

# Springer Tracts in Advanced Robotics

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Cyrill Stachniss

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# Robotic Mapping and Exploration

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For Janna and Maren

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## Series Editor's Foreword

By the dawn of the new millennium, robotics has undergone a major transformation in scope and dimensions. This expansion has been brought about by the maturity of the field and the advances in its related technologies. From a largely dominant industrial focus, robotics has been rapidly expanding into the challenges of the human world. The new generation of robots is expected to safely and dependably co-habitat with humans in homes, workplaces, and communities, providing support in services, entertainment, education, health-care, manufacturing, and assistance.

Beyond its impact on physical robots, the body of knowledge robotics has produced is revealing a much wider range of applications reaching across diverse research areas and scientific disciplines, such as: biomechanics, haptics, neurosciences, virtual simulation, animation, surgery, and sensor networks among others. In return, the challenges of the new emerging areas are providing an abundant source of stimulation and insights for the field of robotics. It is indeed at the intersection of disciplines that the most striking advances happen.

The goal of the series of Springer Tracts in Advanced Robotics (STAR) is to bring, in a timely fashion, the latest advances and developments in robotics on the basis of their significance and quality. It is our hope that the wider dissemination of research developments will stimulate more exchanges and collaborations among the research community and contribute to further advancement of this rapidly growing field.

The monograph written by Cyrill Stachniss is a contribution in the area of self-localization and mapping (SLAM) for autonomous robots, which has been receiving a great deal of attention by the research community in the latest few years. The contents expand the authors doctoral dissertation and are focused on the autonomous mapping learning problem. Solutions include uncertainty-driven exploration, active loop closing, coordination of multiple robots, learning and incorporating background knowledge, and dealing with dynamic environments. Results are accompanied by a rich set of experiments, revealing a promising outlook toward the application to a wide range of

mobile robots and field settings, such as search and rescue, transportation tasks, or automated vacuum cleaning.

Yet another STAR volume on SLAM, a very fine addition to the series!

Naples, Italy  
February 2009

Bruno Siciliano  
STAR Editor

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## Foreword

Simultaneous localization and mapping is a highly important and active area in mobile robotics. The ability to autonomously build maps is widely regarded as one of the fundamental preconditions for truly autonomous mobile robots. In the past, the SLAM has mostly been addressed as a state estimation problem and the incorporation of control into the map learning and localization process is a highly interesting research question. In this book by Cyrill Stachniss, the reader will find interesting and innovative solutions to the problem of incorporating control into the SLAM problem. I know Cyrill since over eight years and I still appreciate his enthusiasm in developing new ideas and getting things done. He has been working with a large number of different robots, participating in several public demonstrations, and has gained a lot of experience which can also be seen from his large number of papers presented at all major robotic conferences and in journals. His work covers a variety of different topics. He has acquired several project grants and received several awards. He furthermore is an associate editor of the IEEE Transactions on Robotics. It's safe to say that he is an expert in his field.

This book is a comprehensive introduction to state-of-the-art technology in robotic exploration and map building. The reader will find a series of solutions to challenging problems robots are faced with in the real world when they need to acquire a model of their surroundings. The book focuses on autonomy and thus the robot is not supposed to be joysticked though the world but should be able to decide about his actions on its own. I regard the ability to learn maps by making own decisions as a key competence for autonomous robots. Cyrill rigorously applies probabilistic and decision-theoretic concepts to systematically reducing the uncertainty in the belief of a robot about its environment and its pose in the environment.

The book contains impressively demonstrates the capabilities of the described solutions by showing results obtained from real robotic datasets. A further strength lies in the sound and thorough evaluation of all presented techniques going beyond the world of simulation. At this point, I would like to encourage the reader to follow Cyrill's example to take real

robots and data obtained with real robots to demonstrate that novel approaches work in reality. For readers not in possession of particular sensors or for comparison purposes, Cyrill and colleagues have created a Web site (<http://www.openslam.org/>) in which the community can share implementations of SLAM approaches and where the reader will find links to datasets to support future research.

Freiburg, Germany  
February 2009

Wolfram Burgard

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## Preface

Models of the environment are needed for a wide range of robotic applications including search and rescue, transportation tasks, or automated vacuum cleaning. Learning maps has therefore been a major research topic in the robotics community over the last decades. Robots that are able to reliably acquire an accurate model of their environment on their own are regarded as fulfilling a major precondition of truly autonomous agents. To autonomously solve the map learning problem, a robot has to address mapping, localization, and path planning at the same time. In general, these three tasks cannot be decoupled and solved independently. Map learning is thus referred to as the simultaneous planning, localization, and mapping problem. Because of the coupling between these tasks, this is a complex problem. It can become even more complex when there are dynamic changes in the environment or several robots are being used together to solve the problem.

This book presents solutions to various aspects of the autonomous map learning problem. The book is separated into two parts. In the first part, we assume the position of the robot to be known. This assumption does not hold in the real world, however, it makes life easier and allows us to better concentrate on certain aspects of the exploration problem such as coordinating a team of robots. We describe how to achieve appropriate collaboration among exploring robots so that they efficiently solve their joint task. We furthermore provide a technique to learn and make use of background knowledge about typical spatial structures when exploring an environment as a team.

In the second part, we relax the assumption that the pose of the robot is known. To deal with the uncertainty in the pose of a robot, we present an efficient solution to the simultaneous localization and mapping problem. The difficulty in this context is to build a map while at the same time localizing the robot in this map. The presented approach maintains a joint posterior about the trajectory of the robot and the model of the environment. It produces accurate maps in an efficient and robust way. After addressing step-by-step the different problems in the context of active map learning, we integrate the main techniques into a single system. We present an integrated approach

that simultaneously deals with mapping, localization, and path planning. It seeks to minimize the uncertainty in the map and in the trajectory estimate based on the expected information gain of future actions. It takes into account potential observation sequences to estimate the uncertainty reduction in the world model when carrying out a specific action. Additionally, we focus on mapping and localization in non-static environments. The approach allows a robot to consider different spatial configurations of the environment and in this way makes the pose estimate more robust and accurate in non-static worlds.

In sum, the contributions of this book are solutions to various problems of the autonomous map learning problem including uncertainty-driven exploration, SLAM, active loop closing, coordination of multiple robots, learning and incorporating background knowledge, and dealing with dynamic environments.

A lot of the work presented in this book has been done in collaboration with other researchers. It was a pleasure for me to work with all the wonderful people in the AIS lab in Freiburg. First of all, I thank Wolfram Burgard for his tremendous support, his inspiration, and for providing a creative atmosphere. My thanks to my friends and colleagues for the great time in the lab, especially to Maren Bennewitz, Giorgio Grisetti, Dirk Hähnel, Óscar Martínez Mozos, Patrick Pfaff, Christian Plagemann, and Axel Rottmann for the great collaboration on the topics addressed in this book. It was a pleasure to work with all these people and to benefit from their knowledge. My thanks also to Mark Moors and Frank Schneider for the collaboration on multi-robot exploration. Special thanks to Nick Roy and Mike Montemerlo who did a great job in developing and maintaining the Carnegie Mellon Robot Navigation Toolkit. It was a pleasure for me to work together with all of them.

Additionally, I thank several people, who published robot datasets and in this way helped to make mapping approaches more robust and more easily comparable. In this context, I would like to thank Patrick Beeson, Mike Bosse, Udo Frese, Steffen Gutmann, Dirk Hähnel, Andrew Howard, and Nick Roy.

Freiburg, Germany  
December 2008

Cyrill Stachniss

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## Part I: Exploration with Known Poses

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## Notation

Throughout this book, we make use of the following notation:

| variable                   | description                                                                                                                                              |
|----------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------|
| $x_t$                      | pose of the robot at time step $t$ . This pose is a three dimensional vector containing the $x, y$ -position and the orientation $\theta$ of the vehicle |
| $x_{1:t}$                  | sequence of poses of the robot from time step 1 to time step $t$                                                                                         |
| $z_t$                      | sensor observation obtained at time step $t$                                                                                                             |
| $u_t$                      | odometry information describing the movement from $x_t$ to $x_{t+1}$                                                                                     |
| $a$                        | action or motion command                                                                                                                                 |
| $w$                        | importance weight                                                                                                                                        |
| $w_t^{[i]}$                | importance weight of the $i$ -th particle at time step $t$                                                                                               |
| $m$                        | grid map                                                                                                                                                 |
| $c$                        | grid cell                                                                                                                                                |
| $r$                        | resolution of a grid map. Each cell covers an area of $r$ by $r$ .                                                                                       |
| $\mathcal{G}$              | topological map                                                                                                                                          |
| $E[\cdot]$                 | expectation                                                                                                                                              |
| $\mathcal{N}(\mu, \Sigma)$ | Gaussian with mean $\mu$ and covariance $\Sigma$                                                                                                         |
| $H$                        | entropy                                                                                                                                                  |
| $I$                        | information gain                                                                                                                                         |
| $U$                        | utility function                                                                                                                                         |
| $V$                        | cost function                                                                                                                                            |
| $\eta$                     | normalizer, typically resulting from Bayes' rule                                                                                                         |
| $N_{eff}$                  | effective number of particles                                                                                                                            |