Zhang-Gradient Control

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ISBN 978-981-15-8256-1 ISBN 978-981-15-8257-8 (eBook) https://doi.org/10.1007/978-981-15-8257-8

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Preface

The tracking-control problems of nonlinear systems have been widely encountered in various applications, such as flight control, pendulum control, and robot control. For the purpose of tracking control, we need to design a controller in terms of control input for nonlinear systems such that the actual output can track the desired output. For solving the tracking-control problems of nonlinear systems, a number of methods have been presented and investigated, such as the input–output linearization (IOL) method, the optimal control method, and the backstepping method. However, most of the conventional control methods are relatively complex for their design procedures of controllers and practical implementations. Therefore, it is necessary and significant for practitioners to propose, develop, and investigate a simple and effective control method for the design of controllers.

From the viewpoint of time-varying (or say, dynamic) problem solving, the tracking control of nonlinear systems can be investigated in a unique manner. In recent years, a special class of neural dynamics has been exploited for the online solution of time-varying problems. As this neural-dynamic method is proposed by Zhang et al. and zeroes out each element of error function, it is called Zhang dynamics (also known as zeroing dynamics, ZD). Specifically, ZD is designed on the basis of an indefinite matrix-/vector-/scalar-valued error function (termed Zhang function, ZF) and takes full advantage of the time-derivative information of timevarying parameters. The ZD method is an error-based dynamic method, of which the core is the ZD design formula that forces each element of ZF to converge to zero exponentially. Such an idea can actually be found in the control field, i.e., forcing the error between the actual output and the desired output to be zero (or near zero in practice). Differing from the ZD, the conventional gradient dynamics (GD) is designed on the basis of a scalar-valued nonnegative error function (termed energy function, EF). The GD method is an energy-based minimization method, of which the core is the GD design formula such that the minimum point of the EF can be reached along the negative gradient direction. Besides, the GD method designed intrinsically for time-invariant (or say, static, constant) problem solving has been extended to solve time-varying problems. It is worth pointing out that such two methods both aim at forcing the error functions to be zero, which is essentially

viii Preface

consistent with the objective of tracking control. However, in the previous studies, the ZD method and the GD method are generally exploited for problem solving individually and comparatively, and other researchers rarely consider combining them to utilize the advantage of each method as well as the superiority of their combination.

In this book, by effectively combining the ZD and GD methods together, a simple and effective controller-design method is developed and presented, which is termed Zhang-gradient (ZG) method. Accordingly, based on the ZG method. a special kind of controllers termed ZG controllers are designed, developed, and investigated for tracking control of various nonlinear systems (including linear systems as a special case), i.e., chaotic systems, integrator systems, pendulum systems, affine-form nonlinear (AFN) systems, as well as time-varying linear and nonlinear systems. In general, under the framework of the ZG method, a ZG controller obtained by adopting the ZD method m times and the GD method ntimes is called a zmgn controller. Specifically, the zmg0 controllers are designed by adopting the ZD method m times and without using the GD method, which can be viewed as a special case of ZG controllers and thus often termed ZD controllers directly for comparisons with the ZG controllers using the GD method; besides, the zmg1 controllers are designed by adopting the ZD method m times and the GD method 1 time. It is worth pointing out that, in most cases, the ZG controllers refer to the zmg1 controllers, which can elegantly conquer the knotty division-by-zero (DBZ) problem. In traditional investigations, the DBZ problem is rarely considered and studied since it is a knotty problem for conventional controller design. In the conventional controller design, the divisor of a controller is simply assumed to be nonzero at any time instant, which often leads to contradictions between theoretical investigations and practical applications. Note that the DBZ problem has existed for thirteen centuries. However, past efforts have been spent on studying the problem under a time-invariant premise, i.e., studying the division operation with fixed operands at a certain time instant. By contrast, this book mainly focuses on investigating the DBZ problem from the perspective of temporal evolution instead of under a time-invariant premise. The simple and effective ZG method presented in this book is capable of designing the ZG controllers in a division-free manner. That is, the ZG controllers get rid of the potential possibility of encountering the DBZ problem and thus remain valid at the DBZ points encountered during the trackingcontrol process of nonlinear systems. Through the related theoretical analyses, the ZD and ZG controllers (more specifically, the zmg0 and zmg1 controllers under the framework of the ZG method) both possess the global and exponential convergence performance, which theoretically guarantee the efficacy of controllers. Computer simulations with various illustrative examples are further performed to substantiate the feasibility and efficacy of the presented ZD and ZG controllers (as well as the ZG method) for tracking control of various nonlinear systems. More importantly, the superiority of ZG controllers in conquering the DBZ problem is also illustrated by comparative simulation results. In brief, the main highlights of this book can be listed as follows.

Preface ix

(1) This book is the first book on the ZG method for controller design in connection with nonlinear/linear, time-varying/time-invariant, and multi-class or various systems.

- (2) This book overcomes the challenges of control singularity and system collapse posed by the DBZ problem.
- (3) This book provides detailed theoretical analyses, as well as abundant and comparative simulation results.

The idea for this book on neural dynamics and control was conceived during the classroom teaching as well as the research discussion in the laboratory and at international academic meetings. Most of the materials of this book are derived from the authors' papers published in journals and proceedings of the international conferences. In fact, since the early 1980s, the field of neural dynamics has undergone the phases of exponential growth, generating many new theoretical concepts and tools (including the authors' ones). At the same time, these theoretical results have been successfully applied to the solution of many practical problems. Our first priority is thus to cover each central topic in enough details to make the material clear and coherent; in other words, each part (and even each chapter) is written in a relatively self-contained manner.

In this book, Chap. 1 presents the introduction, concepts, and preliminaries, and the remainder contains 16 chapters that are classified into the following 5 parts:

- Part I: Chaotic Systems Using ZG Control (Chaps. 2–4);
- Part II: Integrator Systems Using ZG Control (Chaps. 5–7);
- Part III: Pendulum Systems Using ZG Control (Chaps. 8–10);
- Part IV: AFN Systems Using ZG Control (Chaps. 11–14);
- Part V: Time-Varying Systems Using ZG Control (Chaps. 15–17).

Chapter 2—In this chapter, we investigate the tracking-control problems of Lorenz, Chen, and Lu (also written as Lü) chaotic systems. By combining the ZD and GD methods together, a simple and effective controller-design method, termed ZG method, is presented for tracking control of the three chaotic systems. Both theoretical analyses and simulative verifications substantiate that the presented ZG controllers can achieve satisfactory tracking accuracy and successfully conquer the DBZ problem encountered during the tracking-control process.

Chapter 3—In this chapter, the ZG method is investigated for chaos synchronization with multiple inputs (i.e., three or two inputs). Based on the ZG method, the traditional three-input chaos synchronization problem can be successfully solved with desirable convergence rate and satisfactory accuracy. Besides, an important extension of the ZG method is investigated to solve the thorny two-input chaos synchronization problem. Simulation results illustrate that the controller groups designed by the ZG method not only achieve satisfactory synchronization accuracy and exponential convergence rate on the three-input chaos synchronization problem but also successfully solve the chaos synchronization problem with only two inputs.

Chapter 4—In this chapter, the ZG method is studied for solving the tracking-control problem of the modified Lorenz nonlinear system via additive input or mixed

x Preface

inputs (i.e., the mixture of additive and multiplicative inputs). Both theoretical analyses and simulative verifications validate that the ZG controllers with additive input or mixed inputs not only achieve satisfactory tracking accuracy but also successfully conquer the DBZ problem encountered during the tracking-control process.

Chapter 5—In this chapter, we apply the ZG method to the tracking control of Brockett integrator. Based on the ZG method, different types of controller groups are designed for Brockett integrator. Both theoretical analyses and simulative verifications indicate that the tracking errors are bounded and exponentially convergent. More importantly, comparative simulation results illustrate that the ZG controller group is superior to the ZD controller group in conquering the DBZ problem encountered during the tracking-control process.

Chapter 6—In this chapter, the ZG controllers for explicit and implicit tracking control of a double-integrator (DI) system are designed and presented. In addition, we conduct the corresponding computer simulations with different values of the design parameter λ used to illustrate the efficacy of ZG controllers. However, different settings of simulation options in MATLAB ordinary differential equation (ODE) solvers may lead to different simulation results (e.g., failure and success). The successful and failed simulation results are both presented to remind us to pay more attention to MATLAB defaults and options during conducting such simulations.

Chapter 7—In this chapter, the tracking-control problems of multiple-integrator (MI) systems are investigated by using the ZG method. Several types of ZD and ZG controllers are presented for tracking control of MI systems, e.g., triple-integrator (TI) systems. As an example, the design procedures of ZD and ZG controllers for TI systems with a linear output function (LOF) and a nonlinear output function (NOF) are presented. Corresponding theoretical analyses are given to guarantee the convergence performance of ZD and ZG controllers for TI systems. Computer simulations concerning the tracking control of MI systems with different types of output functions are further performed to substantiate the feasibility and efficacy of ZD and ZG controllers for tracking-control problem solving. Moreover, comparative simulation results for the tracking control of MI systems with NOFs substantiate that the ZG controllers can effectively conquer the DBZ problem.

Chapter 8—In this chapter, we firstly design ZD controllers for the explicit and implicit tracking control of a simple pendulum system. For achieving the DBZ-containing implicit tracking control, ZG controllers are further designed for conquering the DBZ problem. Computer simulations with an explicit tracking example and two implicit tracking examples are conducted. Comparative simulation results have substantiated the superiority of the ZG controllers for the DBZ-containing implicit tracking control of simple pendulum system.

Chapter 9—In this chapter, the cart path tracking control of an inverted-pendulum-on-a-cart (IPC) system is considered and investigated. Based on the ZG method, several types of ZD and ZG controllers are developed to achieve the tracking-control purpose. Besides, theoretical analyses are presented to guarantee the global and exponential convergence performance of both ZD and ZG controllers.

Preface xi

Computer simulations are further performed to illustrate the feasibility and efficacy of both ZD and ZG controllers. More importantly, comparative simulation results indicate that ZG controllers can effectively conquer the DBZ problem.

Chapter 10—In this chapter, two tracking controllers based on the ZG method are designed for the IPC system. Importantly, the presented ZG controller not only realizes the simultaneous control of pendulum swinging up and pendulum angle tracking but also conquers the DBZ problem elegantly without using any switching strategy. Besides, corresponding theoretical analyses on the convergence performance of both ZD and ZG controllers are provided. Computer simulations with three illustrative examples are further conducted to show the efficacy of both ZD and ZG controllers for the pendulum tracking control of the IPC system. In particular, comparative simulation results substantiate the superiority of the z2g1 controller for the control of pendulum tracking (including swinging up) of the IPC system in conquering the DBZ problem.

Chapter 11—In this chapter, we incorporate the GD into IOL, which leads to the GD-aided IOL method for conquering the DBZ problem encountered in the AFN system, with the proposition of the loose condition on relative degree. Corresponding theoretical analyses on tracking-error bound and convergence performance of the GD-aided IOL controller are provided. Moreover, comparative simulation results further substantiate that the GD-aided IOL controller is capable of fulfilling the tracking-control task with the DBZ problem conquered.

Chapter 12—In this chapter, a classic nonlinear system of Van der Pol oscillator in the affine-control form is investigated. By applying the ZG method, a ZG controller is designed for trajectory generation of the aforementioned nonlinear oscillator. Simulation results illustrate the feasibility and efficacy of the ZG controller with the DBZ problem conquered. In addition, the effects of ZD and GD design parameters on the performance of ZG controller are further studied.

Chapter 13—In this chapter, by following the ZG method, a ZD controller and a ZG controller are presented for tracking control of AFN system, which may encounter the DBZ problem. For comparison, the conventional IOL controller is also presented. The ZD, ZG, and IOL controllers are compared in different relative-degree cases, i.e., the standard relative-degree case, the pseudo-DBZ (PDBZ) relative-degree case, and the true-DBZ (TDBZ) relative-degree case. In addition, the theoretical analyses on ZD and ZG controllers are provided. Corresponding computer simulations are further performed to illustrate the tracking performance of the ZD, ZG, and IOL controllers, as well as to show the superiority of the ZG controller in conquering the TDBZ problem for tracking control of AFN system.

Chapter 14—In this chapter, according to the impact of DBZ points on the state variables of the controlled nonlinear system, the concepts of the PDBZ problem and the TDBZ problem are presented. Besides, the two classes of DBZ problems are solved under the framework of the ZG method. Specific examples are investigated to illustrate such two concepts and the efficacy of the ZG controllers in conquering PDBZ and TDBZ problems. The practical application to a two-wheeled mobile robot further substantiates the efficacy of the ZG method for tracking control of nonlinear system with physical meaning while conquering the TDBZ problem.

xii Preface

Chapter 15—In this chapter, the output tracking of time-varying linear (TVL) system is investigated. For solving such an output-tracking problem, three different types of controllers are presented, i.e., the conventional controller, ZD controller, and ZG controller. Simulation results with two illustrative examples show that such three types of controllers are feasible and effective for output-tracking problem solving. Especially, the presented ZG controller is capable of conquering the DBZ problem of TVL system.

Chapter 16—In this chapter, the stabilization of TVL system is investigated with PDBZ phenomenon shown. Based on the ZG method, a ZD stabilization controller and a ZG stabilization controller are designed. Simulation results indicate that the ZD stabilization controller is able to realize the stabilization of the TVL system in spite of the controller itself containing DBZ points, and that the ZG stabilization controller not only realizes the stabilization of the TVL system but also solves the PDBZ problem contained in the ZD stabilization controller.

Chapter 17—In this chapter, the ZG method is utilized to design ZD and ZG controllers for the output tracking of TVL and time-varying nonlinear (TVN) systems. Particularly, the investigated TVL and TVN systems may both have PDBZ phenomena. From the simulation results, although the presented ZD and ZG controllers fulfill well the output tracking of TVL and TVN systems, the infinite value of the former and the finite value of the latter at DBZ time instants indicate that the ZG controller is more effective in dealing with the PDBZ problem.

In summary, this book presents a simple and effective ZG method for solving the tracking-control problems of various nonlinear systems in the control field and further applies such a method to the tracking control of practical systems, e.g., IPC system and two-wheeled mobile robot (showing its application prospect). This book is written for undergraduate and postgraduate students as well as academic and industrial researchers studying in the developing fields of neural dynamic-s/neural networks, nonlinear control, computer mathematics, time-varying problem solving, modeling and simulation, analog hardware, and robotics. It provides a comprehensive view of the combined research of these fields, in addition to its accomplishments, potentials, and perspectives. We do hope that this book will generate curiosity and also happiness to its readers for learning more in the fields and the research, and that it will provide new challenges to seek new theoretical tools and practical applications.

At the end of this preface, it is worth pointing out that, in this book, a new and inspiring direction on the control method is provided for the design of controllers, together with the notorious DBZ problem conquered effectively, which has existed and has been investigated for more than 1300 years in academia and has stood in the tracking-control area of nonlinear systems for several decades (specifically, since the work of Alberto Isidori in 1985). This completely opens the door to the theoretical researches, simulative verifications, and practical/industrial applications of the DBZ-conquering ZG controllers designed by the ZG method, as the knotty DBZ problem has now been solved truly, systematically, and methodologically. It may promise to become a major inspiration for studies and researches in neural dynamics/neural networks, nonlinear control, computer mathematics, time-

Preface xiii

varying problem solving, modeling and simulation, analog hardware, and robotics. Without doubt, this book can be extended. Any comments or suggestions are welcome. The authors can be contacted via e-mails: zhynong@mail.sysu.edu.cn, qiubb6@mail.sysu.edu.cn, and lixd@mail.sysu.edu.cn. The web page of Yunong Zhang is available at http://sdcs.sysu.edu.cn/content/2477.

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Acknowledgements

This book is basically composed of many original research papers of the authors' research group, which have done a lot of meticulous and creative research work. Therefore, we are very grateful to our contributors for their high-quality work. During the process of preparing this book, we have the opportunity to discuss its various aspects and the results with many contributors and students. We highly appreciate their contributions, especially the great improvements in the presentation and quality of this book. We are very grateful for the valuable help and suggestions provided by Jinjin Guo, Min Yang, Jian Li, Yang Shi, Chaowei Hu, Dechao Chen, Huanchang Huang, Mengling Xiao, Huihui Gong, Zhiyuan Qi, Zhongxian Xue, Liu He, Shuo Yang, and so on.

The continuous aid by the National Natural Science Foundation of China (with number 61976230), the Project Supported by Guangdong Province Universities and Colleges Pearl River Scholar Funded Scheme (with number 2018), the China Postdoctoral Science Foundation (with number 2018M643306), the Guangdong Basic and Applied Basic Research Foundation (with number 2019A1515012128), the Key-Area Research and Development Program of Guangzhou (with number 202007030004), the Shenzhen Science and Technology Plan Project (with number JCYJ20170818154936083), and also the Fundamental Research Funds for the Central Universities (with number 19lgpy227) is gratefully acknowledged here.

Moreover, we would like to thank the editors (especially Editor Jasmine Dou) sincerely for their very important and constructive comments and suggestions provided, in addition to their time and effort spent in handling this book.

We are always very grateful to the nice people (especially the staff in Springer) for their strong support during the preparation and publishing of this book.

Contents

1	Intro	duction,	, Concepts and Preliminaries	1
	1.1		iction	1
	1.2	Concer	ots	2
		1.2.1	Concept of ZF	2
		1.2.2	Concept of EF	2
		1.2.3	Concept of ZD	2
		1.2.4	Concept of GD	3
		1.2.5	Concept of ZG Control	3
		1.2.6	Illustrative Example	4
	1.3	Prelimi	inaries	5
		1.3.1	Principle of ZG Method for Control	5
		1.3.2	Comparison with Other Methods	9
	1.4	Chapte	er Summary	11
	Refe	_		11
Pa	rt I (Chaotic S	Systems Using ZG Control	
2	ZG T	Fracking	Control of a Class of Chaotic Systems	15
	2.1	_	iction	15
	2.2		ns and Controllers	17
		2.2.1	Chaotic Systems with Single Input	18
		2.2.2	Design of ZD and ZG Controllers	19
	2.3	Conver	rgence Performance Analyses	21
		2.3.1	Analysis on ZD Controller	21
		2.3.2	Analyses on ZG Controller	22
	2.4		tion, Verification and Comparison	26
	2.5		er Summary	31
	Refe	rancas	•	25

xviii Contents

3	ZG S	Synchronization of Lu and Chen Chaotic Systems	37
	3.1	Introduction	37
	3.2	ZG Control via Three Inputs	38
		3.2.1 Problem Description	38
		3.2.2 Design of ZD and ZG Controller Groups	39
		3.2.3 Simulation and Verification	40
	3.3	ZG Control via Two Inputs	43
		3.3.1 Problem Description	4
		3.3.2 Design of ZG Controller Group	4
		3.3.3 Simulation and Verification	4
	3.4	Chapter Summary	4
	Refe	rences	4
4	ZG T	Fracking Control of Modified Lorenz Nonlinear System	4
	4.1	Introduction	49
	4.2	ZG Control via Additive Input	5
		4.2.1 Design of ZG Controller	5
		4.2.2 Convergence Performance Analyses on ZG Controller	5
		4.2.3 Simulation, Verification and Comparison on ZG	
		Controller	5
	4.3	ZG Control via Mixed Inputs	6
	1.0	4.3.1 Design of ZG Controller Group	6
		4.3.2 Convergence Performance Analyses on ZG	Ü
		Controller Group	6
		4.3.3 Simulation and Verification on ZG Controller Group	6
	4.4	Chapter Summary	6
		rences	6
	Reic	Tellecs	U
Pai	rt II	Integrator Systems Using ZG Control	
5	ZG	Tracking Control of Brockett Integrator	7
	5.1	Introduction	7
	5.2	Preliminaries	7
	5.3	Design of ZD and ZG Controller Groups	7
	5.4	Convergence Performance Analyses	7
	5.5	Simulation, Verification and Comparison	7
		5.5.1 Efficacy of ZD and ZG Controller Groups	7
		5.5.2 DBZ Conquering of ZG Controller Group	7
	5.6	Chapter Summary	8
	Refe	rences	8
6	ZG T	Fracking Control and Simulation of DI System	8
	6.1	Introduction	8
	6.2	Explicit Tracking Control of DI System via ZG Method	
	6.2	(ETC-DI-ZG)	8
	6.3	Successful Simulation of ETC-DI-ZG	8

Contents xix

	6.4	Implicit Tracking Control of DI System via ZG Method	
	<i>(5</i>	(ITC-DI-ZG)	8
	6.5	Failed Simulation of ITC-DI-ZG	8
	6.6	Finally Successful Simulation of ITC-DI-ZG	8
	6.7	Chapter Summary	9
	Refe	rences	9
7	ZG ?	Tracking Control of MI Systems	9
	7.1	Introduction	9
	7.2	Design of Controllers	10
		7.2.1 Design of ZD and ZG Controllers for LOF	10
		7.2.2 Design of ZD and ZG Controllers for NOF	10
	7.3	Convergence Performance Analyses on ZD Controllers	10
		7.3.1 Analysis on Tracking Control with LOF	10
		7.3.2 Analysis on Tracking Control with NOF	10
	7.4	Convergence Performance Analyses on ZG Controllers	10
		7.4.1 Analyses on Tracking Control with LOF	10
		7.4.2 Analyses on Tracking Control with NOF	10
	7.5	Simulation, Verification and Comparison	11
	7.6	Chapter Summary	11
	Refe	rences	11
Pai	rt III	Pendulum Systems Using ZG Control	
0	7D -	and 7C Control of Simula Dandalana Suatan	10
8		and ZG Control of Simple Pendulum System	
8	8.1	Introduction	12
8	8.1 8.2	Introduction	12 12
8	8.1 8.2 8.3	Introduction	12 12 12
8	8.1 8.2 8.3 8.4	Introduction ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary	12 12 12 12
8	8.1 8.2 8.3 8.4	Introduction	12 12 12 12
	8.1 8.2 8.3 8.4 Refe	Introduction ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary	12 12 12 12 12 13
	8.1 8.2 8.3 8.4 Refe	Introduction ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences	12 12 12 12 13
	8.1 8.2 8.3 8.4 Refe	Introduction ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences Path Tracking Control of IPC System	12 12 12 12 13
	8.1 8.2 8.3 8.4 Refe Cart 9.1	Introduction. ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences. Path Tracking Control of IPC System Introduction.	12 12 12 13 13 13
	8.1 8.2 8.3 8.4 Refe Cart 9.1 9.2	Introduction ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences. Path Tracking Control of IPC System Introduction Mathematical Model of IPC System	12 12 12 13 13 13 13 13
	8.1 8.2 8.3 8.4 Refe Cart 9.1 9.2	Introduction. ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences. Path Tracking Control of IPC System Introduction. Mathematical Model of IPC System Design of Controllers	12 12 12 13 13 13 13 13 13
	8.1 8.2 8.3 8.4 Refe Cart 9.1 9.2	Introduction. ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences. Path Tracking Control of IPC System Introduction. Mathematical Model of IPC System Design of Controllers 9.3.1 Design of ZD Controllers	12 12 12 13 13
	8.1 8.2 8.3 8.4 Refe Cart 9.1 9.2	Introduction. ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences. Path Tracking Control of IPC System Introduction. Mathematical Model of IPC System Design of Controllers 9.3.1 Design of ZD Controllers 9.3.2 Design of ZG Controllers	12 12 12 13 13 13 13 13 13 13
	8.1 8.2 8.3 8.4 Refe Cart 9.1 9.2 9.3	Introduction ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences Path Tracking Control of IPC System Introduction Mathematical Model of IPC System Design of Controllers 9.3.1 Design of ZD Controllers 9.3.2 Design of ZG Controllers 9.3.3 Discussion on Controller Implementation Convergence Performance Analyses	12 12 12 12 13 13 13 13 13 13 13 13 13 13
8	8.1 8.2 8.3 8.4 Refe Cart 9.1 9.2 9.3	Introduction ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences Path Tracking Control of IPC System Introduction Mathematical Model of IPC System Design of Controllers 9.3.1 Design of ZD Controllers 9.3.2 Design of ZG Controllers 9.3.3 Discussion on Controller Implementation Convergence Performance Analyses 9.4.1 Analyses on ZD Controllers	12 12 12 13 13 13 13 13 13 13 13 13 13 13 13 13
	8.1 8.2 8.3 8.4 Refe Cart 9.1 9.2 9.3	Introduction ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences Path Tracking Control of IPC System Introduction Mathematical Model of IPC System Design of Controllers 9.3.1 Design of ZD Controllers 9.3.2 Design of ZG Controllers 9.3.3 Discussion on Controller Implementation Convergence Performance Analyses 9.4.1 Analyses on ZD Controllers 9.4.2 Analyses on ZG Controllers	12 12 12 12 13 13 13 13 13 13 13 13
	8.1 8.2 8.3 8.4 Refe Cart 9.1 9.2 9.3	Introduction. ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences. Path Tracking Control of IPC System Introduction. Mathematical Model of IPC System Design of Controllers 9.3.1 Design of ZD Controllers 9.3.2 Design of ZG Controllers 9.3.3 Discussion on Controller Implementation Convergence Performance Analyses 9.4.1 Analyses on ZD Controllers. 9.4.2 Analyses on ZG Controllers. Simulation, Verification and Comparison	12 12 12 13 13 13 13 13 13 13 13 14
	8.1 8.2 8.3 8.4 Refe Cart 9.1 9.2 9.3	Introduction ZD Controller for Explicit Tracking Control ZG Controller for Implicit Tracking Control Chapter Summary rences Path Tracking Control of IPC System Introduction Mathematical Model of IPC System Design of Controllers 9.3.1 Design of ZD Controllers 9.3.2 Design of ZG Controllers 9.3.3 Discussion on Controller Implementation Convergence Performance Analyses 9.4.1 Analyses on ZD Controllers 9.4.2 Analyses on ZG Controllers	12 12 13 13 13 13 13 13 14 14 14

xx Contents

10	Pend	ulum Tracking Control of IPC System	157
	10.1	Introduction	157
	10.2	Design of Controllers	159
		10.2.1 Design of ZD Controller	159
		10.2.2 Design of ZG Controller	160
	10.3	Convergence Performance Analyses	161
	10.4	Simulation, Verification and Comparison	167
	10.5	Chapter Summary	174
	Refer	rences	174
Par	t IV	AFN Systems Using ZG Control	
11	GD-A	Aided IOL Tracking Control of AFN System	179
	11.1	Introduction	179
	11.2	AFN System and Problem Description	181
		11.2.1 AFN System	181
		11.2.2 Problem Description	181
	11.3	GD-Aided IOL Controller Design and Analyses	183
		11.3.1 Loose Condition on Relative Degree	183
		11.3.2 Design of GD-Aided IOL Controller	184
		11.3.3 Convergence Performance Analyses	185
	11.4	Simulation, Verification and Comparison	188
	11.5	Chapter Summary	190
	Refer	rences	193
12	ZG T	Prajectory Generation of Van der Pol Oscillator	195
	12.1	Introduction	195
	12.2	Design of ZD Controller	196
	12.3	Design of ZG Controller	197
	12.4	Simulation, Verification and Comparison	198
		12.4.1 Comparison Between ZD and ZG Controllers	198
		12.4.2 Effect of ZD Design Parameter on ZG Controller	200
		12.4.3 Effect of GD Design Parameter on ZG Controller	203
	12.5	Chapter Summary	205
	Refer	rences	206
13	ZD, Z	ZG and IOL Controllers for AFN System	207
	13.1	Introduction	207
	13.2	Design of Controllers	208
		13.2.1 Design of ZD Controller	208
		13.2.2 Design of ZG Controller	211
	13.3	Convergence Performance Analysis on ZD Controller	212
	13.4	Convergence Performance Analyses on ZG Controller	213
		13.4.1 Tight Error Bound	
		13.4.2 Exponential Convergence Rate	215

Contents xxi

	13.5	Simulation, Verification and Comparison 13.5.1 Standard Relative-Degree Case 13.5.2 PDBZ Relative-Degree Case 13.5.3 TDBZ Relative-Degree Case	216 216 218 219
	13.6	Chapter Summary	221
	Refer	ences	226
14	PDBZ	Z and TDBZ Problem Solving and Comparing	229
	14.1	Introduction	229
	14.2	DBZ Analysis and Classification	230
	14.3	PDBZ Example	232
		14.3.1 Problem Description	232
		14.3.2 Design of ZD and ZG Controllers	232
		14.3.3 Simulation, Verification and Comparison	234
	14.4	TDBZ Example	236
		14.4.1 Problem Description	236
		14.4.2 Design of ZD and ZG Controllers	236
		14.4.3 Simulation, Verification and Comparison	238
	14.5	Application to Two-Wheeled Mobile Robot	240
	14.6	Chapter Summary	243
	Refer	ences	244
Par	t V I	Cime-Varying Systems Using ZG Control	
Par 15		Cime-Varying Systems Using ZG Control Output Tracking of TVL System with DBZ Handled	249
			249 249
	ZG O	Output Tracking of TVL System with DBZ Handled	
	ZG O 15.1	Output Tracking of TVL System with DBZ Handled Introduction	249
	ZG 0 15.1 15.2	Output Tracking of TVL System with DBZ Handled Introduction	249 249
	ZG 0 15.1 15.2	Putput Tracking of TVL System with DBZ Handled Introduction	249 249 250
	ZG 0 15.1 15.2	Putput Tracking of TVL System with DBZ Handled	249 249 250 250
	ZG 0 15.1 15.2	Dutput Tracking of TVL System with DBZ Handled. Introduction. Problem Description Design of Controllers 15.3.1 Design of Conventional Controller 15.3.2 Design of ZD Controller	249 249 250 250 251
	ZG 0 15.1 15.2 15.3	Introduction	249 249 250 250 251 251
	ZG 0 15.1 15.2 15.3	Dutput Tracking of TVL System with DBZ Handled Introduction. Problem Description Design of Controllers 15.3.1 Design of Conventional Controller 15.3.2 Design of ZD Controller 15.3.3 Design of ZG Controller	249 249 250 250 251 251 252
15	ZG 0 15.1 15.2 15.3 15.4 15.5 Refer	Dutput Tracking of TVL System with DBZ Handled Introduction. Problem Description Design of Controllers 15.3.1 Design of Conventional Controller 15.3.2 Design of ZD Controller 15.3.3 Design of ZG Controller Simulation, Verification and Comparison Chapter Summary ences	249 249 250 250 251 251 252 256 256
	ZG O 15.1 15.2 15.3 15.4 15.5 Refer	Dutput Tracking of TVL System with DBZ Handled Introduction Problem Description Design of Controllers 15.3.1 Design of Conventional Controller 15.3.2 Design of ZD Controller 15.3.3 Design of ZG Controller Simulation, Verification and Comparison Chapter Summary ences tabilization of TVL System with PDBZ Shown	249 249 250 250 251 251 252 256 256
15	2G O 15.1 15.2 15.3 15.4 15.5 Refer 2G S 16.1	Dutput Tracking of TVL System with DBZ Handled Introduction. Problem Description Design of Controllers 15.3.1 Design of Conventional Controller 15.3.2 Design of ZD Controller 15.3.3 Design of ZG Controller Simulation, Verification and Comparison Chapter Summary ences. tabilization of TVL System with PDBZ Shown Introduction	249 249 250 250 251 251 252 256 256 257 257
15	2G O 15.1 15.2 15.3 15.4 15.5 Refer 2G S 16.1 16.2	Dutput Tracking of TVL System with DBZ Handled Introduction. Problem Description Design of Controllers 15.3.1 Design of Conventional Controller 15.3.2 Design of ZD Controller 15.3.3 Design of ZG Controller Simulation, Verification and Comparison Chapter Summary ences tabilization of TVL System with PDBZ Shown Introduction. Problem Description	249 249 250 250 251 251 252 256 256 257 257 258
15	2G 0 15.1 15.2 15.3 15.4 15.5 Refer 2G S 16.1 16.2 16.3	Introduction. Problem Description Design of Controllers 15.3.1 Design of Conventional Controller 15.3.2 Design of ZD Controller 15.3.3 Design of ZG Controller Simulation, Verification and Comparison Chapter Summary ences tabilization of TVL System with PDBZ Shown Introduction Problem Description Design of ZD Controller	249 249 250 251 251 252 256 257 257 258 258
15	2G O 15.1 15.2 15.3 15.4 15.5 Refer 2G S 16.1 16.2 16.3 16.4	Introduction. Problem Description Design of Controllers 15.3.1 Design of Conventional Controller 15.3.2 Design of ZD Controller 15.3.3 Design of ZG Controller Simulation, Verification and Comparison Chapter Summary ences tabilization of TVL System with PDBZ Shown Introduction Problem Description Design of ZD Controller Design of ZG Controller	2499 2500 2510 2551 2552 2566 2577 2558 2600
15	2G O 15.1 15.2 15.3 15.4 15.5 Refer 2G S 16.1 16.2 16.3 16.4 16.5	Introduction. Problem Description Design of Controllers 15.3.1 Design of Conventional Controller 15.3.2 Design of ZD Controller 15.3.3 Design of ZG Controller Simulation, Verification and Comparison Chapter Summary ences tabilization of TVL System with PDBZ Shown Introduction. Problem Description Design of ZD Controller Design of ZG Controller Simulation, Verification and Comparison	2499 2500 2550 2551 2551 2552 2566 2577 2558 2588 2680 2611
15	2G 0 15.1 15.2 15.3 15.4 15.5 Refer 2G S 16.1 16.2 16.3 16.4 16.5 16.6	Introduction. Problem Description Design of Controllers 15.3.1 Design of Conventional Controller 15.3.2 Design of ZD Controller 15.3.3 Design of ZG Controller Simulation, Verification and Comparison Chapter Summary ences tabilization of TVL System with PDBZ Shown Introduction Problem Description Design of ZD Controller Design of ZG Controller	2499 2500 2510 2551 2552 2566 2577 2558 2600

xxii Contents

Output Tracking of TVL and TVN Systems	27
Introduction	27
Design of Controllers for TVL System	27
17.2.1 Design of ZD Controller for TVL System	27
17.2.2 Design of ZG Controller for TVL System	27
Design of Controllers for TVN System	27
17.3.1 Design of ZD Controller for TVN System	27
17.3.2 Design of ZG Controller for TVN System	27
Simulation, Verification and Comparison	27
Chapter Summary	27
rences	28
	Design of Controllers for TVL System

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Acronyms

AFN Affine-form nonlinear DBZ Division-by-zero DΙ Double-integrator EF **Energy function** GD Gradient dynamics IOL Input-output linearization **IPC** Inverted-pendulum-on-a-cart LOF Linear output function ΜI Multiple-integrator MIMO Multiple-input multiple-output NOF Nonlinear output function **ODE** Ordinary differential equation PDBZ Pseudo-DBZ **TDBZ** True-DBZ ΤI Triple-integrator TVL Time-varying linear TVN Time-varying nonlinear **UBIBS** Uniformly bounded-input bounded-state ZD Zhang dynamics ZF Zhang function ZG Zhang-gradient ZNN Zhang neural network

List of Figures

Fig. 1.1	Flowchart of controller design using ZG method for tracking control of MIMO nonlinear system	8
Fig. 2.1	Crash of Lu chaotic system (2.2) equipped with conventional IOL controller (2.3) for desired trajectory $y_d = \sin(t) + 1.01$ when x_1 approaches zero. (a) Trajectory of x_1 . (b) Control input	19
Fig. 2.2	Tracking performance of Lu chaotic system (2.2) equipped with z2g0 controller (2.8) for desired trajectory $y_d = \sin(t) + 5$. (a) Output trajectory and desired trajectory. (b) Absolute tracking error	26
Fig. 2.3	Tracking performance of Lu chaotic system (2.2) equipped with z2g1 controller (2.11) for desired trajectory $y_d = \sin(t) + 5$. (a) Output trajectory and desired trajectory. (b) Absolute tracking error	27
Fig. 2.4	Effect of parameter γ on convergence error bound of absolute tracking error $ e $ for Lu chaotic system (2.2) equipped with z2g1 controller (2.11) to track desired trajectory $y_d = \sin(t) + 5$. (a) $ e $ in steady state with $\gamma = 10^3$. (b) $ e $ in steady state with $\gamma = 10^4$. (c) $ e $ in steady state with $\gamma = 10^5$. (d) $ e $ in steady state with	
Fig. 2.5	$\gamma = 10^6$	27
Fig. 2.6	Tracking performance of Lu chaotic system (2.2) equipped with z2g0 controller (2.8) for desired trajectory $y_d = \sin(t) + 1.01$ encountering DBZ point. (a) Trajectory of x_1 . (b) Control input	28

xxviii List of Figures

Fig. 2.7	Tracking performance of Lu chaotic system (2.2) equipped with conventional IOL controller (2.3) for desired trajectory $y_d = 2\cos(5t) + 3\sin(2t)$ encountering DBZ point. (a) Trajectories of y , y_d and x_1 . (b) Control input. (c) Absolute tracking error. (d) System states Tracking performance of Lu chaotic system (2.2) equipped with z2g1 controller (2.11) for desired trajectory $y_d = 2\cos(5t) + 3\sin(2t)$ encountering many DBZ points. (a) Trajectories of y , y_d and x_1 . (b) Control input. (c) Absolute tracking error. (d) System states	29
Fig. 3.1	Synchronization performance between Lu chaotic system (2.1) and Chen chaotic system (3.1) equipped with three inputs and using z3g0 controller group (3.8). (a) Trajectories of x_{1r} and x_{1d} . (b) Trajectories of x_{2r} and x_{2d} . (c) Trajectories of x_{3r} and x_{3d} . (d) Three-dimensional trajectories. (e) Synchronization errors. (f) Orders of $ e_1 $, $ e_2 $ and $ e_3 $	41
Fig. 3.2	Synchronization performance between Lu chaotic system (2.1) and Chen chaotic system (3.1) equipped with three inputs and using z3g3 controller group (3.9). (a) Trajectories of x_{1r} and x_{1d} . (b) Trajectories of x_{2r} and x_{2d} . (c) Trajectories of x_{3r} and x_{3d} . (d) Three-dimensional trajectories. (e) Synchronization errors. (f) Orders of $ e_1 $, $ e_2 $ and $ e_3 $	42
Fig. 3.3	Synchronization performance between Lu chaotic system (2.1) and Chen chaotic system (3.10) equipped with two inputs and using z4g2 controller group (3.15). (a) Trajectories of x_{1r} and x_{1d} . (b) Trajectories of x_{2r} and x_{2d} . (c) Trajectories of x_{3r} and x_{3d} . (d) Three-dimensional trajectories. (e) Synchronization errors. (f) Orders of $ e_1 $, $ e_2 $ and $ e_3 $	46
Fig. 4.1	Crash of modified Lorenz nonlinear system (4.3) equipped with conventional IOL controller (4.4) for desired trajectory	5 0
Fig. 4.2	$y_d = \cos(t)\sin(3t) + 3$. (a) Trajectory of x_1 . (b) Control input Tracking performance of modified Lorenz nonlinear system (4.3) equipped with ZG controller (4.11) via additive control input for desired trajectory $y_d = \sin(t)$. (a) System states. (b) Control input. (c) Output trajectory and desired	59
	trajectory. (d) Absolute tracking error	59

List of Figures xxix

Fig. 4.3	Tracking performance of modified Lorenz nonlinear system (4.3) equipped with ZG controller (4.11) via additive control input for desired trajectory $y_d = \cos(t)\sin(3t) + 3$. (a) Trajectory of x_1 . (b) Control input's time derivative. (c) Control input. (d) System states. (e) Output trajectory and	
Fig. 4.4	desired trajectory. (f) Absolute tracking error	60
Fig. 4.5	but suppressed more	62
Fig. 4.6	y_2 and desired trajectory y_{2d}	66
Fig. 5.1	Tracking performance of Brockett integrator (5.1) equipped with z2g0 controller group (5.4) and z2g1 controller group (5.5), respectively, for desired trajectories $y_{1d} = \sin(t) - 2$ and $y_{2d} = \cos(t)$. (a) Output trajectories with z2g0 controller group (5.4) and desired trajectories. (b) Output trajectories with z2g1 controller group (5.5) and desired trajectories. (c) Tracking errors with z2g0 controller group (5.4). (d) Tracking errors with z2g1 controller group (5.5).	77
Fig. 5.2	Tracking performance of Brockett integrator (5.1) equipped with z2g0 controller group (5.4) and z2g1 controller group (5.5), respectively, for desired trajectories $y_{1d} = \sin(t)$ and $y_{2d} = \cos(t) \exp(-t/20)$. (a) Output trajectories with z2g0 controller group (5.4) and desired trajectories. (b) Output trajectories with z2g1 controller group (5.5) and desired trajectories. (c) Trajectory of x_1 with z2g0 controller group	
	(5.4). (d) Trajectory of x_1 with z2g1 controller group (5.5)	78

xxx List of Figures

Fig. 5.3	Tracking errors of Brockett integrator (5.1) equipped with z2g1 controller group (5.5) for desired trajectories $y_{1d} = \sin(t) - \kappa_i$, with $i \in \{1, 2, 3, 4\}$, and $y_{2d} = \cos(t)$. (a) With $\kappa_1 = 1.01$. (b) With $\kappa_2 = 2$. (c) With $\kappa_3 = 5$. (d) With $\kappa_4 = 10$	79
Fig. 6.1	Successful computer simulation with ZG controller (6.8) applied to DI system (6.2) for output $y = x_1$ to track desired trajectory $y_d = \sin(t) + \cos(t)$. (a) Output trajectory and desired trajectory. (b) System states. (c) Control input. (d) Absolute tracking error	86
Fig. 6.2	Absolute tracking errors with different values of parameter λ for ZG controller (6.8) applied to DI system (6.2), where output $y = x_1$ tracks desired trajectory $y_d = \sin(t) + \cos(t)$. (a) With $\lambda = 10$. (b) With $\lambda = 50$. (c) With $\lambda = 100$. (d)	0.7
Fig. 6.3	With $\lambda = 200$	87
Fig. 6.4	(c) Control input. (d) Absolute tracking error	89
Fig. 6.5	Absolute tracking error	90
Fig. 6.6	Failed computer simulation with ZG controller (6.10) applied to DI system (6.9) for output $y = x_1^2 + x_2^2$ to track desired trajectory $y_d = \sin(t) + 2$ using ode45 with option "RelTol=1e-8". (a) Output trajectory and desired trajectory. (b) System states. (c) Control input. (d) Absolute tracking	
	error	92

List of Figures xxxi

Fig. 6.7	Tracking performance of system (6.1) equipped with ZG controller (6.11) for output $y = x_1x_2$ to track desired trajectory $y_d = \sin(t) \exp(-0.1t) + 2$. (a) Output trajectory and desired trajectory. (b) System states. (c) Control input. (d) Absolute tracking error	96
Fig. 7.1	Output trajectories and control inputs of TI system (7.2) equipped with z3g0 controller (7.3) and z3g1 controller (7.4), respectively, for desired trajectory $y_d = \sin(2t)\cos(2t)$. (a) Output trajectory with z3g0 controller (7.3) and desired trajectory. (b) Output trajectory with z3g1 controller (7.4) and desired trajectory. (c) Control input with z3g0 controller (7.3). (d) Control input with z3g1	
Fig. 7.2	controller (7.4)	110 111
Fig. 7.3	Output trajectories, control inputs and absolute tracking errors of TI system (7.2) equipped with z3g0 controller (7.6) and z3g1 controller (7.7), respectively, for desired trajectory $y_d = \sin(t)$. (a) Output trajectory with z3g0 controller (7.6) and desired trajectory. (b) Order of $ e $ with z3g0 controller (7.6). (c) Control input with z3g0 controller (7.6). (d) Output trajectory with z3g1 controller (7.7) and desired trajectory. (e) Order of $ e $ with z3g1 controller (7.7). (f) Control input with z3g1 controller (7.7).	113
Fig. 7.4	Output trajectories and absolute tracking errors of TI system (7.2) equipped with z2g1 controller (7.24) with $y = x_1^2 + x_2^2$ and z1g1 controller (7.25) with $y = x_1x_2x_3$, respectively, for desired trajectory $y_d = \sin(t) \exp(-0.1t) + 2$. (a) Output trajectory with z2g1 controller (7.24) and desired trajectory. (b) Output trajectory with z1g1 controller (7.25) and desired trajectory. (c) Order of $ e $ with z2g1 controller (7.24). (d) Order of $ e $ with z1g1 controller (7.25)	116
Fig. 7.5	Absolute tracking errors of quadruple-integrator system equipped with z4g0 controller (7.26) and z4g1 controller (7.27), respectively, for desired trajectory $y_d = \sin(t)$. (a) Order of $ e $ with z4g0 controller (7.26). (b) Order of $ e $	
	with z4g1 controller (7.27)	117

xxxii List of Figures

Fig. 7.6	Output trajectories and absolute tracking errors of quintuple-integrator system equipped with z4g0 controller (7.28) and z4g1 controller (7.29), respectively, for desired trajectory $y_d = \cos(t) + 2$. (a) Output trajectory with z4g0 controller (7.28) and desired trajectory. (b) Output trajectory with z4g1 controller (7.29) and desired trajectory. (c) Order of $ e $ with z4g0 controller (7.28). (d) Order of $ e $ with z4g1 controller (7.29)	118
Fig. 8.1 Fig. 8.2	Schematic of simple pendulum system	124
Fig. 8.3	Tracking performance and crash of simple pendulum system (8.1) equipped with z1g0 controller (8.5) for DBZ-containing implicit tracking control with desired trajectory (8.3). (a) Output trajectory and desired trajectory. (b) Tracking error. (c) System states. (d) Control input	127
Fig. 8.4	Tracking performance of simple pendulum system (8.1) equipped with z1g1 controller (8.6) for DBZ-containing implicit tracking control with desired trajectories (8.3) and (8.4), respectively. (a) Output trajectory and desired trajectory (8.3). (b) Output trajectory and desired trajectory (8.4). (c) Tracking error with desired trajectory (8.3). (d) Tracking error with desired trajectory (8.4). (e) System states and control input with desired trajectory (8.3). (f) System states and control input with desired trajectory (8.4)	128
Fig. 8.5	Tracking performance of simple pendulum system (8.1) equipped with z1g1 controller (8.7) for DBZ-containing implicit tracking control with desired trajectory (8.3), which gets through DBZ point of $\alpha_1 = 0$ successfully. (a) Output trajectory and desired trajectory. (b) Tracking error. (c) System states and control input. (d) Trajectory of α_1	129
Fig. 9.1 Fig. 9.2	Schematic of IPC system	133
	controller (9.7)	139

List of Figures xxxiii

Fig. 9.3	Output trajectories and control inputs of IPC system (9.2) equipped with z2g0 controller (9.5) and z2g1 controller	
	(9.7), respectively, for desired trajectory $y_d = \cos(\pi t/10)$.	
	(a) Output trajectory with z2g0 controller (9.5) and desired	
	trajectory. (b) Output trajectory with z2g0 controller (9.5) and desired trajectory. (b) Output trajectory with z2g1 controller (9.7)	
	and desired trajectory. (c) Control input with z2g0 controller	1 47
Ei. 0.4	(9.5). (d) Control input with z2g1 controller (9.7)	147
Fig. 9.4	Tracking errors of IPC system (9.2) equipped with z2g0	
	controller (9.5) and z2g1 controller (9.7), respectively, for	
	desired trajectory $y_d = \cos(\pi t/10)$. (a) Tracking error	
	with z2g0 controller (9.5). (b) Tracking error with z2g1	
	controller (9.7). (c) Order of $ e $ with z2g0 controller (9.5).	4.40
	(d) Order of $ e $ with z2g1 controller (9.7)	148
Fig. 9.5	Output trajectories and absolute tracking errors of IPC	
	system (9.2) equipped with z2g0 controller (9.6) and	
	z2g1 controller (9.8), respectively, for desired trajectory	
	$y_d = \sin(t) \exp(-t/5) + 0.12$. (a) Output trajectory with	
	z2g0 controller (9.6) and desired trajectory. (b) Output	
	trajectory with z2g1 controller (9.8) and desired trajectory.	
	(c) Order of $ e $ with z2g0 controller (9.6). (d) Order of $ e $	
	with z2g1 controller (9.8)	149
Fig. 9.6	Control inputs and trajectories of denominator α_5 of IPC	
	system (9.2) equipped with z2g0 controller (9.6) and	
	z2g1 controller (9.8), respectively, for desired trajectory	
	$y_d = \sin(t) \exp(-t/5) + 0.12$. (a) Control input with z2g0	
	controller (9.6). (b) Control input with z2g1 controller	
	(9.8). (c) Trajectory of α_5 with z2g0 controller (9.6). (d)	
	Trajectory of α_5 with z2g1 controller (9.8)	150
Fig. 9.7	Output trajectories and absolute tracking errors of IPC	
	system (9.2) equipped with z2g0 controller (9.6) and	
	z2g1 controller (9.8), respectively, for desired trajectory	
	$y_d = \sin(t)\cos(t) + 0.25$. (a) Output trajectory with z2g0	
	controller (9.6) and desired trajectory. (b) Output trajectory	
	with z2g1 controller (9.8) and desired trajectory. (c) Order	
	of $ e $ with z2g0 controller (9.6). (d) Order of $ e $ with z2g1	
	controller (9.8)	151
Fig. 9.8	Control inputs and trajectories of denominator α_5 for	
8. >	IPC system (9.2) equipped with z2g0 controller (9.6) and	
	z2g1 controller (9.8), respectively, for desired trajectory	
	$y_d = \sin(t)\cos(t) + 0.25$. (a) Control input with z2g0	
	controller (9.6). (b) Control input with z2g1 controller	
	(9.8). (c) Trajectory of α_5 with z2g0 controller (9.6). (d)	
	Trajectory of α_5 with z2g1 controller (9.8).	152
	114,00001, 01 4 1 1141 DEST 00114 OHO! (1.0)	104

xxxiv List of Figures

Fig. 9.9	Output trajectories, control inputs and tracking errors of IPC system in Remark 9.1 respectively equipped with z2g0 controller and z2g1 controller for explicit tracking control, shown in Table 9.3, for desired trajectory $y_d = \cos(\pi t/10)$. (a) Output trajectory with z2g0 controller and desired trajectory. (b) Output trajectory with z2g1 controller and desired trajectory. (c) Control input with z2g0 controller. (d) Control input with z2g1 controller. (e) Tracking error with z2g0 controller. (f) Tracking error with z2g1 controller.	154
Fig. 9.10	Tracking errors with different values of design parameters for IPC system in Remark 9.1 equipped with z2g1 controller for explicit tracking control, shown in Table 9.3, for desired trajectory $y_d = \cos(\pi t/10)$. (a) With $\lambda_1 = \lambda_2 = 8$ and $\gamma = 10$. (b) With $\lambda_1 = \lambda_2 = 8$ and $\gamma = 20$. (c) With $\lambda_1 = \lambda_2 = 15$ and $\gamma = 20$. (d) With $\lambda_1 = \lambda_2 = 15$ and $\gamma = 40$.	155
Fig. 10.1	Output trajectory, control input and tracking error of IPC system (9.2) equipped with z2g0 controller (10.4) for desired trajectory $y_d = \sin(0.1\pi t)\cos(0.2\pi t)$. (a) Output trajectory and desired trajectory. (b) Control input. (c) Tracking error. (d) Order of $ e $	168
Fig. 10.2	Output trajectory, control input and tracking error of IPC system (9.2) equipped with z2g1 controller (10.5) for desired trajectory $y_d = \sin(0.1\pi t)\cos(0.2\pi t)$. (a) Output trajectory and desired trajectory. (b) Control input. (c) Tracking error. (d) Order of $ e $	169
Fig. 10.3	Output trajectories and tracking errors of IPC system (9.2) equipped with z2g0 controller (10.4) and z2g1 controller (10.5), respectively, for desired trajectory $y_d = 0.3\pi \cos(0.5t) \exp(-0.2t)$. (a) Output trajectory with z2g0 controller (10.4) and desired trajectory. (b) Tracking error with z2g0 controller (10.4). (c) Output trajectory with z2g1 controller (10.5) and desired trajectory. (d) Tracking error with z2g1 controller (10.5)	170
Fig. 10.4	Control inputs and trajectories of denominator $\cos x_3$ of IPC system (9.2) equipped with z2g0 controller (10.4) and z2g1 controller (10.5), respectively, for desired trajectory $y_d = 0.3\pi \cos(0.5t) \exp(-0.2t)$. (a) Control input with z2g0 controller (10.4). (b) Trajectory of $\cos x_3$ with z2g0 controller (10.4). (c) Control input with z2g1 controller	
	(10.5). (d) Trajectory of $\cos x_3$ with z2g1 controller (10.5)	171

List of Figures xxxv

Fig. 10.5	Output trajectories and control inputs of IPC system (9.2) equipped with z2g0 controller (10.4) and z2g1 controller (10.5), respectively, for desired trajectory $y_d = 0.5(\sin(t) + \cos(0.5\pi t))$. (a) Output trajectory with z2g0 controller (10.4) and desired trajectory. (b) Control input with z2g0 controller (10.4). (c) Output trajectory with z2g1 controller (10.5) and desired trajectory. (d) Control input with z2g1 controller (10.5)	172
Fig. 10.6	Absolute tracking errors with different small values of design parameters for IPC system (9.2) equipped with z2g1 controller (10.5) for desired trajectory $y_d = 0.5(\sin(t) + \cos(0.5\pi t))$. (a) With $\lambda_1 = \lambda_2 = 12$ and $\gamma = 30$. (b) With $\lambda_1 = \lambda_2 = 12$ and $\gamma = 45$. (c) With $\lambda_1 = \lambda_2 = 16$ and $\gamma = 45$. (d) With $\lambda_1 = \lambda_2 = 16$ and $\gamma = 60$	173
Fig. 11.1	Crash of AFN system (11.12) equipped with conventional IOL controller (11.2) for desired trajectory $y_d = \sin(t) + 1.05$ encountering DBZ point. (a) Trajectory of $L_h L_g^2 y$. (b)	
Fig. 11.2	Control input	189 190
Fig. 11.3	Absolute tracking errors of AFN system (11.12) equipped with GD-aided IOL controller (11.5) using different values of parameter γ for desired trajectory $y_d = \sin(t) + 1.05$ encountering DBZ points. (a) With $\gamma = 10^2$. (b) With $\gamma = 10^3$. (c) With $\gamma = 10^4$. (d) With $\gamma = 10^5$	191
Fig. 12.1	Trajectory-generation performance of Van der Pol oscillator (12.1) equipped with z2g0 controller (12.3) and z2g1 controller (12.4), respectively, for desired trajectory $y_d = \sin(t)$. (a) Output trajectory with z2g0 controller (12.3) and desired trajectory. (b) Output trajectory with z2g1 controller (12.4) and desired trajectory. (c) System states with z2g0 controller (12.3). (d) System states with z2g1 controller (12.4). (e) Absolute tracking error with z2g0 controller (12.3). (f) Absolute tracking error with z2g1 controller (12.4).	199

xxxvi List of Figures

Fig. 12.2	Control inputs of Van der Pol oscillator (12.1) equipped with z2g0 controller (12.3) and z2g1 controller (12.4), respectively, for desired trajectory $y_d = \sin(t)$. (a) Control input with z2g0 controller (12.3). (b) Control input with	
	z2g1 controller (12.4)	200
Fig. 12.3	Trajectory-generation performance of Van der Pol oscillator	
	(12.1) equipped with z2g0 controller (12.3) and z2g1	
	controller (12.4), respectively, for desired trajectory	
	$y_d = \cos(2t) \exp(0.1t)$. (a) Output trajectory with z2g0	
	controller (12.3) and desired trajectory. (b) Output trajectory	
	with $z2g1$ controller (12.4) and desired trajectory. (c)	
	System states with z2g0 controller (12.3). (d) System states	
	with z2g1 controller (12.4). (e) Absolute tracking error with	
	z2g0 controller (12.3). (f) Absolute tracking error with z2g1	
	controller (12.4)	201
Fig. 12.4	Control inputs of Van der Pol oscillator (12.1) equipped	
	with z2g0 controller (12.3) and z2g1 controller (12.4),	
	respectively, for desired trajectory $y_d = \cos(2t) \exp(0.1t)$.	
	(a) Control input with z2g0 controller (12.3). (b) Control	
	input with z2g1 controller (12.4)	202
Fig. 12.5	Absolute tracking errors of Van der Pol oscillator (12.1)	
	equipped with z2g1 controller (12.4) using different values	
	of ZD design parameter λ for desired trajectory $y_d = \sin(t)$.	
	(a) Absolute tracking error with $\lambda = 5$. (b) Absolute	
	tracking error with $\lambda = 10$. (c) Absolute tracking error with	
	$\lambda = 20$. (d) Absolute tracking error with $\lambda = 30$	202
Fig. 12.6	Control inputs of Van der Pol oscillator (12.1) equipped with	
	z2g1 controller (12.4) using different values of ZD design	
	parameter λ for desired trajectory $y_d = \sin(t)$. (a) Control	
	input with $\lambda = 5$. (b) Control input with $\lambda = 10$. (c) Control	
	input with $\lambda = 20$. (d) Control input with $\lambda = 30$	203
Fig. 12.7	Absolute tracking errors of Van der Pol oscillator (12.1)	
	equipped with z2g1 controller (12.4) using different	
	values of GD design parameter γ for desired trajectory	
	$y_d = \cos(2t) \exp(0.1t)$. (a) Absolute tracking error with	
	$\gamma = 10$. (b) Absolute tracking error with $\gamma = 10^3$. (c)	
	Absolute tracking error with $\gamma = 10^5$. (d) Absolute tracking	
	error with $\gamma = 10^7$	204

List of Figures xxxvii

Fig. 12.8	Control inputs of Van der Pol oscillator (12.1) equipped with z2g1 controller (12.4) using different values of GD design parameter γ for desired trajectory $y_d = \cos(2t) \exp(0.1t)$. (a) Control input with $\gamma = 10$. (b) Control input with $\gamma = 10^3$. (c) Control input with $\gamma = 10^5$. (d) Control input with $\gamma = 10^7$	205
Fig. 13.1	Tracking performance of AFN system (13.14) equipped with IOL, ZD and ZG controllers, respectively, for desired trajectory $y_d = \sin(t)$. (a) Control inputs. (b) Trajectories of $L_h L_g y$. (c) Output trajectories and desired trajectory. (d) Absolute tracking errors	218
Fig. 13.2	Tracking performance of AFN system (13.15) equipped with IOL, ZD and ZG controllers, respectively, for desired trajectory $y_d = \sin(t)$. (a) Control inputs. (b) Trajectories of $L_h L_g y$. (c) Output trajectories and desired trajectory. (d) Absolute tracking errors	220
Fig. 13.3	Chaotic characteristic and tracking performance of Lu chaotic system (13.16) equipped with IOL, ZD and ZG controllers, respectively, for desired trajectory $y_d = \sin(t) + 1.05$. (a) Chaotic characteristic. (b) Trajectories of $L_h L_g y$. (c) Output trajectories and desired trajectory. (d) Absolute tracking errors	221
Fig. 14.1	Tracking performance of system (14.2) equipped with z2g0 controller (14.3) and z2g1 controller (14.4), respectively, for desired trajectory $y_d = \sin(0.5t)$. (a) System states with z2g0 controller (14.3). (b) System states with z2g1 controller (14.4). (c) Output trajectory with z2g0 controller (14.3) and desired trajectory. (d) Output trajectory with z2g1 controller (14.4) and desired trajectory. (e) Absolute tracking error with z2g0 controller (14.3). (f) Absolute tracking error with z2g1 controller (14.4)	235
Fig. 14.2	Control inputs of system (14.2) equipped with z2g0 controller (14.3) and z2g1 controller (14.4), respectively, for desired trajectory $y_d = \sin(0.5t)$. (a) Control input with z2g0 controller (14.3). (b) Control input with z2g1 controller (14.4)	236
Fig. 14.3	Trajectories of denominator α_3 for system (14.5) equipped with z2g0 controller (14.9) and z2g1 controller (14.10), respectively, for desired trajectory $y_d = 0.5 \sin(3t) + 0.25$. (a) Trajectory of α_3 with z2g0 controller (14.9). (b) Trajectory of α_3 with z2g1 controller (14.10)	
	Trajectory of α_3 with z/g1 controller (14.10)	238

xxxviii List of Figures

Fig. 14.4	Tracking performance of system (14.5) equipped with z2g0 controller (14.9) and z2g1 controller (14.10), respectively,	
	for desired trajectory $y_d = 0.5 \sin(3t) + 0.25$. (a) System	
	states with z2g0 controller (14.9). (b) System states with	
	z2g1 controller (14.10). (c) Output trajectory with z2g0	
	controller (14.9) and desired trajectory. (d) Output trajectory	
	with z2g1 controller (14.10) and desired trajectory. (e)	
	Absolute tracking error with z2g0 controller (14.9). (f)	
	Absolute tracking error with z2g1 controller (14.10)	239
Fig. 14.5	Control inputs of system (14.5) equipped with z2g0	
	controller (14.9) and z2g1 controller (14.10), respectively,	
	for desired trajectory $y_d = 0.5 \sin(3t) + 0.25$. (a) Control	
	input with z2g0 controller (14.9). (b) Control input with	
	z2g1 controller (14.10)	240
Fig. 14.6	Schematic diagram of two-wheeled mobile robot	241
Fig. 14.7	Tracking performance of two-wheeled mobile robot (14.11)	
	equipped with ZG controller group (14.15) for desired	
	circular trajectory (14.16). (a) Actual trajectory and desired	
	trajectory. (b) Absolute tracking errors. (c) State variables.	
	(d) Translational velocity and angular velocity	243
Fig. 15.1	Tracking performance of TVL system (15.9) equipped	
11g. 13.1	with conventional controller (15.2) for desired trajectory	
	$y_d = \sin(0.5t)$. (a) Output trajectory and desired trajectory.	
	(b) Absolute tracking error	252
Fig. 15.2	Tracking performance of TVL system (15.9) equipped with	232
11g. 13.2	ZD controller (15.6) for desired trajectory $y_d = \sin(0.5t)$.	
	(a) Output trajectory and desired trajectory. (b) Absolute	
	tracking error	253
Fig. 15.3	Tracking performance of TVL system (15.9) equipped with	233
11g. 15.5		
	ZG controller (15.8) for desired trajectory $y_d = \sin(0.5t)$.	
	(a) Output trajectory and desired trajectory. (b) Absolute	253
Eig 15 4	Tracking performance of TVL system (15.10) equipped	233
Fig. 15.4	with conventional controller (15.2) for desired trajectory	
	$y_d = 10 \sin(2t) + 0.5t$. (a) Output trajectory and desired	254
Eig 155	trajectory. (b) Absolute tracking error	234
Fig. 15.5	Tracking performance of TVL system (15.10) equipped with TD controller (15.6) for desired trainetery	
	with ZD controller (15.6) for desired trajectory $v_{1} = 10 \sin(2t) + 0.5t \text{ (a) Output trajectory and desired}$	
	$y_d = 10 \sin(2t) + 0.5t$. (a) Output trajectory and desired trajectory (b) Absolute tracking error	255
	HAICCIOI V. UD) ADSOILLE HACKING CITOF	7.17

List of Figures xxxix

Fig. 15.6	Tracking performance of TVL system (15.10) equipped with ZG controller (15.8) for desired output trajectory $y_d = 10 \sin{(2t)} + 0.5t$. (a) Output trajectory and desired trajectory. (b) Absolute tracking error. (c) System states. (d) Control input	255
Fig. 16.1	Stabilization performance of TVL system (16.1) equipped with ZD controller (16.10) using $w = 0.2 \text{ rad/s}$. (a) System state x_1 . (b) System state x_2 . (c) Control input. (d) Square sum of x_1 and x_2	262
Fig. 16.2	Stabilization performance of TVL system (16.1) equipped with ZG controller (16.17) using $w = 0.2$ rad/s. (a) System state x_1 . (b) System state x_2 . (c) Control input. (d) Square sum of x_1 and x_2	263
Fig. 16.3	Stabilization performance of TVL system (16.1) equipped with ZD controller (16.10) using $w = 2 \text{ rad/s}$. (a) System state x_1 . (b) System state x_2 . (c) Control input. (d) Square	
Fig. 16.4	sum of x_1 and x_2	264
Fig. 16.5	sum of x_1 and x_2	265
Fig. 16.6	sum of x_1 and x_2	266
Fig. 16.7	Stabilization performance of TVL system (16.1) equipped with ZD controller (16.10) using $w = 2$ rad/s when specially simulated to DBZ time instant. (a) System state x_1 . (b) System state x_2 . (c) Control input. (d) Square sum of x_1 and x_2	
Fig. 16.8	Stabilization performance of TVL system (16.1) equipped with ZG controller (16.17) using $w = 2$ rad/s when specially simulated to DBZ time instant. (a) System state x_1 . (b) System state x_2 . (c) Control input. (d) Square sum of x_1 and x_2	
Fig. 17.1	Tracking performance of TVL system (17.1) equipped with ZD controller (17.4) for desired trajectory $y_d = \cos(t) + \sin(2t) + 2$. (a) Output trajectory and desired trajectory. (b) Absolute tracking error. (c) Control input. (d) Control input from beginning to DBZ time instant $t \approx 5.236$ s	

xl List of Figures

Fig. 17.2	Tracking performance of TVL system (17.1) equipped	
	with ZG controller (17.5) for desired trajectory	
	$y_d = \cos(t) + \sin(2t) + 2$. (a) Output trajectory and desired	
	trajectory. (b) Absolute tracking error. (c) Control input. (d)	
	Control input from beginning to DBZ time instant $t \approx 5.236$ s	277
Fig. 17.3	Tracking performance of TVN system (17.6) equipped with	
	ZD controller (17.8) for desired trajectory $y_d = \exp(\sin(t))$.	
	(a) Output trajectory and desired trajectory. (b) Absolute	
	tracking error. (c) Control input. (d) Control input from	
	beginning to DBZ time instant $t \approx 5.236 \mathrm{s}$	278
Fig. 17.4	Tracking performance of TVN system (17.6) equipped with	
	ZG controller (17.9) for desired trajectory $y_d = \exp(\sin(t))$.	
	(a) Output trajectory and desired trajectory. (b) Absolute	
	tracking error. (c) Control input. (d) Control input from	
	beginning to DBZ time instant $t \approx 5.236$ s	279

List of Tables

Table 2.1	Conventional IOL controllers and DBZ problems of Lorenz,	10
Table 2.2	Chen and Lu chaotic systems with single control input	19
	Chen and Lu chaotic systems with single control input	21
Table 5.1	ZD and ZG Controller groups with different output combinations	73
Table 5.2	ζ	
	integrator (5.1) equipped with z2g1 controller group (5.5)	
	for desired trajectories $y_{1d} = \sin(t) - \kappa_i$, with	
	$i \in \{1, 2, 3, 4\}, \text{ and } y_{2d} = \cos(t) \dots$	80
Table 6.1	Statistics of failed and successful simulation tests	93
Table 8.1	Parameter values of simple pendulum system	125
Table 9.1	Parameter values of IPC system	134
Table 9.2	Controllers of z2g0 and z2g1 types for explicit and implicit tracking control of IPC system with pendulum rod being	
	zero mass	137
Table 9.3	Controllers of z2g0 and z2g1 types for explicit and implicit tracking control of IPC system with pendulum rod being	
	nonzero mass	138