

Chi-Keong Goh and Kay Chen Tan

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Evolutionary Multi-objective Optimization in Uncertain Environments

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Chi-Keong Goh  
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# Evolutionary Multi-objective Optimization in Uncertain Environments

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# Preface

Many real-world problems involve the simultaneous optimization of several competing objectives and constraints that are difficult, if not impossible, to solve without the aid of powerful optimization algorithms. What makes multi-objective optimization so challenging is that, in the presence of conflicting specifications, no one solution is optimal to all objectives and optimization algorithms must be capable of finding a number of alternative solutions representing the tradeoffs. However, multi-objectivity is just one facet of real-world applications. Most optimization problems are also characterized by various forms of uncertainties stemming from factors such as data incompleteness and uncertainties, environmental conditions uncertainties, and solutions that cannot be implemented exactly.

Evolutionary algorithms are a class of stochastic search methods that have been found to be very efficient and effective in solving sophisticated multi-objective problems where conventional optimization tools fail to work well. Evolutionary algorithms' advantage can be attributed to it's capability of sampling multiple candidate solutions simultaneously, a task that most classical multi-objective optimization techniques are found to be wanting. Much work has been done to the development of these algorithms in the past decade and it is finding increasingly application to the fields of bioinformatics, logical circuit design, control engineering and resource allocation. Interestingly, many researchers in the field of evolutionary multi-objective optimization assume that the optimization problems are deterministic, and uncertainties are rarely examined. While multi-objective evolutionary algorithms draw its inspiration from nature where uncertainty is a common phenomenon, it cannot be taken for granted that these algorithms will hence be inherently robust to uncertainties without any further investigation.

The primary motivation of this work is to provide a comprehensive treatment on the design and application of multi-objective evolutionary algorithms for multi-objective optimization in the presence of uncertainties. Chapter 1 provides the necessary background information required to appreciate this work, covering key concepts and definitions of multi-objective optimization

as well as a survey of the state-of-the-arts which highlights the major design issues of multi-objective evolutionary techniques.

The rest of this work is divided into three parts, which each part considering a different form of uncertainties: 1) noisy fitness functions, 2) dynamic fitness functions, and 3) robust optimization. The first part comprises of Chapters 2-4 and addresses the issues of noisy fitness functions. Chapter 2 investigates the effect of noise on multi-objective evolutionary algorithms and Chapter 3 provides a comprehensive survey of noisy evolutionary multi-objective optimization literature and presents a comparative study between existing algorithms for noisy multi-objective optimization. As a specific instance of a noisy multi-objective problem, Chapter 4 presents a hybrid multi-objective evolutionary algorithm for the evolution of artificial neural network classifiers.

Part II is concerned with dynamic multi-objective optimization and comprises of Chapters 5 and 6. Chapter 5 provides a survey of dynamic evolutionary multi-objective optimization literature as well as a discussion on the different types of dynamic multi-objective test functions and performance indicators. Chapter 6 extends the notion of coevolution to track the Pareto front in a dynamic environment. Since problem characteristics may change with time, it is not possible to determine one best approach to problem decomposition. Therefore, this chapter introduces a new coevolutionary paradigm that incorporates both competitive and cooperative mechanisms observed in nature to facilitate the adaptation and emergence of the decomposition process with time.

The final part of this work addresses the issues of robust multi-objective optimization where the optimality of the solutions is sensitive to parameter variations. Analyzing the existing benchmarks applied in the literature reveals that the current corpus has severe limitations. Therefore, Chapter 7 presents a robust multi-objective test suite with noise-induced solution space, fitness landscape and decision space variation. In addition, the vehicle routing problem with stochastic demand (VRPSD) is presented a practical example of robust combinatorial multi-objective optimization problems. A survey of existing robust multi-objective evolutionary techniques are presented in Chapter 8 and simulations are conducted to solve the test suite suggested in Chapter 7. In Chapter 9, a hybrid MOEA is developed to optimize robust route schedules for the VRPSD problem.

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# Contents

<b>1</b>	<b>Introduction</b>	<b>1</b>
1.1	Multi-objective Optimization	1
1.1.1	Totally Conflicting, Non-conflicting, and Partially Conflicting Multi-objective Problems	2
1.1.2	Pareto Dominance and Optimality	3
1.1.3	Multi-objective Optimization Goals	5
1.2	Evolutionary Multi-objective Optimization	5
1.2.1	MOEA Framework	6
1.2.2	Basic MOEA Components	8
1.2.3	Benchmark Problems	16
1.2.4	Performance Metrics	18
1.3	Empirical Analysis and Performance Assessment	
Adequacy for EMO Techniques	21	
1.3.1	Preliminary Discussions	21
1.3.2	Systematic Design for Empirical Assessment	25
1.3.3	Survey on Experimental Specifications	31
1.3.4	Conceptualizing Empirical Adequacy	33
1.3.5	Case Studies	36
1.4	Overview of This Book	38
1.5	Conclusion	39

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## Part I: Evolving Solution Sets in the Presence of Noise

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<b>2</b>	<b>Noisy Evolutionary Multi-objective Optimization</b>	<b>43</b>
2.1	Noisy Multi-objective Optimization Problems	44
2.2	Performance Metrics for Noisy Multi-objective Optimization	45
2.3	Empirical Results of Noise Impact	46

2.3.1	General MOEA Behavior under Different Noise Levels .....	47
2.3.2	MOEA Behavior in the Objective Space .....	50
2.3.3	MOEA Behavior in Decision Space .....	53
2.4	Conclusion .....	54
<b>3</b>	<b>Handling Noise in Evolutionary Multi-objective Optimization .....</b>	<b>55</b>
3.1	Estimate Strength Pareto Evolutionary Algorithm .....	56
3.2	Multi-Objective Probabilistic Selection Evolutionary Algorithm .....	60
3.3	Noise Tolerant Strength Pareto Evolutionary Algorithm .....	63
3.4	Modified Non-dominated Sorting Genetic Algorithm II .....	65
3.5	Multi-objective Evolutionary Algorithm for Epistemic Uncertainty .....	67
3.6	Indicator-Based Evolutionary Algorithm for Multi-objective Optimization .....	70
3.7	Multi-Objective Evolutionary Algorithm with Robust Features .....	72
3.8	Comparative Study .....	80
3.9	Effects of the Proposed Features .....	92
3.10	Further Examination .....	97
3.11	Conclusion .....	98
<b>4</b>	<b>Handling Noise in Evolutionary Neural Network Design .....</b>	<b>101</b>
4.1	Singular Value Decomposition for ANN Design .....	102
4.1.1	Rank-Revealing Decomposition .....	102
4.1.2	Actual Rank of Hidden Neuron Matrix .....	103
4.1.3	Estimating the Threshold .....	106
4.1.4	Moore-Penrose Generalized Pseudoinverse .....	107
4.2	Hybrid Multi-Objective Evolutionary Neural Networks .....	107
4.2.1	Algorithmic Flow of HMOEN .....	107
4.2.2	Multi-objective Fitness Evaluation .....	108
4.2.3	Variable-Length Representation for ANN Structure .....	109
4.2.4	SVD-Based Architectural Recombination .....	109
4.2.5	Micro-Hybrid Genetic Algorithm .....	112
4.3	Experimental Study .....	114
4.3.1	Experimental Setup .....	114
4.3.2	Analysis of HMOEN Performance .....	116
4.4	Conclusion .....	121

---

**Part II: Tracking Dynamic Multi-objective Landscapes**

---

<b>5</b>	<b>Dynamic Evolutionary Multi-objective Optimization</b>	125
5.1	Dynamic Multi-objective Optimization Problems	126
5.2	Dynamic Multi-objective Problem Categorization	126
5.3	Dynamic Multi-objective Test Problems	128
5.3.1	TLK2 Dynamic Test Function	129
5.3.2	FDA Dynamic Test Functions	130
5.3.3	dMOP Test Functions	131
5.3.4	DSW Test Functions	133
5.3.5	JS Test Functions	134
5.4	Performance Metrics for Dynamic Multi-objective Optimization	135
5.4.1	Illustrating Performance Using Static Performance Measures	135
5.4.2	Time Averaging Static Performance Measures	136
5.5	Evolutionary Dynamic Optimization Techniques	138
5.5.1	Design Issues	138
5.5.2	Directional-Based Dynamic Evolutionary Multi-objective Optimization Algorithm	141
5.5.3	Dynamic Non-dominated Sorting Genetic Algorithm II	142
5.5.4	Dynamic Multi-objective Evolutionary Algorithm Based on an Orthogonal Design	144
5.5.5	Dynamic Queuing Multi-objective Optimizer	146
5.5.6	Multi-objective Immune Algorithm	148
5.6	Conclusion	152
<b>6</b>	<b>A Coevolutionary Paradigm for Dynamic Multi-Objective Optimization</b>	153
6.1	Competition, Cooperation, and Competitive-Cooperation in Coevolution	154
6.1.1	Competitive Coevolution	154
6.1.2	Cooperative Coevolution	155
6.1.3	Competitive-Cooperative Coevolution	158
6.2	Applying Competitive-Cooperation Coevolution for Multi-objective Optimization	160
6.2.1	Cooperative Mechanism	161
6.2.2	Competitive Mechanism	162
6.2.3	Implementation	164
6.3	Adapting COEA for Dynamic Multi-objective Optimization	165
6.3.1	Introducing Diversity via Stochastic Competitors	165
6.3.2	Handling Outdated Archived Solutions	167

6.4	Static Environment Empirical Study .....	168
6.4.1	Comparative Study of COEA .....	168
6.4.2	Effects of the Competitive Mechanism .....	172
6.4.3	Effects of Different Competition Schemes.....	174
6.5	Dynamic Environment Empirical Study .....	177
6.5.1	Comparative Study .....	177
6.5.2	Effects of Stochastic Competitors .....	182
6.5.3	Effects of Temporal Memory .....	182
6.6	Conclusion .....	185

---

**Part III: Evolving Robust Solution Sets**

---

7	<b>Robust Evolutionary Multi-objective Optimization .....</b>	189
7.1	Robust Multi-objective Optimization Problems .....	189
7.2	Robust Measures .....	190
7.3	Robust Optimization Problems .....	191
7.4	Robust Continuous Multi-objective Test Problem Design ...	192
7.4.1	Robust Multi-objective Problem Categorization ...	192
7.4.2	Empirical Analysis of Existing Benchmark Features .....	194
7.5	Robust Continuous Multi-objective Test Problem Design ...	197
7.5.1	Basic Landscape Generation .....	199
7.5.2	Changing the Decision Space .....	202
7.5.3	Changing the Solution Space.....	202
7.5.4	Example of a Robust Multi-objective Test Suite .....	203
7.6	Vehicle Routing Problem with Stochastic Demand .....	207
7.6.1	Problem Features .....	208
7.6.2	Problem Formulation .....	210
7.7	Conclusion .....	211
8	<b>Evolving Robust Solutions in Multi-Objective Optimization .....</b>	213
8.1	Evolutionary Robust Optimization Techniques .....	214
8.1.1	Single-Objective Approach.....	214
8.1.2	Multi-objective Approach .....	215
8.1.3	Robust Multi-Objective Optimization Evolutionary Algorithm .....	216
8.2	Empirical Analysis .....	219
8.2.1	Fitness Inheritance for Robust Optimization .....	219
8.2.2	Evaluating GTCO Test Suite .....	219
8.2.3	Evaluating VRPSD Test Problems.....	225
8.3	Conclusion .....	227

<b>9 Evolving Robust Routes . . . . .</b>	229
9.1 Overview of Existing Works . . . . .	229
9.2 Hybrid Evolutionary Multi-Objective Optimization . . . . .	230
9.2.1 Variable-Length Chromosome . . . . .	231
9.2.2 Local Search Exploitation . . . . .	232
9.2.3 Route-Exchange Crossover . . . . .	232
9.2.4 Multi-mode Mutation . . . . .	233
9.2.5 Route Simulation Method . . . . .	235
9.2.6 Computing Budget . . . . .	236
9.2.7 Algorithmic Flow of HMOEA . . . . .	237
9.3 Simulation Results and Analysis . . . . .	238
9.3.1 Performance of Hybrid Local Search . . . . .	239
9.3.2 Comparison with a Deterministic Approach . . . . .	241
9.3.3 Effects of Sample Size, H . . . . .	244
9.3.4 Effects of M . . . . .	246
9.4 Conclusion . . . . .	247
<b>10 Final Thoughts . . . . .</b>	249
<b>References . . . . .</b>	253