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IN SCIENCE AND TECHNOLOGY IN CHINA

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Zengchang Qin
Yongchuan Tang

Uncertainty Modeling for Data Mining

A Label Semantics Approach

With 61 figures

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Authors
Prof. Zengchang Qin
Intelligent Computing and Machine Learning Lab, School of ASEE,
Beihang University, Beijing, China
E-mail: zengchang.qin@gmail.com

Prof. Yongchuan Tang
College of Computer Science
Zhejiang University,
Hangzhou, Zhejiang, China
E-mail: tyongchuan@gmail.com

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This book is dedicated to my parents Li-zhong Qin (1939–1995) and Feng-xia Zhang (1936–2003)

Zengchang Qin

Preface

Uncertainty is one of the characteristics of the nature. Many theories have been proposed in dealing with uncertainties. Fuzzy logic has been one of such theories. Both of us were inspired by Zadeh's fuzzy theory and Jonathan Lawry's label semantics theory when we both worked in University of Bristol.

Machine learning and data mining are inseparably connected with uncertainty. To begin with, the observable data for learning is usually imprecise, incomplete or noisy. Even the observations are perfect, the generalization beyond that data is still afflicted with uncertainty; e.g., how can we be sure which one from a set of candidate theories that all of them explain the data. Though Occam's razor tells us to favor the simplest models, this principle does not guarantee this simple model is the truth of the data. In recent research, we have found that some complex models seem to be more appropriate comparing to simple ones because of our complex nature and the complicated mechanism of data generation in social problems.

In this book, we introduce a fuzzy logic basesd theory for modeling uncertainty in data mining. The content of this book can be roughly split into three parts: Chapters 1-3 give a general introduction of data mining and the basics of label semantics theory. Chapters 4–8 introduce a number of data mining algorithms based on label semantics and detailed theoretical aspects, and experimental results are given. Chapters 9–12 introduce prototype theory interpretation of label semantics and data mining algorithms developed based on this interpretation. This book is for the readers like postgraduates and researchers in AI, data mining, soft computing and other related areas.

Zengchang Qin
Pittsburgh, PA, USA
Yongchuan Tang
Hangzhou, China
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Contents

Acronyms

AI Artificial Intelligence
ANN Artificial Neural Networks
AUC Area Under the ROC Curve
AVE Average Error
BLDT Bayesian LDT
BP Back Propagation
CAD Computer Aided Diagnosis
CW Computing with Words
D-S Dempster-Shafer
DT Decision Tree
EM Expectation-Maximization
FDT Fuzzy Decision Tree
FLDT Forest of LDTs
FOIL First-Order Inductive Learning
FPR False Positive Rate
FRBS Fuzzy Rule-Based Systems
FRIL Fuzzy Relational Inference Language
FSNB Fuzzy Semi-Naive Bayes
GTU General Theory of Uncertainty
IBL Instance-Based Learning
ICMM Information Cell Mixture Model
ID3 Iterative Dichotomiser 3
IG Information Gain
ILP Inductive Logical Programming
KDD Knowledge Discovery in Database
k-NN *k*-Nearest Neighbors
LD Linguistic Data
LDT Linguistic Decision Tree
LFOIL Linguistic FOIL
LID3 Linguistic ID3

LLE Locally Linear Embedding
LLR Locally Linear Reconstruction
LPT Linguistic Prediction Tree
LS Least Square
LT Linguistic Translation
MB Merged Branch
MLP Multi-Layer Perceptrons
MSE Mean Square Error
MW Modeling with Words
NB Naive Bayes
NN Neural Networks
PDF Probability Density Function
PET Probability Estimation Tree
PNL Precisiated Natural Language
QP Quadratic Programming
ROC Receiver Operating Characteristics
SNB Semi-Naive Bayes
SRM Structural Risk Minimization
SVM Support Vector Machines
SVR Support Vector Regression
TPR True Positive Rate

Notations

$\|A\|$	Absolute value of A when A is a number or cardinality of A when A is a set
DB	Database with the size of $\|DB\|$: $DB = \{\mathbf{x}_1, \ldots, \mathbf{x}_{\|DB\|}\}$
$\mathbf{x}_i$	n-dimensional variable that: $\mathbf{x}_i \in DB$ for $i = 1, \ldots, \|DB\|$
$\mathbb{L}_x$	Set of labels defined on random variable x
LE	Logical expressions set given $\mathbb{L}$
$\mathbb{F}_x$	Focal set of random variable x
T	Linguistic decision tree that contains $\|T\|$ branches: $T = \{B_1, \ldots, B_{\|T\|}\}$
$\mathbb{B}$	A set of branches: $\mathbb{B} = \{B_1, \ldots, B_M\}$ $T \equiv \mathbb{B}$ iff: $M = \|T\|$
B	A branch of LDT, it has $\|B\|$ focal elements: $B = \{F_1, \ldots, F_{\|B\|}\}$
$\mathbb{C}$	A set of classes: $\mathbb{C} = \{C_1, \ldots, C_{\|\mathbb{C}\|}\}$
m_x	Mass assignment of x
$m_{\mathbf{x}}$	Mass assignment on a multi-dimensional variable $\mathbf{x}$
$\mu_L(x)$	Appropriateness degree of using label L to describe x
$\mu_\theta(x)$	Appropriateness measure of using logical expression θ to describe x where $\theta \in LE$
$p(x\|y)$	Conditional probability of x given y
$Bel(\cdot)$	Belief function
$Pl(\cdot)$	Plausibility function
$\lambda(\theta)$	λ-function to transfer the logical expression θ into a set of labels
$\mu_\theta x$	Appropriateness measure of using logical expression θ to label x
$IG(\cdot)$	Information Gain function
FD	Fuzzy database $FD = \{\langle \theta_1(i), \ldots, \theta_n(i)\rangle : i = 1, \ldots, N\}$
$\hat{x}$	Estimated value of x based on a training database
$\tilde{p}$	Updated value of p at iterative updating process
$P(x\|m)$	Conditional distribution of x given mass assignment m
$pm(\cdot)$	Prior mass assignment
$\mathscr{LP}$	Information cell mixture model $\mathscr{LP} = \langle \mathbb{L}, Pr\rangle$