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# Preface

Since it was first organized in 1997, the Japan Conference on Discrete and Computational Geometry (JCDCG) continues to attract an international audience. The first five conferences of the series were held in Tokyo, the sixth in Manila, Philippines. This volume consists of the refereed papers presented at the seventh conference, JCDCG 2002, held in Tokai University, Tokyo, December 6–9, 2002. An eighth conference is planned to be held in Bandung, Indonesia.

The proceedings of JCDCG 1998 and JCDCG 2000 were published by Springer-Verlag as part of the series Lecture Notes in Computer Science: LNCS volumes 1763 and 2098, respectively. The proceedings of JCDCG 2001 were also published by Springer-Verlag as a special issue of the journal *Graphs and Combinatorics*, Vol. 18, No. 4, 2002.

The organizers are grateful to Tokai University for sponsoring the conference. They wish to thank all the people who contributed to the success of the conference, in particular, Chie Nara, who headed the conference secretariat, and the principal speakers: Takao Asano, David Avis, Greg N. Frederickson, Ferran Hurtado, Joseph O'Rourke, János Pach, Rom Pinchasi, and Jorge Urrutia.

October 2003

Jin Akiyama  
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