

Real-Time C++

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Real-Time C++

Efficient Object-Oriented and Template
Microcontroller Programming

Fourth Edition

 Springer

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*To those who pursue the art of technical
creativity*

Preface to the Fourth Edition

C++20, the newest evolution of C++, adds various major new language features that can significantly simplify and clarify program expression. At the same time, using C++ in microcontroller programming is steadily gaining popularity and the methods of its use are maturing in the embedded systems community. These steps are matched by the widespread support of modern post-C++11,14,17 adherence delivered by many high-quality microcontroller compiler vendors.

The fourth edition of this book keeps up with these progressions in C++. In addition to covering new C++ language elements, particular emphasis is placed on improving and extending the depth of the examples. Several interesting sample projects requiring additional chips and exercising advanced software and laboratory techniques have been added. Furthermore, one of the new computationally intensive examples has also been adapted to both our target with the 8-bit microcontroller as well as to a modern single-board computer with a powerful 32-bit processor.

These efforts are intended to widen the scope of applicability of this book for students, practitioners, and hobbyists alike by exemplifying practical, hands-on methods to leverage the power of portable C++ with lean, efficient real-time code.

New or Significantly Modified Sections

The fourth edition of this book contains several new or significantly modified parts. These include:

- Section 1.10 adapted to add detailed comments regarding using `reinterpret_cast` sparingly,
- Section 3.2 extended to include example `chapter03_02` that calculates prime numbers and provides an insightful preview of numerous C++ techniques,
- Section 3.21 (new) on `std::span` from C++20's `` library that can be used for delimiting pointer ranges,

- Section 3.22 (new) briefly showing how to use the `<random>` library for generating sequences of pseudo-random integers,
- Section 4.4 which has been significantly expanded to include two full detailed examples exercising dynamic polymorphism with an intuitive LED class hierarchy,
- Chapters 4, 7, and 8 which have been reworked in order to improve code sequences and clarity of text passages,
- Section 5.13 (new) describing how to make effective and powerful use of template integer sequences at compile time with `std::integer_sequence`,
- Section 6.14 with the addition of example `chapter06_14` extending the original CRC32 calculation of example `chapter06_01` to make use of custom ROM-based iterators and containers specifically designed for accessing read-only program code,
- Section 6.21 (new) quantifying potential resource consumption resulting from using runtime type information (RTTI),
- Section 9.5 has been reworked to implement a portable, all-software SPITM driver subsequently used in examples `chapter04_04`, `chapter04_04a`, `chapter10_08`, `chapter10_08a`, `chapter10_09`, and `chapter16_08`,
- Section 10.8 (new) providing a detailed example that uses external SRAM ICs to calculate up to 100,001 decimal digits of π with an application architecture that uses custom SRAM pointers, iterators and containers, and numerical algorithms,
- Section 10.9 (new) which adapts the π calculations of Sect. 10.8 to the powerful 32-bit Arm[®]-based Raspberry Pi[®]Zero WH single-board computer system,
- Section 11.7 has been modified to include a sample that exemplifies preemptive multitasking scheduling,
- Section 12.2 has been slightly expanded to include common standardized mathematical constants such as $\sqrt{2}$, π , $\log 2$, e , etc. in the `<numbers>` header,
- Section 16.7 (new) describing a portable implementation of big integer types such as `uint128_t`, `uint256_t`, `uint512_t`, etc.,
- Section 16.8 (new) which develops a basic hardware-based custom random engine that can serve as an efficient and practical, hobby-quality drop-in replacement for `std::default_random_engine` and also presents example `chapter16_08` which performs primality testing of random 128-bit big integers,
- Section 16.9 (new) on the *freestanding* implementation,
- Section A.9 enlarged to treat C++20 enhancements of lambda expression syntax including template parameter lists and new capture style for **this**,
- Section A.16 broadened to include `std::variant` from C++20 in the new `<variant>` addition to the STL,
- Section A.18 (new) covering a three-way comparison with the co-called *space-ship* operator within the context of generalized equality and inequality,

Improved or New Examples and Code Snippets

Several new examples have been added. All of the example projects have been modernized and checked for compatibility with GCC version 10.1.0 built for `avr-g++`. The portability and range of use of each example project have been improved. In particular, test and verification of the examples have been carried out with various GCC versions ranging from 5 through 9 using the language standards flags `-std=c++11`, `-std=c++14`, `-std=c++17`, and `-std=c++20` (as available).

- ☞ The `chapter03_02` sample project (new) in Sect. 3.2 uses fixed-size integer types and various other C++ techniques to compute the first 100 prime numbers.
- ☞ The `chapter04_04` and `chapter04_04a` sample projects (new) in Sect. 4.4 exercise various forms of polymorphism and class relationships through the example of an LED class hierarchy.
- ☞ The `chapter06_14` sample project (new) in Sect. 6.14 shows how to create custom ROM-based iterators and containers used to calculate a CRC32 checksum.
- ☞ The sample projects `chapter10_08` and `chapter10_08a` (new, advanced) found in Sect. 10.8 use external memory ICs to extend available SRAM to up to 2 Mbyte for calculations of as many as 100,001 decimal digits of the mathematical constant π .
- ☞ The `chapter10_09` sample project (new, advanced) in Sect. 10.9 adapts the π calculations of example `chapter10_08a` to the well-known 32-bit Arm[®]-based Raspberry Pi[®] Zero WH single-board computer system, running OS-less in bare metal mode. Seamlessly porting this application's C++ algorithms from an 8-bit platform to a high-performance 32-bit Arm[®]-based system provides keen insight into effective cross development on multiple systems.
- ☞ The `chapter11_07` sample project (new, advanced) exemplifies intuitive use of a preemptive multitasking scheduler constrained by small RAM/ROM resource footprint.
- ☞ The `chapter16_08` sample project (new, advanced) in Sect. 16.8 computes 128-bit prime numbers using a Miller–Rabin primality test.

With the fourth edition of this book, the detailed code snippets available in the public domain now cover approximately two-thirds of code samples in the text. Each code snippet comprises a complete and portable, single-file C++ program. Every program can be compiled and run on a PC or easily adapted to a microcontroller environment.

To obtain run-ability on a PC, code snippets have usually been embellished with a `main()` subroutine. Some code snippets have been augmented with `<thread>` support, simulated hardware registers or other C++ mechanisms in order to elucidate the topic of the program. Outputs of the code snippets are typically printed to the console with `<iostream>` and potentially formatted with the help of `<iomanip>`. File names of the code snippets correspond to chapter and section numbers in the book.

Companion Code

Based on new and reworked material in the fourth edition, the companion code has been significantly improved and extended.

The entire companion code can be found here:

<http://github.com/ckormanyos/real-time-cpp>

The complete reference application is at:

http://github.com/ckormanyos/real-time-cpp/tree/master/ref_app

Example projects are stored here:

<http://github.com/ckormanyos/real-time-cpp/tree/master/examples>

Code snippets are located at:

http://github.com/ckormanyos/real-time-cpp/tree/master/code_snippets

Further Notes on Coding Style

The coding style in the fourth edition of this book stays consistent with that used in the first through third editions. The code is intended to be easy to read and straightforward to comprehend while simultaneously utilizing the full spectrum of C++’s traditional and modern features.

Reutlingen, Germany
November 2020

Christopher Kormanyos

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- The circuits of all target hardware described and depicted in various chapters and appendices have been designed and assembled on solderless prototyping breadboards by myself.
- All photographs of target hardware shown in various chapters and appendices were taken by myself.

Preface to the Third Edition

C++ is a modern, expressive object-oriented programming language that continues to evolve. In keeping up with the exciting development of C++, the third edition of this book has been updated for C++17.¹

With this iteration of the language, the purpose of this book remains the same—to show through example and text how to leverage C++’s powerful object-oriented and template features in the realm of microcontroller programming with the goal of improving software quality and robustness while simultaneously fulfilling efficiency requirements.

Several new sections have been added and others have been modified or adapted. These changes cover new language elements and library features in C++17. They also reflect the trend of improved compiler support for C++11 and C++14.

More errors have been identified, predominantly reported by careful and patient readers. All errors that have been found have been corrected.

New or Significantly Modified Sections

The third edition of this book contains several new or significantly modified sections. These include:

- Section 2.2 updated for a newer GCC toolchain with a more simple decorated name (i.e., GCC version 7.2.0 built for the target `avr-g++`).
- Section 3.4 adding information on C++17 nested namespace definitions,
- Section 3.17 now including descriptions of the (in the second edition of this book missing) standardized suffixes `if`, `i`, and `il` from the `<complex>` library,
- Section 3.18 (new) detailing the specifiers **`alignof`** and **`alignas`**,

¹At the time of writing the third edition of this book, state-of-the-art compilers support C++17. The specification process is ongoing, and some language experts predict that C++20 will be the next revision of the C++ standard, potentially available in 2020.

- Section 3.19 (new) for the specifier `final`,
- Section 3.20 (new) on defining types with C++11 alias,
- Section 9.8 (new) portraying a full example that animates an RGB LED to produce a colorful light display,
- Section 12.4 covering inclusion of additional mathematical special functions in `<cmath>` specified in the C++17 standard,
- several sections in Chap. 13 reflecting improvements of the `fixed_point` class in the companion code,
- Section 16.6 (new) presenting an extended-complex template class that promotes the functionality of the `<complex>` library to user-defined types other than **float**, **double**, and **long double**,
- Chapter 17 (new) showing how to use C code in a C++ project (hereby “Additional Reading” has been moved from Chaps. 17 to 18),
- the tutorial of Appendix A, in particular Sect. A.4 updating **static_assert** for C++17, Sect. A.15 (new) about the `<type_traits>` library, Sect. A.16 (new) on using `std::any` from the C++17 `<any>` library, and Sect. A.17 (new) introducing structured binding declarations (also from C++17).

Improved or New Examples and Code Snippets

All sample projects have been modernized for GCC version 7.2.0 built for `avr-g++`, and five new examples have been added.

- ☞ The `chapter06_01` sample project (new) shows step-by-step how to perform the benchmark of the CRC calculation described in Sects. 6.1 and 6.2.
- ☞ The `chapter09_07` example in Sect. 9.7 has been adapted to architectural improvements found in the new `chapter09_08` sample of Sect. 9.8,
- ☞ The `chapter09_08` sample project (new) animates an industry-standard off-the-shelf RGB LED. This example incorporates several real-time C++ features including object-oriented design, peripheral driver development, and multitasking. They are merged together within the context of a coherent, intuitive, and visible project. By means of simulation on a PC, the `chapter09_08` sample also exemplifies cross-development and methods for creating portable code.
- ☞ The `chapter12_04` example (new) performs highly detailed calculations of several mathematical special functions. These are used to provide a benchmark of floating-point operations.
- ☞ The `chapter17_03` sample project (new) takes an existing C library used for CRC calculations and wraps the procedural functions in classes that can be employed in object-oriented C++. This practical exercise shows how to leverage the power of valuable existing C code within a modern C++ project.
- ☞ The `chapter17_03a` sample project (new) uses the CRC classes of the `chapter17_03` example and distributes the work of the calculations among successive time slices in a multitasking environment.

With the third edition of this book, code snippets have been made available in the public domain. The code snippets correspond to certain code samples that appear in the text. Each code snippet comprises a complete and portable, single-file C++ program. Every program can be compiled and run on a PC or easily adapted to a microcontroller environment.

To obtain run-ability on a PC, code snippets have been embellished with a `main()` subroutine. Some code snippets have been augmented with `<thread>` support or other higher-level mechanisms in order to elucidate the topic of the program. Outputs are printed to the console with `<iostream>`. The file names of the code snippets correspond to chapter and section numbers in the book.

Companion Code

The companion code has been improved and extended based on new and reworked sections of the third edition. Contemporary compiler toolchains are used. Legacy directories that previously provided for certain aspects of C++11 compatibility have been removed, as modern compilers now support these.

The entire companion code can be found here:

<http://github.com/ckormanyos/real-time-cpp>

The reference application is at:

http://github.com/ckormanyos/real-time-cpp/tree/master/ref_app

Example projects can be found here:

<http://github.com/ckormanyos/real-time-cpp/tree/master/examples>

Code snippets are located at:

http://github.com/ckormanyos/real-time-cpp/tree/master/code_snippets

Further Notes on Coding Style

The coding style in the third edition of this book stays consistent with that used in the first and second editions. The code is intended to be easy to read and straightforward to comprehend while simultaneously utilizing the full spectrum of C++'s traditional and modern features.

Updated Trademarks and Acknowledgments

In the preface to first edition of this book, we listed several trademarks and acknowledgments. Meanwhile the authors/holders of certain trademarks/copyrights and the scope of some of the acknowledgments have changed.

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- The circuits of all target hardware described in this book and depicted in various chapters such as Chaps. 2, 9, and Appendix D, were designed and assembled on solderless prototyping breadboards by Christopher Kormanyos.
- All photographs of target hardware in this book shown in chapters including Chaps. 2, 9, Appendix D and any others were taken by Christopher Kormanyos.

Reutlingen, Germany
February 2018

Christopher Kormanyos

Preface to the Second Edition

C++ seamlessly blends object-oriented techniques with generic template methods, creating a modern powerful programming language useful for problem-solving in countless domains. The most recent evolution of C++ from C++11 to C++14 has brought yet further improvements to this rich language.¹ As C++ becomes even more expressive, growing numbers of embedded systems developers are discovering new and fascinating ways to utilize its multifaceted capabilities for creating efficient and effective microcontroller software.

The second edition of this book retains its original purpose to serve as a practical guide to programming real-time embedded microcontroller systems in C++. New material has been incorporated predominantly reflecting changes introduced in the C++14 standard. Various sections have been reworked according to reader suggestions. Selected passages have been reformulated in a continued effort to improve clarity. In addition, all known errors throughout the text have been corrected.

New sections have been added (in particular for C++14) covering:

- digit separators (Sect. 3.15),
- binary literals (Sect. 3.16),
- user-defined literals (Sect. 3.17),
- variable templates (Sect. 5.12),
- and the `chapter09_07` sample project (Sect. 9.7) controlling an industry-standard seven-segment display.

Two new sample projects, `chapter02_03a` and `chapter09_07`, have been added to the companion code.

¹At the time of writing the second edition of this book, C++14 is brand new. World-class compilers are shipped with support for C++14. Work is in progress on C++1z, the next specification of C++ (sometimes known as C++17). Experts anticipate that the specification of C++1z could be finished in 2017.

- ☞ The `chapter02_03a` sample project implements LED toggling at 1/2 Hz with timing provided by a simple multitasking scheduler in combination with a timer utility.
- ☞ The `chapter09_07` sample project in the newly added Sect. 9.7 uses many of the advanced programming methods in this book to animate an industry-standard seven-segment display.

Significantly reworked or corrected parts of this book include:

- ✓ corrections and clarifications in Chap. 1 on getting started with C++,
- ✓ the description of the `chapter02_02` project in Sect. 2.2,
- ✓ parts of Chap. 3 on the jump-start in real-time C++,
- ✓ corrections and clarifications in Chap. 5 on templates,
- ✓ Sects. 6.1 and 6.2 on optimization and performance,
- ✓ parts of Chap. 10 on custom memory management,
- ✓ parts of Chaps. 12 and 13 on mathematics,
- ✓ the literature list in Sect. 18.1,
- ✓ parts of Appendix A in the C++ tutorial,
- ✓ and repairs and extensions of the citations in some chapter references.

Companion Code

The companion code continues to be supported and numerous developers have successfully worked with it on various cross-development platforms. The scope of the companion code has been expanded to include a much wider range of target microcontrollers. In addition, the `chapter02_03a` and `chapter09_07` sample projects that are mentioned above have been added to the companion code.

The companion code is available at:

<http://github.com/ckormanyos/real-time-cpp>

More Notes on Coding Style

The second edition of this book features slight changes in coding style. These can be encountered in the code samples throughout the text.

Compiler support for standard C99 and C++11 macros of the form `UINT8_C()`, `UINT16_C()`, `UINT32_C()`, etc. and corresponding macros for signed types in the `<stdint.h>` and `<cstdint>` headers has become more prevalent (see also Sect. 3.2). Consequently, these macros are used more frequently throughout the code samples.

These macros are useful for creating integer numeric literal values having specified widths. The code below, for example, utilizes `UINT8_C()` to initialize an 8-bit integer variable with a numeric literal value.

```
#include <stdint>

std::uint8_t byte_value = UINT8_C(0x55);
```

Digit separators have become available with C++14 (Sect. 3.15). These are used in selected code samples to improve clarity of long numeric literals. Digit separators are shown in the code sample below.

```
#include <stdint>

constexpr std::uint32_t prime_number =
    UINT32_C(10'006'721);

constexpr float pi = 3.1415926535'8979323846F;
```

Other than these minor changes, however, the coding style in the second edition of this book remains consistent with that of the first edition and is intended to be clean and clear.

Reutlingen, Germany
Seattle, Washington
May 2015

Christopher Kormanyos

Preface to the First Edition

This book is a practical guide to programming real-time embedded microcontroller systems in C++. The C++ language has powerful object-oriented and template features that can improve software design and portability while simultaneously reducing code complexity and the risk of error. At the same time, C++ compiles highly efficient native code. This unique and effective combination makes C++ well-suited for programming microcontroller systems that require compact size, high performance, and safety-critical reliability.

The target audience of this book includes hobbyists, students, and professionals interested in real-time C++. The reader should be familiar with C or another programming language and should ideally have had some exposure to microcontroller electronics and the performance and size issues prevalent in embedded systems programming.

About This Book

This is an interdisciplinary book that includes a broad range of topics. Real-world examples have been combined with brief descriptions in an effort to provide an intuitive and straightforward methodology for microcontroller programming in C++. Efficiency is always in focus, and numerous examples are backed up with real-time performance measurements and size analyses that quantify the true costs of the code down to the very last byte and microsecond.

Throughout the chapters, C++ is used in a bare-bones, no-frills fashion without relying on any libraries other than those specified in the language standard itself. This approach facilitates portability.

This book has three parts and several appendices. The three parts generally build on each other with the combined goal of providing a coherent and effective set of C++ methods that can be used with a wide range of embedded microcontrollers.

- Part I provides a foundation for real-time C++ by covering language technologies. Topics include getting started in real-time C++, object-oriented methods, template programming, and optimization. The first 3 chapters have a particularly hands-on nature and are intended to boost competence in real-time C++. Chapter 6 has a unique and important role in that it is wholly dedicated to optimization techniques appropriate for microcontroller programming in C++.
- Part II presents detailed descriptions of a variety of C++ components that are widely used in microcontroller programming. These components can be either used as presented, or adapted for other projects. This part of the book uses some of C++'s most powerful language elements, such as class types, templates, and the STL, to develop components for microcontroller register access, low-level drivers, custom memory management, embedded containers, multitasking, etc.
- Part III describes mathematical methods and generic utilities that can be employed to solve recurring problems in real-time C++.
- The appendices include a C++ language tutorial, information on the real-time C++ development environment, and instructions for building GNU GCC cross-compilers and a microcontroller circuit.

C++ is a rich language with many features and details, the description of which can fill entire bookshelves. This book, however, primarily concentrates on how to use C++ in a real-time microcontroller environment. Along those lines, C++ language tutorials have been held terse, and information on microcontroller hardware and compilers is included only insofar as it is needed for the examples. A suggested list of additional reading material is given in Chap. 18 for those seeking supplementary information on C++, the C++ standard library and STL, software design, C++ coding guidelines, the embedded systems toolchain, and microcontroller hardware.

When units are needed to express physical quantities, the MKS (meter, kilogram, second) system of units is used.

Companion Code, Targets, and Tools

The companion code includes three introductory projects and one reference project. The introductory projects treat various aspects of the material presented in Chaps. 1 and 2. The reference project is larger in scope and exercises many of the methods from all the chapters.

The companion code is available at:

<http://github.com/ckormanyos/real-time-cpp>

The C++ techniques in this book specifically target microcontrollers in the *small-to-medium* size range. Here, small-to-medium spans the following approximate size and performance ranges.

- 4 kbyte . . . 1 Mbyte program code
- 256 byte . . . 128 kbyte RAM

- 8-bit . . . 32-bit CPU
- 8 MHz . . . 200 MHz CPU frequency

Most of the methods described in this book are, however, scalable. As such, they can be used equally well on larger or smaller devices, even on PCs and workstations. In particular, they can be employed if the application has strict performance and size constraints.

A popular 8-bit microcontroller clocked with a frequency of 16 MHz has been used as the primary target for benchmarking and testing the code samples in this book. Certain benchmarks have also been performed with a well-known 32-bit microcontroller clocked at 24 MHz. An 8-bit microcontroller and a 32-bit microcontroller have been selected in order to exercise the C++ methods over a wide range of microcontroller performance.

All the C++ examples and benchmarks in the book and the companion code have been compiled with GNU GCC versions 4.6.2 and 4.7.0. Certain examples and benchmarks have also been compiled with other PC-based compilers.

The most recent specification of C++11 in ISO/IEC 14882:2011 is used throughout the text. At the time this book is written, the specification of C++11 is brand new. The advent of C++11 has made C++ significantly more effective and easy-to-use. This will profoundly influence C++ programming. The well-informed reader will, therefore, want to keep in touch with C++11 best practice as it evolves in the development community.

Notes on Coding Style

A consistent coding style is used throughout the examples in this book and in the companion code.

Code samples are written with a *fixed-width font*. C++ language keywords and built-in types use the same font, but they are in boldface. For instance,

```
constexpr int version = 7;
```

In general, the names of all symbols such as variables, class types, members, and subroutines are written in lower case. A single underscore (`_`) is used to separate words and abbreviations in names. For instance, a system-tick variable expressed with this style is shown in the code sample below.

```
unsigned long system_tick;
```

Using prefixes, suffixes, or abbreviations to incorporate type information in a name, sometimes known as *Hungarian notation*, is not done. Superfluous prefixes,

suffixes, and abbreviations in Hungarian notation may obscure the name of a symbol, and symbol names can be more intuitive and clear without them. For example,

```
std::uint16_t name_of_a_symbol;
```

Names that are intended for use in public domains are preferentially long and descriptive rather than short and abbreviated. Here, clarity of expression is preferred over terseness. Symbols used for local subroutine parameters or private implementation details with obvious meanings, however, often have terse or abbreviated names.

The global subroutine below, for example, uses this naming style. It returns the **float** value of the squared Euclidean distance from the origin of a point in two-dimensional Cartesian space \mathbb{R}^2 .

```
float squared_euclidean_distance(const float& x,
                                const float& y)
{
    return (x * x) + (y * y);
}
```

C++ references are heavily used because this can be advantageous for small microcontrollers. Consider an 8-bit microcontroller. The work of copying subroutine parameters or the work of pushing them onto the stack for anything wider than 8-bits can be significant. This workload can potentially be reduced by using references. In the previous code sample, for instance, the floating-point subroutine parameters *x* and *y*, each four bytes wide, have been passed to the subroutine by reference (i.e., **const float&**).

Fixed-size integer types defined in the `std` namespace of the C++ standard library such as `std::uint8_t`, `std::uint16_t`, `std::uint32_t`, and the like are preferentially used instead of plain built-in types such as **char**, **short**, **int**, etc. This improves clarity and portability. An unsigned login response with exactly 8 bits, for instance, is shown below.

```
std::uint8_t login_response;
```

Code samples often rely on one or more of the C++ standard library headers such as `<algorithm>`, `<array>`, `<cstdint>`, `<limits>`, `<tuple>`, `<vector>`, etc. In general, code samples requiring library headers do not explicitly include their necessary library headers.

The declaration of `login_response` above, for example, actually requires `<cstdint>` for the definition of `std::uint8_t`. The library file is, however, not included. In general, the code samples focus on the core of the code, not on the inclusion of library headers.

It is easy to guess or remember, for example, that `std::array` can be found in `<array>` and that `std::vector` is located `<vector>`. It can, however, be more difficult to guess or remember that `std::size_t` is in `<cstddef>` or that `std::accumulate()` is in `<numeric>`. With assistance from online help and other resources and with a little practice, though, it becomes routine to identify what standard library parts can be found in which headers.

In cases for which particular emphasis is placed on the inclusion of a header file, the relevant **#include** line(s) may be explicitly written. For instance,

```
#include <cstdint>
```

```
std::uint8_t login_response;
```

Namespaces are used frequently. In general, though, the **using** directive is not used to inject symbols in namespaces into the global namespace. This means that the entire namespace must be typed with the name of a symbol in it. This, again, favors non-ambiguity over brevity.

The unsigned 16-bit counter below, for example, uses a type from the `std` namespace. Since the “**using namespace std**” directive is not used, the name of the namespace (`std`) is explicitly included in the type.

```
std::uint16_t counter;
```

Suffixes are generally appended to literal constant values. When a suffix is appended to a literal constant value, its optional case is uppercase. For example,

```
constexpr float pi = 3.14159265358979323846F;
```

```
constexpr std::uint8_t login_key = 0x55U;
```

Certain established C++ coding guidelines have strongly influenced the coding style. For the sake of terseness and clarity, however, not every guideline has been followed all the time.

One clearly recognizable influence of the coding guidelines is the diligent use of C++-style casts when converting built-in types. The following code, for instance, explicitly casts from **float** to an unsigned integer type.

```
float f = 3.14159265358979323846F;

std::uint8_t u = static_cast<std::uint8_t>(f);
```

Even though explicit casts like these are not always mandatory, they can resolve ambiguity and eliminate potential misinterpretation caused by integer promotion.

Another influence of the coding guidelines on the code is the ordering of class members according to their access level in the class. The `communication` class below, for example, represents the base class in a hierarchy of communication objects. The members in the class definition are ordered according to access level. In particular,

```
class communication
{
public:
    virtual ~communication();

    virtual bool send(const std::uint8_t) const;
    virtual bool recv(std::uint8_t&);

protected:
    communication();

private:
    bool recv_ready;
    std::uint8_t recv_buffer;
};
```

C-style preprocessor macros are used occasionally. Preprocessor macros are written entirely in uppercase letters. Underscores separate the words in the names of preprocessor macros. The `MAKE_WORD()` preprocessor macro below, for example, creates an unsigned 16-bit word from two unsigned 8-bit constituents.

```
#define MAKE_WORD(lo, hi) \
    (uint16_t) (((uint16_t) (hi) << 8) | (lo))
```

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Contents

Part I Language Technologies for Real-Time C++

1	Getting Started with Real-Time C++	3
1.1	The LED Program	3
1.2	The Syntax of C++	6
1.3	Class Types	6
1.4	Members	10
1.5	Objects and Instances	12
1.6	<code>#include</code>	13
1.7	Namespaces	14
1.8	C++ Standard Library	16
1.9	The <code>main()</code> Subroutine	16
1.10	Low-Level Register Access	17
1.11	Compile-Time Constant	18
	References	19
2	Working with a Real-Time C++ Program on a Board	21
2.1	The Target Hardware	21
2.2	Build and Flash the LED Program	22
2.3	Adding Timing for Visible LED Toggling	26
2.4	Run and Reset the LED Program	28
2.5	Recognizing and Handling Errors and Warnings	28
2.6	Reaching the Right Efficiency	30
	References	33
3	An Easy Jump Start in Real-Time C++	35
3.1	Declare Locals When Used	35
3.2	Fixed-Size Integer Types and Prime Number Example	36
3.3	The <code>bool</code> Type	42
3.4	Organization with Namespaces	42
3.5	Basic Classes	45
3.6	Basic Templates	46

3.7	nullptr Replaces NULL	48
3.8	Generalized Constant Expressions with constexpr	49
3.9	static_assert	51
3.10	Using <code><limits></code>	51
3.11	<code>std::array</code>	52
3.12	Basic STL Algorithms.....	53
3.13	<code><numeric></code>	54
3.14	<code>atomic_load()</code> and <code>atomic_store()</code>	55
3.15	Digit Separators.....	55
3.16	Binary Literals	56
3.17	User-Defined Literals.....	57
3.18	Using alignof and alignas	60
3.19	The Specifier final	61
3.20	Alias as an Alternative to typedef	62
3.21	Delimiting Pointer Ranges with <code></code>	64
3.22	Generating Random Numbers with <code><random></code>	64
	References.....	68
4	Object-Oriented Techniques for Microcontrollers	69
4.1	Object Oriented Programming	69
4.2	Objects and Encapsulation	74
4.3	Inheritance	76
4.4	Dynamic Polymorphism and a Detailed LED Example	77
4.5	The Real Overhead of Dynamic Polymorphism	84
4.6	Pure Virtual and Abstract.....	85
4.7	Class Relationships	86
4.8	Non-copyable Classes	88
4.9	Constant Methods	89
4.10	Static Constant Integral Members	93
4.11	Class Friends.....	95
4.12	Virtual Is Unavailable in the Base Class Constructor	97
	References.....	100
5	C++ Templates for Microcontrollers	101
5.1	Template Functions	101
5.2	Template Scalability, Code Re-Use and Efficiency	103
5.3	Template Member Functions	106
5.4	Template Class Types.....	109
5.5	Template Default Parameters.....	110
5.6	Template Specialization	111
5.7	Static Polymorphism	113
5.8	Using the STL with Microcontrollers.....	116
5.9	Variadic Templates	118
5.10	Template Metaprogramming	121
5.11	Tuples and Generic Metaprogramming.....	125
5.12	Variable Templates	129

5.13	Template Integer Sequences	132
	References	136
6	Optimized C++ Programming for Microcontrollers	137
6.1	Use Compiler Optimization Settings	137
6.2	Know the Microcontroller's Performance	141
6.3	Know an Algorithm's Complexity	142
6.4	Use Assembly Listings	144
6.5	Use Map Files	145
6.6	Understand Name Mangling and De-mangling	145
6.7	Know When to Use Assembly and When Not to	147
6.8	Use Sensible Comments	149
6.9	Simplify Code with typedef and Alias	149
6.10	Use Native Integer Types	152
6.11	Use Scaling with Powers of Two	154
6.12	Potentially Replace Multiply with Shift-and-Add	156
6.13	Consider Advantageous Hardware Dimensioning	156
6.14	Consider ROM-ability	158
6.15	Minimize the Interrupt Frame	163
6.16	Use Custom Memory Management	166
6.17	Use the STL Consistently	167
6.18	Use Lambda Expressions	169
6.19	Use Templates and Scalability	170
6.20	Use Metaprogramming to Unroll Loops	171
6.21	Potential Costs of Runtime Type Information (RTTI)	171
	References	174

Part II Components for Real-Time C++

7	Accessing Microcontroller Registers	177
7.1	Defining Constant Register Addresses	177
7.2	Using Templates for Register Access	179
7.3	Generic Templates for Register Access	182
7.4	Bit-Mapped Structures	185
	Reference	188
8	The Right Start	189
8.1	The Startup Code	189
8.2	Initializing RAM	192
8.3	Initializing the Static Constructors	194
8.4	The Connection Between the Linker and Startup	196
8.5	Understand Static Initialization Rules	198
8.6	Avoid Using Uninitialized Objects	200

8.7	Jump to <code>main()</code> and Never return	202
8.8	When in <code>main()</code> , What Comes Next?.....	203
	References.....	204
9	Low-Level Hardware Drivers in C++	205
9.1	An I/O Port Pin Driver Template Class	205
9.2	Programming Interrupts in C++.....	207
9.3	Implementing a System Tick.....	212
9.4	A Software PWM Template Class	215
9.5	A Serial SPI TM Driver Class	219
9.6	CPU-Load Monitors	222
9.7	Controlling a Seven-Segment Display	225
9.8	Animating an RGB LED	232
	References.....	237
10	Custom Memory Management	239
10.1	Dynamic Memory Considerations	239
10.2	Using Placement- new	241
10.3	Allocators and STL Containers	242
10.4	The Standard Allocator.....	243
10.5	Writing a Specialized <code>ring_allocator</code>	244
10.6	Using <code>ring_allocator</code> and Other Allocators	247
10.7	Recognizing and Handling Memory Limitations	249
10.8	Off-Chip Memory and Computing 100,001 Digits of π	251
10.9	Using Ample RAM on Arm [®] -Based Single-Board Computer	266
	References.....	276
11	C++ Multitasking	279
11.1	Multitasking Schedulers.....	279
11.2	Task Timing.....	281
11.3	The Task Control Block	282
11.4	The Task List.....	284
11.5	The Scheduler.....	285
11.6	Extended Multitasking	286
11.7	Preemptive Multitasking	288
11.8	The C++ Thread Support Library	291
	References.....	292
Part III Mathematics and Utilities for Real-Time C++		
12	Floating-Point Mathematics	295
12.1	Floating-Point Arithmetic	295
12.2	Mathematical Constants	298
12.3	Elementary Functions	300
12.4	Special Functions	302

12.5	Complex-Valued Mathematics	312
12.6	Compile-Time Evaluation of Functions with constexpr	316
12.7	Generic Numeric Programming	320
	References	327
13	Fixed-Point Mathematics	329
13.1	Fixed-Point Data Types.....	329
13.2	A Scalable Fixed-Point Template Class	332
13.3	Using the <code>fixed_point</code> Class	336
13.4	Fixed-Point Elementary Transcendental Functions	338
13.5	A Specialization of <code>std::numeric_limits</code>	349
	References.....	351
14	High-Performance Digital Filters	353
14.1	A Floating-Point Order-1 Filter	353
14.2	An Order-1 Integer Filter.....	356
14.3	Order- <i>N</i> Integer FIR Filters	360
14.4	Some Worked-Out Filter Examples.....	365
	References.....	369
15	C++ Utilities	371
15.1	The <code>nothing</code> Structure	371
15.2	The <code>noncopyable</code> Class.....	374
15.3	A Template <code>timer</code> Class	376
15.4	Linear Interpolation.....	379
15.5	A <code>circular_buffer</code> Template Class	382
15.6	The Boost Library	386
	References.....	387
16	Extending the C++ Standard Library and the STL	389
16.1	Defining the Custom <code>dynamic_array</code> Container.....	389
16.2	Implementing and Using <code>dynamic_array</code>	392
16.3	Writing Parts of the C++ Library if None Is Available	396
16.4	Implementation Notes for Parts of the C++ Library and STL.....	396
16.5	Providing <code>now()</code> for <code><chrono></code> 's High-Resolution Clock.....	405
16.6	Extended-Complex Number Templates	407
16.7	An Embeddable Big Integer Class	410
16.8	Customizing <code><random></code>	414
16.9	Freestanding Implementation	424
	References.....	425
17	Using C-Language Code in C++	427
17.1	Accessing C Language Code in C++	427
17.2	An Existing C-Language CRC Library	428
17.3	Wrapping the C-Based CRC Library with C++ Classes	430
17.4	Return to Investigations of Efficiency and Optimization	433
	References.....	434

18	Additional Reading	435
18.1	Literature List	435
	References	437
A	A Tutorial for Real-Time C++	439
A.1	C++ Cast Operators	439
A.2	Uniform Initialization Syntax	440
A.3	Overloading	443
A.4	Compile-Time Assert	443
A.5	Numeric Limits	444
A.6	STL Containers	448
A.7	STL Iterators	450
A.8	STL Algorithms	453
A.9	Lambda Expressions	457
A.10	Initializer Lists	458
A.11	Type Inference and Type Declaration with auto and decltype	460
A.12	Range-Based for (:)	462
A.13	Tuple	462
A.14	Regular Expressions	466
A.15	The <code><type_traits></code> Library	468
A.16	Using <code>std::any</code> and <code>std::variant</code>	471
A.17	Structured Binding Declarations	474
A.18	Three-Way Comparison	475
	References	475
B	A Robust Real-Time C++ Environment	477
B.1	Addressing the Challenges of Real-Time C++	477
B.2	Software Architecture	479
B.3	Establishing and Adhering to Runtime Limits	480
	References	481
C	Building and Installing GNU GCC Cross Compilers	483
C.1	The GCC Prerequisites	483
C.2	Getting Started	484
C.3	Building GMP	485
C.4	Building MPFR	486
C.5	Building MPC	486
C.6	Building PPL	487
C.7	Building ISL	488
C.8	Building the Binary Utilities for the Cross Compiler	488
C.9	Building the Cross Compiler	490
C.10	Using the Cross Compiler	491
	References	492

D Building a Microcontroller Circuit 493

 D.1 The Circuit Schematic 493

 D.2 Assembling the Circuit on a Breadboard 495

 References 496

Glossary 497

Index 499

Acronyms

\mathbb{C}	\mathbb{C} represents the set of complex numbers in mathematics.
\mathbb{R}	\mathbb{R} represents the set of real numbers on the real axis in mathematics.
\mathbb{R}^2	\mathbb{R}^2 represents two-dimensional Cartesian space in mathematics and geometry.
\mathbb{R}^3	\mathbb{R}^3 represents three-dimensional Cartesian space in mathematics and geometry.
\mathbb{Z}	\mathbb{Z} represents the set of integer numbers in mathematics.
ADC	Analog-Digital Converter.
ASCII	American Standard Code for Information Interchange [25] is a numerical representation of characters, often used in areas such as computer programming and telecommunication.
AUTOSAR	AUTomotive Open System ARchitecture [2] is a worldwide cooperation of automotive manufacturers and companies supplying electronics, semiconductors and software that concentrates on, among other things, a standardized architecture for automotive microcontroller software.
AWG	American Wire Gauge.
binutils	Binary Utilities [6] are the GNU binary utilities such as archiver, assembler, linker, object file parsers, etc. for GCC.
C	C is the C programming language, which is often referred to as ANSI-C [1] or C89 [2]. Later versions of C include C99 [13] and C11 [17].
C99	C99 refers to the C programming language, as specified in ISO/IEC 9899:1999 [13].
C11	C11 refers to the C programming language, as specified in ISO/IEC 9899:2011 [17].
C++	C++ refers to the C++ programming language.
C++98	C++98 refers to the C++ programming language, as specified in ISO/IEC 14882:1998 [12].
C++03	C++03 refers to the C++ programming language, as specified in ISO/IEC 14882:2003 [15].

C++11	C++11 refers to the C++ programming language, as specified in ISO/IEC 14882:2011 [18].
C++14	C++14 refers to the C++ programming language, as specified in ISO/IEC 14882:2014 [19].
C++17	C++17 refers to the C++ programming language, as specified in ISO/IEC 14882:2017 [20].
C++20	C++20 [26] is predicted by some C++ language experts to be the next revision of the C++ standard, possibly to become available in the year 2020.
CLooG	Chunky Loop Generator [4] is a software library used for geometric polyhedron analysis.
CRC	Cyclic Redundancy Check [27].
CPU	Central-Processing Unit.
ctor	constructor of a class object in object-oriented programming is a special subroutine that is called when an object is created.
DIL	Dual In-Line electronic component packaging.
DSP	Digital Signal Processor.
dtor	destructor of a class object in object-oriented programming is a special subroutine that is called when an object is destroyed or deleted.
FIR	Finite-Impulse Response is a kind of digital filter.
FLASH	Flash Memory is a nonvolatile computer memory that can be electrically written and erased. Flash is commonly used as an alternative to ROM.
FPU	Floating-Point Unit implements floating-point arithmetic in hardware. Many modern high-performance microcontrollers use an FPU to accelerate floating-point calculations.
GAS	is the GNU ASsembler.
GCC	GNU Compiler Collection [7] is a collection of free compilers for several popular programming languages including, among others, C and C++. GCC is supported for a wide range of targets.
GMP	GMP is the GNU Multiple-Precision library [9]. It implements highly efficient multiple-precision representations of integer and floating-point data types.
GNU	Is a *nix-like computer operating system consisting entirely of free software [8].
GUI	Graphical User Interface.
HEX	Hexadecimal representation is a base-16 numerical representation commonly used to store program data in computer engineering.
ICE	In-Circuit Emulator is a highly sophisticated hardware device used to debug embedded microcontroller software with an emulated bond-out processor.
ISL	Integer Set Library [11] is a software library used for manipulating sets of integers.

ISP	In-System-Programming is the act of programming the program code of a microcontroller using a communication interface while the microcontroller is fitted in the application, rather than as a standalone non-soldered component.
ISR	Interrupt Service Routine.
JTAG	Joint Test Action Group, later standardized as IEEE 1149.1 [10], is a protocol and hardware interface used for printed circuit board testing, boundary scan and recently more and more for debugging embedded systems.
LED	Light-Emitting Diode is a semiconductor-based light source used in diverse applications such as lighting, consumer electronics, and toys.
MCAL	Microcontroller Abstraction Layer is a low-level layer in a layered software architecture (such as AUTOSAR). The interface of the MCAL is typically written in a portable fashion. The MCAL implementation itself, however, contains partially non-portable components that access microcontroller peripherals and their registers, such as PWM signal generators, timers, serial UARTs, and other communication interfaces.
MinGW	Minimalist GNU [21] is an open-source programming toolset that emulates *nix-like environments.
MKS	Meter, Kilogram, Second is a system of units used to express physical quantities.
MPC	Multiple-Precision Complex [22] is a GNU C library that implements multiple-precision arithmetic of complex numbers.
MPFR	Multiple-Precision Floating-Point with correct Rounding [5, 23] is the GNU multiple-precision floating-point library. It is built on top of GMP and places special emphasis on efficiency and correct rounding.
MSYS	Minimal SYStem [21] is a collection of GNU utilities that enhance and extend the MinGW shell.
newlib	newlib [24] is a free implementation of the C standard library. It is well-suited for use with embedded systems and has been ported to a variety of CPU architectures.
nop	No OPERATION is a common assembly instruction that simply does <i>no operation</i> . One or more nops are often chained sequentially in order to be used for ultra low-level functions such as creating very short delays or flushing an instruction pipeline.
opcode	Operation CODE is a machine language instruction containing the operation to be done.
PC	Personal Computer.
POSIX	Portable Operating System Interface is an open standardized operating system specified in ISO/IEC 9945:2003 [14].
PPL	Parma Polyhedra Library [3] is a software library for abstract geometrical polyhedron representations.
PWM	Pulse-Width Modulated signal is a square wave that usually has a fixed period and a variable duty cycle.

RAM	Random Access Memory is computer memory with nearly constant access time regardless of address or memory size. RAM is volatile in the sense that data are typically lost when the power is switched off.
ROM	Read-Only Memory is a class of computer memory that, once written, can only be modified with external programming tools—or not be modified at all. ROM has permanent character in the sense that data are retained throughout power on/off cycles.
SPI™	Serial Peripheral Interface bus is a four-wire serial communication interface commonly used for communication between a microcontroller and one or more off-chip devices on the printed circuit board.
STL	Standard Template Library is part of the C++ standard library. The standard template library contains a vast collection of generic containers, iterators and algorithms.
TO-220	Transistor Outline electronic component packaging, number 220.
TR1	C++ Technical Report 1 includes the standard library extensions that are specified in ISO/IEC TR 19768:2007 [16]. TR1 has been predominantly integrated in C++11 (ISO/IEC 14882:2011 [18]).
UART	Universal Asynchronous Receiver/Transmitter is an asynchronous receiver and transmitter commonly used for serial communication between a PC and a microcontroller.

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