

Studies in Computational Intelligence

Volume 750

Series editor

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Olga Kosheleva · Karen Villaverde

How Interval and Fuzzy Techniques Can Improve Teaching

Processing Educational Data: From
Traditional Statistical Techniques
to an Appropriate Combination
of Probabilistic, Interval, and Fuzzy
Approaches

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Dedicated to the memory of Lotfi A. Zadeh

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