of only inputs on its interfaces). A schedule could, of course, prevent events from happening; to prevent this from being a trivial method to cause executions where the adversary wins, our definitions of games (later) consider the adversary as winning only if some event happens, rather than by the absence of some event.

A similar issue, where we tried to avoid non-determinism, involves how we handle multiple pending inputs, submitted on the same input interface. Our definition delivers inputs on an interface, in the order in which they were submitted. We do this by keeping a FIFO queue $Q[p, \iota]$, for protocol instance p and input interface ι , with regular semantics for the enqueue, dequeue, and is_non_empty operations. Other choices may be possible.

Definition 3 (Execution). Let $C = \langle \mathsf{P}, \mathsf{il}, \mathsf{ol}, \mathsf{nP}, \mathsf{nl} \rangle$ be a configuration. Let $\mathcal{S} = \{\langle p_i \in \mathsf{P}, \iota_i \in \mathsf{il}(p_i) \rangle\}_{i \in \mathbb{N}}$ be a schedule of C. Let $\Gamma : \mathsf{P} \to \Pi$ be a mapping of the protocol identifiers P to specific protocols.

The execution $X_k(C, \Gamma, \mathcal{S}; R)$ of security parameter $k \in 1^*$, configuration C, protocol mapping Γ , schedule \mathcal{S} and sequence (of random bits) $R = \{R_i\} \in \mathbb{R}$, is the sequence of execution events $\{\xi_i\} = \{\langle p_i \in \mathsf{P}, \iota_i \in \mathsf{II}(p_i), iv_i, ov_i[\cdot] \rangle$ resulting from the following process:

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FOR ALL p \in P: s[p] := \bot; Q[p_1, \iota_1]. Enqueue(0); X := \{\}

FOR i := 1 to \infty do:

If (p_i \in P, \iota_i \in I_{IN}(p_i) \text{ and } Q[p_i, \iota_i]. Is_non_empty()) then:

1. iv_i := Q[p_i, \iota_i]. Dequeue();

2. \langle S, I_{IN}, I_{OUT}, \delta \rangle := \Gamma(p_i).

3. \langle s[p_i], ov_i[\iota \in I_{OUT}] \rangle := \delta(k, s[p_i], \iota_i, iv_i; R_i);

4. \forall \iota \in I_{OUT}: If ov_i[\iota] \neq \bot

Then: Q[nP(p_i, \iota), nl(p_i, \iota]. Enqueue(ov_i[\iota]);
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Let $X_k(C, \Gamma, S)$ be the random variable $X_k(C, \Gamma, S; R)$ for $R \in_R \mathbb{R}$.

If all protocols in the range of Γ are polynomial, we say that Γ is polynomial. If Γ is polynomial, then $X_k(C, \Gamma, \mathcal{S})[l]$ is sampleable in time polynomial in k and l, where $X_k(C, \Gamma, \mathcal{S})[l]$ denotes the l first events of $X_k(C, \Gamma, \mathcal{S})$. This allows a polynomial protocol to run polynomial number of steps of an execution containing polynomial protocols, as part of its computational process (e.g. for reduction proofs). We restate this observation in the following proposition.

Proposition 1 (Executions of polynomial protocols are efficiently sampleable). Let $C = \langle P, il, ol, nP, nl \rangle$ be a configuration and $\Gamma : P \to \Pi_{poly}$ be a mapping of the protocol identifiers P to specific polynomial protocols. Then $X_k(C, \Gamma, S)[l]$ is sampleable in probabilistic polynomial time (as a function of k and l).

3 Layer Games, Models and Realizations

From this section, our discussion is focused, for simplicity, on *layered architectures*, as in Figure 1. We believe that it is not too difficult to generalize our concepts and results, but that this will cause (mostly technical) complexities, that may make the resulting definitions less easy to understand and use.

The basic idea of layered architectures, is abstraction. Namely, the designer of protocol π_i for layer i, is oblivious to details of lower layers, and only cares about the layer model of layer i-1, denoted L_{i-1} . The layer model L_{i-1} defines all possible behaviors observable to layer i, resulting from the operation of layer i-1 protocols and of all lower layers. The goal of the designer of protocol π_i , for layer i, is to ensure that when instances of π_i operate over any instantiation of Γ_{i-1} of layer model L_{i-1} , the resulting operation satisfies layer model L_i .

In the first subsection below, we give a game-based definition of a layer model, with conditions on the outcomes of the game, defining when a protocol Γ_{L} is considered to satisfy layer model L; we denote this by $\mathsf{L} \models \Gamma_{\mathsf{L}}$. In the second subsection, we define the realization relation, denoted $\mathsf{L}_U \vdash \begin{bmatrix} \pi_U \\ \mathsf{L}_L \end{bmatrix}$, indicating that protocol π_U , when running over lower layer L_L , realizes layer model L_U .

3.1 Layer Models

We define the layer model L, by a simple zero-sum (win-lose) game between an adversary protocol, with identifier A, and a layer protocol, with identifier $I_{\rm L}$. These protocols interact only via a third protocol, the experiment protocol, with identifier Exp, as shown in Figure 3. The experiment protocol defines the 'rules of the game', and in particular the outcome, which Exp produces on a designated output interface outcome. Specifically, in every execution, Exp outputs a value on outcome (at most) once, and this value is a single bit: 1 if the adversary wins (protocol failed the game), and 0 if the adversary losses (protocol passed the game). The game includes an expected winning rate $\alpha \in [0,1]$ (typically $\alpha = 0$ or $\alpha = \frac{1}{2}$), defining the expected (or permitted) probability that the adversary will win, i.e. eventually have 1 on outcome.

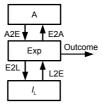


Fig. 3. Layer Model Configuration. If for every Γ_{A} holds $\Pr(\mathsf{outcome} = 1) \leq \alpha + +\mathsf{negl}(k)$, then the layer protocol Γ_{L} satisfies $\mathsf{L} = (\Gamma_{\mathsf{Exp}}, \alpha)$, or: $\mathsf{L} \models \Gamma_{\mathsf{L}}$.

We later implement layer i over layer i-1, by multiple instances of protocol π_i , one in each processor in the network. For simplicity, we assume a constant number of instances n; it seems straightforward to extend the results to allow n to be a parameter. It is convenient to define a separate input and output interfaces between the experiment and each instance. Namely, for $j \in \{1, \ldots, n\}$, the configuration includes interface $\mathsf{E2L}_j$ from Exp to I_L , and interface $\mathsf{L2E}_j$ from I_L to Exp . Finally, we use a single interface $\mathsf{E2A}$ from Exp to A , and a single interface $\mathsf{A2E}$ from A to Exp . This completes the definition of the layer modeling game configuration C_{LM} (for some constant number n of instances).

For $\phi \in \{\text{Exp}, A\}$, let $\Gamma(\phi) = \Gamma_{\phi}$ be the protocol instantiating node ϕ ; similarly, let $\Gamma(I_{\mathsf{L}}) = \Gamma_{\mathsf{L}}$ be a protocol realizing I_{L} . Given schedule \mathcal{S} , let $\operatorname{\mathsf{Exp}}_{\Gamma_{\mathsf{A}},\Gamma_{\mathsf{L}},\mathcal{S}}^{\Gamma_{\mathsf{Exp}}}(k,l;R)$ denote the output of outcome after l events in the execution $X_k(C_{LM},\Gamma,\mathcal{S};R)$, for $R \in \mathbb{R}$, or \bot if there was no such output.

Definition 4 (Layer model). A (polynomial) layer model is a pair $L = (\Gamma_{\mathsf{Exp}}, \alpha)$, where Γ_{Exp} is a (polynomial) protocol and $\alpha \in [0, 1]$. We say that protocol $\Gamma_{\mathsf{L}} \in \Pi_{\mathsf{poly}}$ computationally satisfies layer model L, and write $L \models_{\mathsf{poly}} \Gamma_{\mathsf{L}}$, if for every $\Gamma_{\mathsf{A}} \in \Pi_{\mathsf{poly}}$, schedule S, polynomial l and large enough k, holds:

$$\Pr_{R \in \mathbb{R}} \left(\mathsf{Exp}_{\varGamma_{\mathsf{A}},\varGamma_{\mathsf{L}},\mathcal{S}}^{\varGamma_{\mathsf{Exp}}}(k,l(k);R) = 1 \right) \leq \alpha + \mathit{negl}(k)$$

where negl is some negligible function (asymptotically smaller than any strictly positive polynomial), and $\operatorname{Exp}_{\Gamma_{\!\!A},\Gamma_{\!\!L},\mathcal{S}}^{\Gamma_{\!\!Exp}}(k,l;R)$ is defined as above.

Protocol Γ_L statistically satisfies L, if the above holds when protocols are not required to be polynomial, and perfectly satisfies L if this holds even when we remove the negl(k) term. These notions are denoted $L \models_{\sf stat} \Gamma_L$ and $L \models_{\sf perf} \Gamma_L$, respectively.

We observe the trivial relation among the three notions of satisfaction.

Proposition 2. For any layer model L and any protocol Γ_L holds:

$$\mathsf{L} \models_{\mathsf{perf}} \varGamma_{\mathsf{L}} \Rightarrow \mathsf{L} \models_{\mathsf{stat}} \varGamma_{\mathsf{L}} \Rightarrow \mathsf{L} \models_{\mathsf{poly}} \varGamma_{\mathsf{L}}$$

Notation: we may write $L \models \Gamma_L$, when it is obvious that we refer to \models_{poly} .

3.2 Layer Realization Indistinguishability Game

We now define and investigate another game, which we call *indistinguishable* layer realization games, which is similar to indistinguishability games used in many cryptographic definitions, e.g. pseudo-random functions [19], and especially to the 'left-or-right indistinguishability' (LOR) of [7]. Layer realization games are convenient for the common layered and modular ('top-down') design methodologies. As in previous sections, we had to tradeoff generality for simplicity and ease-of-use.

The configuration of layer realization indistinguishability games is illustrated in Figure 4. Like in layer model games, the configuration contains nodes A, Exp and I_L , where A and I_L are connected only via Exp. There are n+1 additional nodes, where n is the (constant) number of instances: n realization nodes (instances) $\{R_i\}_{i=1,...,n}$, and one lower layer node I_{LL} .

As in the layer model games, without loss of generality, we use a single input and output interface from the experiment (or 'higher layer') to each instance in I_L , and therefore we will have the interfaces $\mathsf{E2L}_j$, $\mathsf{L2E}_j$, $\mathsf{E2A}$ and $\mathsf{A2E}$ as before. The configuration also includes interfaces $\mathsf{E2R}_j$, $\mathsf{R2E}_j$, $\mathsf{R2L}_j$ and $\mathsf{L2R}_j$, connecting between Exp and R , and between R and I_{LL} . This completes the definition of the layer realization configuration C_{LR} (for a fixed number n of instances).

All the realization nodes are instantiated by (mapped to) the same protocol π , which is tested for realization of layer L over lower layer LL. Namely, $(\forall j \in \{1,\ldots,n\})\Gamma(\mathsf{R}_j) = \pi$, where Γ is the mapping we will use in the execution of the game (with n instances).

In layer realization indistinguishability games, we use a specific experiment protocol $\operatorname{Exp}^{\mathsf{IND}}$, which we define below, i.e. $\Gamma(\operatorname{Exp}) = \operatorname{Exp}^{\mathsf{IND}}$. Here are some basic details about $\operatorname{Exp}^{\mathsf{IND}}$. Upon initialization, $\operatorname{Exp}^{\mathsf{IND}}$ flips a fair $\operatorname{coin} b \in_R \{L, R\}$, where L stands for either Layer or Left, and R stands for either Realization or Right. The game ends when $\operatorname{Exp}^{\mathsf{IND}}$ receives a guess b' of either L or R from the adversary A, which arrives on a dedicated Guess input interface. Upon receiving the guess b', $\operatorname{Exp}^{\mathsf{IND}}$ outputs on its outcome output interface 1 if b=b', and 0 otherwise.

Given adversary protocol $\Gamma(A) = \Gamma_A$, protocols for the two layers $\Gamma(I_L) = \Gamma_L$, $\Gamma(I_{LL}) = \Gamma_{LL}$, sequence of random bit sequences $R \in \mathbb{R}$ and schedule S, let $\mathsf{Exp}^{\mathsf{IND}}_{\Gamma_A,\Gamma_L,\Gamma_{LL},\pi,S}(k,l;R)$ denote the output of outcome after l events in the execution $X_k(C_{LR},\Gamma,S;R)$, or \bot if there was no such output.

Definition 5 (Layer realization). Let L, LL be two polynomial layer models. Protocol π computationally realizes layer model L over layer model LL, which we denote by $L \vdash_{\mathsf{poly}} \begin{bmatrix} \pi \\ LL \end{bmatrix}$, if for every polynomial algorithm Γ_{LL} s.t. $LL \models \Gamma_{\mathsf{LL}}$, there exists a polynomial algorithm Γ_{L} s.t. $L \models \Gamma_{\mathsf{L}}$, s.t. every polynomial algorithm Γ_{A} and for every schedule S and every polynomial l, for sufficiently large k holds

$$\Pr_{R \in \mathbb{R}} \left(\mathsf{Exp}^{\mathsf{IND}}_{\Gamma_{\mathsf{A}}, \Gamma_{\mathsf{L}}, \Gamma_{\mathsf{LL}}, \pi, \mathcal{S}}(k, l(k); R) = 1 \right) \leq \frac{1}{2} + \mathsf{negl}(k)$$

Protocol π statistically realizes layer model L over layer model LL, which we denote by $L \vdash_{\mathsf{stat}} \left[\overset{\pi}{\mathsf{LL}} \right]$, if the above holds when protocols are not required to be polynomial, and perfectly realizes L over LL, which we denote by $L \vdash_{\mathsf{perf}} \left[\overset{\pi}{\mathsf{LL}} \right]$ if this holds even when we remove the $\mathsf{negl}(k)$ term.

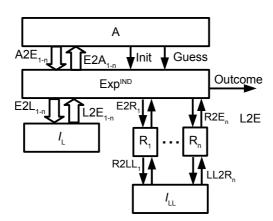


Fig. 4. The Layer Realization Indistinguishability game. Protocol π realizes layer L over layer LL, if for every adversary Γ_{A} and every lower-layer protocol Γ_{LL} , there is some protocol Γ_{L} satisfying layer model L, s.t. the adversary cannot distinguish between Γ_{L} and between the composition of n instances of π over Γ_{LL} .

In summary, protocol π realizes layer model Lover layer model LL, if for every adversary protocol Γ_{L} and every lower-layer protocol Γ_{LL} , there is some protocol Γ_{L} satisfying layer L, s.t. the Γ_{A} cannot distinguish between interacting with Γ_{L} and interacting with π operating over Γ_{LL} , where Γ_{A} interacts only via Exp^{IND}. Intuitively, Γ_{LL}^{π} is a good implementation of L, if the adversary A cannot

distinguish between it and between some protocol Γ_L which satisfies L, when interacting via $\mathsf{Exp}^\mathsf{IND}$, better than the trivial winning rate of $\frac{1}{2}$. To complete the description, we now present the *indistinguishability experiment* $\mathsf{Exp}^\mathsf{IND}$.

Definition 6 (Layer realization indistinguishability experiment). Let $\mathsf{Exp}^{\mathsf{IND}} = \langle S, I_{IN}, I_{OUT}, \delta \rangle$ be the following protocol:

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\begin{split} S &= \{\bot, \mathsf{testing}, \mathsf{done} \} \\ I_{IN} &= \{\mathsf{Init}, \mathsf{Guess} \} \cup \{\mathsf{A2E}_j\}_{j=1,...,n} \cup \{\mathsf{L2E}_j\}_{j=1,...,n} \cup \{\mathsf{R2E}_j\}_{j=1,...,n} \\ I_{OUT} &= \{\mathsf{outcome} \} \cup \{\mathsf{E2A}_j\}_{j=1,...,n} \cup \{\mathsf{E2L}_j\}_{j=1,...,n} \cup \{\mathsf{E2R}_j\}_{j=1,...,n} \\ \delta &\cdot \end{split}
```

- 1. In initialization state \bot , upon any input, select randomly $b \in_R \{L, R\}$, and move to testing state.
- 2. In testing state, pass all input events on interface $A2E_i$, for $i \in \{1, ..., n\}$, to corresponding output event on output interface $E2L_i$ (if b = L) or $E2R_i$ (if b = R), and all input events on interfaces $L2E_i$ (if b = L) or $R2E_i$ (if b = R), to corresponding output events on interface $E2A_i$.
- 3. When, in testing state, the guess input interface Guess is invoked with input (guess) $b' \in \{L,R\}$, output on outcome the value 1 if b=b', and 0 otherwise ($b \neq b'$). Move to the done state (and ignores all further inputs).

4 The Fundamental Lemma of Layering

We now show the fundamental lemma of layering, allowing compositions of protocols of multiple layers. This provides firm foundations to the accepted methodology of designing, implementing, analyzing and testing of each layer independently, yet relying on their composition to ensure expected properties.

We first need to define layering of *protocols*. We actually consider two different variants of protocol layering:

- Layering of two realization protocols π_{L} , π_{LL} . As discussed, we assumed (for simplicity) that there are n instantiations of the realization protocol of each layer; each of these has two input interfaces and two output interfaces, one for the higher layer and one for the lower layer. We define $\pi_{\mathsf{LL}||\mathsf{L}} = \begin{bmatrix} \pi_{\mathsf{LL}}^{\mathsf{L}} \end{bmatrix}$ in the obvious way.
- Layering of the n instances of the realization protocol π_{L} , on top of a protocol realizing the lower-layer model Γ_{LL} . We define $\Gamma_{\mathsf{LL}||\mathsf{L}} = \begin{bmatrix} \pi_{\mathsf{L}} \\ \Gamma_{\mathsf{LL}} \end{bmatrix}$ in the obvious way.

Note our convention of using π_x for protocols instantiating realizations (of n instances), and Λ_x for instantiations of a (lower) layer model. Also, note that if π_L and π_{LL} (or Γ_{LL}) are polynomial, then $\Gamma_{LL||L}$ is also polynomial.

We first present the 'composition preserves satisfaction' lemma, which justifies considering abstraction of all lower layers, into a single 'virtual protocol'. For both this and the fundamental lemma of layering (below), we present only the computational version (the statistical and perfect versions are similar).

Lemma 1 (Composition preserves satisfaction). Let L, LL be two polynomial layer models, and π_{L} , Γ_{LL} be polynomial protocols, such that π_{L} computationally realizes L over LL, namely $L \vdash_{\mathsf{poly}} \left[\overset{\pi_{\mathsf{L}}}{\mathsf{LL}} \right]$, and and Γ_{LL} computationally satisfies LL, namely LL $\models_{poly} \Gamma_{LL}$. Then the composite protocol $\Gamma_{LL||L}$ satisfies L, namely $L \models_{poly} \Gamma_{LL||L}$. Or, as a formula:

$$\left(\mathsf{L} \vdash_{\mathsf{poly}} \left[\begin{smallmatrix} \pi_\mathsf{L} \\ \mathsf{L} \mathsf{L} \end{smallmatrix} \right] \right) \bigwedge \left(\mathsf{L} \mathsf{L} \models_{\mathsf{poly}} \varGamma_\mathsf{LL} \right) \Rightarrow \left(\mathsf{L} \models_{\mathsf{poly}} \varGamma_\mathsf{LL||\mathsf{L}} \right)$$

The composite realization lemma shows that we can prove realization of each layer separately, and the composition of the realizations will be a realization of the highest layer over the lowest layer. We state the lemma for only three layers - generalization for an arbitrary stack is immediate.

Lemma 2 (The Fundamental Lemma of Layering). Let L_3, L_2, L_1 be three polynomial layer models, and π_2, π_3 be polynomial protocols, such that π_3 compu-

tationally realizes L_3 over L_2 , and π_2 computationally realizes L_2 over L_1 . Then $\pi_{2||3} = \begin{bmatrix} \pi_3 \\ \pi_2 \end{bmatrix}$ computationally realizes L_3 over L_1 .

Furthermore, let Γ_{L_1} be a polynomial protocol that computationally satisfies L_1 , namely $L_1 \models_{\mathsf{poly}} \Gamma_{L_1}$. Then $\Gamma_{1||2||3} = \begin{bmatrix} \pi_{2||3} \\ \Gamma_1 \end{bmatrix}$ satisfies L_3 , i.e. $L_3 \models_{\mathsf{poly}} \Gamma_{1||2||3}$.

Conclusions and Research Directions 5

In this work, we try to lay solid, rigorous foundations, to the important methodology of layered decomposition of distributed systems and network protocols, particularly concerning security in adversarial settings. The framework is built on previous works on modeling and analysis of (secure) distributed systems, as described in the introduction, but it is clearly a very ambitious goal, possibly overambitious, and certainly beyond the reach of a single publication. There are many directions that require further research. Here are some:

- The best way to test and improve such a framework, is simply by using it to analyze different problems and protocols; there are many interesting and important problems, that can benefit from such analysis. As one important example, consider the secure channel layer problem. Many protocols and applications assume they operate over 'secure, reliable connections'. In practice, this is often done using the standard layers in Figure 1, in one of two methods. In the first method, we use TLS (for security) over TCP (for reliability) over the 'best effort' service of IP. In the second method, we use TCP (for reliability) over IP-Sec (for security), again over 'best effort' (IP). It would be interesting to define a 'secure, reliable connection' layer, and to analyze these two methods with respect to it.
- There are many desirable extensions to the framework, including: support for corruptions of nodes, including adaptive and/or mobile corruptions (proactive security and forward security); adaptive control of the number of nodes; support for side channels such as timing and power.

- In this work, we focused on layered configurations. These are sufficient for many scenarios. However, there are other scenarios. It would be interesting to identify important non-layered scenarios, and find appropriate games, specifications and composition properties, which will support them, possibly as generalizations of our definitions and results.
- It would be interested to explore the relationships between the layered games framework, and other formal frameworks for study of distributed algorithms and protocols (see introduction).
- The framework is based on the computational approach to security, where attackers can compute arbitrary functions on information available to it (e.g. ciphertext). Many results and tools are based on symbolic analysis, see introduction (and [18, 10, 1]). It can be very useful to find how to apply such techniques and tools, within the framework.

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