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Prof. Janusz Kacprzyk
Systems Research Institute
Polish Academy of Sciences
ul. Newelska 6
01-447 Warsaw
Poland
E-mail: kacprzyk@ibspan.waw.pl

Prof. Lakhmi C. Jain
University of South Australia
Adelaide
Mawson Lakes Campus
South Australia 5095
Australia
E-mail: Lakhmi.jain@unisa.edu.au

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Between Certainty and Uncertainty

Statistics and Probability in Five Units
with Notes on Historical Origins and Illustrative
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Author

Ludomir M. Laudanski
Rzeszow Technical University
Rzeszow
Poland

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Ludomir M. Laudański

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