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Ludomir M. Laudański

Between Certainty and Uncertainty

Statistics and Probability in Five Units with Notes on Historical Origins and Illustrative Numerical Examples

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Ludomir M. Laudański

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