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# Verbumculus and the Discovery of Unusual Words

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## Abstract

Measures relating word frequencies and expectations have been constantly of interest in Bioinformatics studies. With sequence data becoming massively available, exhaustive enumeration of such measures have become conceivable, and yet pose significant computational burden even when limited to words of bounded maximum length. In addition, the display of the huge tables possibly resulting from these counts poses practical problems of visualization and inference.

VERBUMCULUS is a suite of software tools for the efficient and fast detection of over- or under-represented words in nucleotide sequences. The inner core of VERBUMCULUS rests on subtly interwoven properties of statistics, pattern matching and combinatorics on words, that enable one to limit drastically and *a priori* the set of over- or under-represented candidate words of all lengths in a given sequence, thereby rendering it more feasible both to detect and visualize such words in a fast and practically useful way. This paper is devoted to the description of the facility at the outset and to report experimental results, ranging from simulations on synthetic data to the discovery of regulatory elements on the upstream regions of a set of genes of the yeast.

The software VERBUMCULUS is accessible at <http://www.cs.ucr.edu/~stelo/Verbumculus/> or <http://wwdbl.dei.unipd.it/Verbumculus/>

**Keywords:** verbumculus, unusual words, subword statistics, pattern discovery, regulatory elements, suffix trees

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# 1 Introduction

Over one decade after National Research Council mapped out the plan for the Human Genome Project, the project has been developed into a full fledged research field – Genomics, which transforms biology researches from cottage endeavor into enterprise operation. Genomic researches are mainly organized around two areas: high throughput DNA sequencing and genome-wise detection of gene expression. Sequence data in both public and private databases have been accumulating at exponential rate under continuous improvement of sequencing technology and steady increase of funding [24, 16]. Whole genome sequences have been constantly churning out from the genomic centers around the world since the first whole genome sequence was published [19]. Over fifty whole genome sequences are currently available for prokaryotic and eukaryotic organisms.

High density array technologies such as DNA microarray and gene chip not only provide a systematic and global snapshot of genome expression in relation to developmental stages, anatomical structures, and/or external cues, but also offer a powerful means to cluster genes based on their temporal, spatial and amplitude patterns of expression [44, 32, 17, 15]. Together with sequence data, expression data would enable the assignment of functional information to genes of otherwise unknown functions. The conceptual assumption of the approach is that genes that exhibit similar expression patterns contribute to the same biological process or functions. Therefore such genes share more or less common regulatory domains in the upstream regions for the coordinated control of gene expression.

A large number of nucleotide motifs show distinct distribution patterns within the genomes of various organisms, and can be distinguished from each other. Moreover, during the evolutionary process, living organisms have accumulated certain biases towards or against some specific motifs in their genomes, which are used as regulatory elements. Highly recurring nucleotide words are often observed to correspond to regulatory regions or protein binding sites of genes. Vice versa, rare nucleotide motifs may be discriminated against due to structural constraints of genomes or specific reservations for global transcription controls, such as in early cascade of embryo development.

Whole genome sequences together with genome-wise expression data offer a global view of genomic structure and functions of a living system. However, it is a great challenge to assign functions to DNA sequences. For example, out of circa 30-40 thousands genes in human genome, only about 10,000 are associated with known functions. Thus, global and systematic search for sequence patterns in genomes is a necessary step to link structural sequences to defined functions. This paper describes our software development (VERBUMCULUS) in a genome-wise searching system for over- or under-represented nucleotide motifs, and our initial effort to attribute biological functions to those motifs. The main advantages brought about by VERBUMCULUS are in terms of speed, flexibility and visualization efficiency. This rests on the core structure of the program, which takes advantage of strong properties at the intersection of statistics, pattern matching and combinatorics on words [5, 4]. The facility at the outset can conduct global pattern discovery in linear time and space.

In general, the task of detecting, enumerating and testing nucleotide word frequencies in large genomes, which are typical cases for eukaryotic organisms, requires significant computational resources even when limited to the words up to some maximum length. It often becomes infeasible to detect and visualize such words in a fast and practically useful way. Among the tools available for these purposes, we list WORDUP [39], YEAST-TOOLS [49], and R'MES [43, 42]. Conceived primarily as an aid in intercepting conserved segments in related sequences in a family, WORDUP is based on a first order Markov model. It detects statistically significant sequence motifs of 6-10 nucleotides in a family of sequences by comparing the expected number of sequences containing a

given pattern with the number of observed sequences that contain that pattern. The facilities under YEAST-TOOLS comprise tables of frequencies for nucleotide words of up to 10 bases as observed in all coding and non-coding regions of the yeast genome. The related analyses of frequencies and expectations invest the entire target genome, with the objective of identifying relatively simple statistically relevant patterns represented by short motifs with a highly conserved core. R'MES is a general-purpose set of programs to detect words that appear in a given DNA sequence with unexpected frequency. Two classes of models are used to model the sequence: stationary Markov chains and 3-periodic stationary Markov chains. Under either probabilistic model, the number of occurrences of a word in a sequence is considered to be statistically interesting if it differs significantly from an estimator of its expected value. Estimators of the expected counts are obtained using a Gaussian or (for long words) a compound Poisson approximation. In either case, R'MES provides a score indicating whether the word is under- or over-represented.

The search for unexpectedly frequent or rare substrings is only one component of the broader quest for interesting patterns of more general kinds. Along these lines, patterns and families thereof have been variously characterized, and criteria, algorithms and software developed in correspondence. Without pretending to be exhaustive, we mention SPEXS [10, 11], MEME [8], PRATT [28, 27], YEBIS [52], SPLASH [14], TEIRESIAS [41], CONSENSUS [25], GIBBS SAMPLER [30, 36], WINNOWER [40, 29], PROJECTION [13], WEEDER [38] MITRA [18], among others. The performance of these tools has been increasing dramatically over the years, though the hardest challenges (see, e.g., [40]) are still terrain for contests.

This paper is organized as follows. In the next three sections, we describe the basic structure and features of the VERBUMCULUS facility, leaving out most algorithmic and combinatorial details, for which we refer to [5, 4]. Following that, we show the results of its application to the test analysis of regulatory motifs of genes.

## 2 Statistical analysis of sequences

In the following, we use  $w$  to denote a generic nucleotide word, and  $w_{[i,j]}$  to indicate the substring of  $w$  that begins at position  $i$  and ends at position  $j$ . Two main notions of frequency are considered of interest in our context. The first notion is given in terms of the number of occurrences of  $w$  within a single given sequence. The second is concerned instead with the number of sequences containing at least one occurrence of  $w$  out of the total number of sequences in a family. The expressions and computations of the expected values, moments and related scores of significance depend substantially on the particular notion at hand. We discuss first those based on a single sequence, where we identified five common scores used in the scientific literature (shown on the left of Table 1).

Here,  $f(w)$  is the number of observed occurrences of  $w$  in the input sequence,  $E(w)$  is the number of expected occurrences of  $w$  under a Bernoulli (i.i.d.) model,  $Var(w)$  is the variance on the number of occurrences of  $w$  under the same model, and  $\hat{Var}(w)$  is an easier to compute, first-order approximation of the true variance, which matches in fact the simplifying assumption of uncorrelated symbol occurrences. Specifically, it is seen [5, 4] that for an input sequence of length  $n$  and a pattern  $w$  of length  $m \leq (n + 1)/2$  we have:

$$E(w) = (n - m + 1)p(w)$$

and

$$Var(w) = E(w)(1 - p(w)) - p(w)^2(2n - 3m + 2)(m - 1)$$

$ \begin{aligned} z_1(w) &= f(w) - E(w) \\ z_2(w) &= \frac{f(w)}{E(w)} \\ z_3(w) &= \frac{f(w) - E(w)}{\sqrt{\hat{V}ar(w)}} \\ z_4(w) &= \frac{f(w) - E(w)}{\sqrt{V\hat{a}r(w)}} \\ z_5(w) &= \frac{f(w) - \mathcal{E}(w)}{\max\{\sqrt{\mathcal{E}(w)}, 1\}} \end{aligned} $	$ \begin{aligned} z_7(w) &= c(w) - E_c(w) \\ z_8(w) &= \frac{c(w)}{E_c(w)} \\ z_9(w) &= \frac{(c(w) - E_c(w))^2}{E_c(w)} \end{aligned} $
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Figure 1: Scores based on the number of occurrences (left) and scores based on the number of sequences containing at least one occurrence (right)

$$+ 2p(w) \sum_{l=1}^s (n - m + 1 - d_l) \prod_{j=m-d_l+1}^m p(w_{[j]})$$

where  $p(w)$  is the probability of occurrence of  $w$  and  $\{d_1, d_2, \dots, d_s\}$  are the lengths of the periods of  $w$ . A string  $w$  has a *period*  $z$  if  $w$  is a prefix of  $z^k$  for some integer  $k$ . Alternatively, a string  $z$  is a period of a string  $w$  if  $w = z^l v$  and  $v$  is a possibly empty prefix of  $z$ . We refer to [6, 5, 4] for details and discussion. Truncating  $Var(w)$  after the first term yields  $\hat{V}ar(w) = E(w)(1 - p(w))$ . Score  $z_5$  is after Brendel *et al.* (see [12] for details):  $\mathcal{E}(w)$  is the expected frequency of  $w$  based on the observed frequency of  $(m-1)$ -mers and  $(m-2)$ -mers, i.e.,

$$\mathcal{E}(w) = \frac{f(w_{[1,m-1]})f(w_{[2,m]})}{f(w_{[2,m-1]})}.$$

We now turn to the scores associated with frequencies defined on a set of strings  $\{x_1, x_2, \dots, x_k\}$ , also called a *multisequence*. For multisequences, the three additional scores shown on the right of Table 1 have been selected. Here  $E_c(w)$  and  $c(w)$  are, respectively, the expected and observed number of sequences that contain at least one occurrence of  $w$ . Given  $k$  sequences of respective sizes  $n_i$  for  $i \in [1, k]$ , Pesole *et al.* [39] define  $E_c(w)$  as follows

$$E_c(w) = \sum_{i=1}^k \left(1 - e^{-\mathcal{E}_i(w)}\right)$$

where  $\mathcal{E}_i(w)$  is the expected number of occurrences of  $w$  in the  $i$ -th sequence. An estimator of the true expectation is calculated after Stuckle *et al.* [48] by assuming a first order stationary Markov chain

$$\mathcal{E}_i(w) = \frac{f_i(w_{[1,2]})f_i(w_{[2,3]}) \dots f_i(w_{[m-1,m]})}{f_i(w_{[2]})f_i(w_{[3]}) \dots f_i(w_{[m-1]})}$$

where  $f_i(w)$  is the observed number of occurrences of  $w$  in the  $i$ -th sequence.

In a typical, on-line application, parameters such as the probabilities of the individual symbols are estimated from the corresponding frequencies in the input sequence. Alternatively, our algorithm allows the submission of a separate model sequence from which probabilities are estimated. Likewise, the analysis of the target sequence may proceed considering the sequence as a whole as well as by performing computations independently within a number of consecutive segments in a suitable cover of the input, and analyzing one such “window” at a time.

### 3 Methods

For a given choice of a probabilistic setting and score(s) one would like ideally to compute exhaustive frequency tables reporting values for all substrings of a sequence, or perhaps at least for the statistically most “surprising” among them. Even setting aside for a moment the effort involved in the computation of the necessary parameters and scores, the sheer number of entries associated with such an exhaustive tabular presentation would quickly become unfit for human inspection, hence hardly useful at the outset. To see this, assume to be given *a priori* a source model, one of the above  $z$ -scores, and some arbitrarily fixed threshold value  $t$  for that score, whereby a word will be considered surprising and thus included in the output table if its score exceeds  $t$ . Now an observed sequence  $x$  of  $n$  bases might in principle exceed  $t$  with all of its substrings. Since  $x$  may contain about  $n^2/2$  distinct substrings, then a sequence of a modest  $n = 1,000$  bases might force us to output about half a million subwords as being surprisingly frequent. While such an extreme case seems entirely unrealistic, it does help illustrating a point of great practical relevance, namely, that the volumes of data produced in this and other tasks of motif discovery risk to rapidly saturate the perceptual bandwidth of the final user [3].

One of the main assets of VERBUNCULUS comes in form of a powerful property that limits drastically the number of surprising subwords that one needs to consider. The property holds under reasonable assumptions for scores that fit the general format  $z(w) = (f(w) - E(w))/N(w)$ , where  $N(w)$  is a nonnegative normalizing factor for the difference such as, e.g., the standard deviation for the count. For scores of this kind, it is possible [5, 4] to confine the computation to only a number of candidate surprising words linear in the length of the host sequence. Moreover, the set  $\mathcal{W}$  of these candidates can be identified *a priori*, and their relationship to any other, e.g., over-represented word not in  $\mathcal{W}$  is as follows (under-represented words obey a symmetric property). For any word  $w$  not in  $\mathcal{W}$  such that  $z(w) > t$ , there is a word  $w'$  in  $\mathcal{W}$  such that:

1.  $w' = wv$  for some nonempty word  $v$ , i.e., the “neglected” word is embedded in a word of  $\mathcal{W}$  as a prefix;
2.  $z(w') > z(w)$ , i.e.,  $w'$  is at least as surprising as  $w$ .

Such a drastic limitation on the order of the number of candidates, as well as their identification, weighing and display are all inextricably interwoven reflections of a same combinatorial property, which has to do with the score being monotone within certain families of patterns. This property requires that if  $w$  and an extension  $w' = wv$  of  $w$  are nonempty substrings of the text  $x$  such that  $f(w) = f(wv)$ , then the score of  $w$  does not exceed that of  $w'$ . Under these conditions,  $w$  can be neglected as the surprise it conveys is subsumed by  $w'$ .

The tables below display a collection of monotonicity results established about the models and  $z$ -scores considered. We refer to [4] for the corresponding proofs and discussion. For convenience of notation, we set  $\rho(w) \equiv E(w)/N(w)$ , where  $N(w)$  appears in the score as the expected value of some function of  $w$ . The interpretation of the tables is straightforward. For example, Property 1.1 states a simple fact on the monotonicity of  $E(w)$  given the monotonicity of  $\rho(w)$  and  $N(w)$ . Under some general conditions on  $N(w)$  and  $\rho(w)$  we can prove the monotonicity of any score functions of the form described above.

Some of the properties are not straightforward. For example, Property 1.2 says that these scores are monotonically decreasing when

$$f < E^* = E(w) \frac{\gamma N(w) + N(wv)}{N(w) + N(wv)}$$

	Property	Conditions
(1.1)	$\frac{f(wv) - E(wv)}{N(wv)} > \frac{f(w) - E(w)}{N(w)}$	$N(wv) < N(w), \quad \rho(wv) \leq \rho(w)$
(1.2)	$\left  \frac{f(wv) - E(wv)}{N(wv)} \right  > \left  \frac{f(w) - E(w)}{N(w)} \right $	$N(wv) < N(w), \quad \rho(wv) \leq \rho(w)$ and $f(w) > E(w) \frac{\gamma N(w) + N(wv)}{N(w) + N(wv)}$
(1.3)	$f(wv) - E(wv) > f(w) - E(w)$	$E(wv) < E(w)$
(1.4)	$\frac{f(wv)}{E(wv)} > \frac{f(w)}{E(w)}$	$E(wv) < E(w)$
(1.5)	$\frac{f(wv) - E(wv)}{E(wv)} > \frac{f(w) - E(w)}{E(w)}$	$E(wv) < E(w)$
(1.6)	$\frac{f(wv) - E(wv)}{\sqrt{E(wv)}} > \frac{f(w) - E(w)}{\sqrt{E(w)}}$	$E(wv) < E(w)$
(1.7)	$\left  \frac{f(wv) - E(wv)}{\sqrt{E(wv)}} \right  > \left  \frac{f(w) - E(w)}{\sqrt{E(w)}} \right $	$E(w) > E(wv), \quad f(w) > E(w)\sqrt{\gamma}$
(1.8)	$\frac{(f(wv) - E(wv))^2}{E(wv)} > \frac{(f(w) - E(w))^2}{E(w)}$	$E(w) > E(wv), \quad f(w) > E(w)\sqrt{\gamma}$

Table 1: General monotonicities for scores associated with the counts  $f$ , under the hypothesis  $f(w) = f(wv)$ . We have set  $\rho(w) \equiv E(w)/N(w)$  and  $\gamma \equiv E(wv)/E(w)$ .

	Property	Conditions
(2.1)	$E(wv) < E(w)$	none
(2.2)	$f(wv) - E(wv) > f(w) - E(w)$	$f(w) = f(wv)$
(2.3)	$\frac{f(wv)}{E(wv)} > \frac{f(w)}{E(w)}$	$f(w) = f(wv)$
(2.4)	$\frac{f(wv) - E(wv)}{E(wv)} > \frac{f(w) - E(w)}{E(w)}$	$f(w) = f(wv)$
(2.5)	$\frac{f(wv) - E(wv)}{\sqrt{E(wv)}} > \frac{f(w) - E(w)}{\sqrt{E(w)}}$	$f(w) = f(wv)$
(2.6)	$\left  \frac{f(wv) - E(wv)}{\sqrt{E(wv)}} \right  > \left  \frac{f(w) - E(w)}{\sqrt{E(w)}} \right $	$f(w) = f(wv), \quad f(w) > E(w)\sqrt{\gamma}$
(2.7)	$\frac{(f(wv) - E(wv))^2}{E(wv)} > \frac{(f(w) - E(w))^2}{E(w)}$	$f(w) = f(wv), \quad f(w) > E(w)\sqrt{\gamma}$
(2.8)	$\frac{f(wv) - E(wv)}{\sqrt{E(wv)(1 - p(w)q(v))}} > \frac{f(w) - E(w)}{\sqrt{E(w)(1 - p(w))}}$	$f(w) = f(wv), \quad p(w) < 1/2$
(2.9)	$\text{Var}(wv) < \text{Var}(w)$	$p_{max} < 1/\sqrt[3]{4m}$
(2.10)	$\frac{E(wv)}{\sqrt{\text{Var}(wv)}} < \frac{E(w)}{\sqrt{\text{Var}(w)}}$	$p_{max} < \sqrt{2} - 1$
(2.11)	$\frac{f(wv) - E(wv)}{\sqrt{\text{Var}(wv)}} > \frac{f(w) - E(w)}{\sqrt{\text{Var}(w)}}$	$f(w) = f(wv), \quad p_{max} < \min\{1/\sqrt[3]{4m}, \sqrt{2} - 1\}$
(2.12)	$\left  \frac{f(wv) - E(wv)}{\sqrt{\text{Var}(wv)}} \right  > \left  \frac{f(w) - E(w)}{\sqrt{\text{Var}(w)}} \right $	$f(w) = f(wv), \quad p_{max} < \min\{1/\sqrt[3]{4m}, \sqrt{2} - 1\}$ and $f(w) > E(w) \frac{\gamma \sqrt{\text{Var}(w)} + \sqrt{\text{Var}(wv)}}{\sqrt{\text{Var}(w)} + \sqrt{\text{Var}(wv)}}$

Table 2: Monotonicities for scores associated with the number of occurrences  $f$  under the Bernoulli model. We set  $\gamma \equiv E(wv)/E(w)$ .

and monotonically increasing when  $f > E^*$ . We can picture the dynamics of the score as follow. Initially, we can assume  $E^* > f$ , in which case the score is decreasing. As we extend the word, keeping the count  $f$  constant,  $E^*$  decreases (recall that  $E^*$  is always in the interval  $[E(wv), E(w)]$ ). At some point,  $E^* = f$ , in which case the score stays constant. By extending the word even more,  $E^*$  becomes smaller than  $f$ , and the score starts to grow. Some consequences of Property 1.2 are captured by Properties 1.7 and 1.8. Property 1.2 also holds by exchanging the condition  $\rho(wv) \leq \rho(w)$  with  $f(w) > E(w) > E(wv)$ .

Turning now to Table 2, we summarize monotonicity results for the Bernoulli, or i.i.d., model. In this case, each symbol is generated from the same probability distribution, and independently from its context. A comprehensive study of other models and scores can be found in [4].

As already observed, a tabular representation of surprising words in a sequence is bound to become rapidly bulky with increasing sequence length, even if the number of candidates is linear in that length. In our approach, the computation, storage and display of the statistical parameters of interest are all organized around the structure of a special compact trie represented by a suitably pruned version of a *suffix tree*, the trie of all suffixes of a given sequence (see e.g., [34, 2, 23]). By the trie being implemented in compact form it is meant that all nodes in it are branching nodes, whence arcs are labeled by substrings of the input sequence rather than by individual symbols. In a full-fledged tree, the leaves are in one-to-one correspondence with the suffixes of the input. Since every subword of the input is a prefix of some such suffix(es), then any subword of the input will be spelled out on a unique path leading from the root to some leaf and ending at a node or perhaps in the middle of an arc. For a sequence of length  $n$ , the tree will have a number of leaves and hence also of internal nodes bounded by  $n$ , so that always less than  $2n$  subwords of the input can end precisely at a node in any pruned version of the trie. The property exploited by VERBUMCULUS is that, within the ample domains of monotonicity of the scores considered, the set  $\mathcal{W}$  coincides precisely with the set of these subwords [5, 4]. In other words, for a monotone score  $z$

*the largest positive values of  $z$  and hence most over-represented words will occur at the internal nodes of the trie rather than in the middle of an arc. Symmetrically, the most under-represented words occur only as unit symbol extensions of those nodes.*

Combined with the advantages of trie visualization over table listing, this remarkable property opens the way to compactly displaying all of the unusual subwords of a sequence at once. Moreover, the computations involved can be speeded up significantly. The tree itself is built in time linear in the input by a number of well known methods. Once the tree is built and perhaps pruned to some preliminary maximum length, subword occurrences and other similar counts can be similarly obtained in linear time. For instance, the number of leaves in the subtree rooted at some node represents the number of observed occurrences of the word spelled out on a path from the root to that node or anywhere on the immediately preceding arc. VERBUMCULUS annotates the tree with one or more of the above scores, depending on the type of analysis one wants to perform. The typical process of annotation also takes linear time, which in cases like  $z_4$  is achieved through resort to rather complex algorithmics, due to the structure of *Var*. For scores that require multiple tries to be built and superimposed to one another, like in the computation of  $c(w)$  for  $z_7$ ,  $z_8$  and  $z_9$ , the linear time algorithm by Hui [26] is used.

## 4 Software description and usage

VERBUMCULUS is composed by three modules: the tree builder VERBUM, the graph drawing program DOT, and the graphic interface TREEVIZ. The entire package consists of about ten thousand



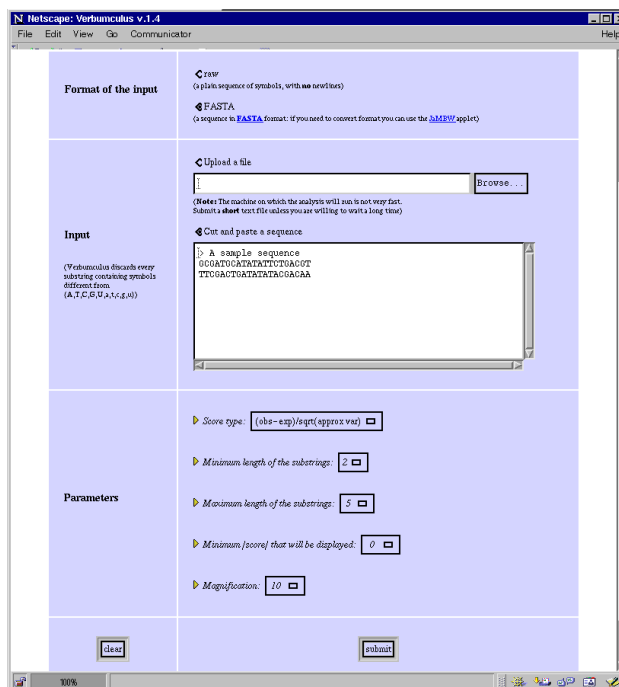


Figure 2: VERBUMCULUS' web interface

lines of code.

VERBUM is written in C++ using the Standard Template Library which should allow great portability under different platforms. The code has been compiled, without any change, under Solaris and Linux. VERBUM reads the input sequence(s) and the various parameters supplied by the user, and creates a (possibly pruned) suffix trie annotated with the score selected at the beginning by the user. The output is a text file representing the tree in the `dot` format (see below). VERBUM is particularly fast: although the time taken for the analysis depends heavily on the particular score and other input parameters, it is typically in the order of few seconds for the most common choices.

`DOT` is the graph drawing program by AT&T Labs, part of the `GRAPHVIZ` package [20]. It reads graphs in the `dot` representation and outputs drawings in a dozen of formats, among which Postscript and GIF. The source code and binary executables for common platforms are available from their site, and licensing is almost open source.

`TREEVIZ` is the graphical user interface that runs on the client side, and more specifically on the browser of the user. It is entirely written in Java, and uses the `GRAPPA` libraries by AT&T Labs.

A couple of thousand lines of Perl glue everything together. Perl scripts generate the HTML for the input forms and control the execution of the various stages, handling exceptions and errors.

The user of VERBUMCULUS is presented with the form shown in Fig. 2. He has the option of submitting the input either as a raw sequence of letters or in FASTA format. The input can be “pasted” into the window or uploaded to the server. For analyzing long sequences, we strongly advise to download the executable VERBUM and DOT and work locally, in order to avoid the overhead of network communications and the relative inefficiencies of Perl scripts and Java.

Various parameters can be adjusted. The most important choice is the type of score to be used in tree annotation. Additionally, a wide range of different filters is available to limit the size of the

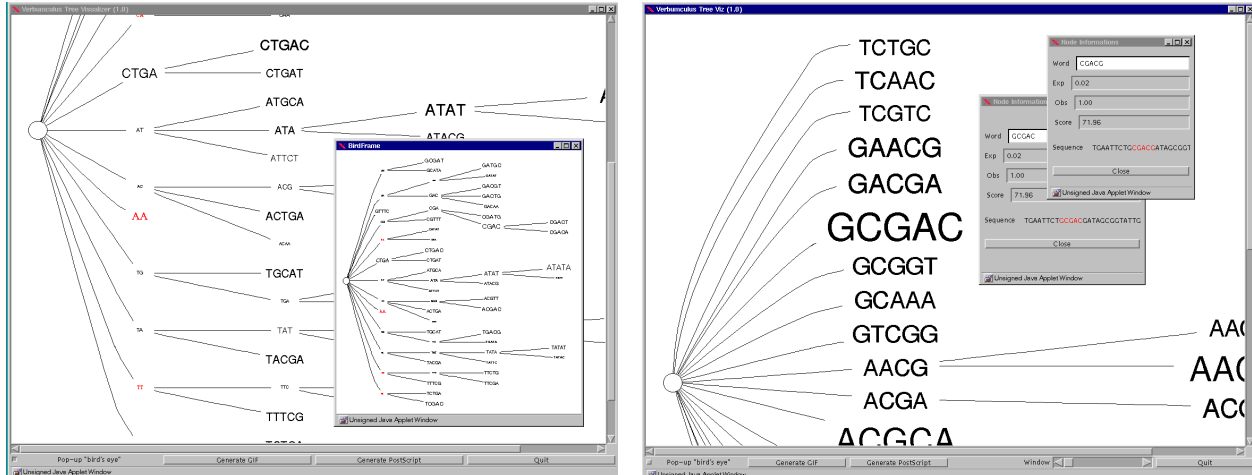


Figure 3: Example outputs of TREEVIZ

tree. The user can set the minimum and maximum length of the nucleotide words, a lower bound on the absolute value of the score, a lower bound on the value of the expectation (to avoid “rare” words) and a forbidden substring (to avoid, for example, words contains TATA).

For better performance, we have limited the visualization of TREEVIZ to 100 nodes: if the tree is bigger, VERBUMCULUS will send a Postscript file with the drawing of the tree. If the user wants to take advantage of the interactive facilities of TREEVIZ, he will have to increase the effectiveness of the filters in order to produce a smaller tree.

The magnitude of a score value is transduced through font size, in the sense that for every word  $w$ , the higher the absolute value of the score of  $w$ , the bigger the font used to represent  $w$ . Words with a negative score are, in addition, printed in red italics (see Fig. 3, on the left).

Once TREEVIZ has drawn the tree, the user can navigate it looking for conspicuous nucleotide motifs. At any time, clicking on an nucleotide word will visualize information about its number of occurrences, the expected value of this number, and the corresponding value of the  $z$ -score. Along with these values, a graphical representation of the positions of the occurrences of the nucleotide word in the original sequence is produced and displayed (see Fig. 3, on the right).

Since the tree can be fairly big, TREEVIZ offers the option to get an overall picture of the tree by clicking on the “bird’s eye” button, which produces the small window inset of Fig. 3. Finally, TREEVIZ can generate a drawing of the tree in Postscript or GIF that can be saved on the machine of the user for further and more accurate scrutiny.

## 5 Simulations and Dithering

Before showing the results of using VERBUMCULUS on real biological data, we report on some tests performed on artificial sequences. In our present context, this is meant primarily to show the effectiveness of the tool in the pattern discovery process. In practice, this or a similar procedure may be followed fruitfully as a preliminary treatment, for the purpose of fine tuning the sensitivity of the tool and adapt it to the particular sequence or family under study.

An example dithering procedure could be as follows. First, we generate and process several pseudo-random strings assuming a symmetric Bernoulli model. For every random sequence produced, we generate and annotate the corresponding tree. As expected, we find that unless the

random sequence is very short the tree does not display any surprising word.

Next, we inject into the random sequences a controlled number of non-overlapping repetitions of words. In our example, we use the two words **GATTA** and **AAAAA**, in separate experiments. Since the process of overwriting the original random letters with occurrences of a given word changes the probability distribution, we have to make some adjustments in the probability distribution. Let  $p_a$  denote the probability of symbol  $a \in \Sigma$  in the original sequence and  $w$  some word of length  $|w| = m$ , with a proportion of  $a$ 's given by  $q_a$ . Forcing  $h$  substrings in our sequence to coincide with  $w$  will change the probability accounting for the “free” occurrences of  $a$  outside the  $h$  copies of  $w$  into

$$\bar{p}_a = \frac{p_a n - h m q_a}{n - h m}.$$

As the left part of Figure 4 displays, five occurrences of **GATTA** in a text of size 1,000 can be enough, with our settings, in order for the program to output that word as the highest scoring pattern. If the size of the text is increased to 10,000, then typically twenty occurrences of the word turn out to be enough to produce the same visual effect (see right half of Figure 4).

For a broader analysis, we run 1,000 trials for all choices of  $h = 0, 1, \dots, 15$ ,  $n = 1,000$  counting the number of times that **GATTA** is the highest scoring pattern in the entire tree. The graph on the left of Figure 5 shows the relative proficiency of the scores  $z_2, z_3$  and  $z_4$  in separating the “signal” **GATTA**, from “noise”. Specifically, the plots show the fraction of the 1,000 trials in which the word **GATTA** was the highest scoring word in the tree, for increasing number  $h$  of injections. From the graph we can observe that scores  $z_3$  and  $z_4$  have identical performance (as one would expect, since **GATTA** has no periods) and they seem to be better than  $z_2$ . On the right of Figure 5 we instead plotted three pairs of curves respectively for scores  $z_2, z_3, z_4$  (it so happens that in this particular case the pairs for  $z_3$  and  $z_4$  are on top of each other) with increasing number  $h$  of injections. For each pair, the upper curve represents the average score for the word that achieves the largest score in the tree, while the lower curve represents the average score for the word **GATTA**. Some observations are in order. First, the score of **GATTA** grows linearly with  $h$ . Second, the average of the highest  $z_2$ -score is bigger than  $z_3$  and  $z_4$ . Third, at some point  $h^*$  the lower curve touches the upper curve and the pattern is “discovered”. Note that the lower curve touches the upper curve sooner for  $z_3$  and  $z_4$  than  $z_2$ .

If the pattern is periodic, like e.g. **AAAAA**, then we need fewer copies, i.e., a smaller value of  $h$  in order to obtain a comparable visual impact. Figure 6 displays the results using four forced occurrences in a sequence of size 1,000 and ten in a sequence of size 10,000. We run the same simulation on 1,000 trials as before, this time injecting  $h = 0, 1, \dots, 15$  occurrences of **AAAAA** (see left half of Figure 7). We were expecting the score  $z_4$  to have an advantage over the other because of the high periodicity of the word. Surprisingly, the figure shows that the score that detects sooner the presence of **AAAAA** is  $z_3$ . In the right half of Figure 7 we collected as before the average scores for the words achieving the largest score in the tree (upper curve), and the average score for the word **AAAAA** (lower curve). This time, the tree families of curves corresponding to  $z_2, z_3$  and  $z_4$  are clearly distinguishable. The function that returns the biggest scores is again  $z_2$ , followed by  $z_3$  and then  $z_4$ . For all three, the score of **AAAAA** grows linearly with  $h$ . Note, however that  $z_2$  and  $z_3$  have different slopes than  $z_4$ .

## 6 Tests and Experiments

We report here some results on experiments running VERBUMCULUS on the *upstream regions* of some genes of the yeast. The upstream region of a gene is the untranslated region that precedes the

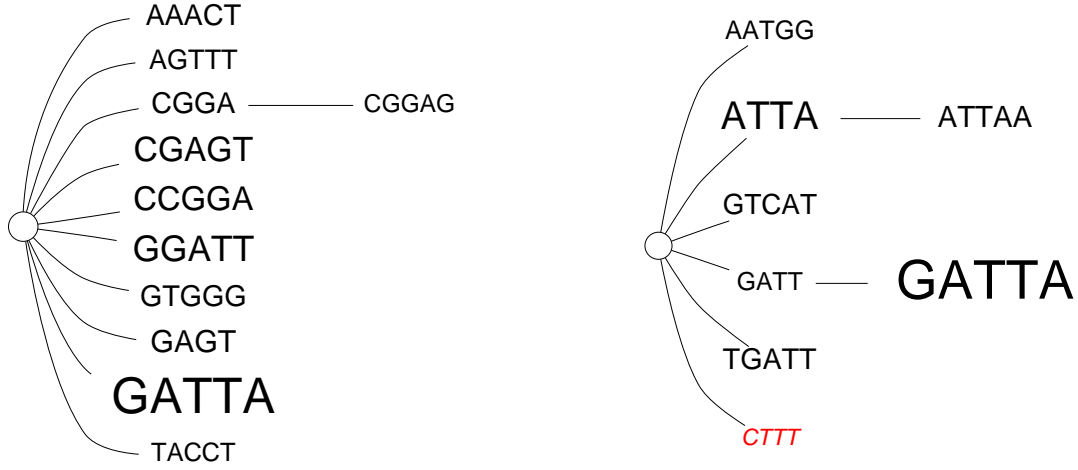


Figure 4: LEFT: trie from a random string of size 1,000 with 5 forced occurrences of the word **GATTA**. RIGHT: trie from another random string of size 10,000 with 20 forced occurrences of **GATTA**. Both tries are annotated using  $z_3$ , with threshold 3.0

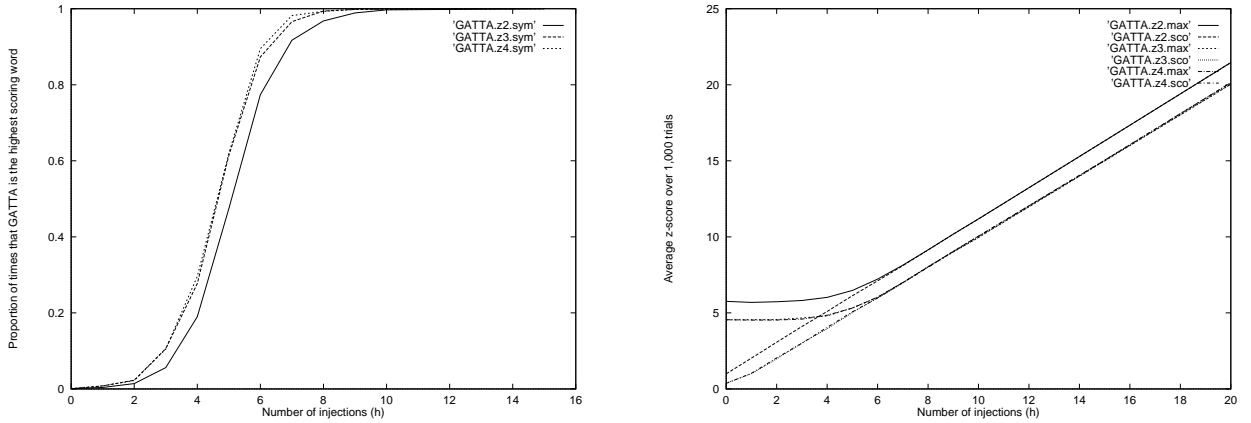


Figure 5: LEFT: The fraction of 1,000 trials in which the word **GATTA** is the *highest* scoring word in the tree for  $z$ -scores  $z_2, z_3, z_4$ , versus number of injections  $h$ . RIGHT: Curve pairs for scores  $z_2, z_3, z_4$  versus  $h$ . The upper curve in each pair represents the average score for the word that achieves the maximum score, the lower curve represents the average score of the word **GATTA**. The curves for  $z_3$  and  $z_4$  are hardly distinguishable due to substantial overlap.

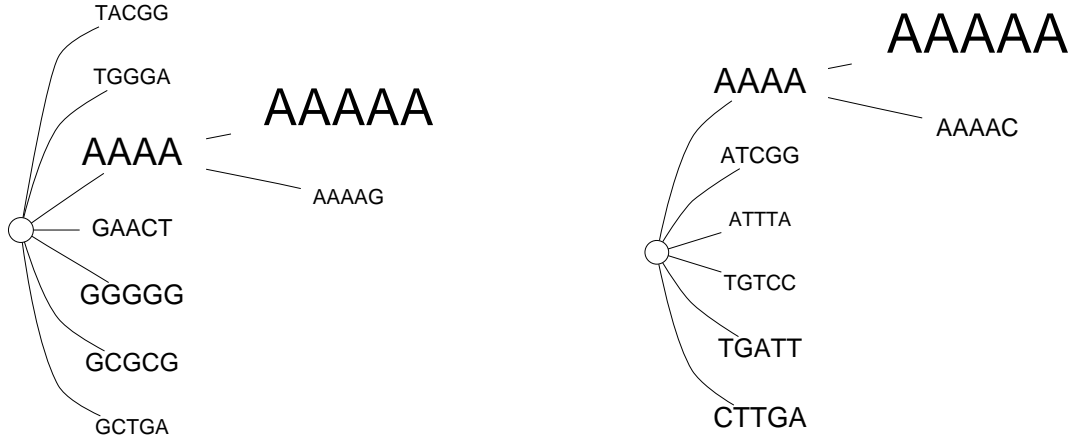


Figure 6: LEFT: trie from a random string of size 1,000 with 4 forced occurrences of the word **AAAAA**. RIGHT: trie from another random string of size 10,000 with 10 forced occurrences of **AAAAA**. Both trees are annotated using  $z_3$ , with threshold 3.0

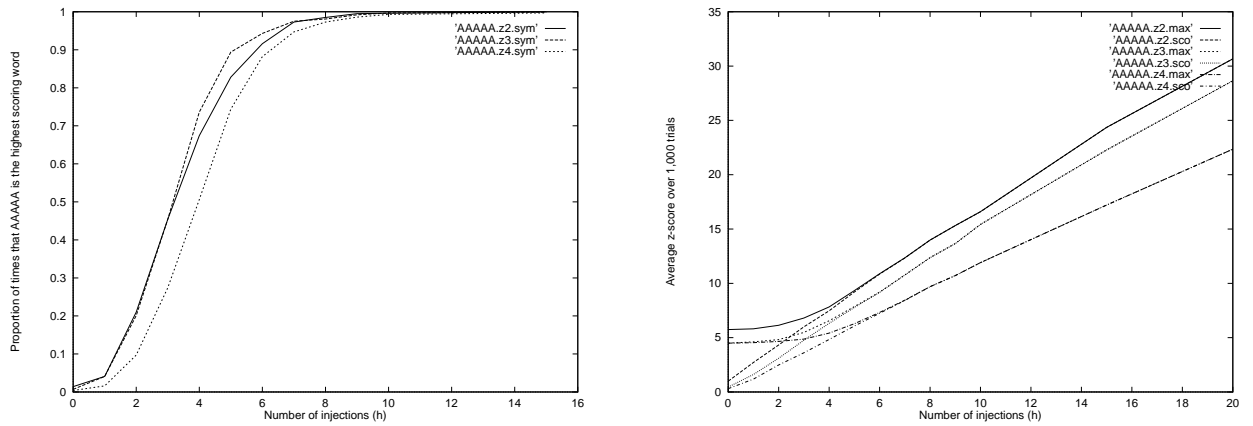


Figure 7: LEFT: fraction of times versus  $h$  that **AAAAA** is the *highest* scoring word in the tree, for  $z$ -scores,  $z_2, z_3, z_4$ . RIGHT: curve pairs for the word **AAAAA** and the highest scoring words under scores  $z_2, z_3, z_4$ .

start codon ATG of size 500-1000 base pairs, when reading the sequence in the standard orientation 5' to 3'. It is usually known to contain several control signals that regulates the production of the mRNA, called *promoters* or *regulatory sites*. Finding such motifs is usually the first step in understanding how genes interact with the environment and with each other.

The first dataset we analyze is related to ten families of genes isolated by van Helden *et al.* [49]. Each family contains a set of co-regulated genes, that is, genes that have similar expression under the same external conditions. The hypothesis is that in each family the upstream region will contain some common motif. Moreover, one can also expect that such signals are going to be over-represented across the family. In this first experiment we use the same parameters and score type on all the multisequences to test the general performance of our tool.

The second dataset comes from the work on the *sporulation* of the budding yeast conducted by Chu *et al.* [15]. Seven families of co-regulated genes have been characterized using DNA microarray technology. Again, one of the purposes of the investigation is to find unusual words in the upstream regions of these genes. Here we concentrate on a couple of families and we show the sensitivity of our tool to different choices of parameters and score functions. Both experiments also expose the limitations of our approach.

## 6.1 Regulatory sites in yeast

The metabolism of the yeast has been widely studied and provides several examples of known regulatory sites. In many cases, the transcriptional factor involved in the common response is known, as well as its binding site. van Helden *et al.* selected ten families of genes based on prior biological knowledge on their activity. For each gene in a family its 800 bps upstream sequence was extracted. The set of all upstream sequences belonging to the same family constitutes the multisequence on which we performed the analysis using VERBUMCULUS.

The parameters of the analysis are as follows. We use scores based on the number of occurrences ( $z_3$  and  $z_4$ ), a threshold between 3 and 10 depending of the maximum size of pattern, the latter being between 5 and 8 symbols. We adjusted the threshold to obtain a tree of about twenty nodes. We also filtered out words containing one or more of the subwords TATA, AAAA and TTTT, when these words were predominant.

Tables 3, 4 and 5 summarize the result of our tests. For each multisequence we report the identifier, the number  $k$  of sequences, the motif previously known and characterized by experiments, the motifs found by van Helden *et al.*, and the trees produced with VERBUMCULUS. For the sake of clarity, we manually circled the words that match the biologically significant motif.

VERBUMCULUS is capable of discovering the biologically significant patterns in families NIT, MET, PHO, PDR, GAL, GCN and TUP, although sometimes partially. Moreover, these motifs can be found among the highest scoring words. Also note that other patterns which are also scoring high are usually in a suffix-prefix relation with the highest, suggesting that their occurrences are correlated.

However, in the multisequences INO, HAP and YAP VERBUMCULUS assigns low scores to the motifs and therefore they do not show up in the final tree. In two of these three cases, though, the tool by van Helden *et al.* is also not capable of detecting these patterns as shown in the Tables. Additionally, the tool by van Helden *et al.* does not give any satisfactory answer for the GAL family, where instead VERBUMCULUS catches CGGCG and GCCGC which correspond the the beginning and the end of the motif. Finally, note that, in general, VERBUMCULUS has great difficulty to handle motifs contains multi-valued symbols, for example the ones for GAL and TUP families.

Family	$k$	Motif	van Helden <i>et al.</i>	VERBUMCULUS
NIT	7	GATAAG	CTGATAAGA CCGCGC CGGCAC ACATCT	
MET	11	TCACGTG AAAACTGTGG	GTCACGTG AACTGTGGC ATATAT TATATA GCTTCC	
PHO	5	GCACGTGGG GCACGTTTT	CGCACGTGGG CACGTTT CTGCAC TGCCAA	
PDR	7	TCCGCGGA	TCCG{C T}GGAA GCGCGA AGGCACC	

Table 3: van Helden dataset of co-regulated genes

Family	$k$	Motif	van Helden <i>et al.</i>	VERBUMCULUS
GAL	6	CGGN <sup>5</sup> WN <sup>5</sup> CCG	?	
GCN	38	RRTGACTCTTT	A{G A}TGA <sup>5</sup> CTC{A T}	
INO	10	CATGTGAAWT	CAACAA{C G}	
HAP	8	CCAA{T C}	AGAGAGA ATGGGGC	

Table 4: van Helden dataset of co-regulated genes (continued)



Family	$k$	Motif	van Helden <i>et al.</i>	VERBUMCULUS
YAP	16	TTACTAA	CGTTCGGT CATTAC CTGAAG	
TUP	25	KANW <sup>4</sup> ATSYG <sup>4</sup> W	TT{C T}{C G}NG <sup>4</sup> {T C}{A C} AGGCACGGG AAA{A G}AA AAGGAGGA ACAAACA CTCCGC {T C}CTGCA CGTCGC	

Table 5: van Helden dataset of co-regulated genes (continued)

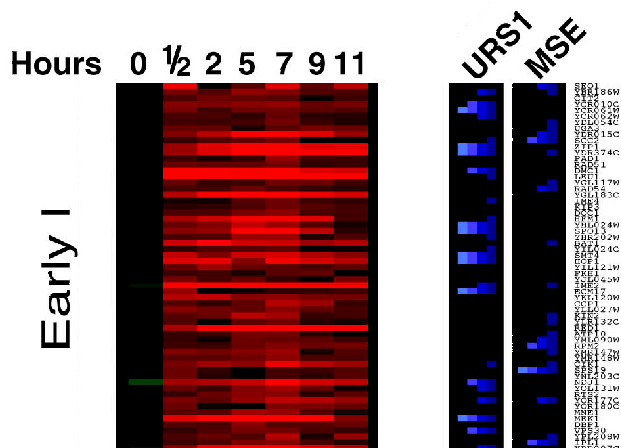


Figure 8: Genes of the Early(I) cluster induced or repressed during sporulation. Adapted, by kind permission, from a figure at <http://cmgm.stanford.edu/pbrown/sporulation/figures/fig5ss.html>

## 6.2 Sporulation of the Yeast

We report here some results from testing VERBUMCULUS on the dataset involved in the work on sporulation conducted at Stanford by Chu *et al.* [15]. The authors used DNA micro-array technology to expose the temporal patterns of gene expression of *Saccharomyces Cerevisiae* during meiosis and spore formation. This was done along the lines of a rather standard procedure, as follows. First, changes in the concentration of mRNA transcript from known genes of the budding yeast were measured during seven consecutive intervals. Next, the average expression profiles were used to classify the genes. Figure 8 reproduces an adaptation of the image at the outset, available in full view at <http://cmgm.stanford.edu/pbrown/sporulation/figures/fig5ss.html>. As usual, higher and higher degrees of expression translate into darker and darker shades of red, while lower concentrations yield progressively darker shades of green. Seven clusters were produced in this particular experiment, labeled as **Metabolic**, **Early(I)**, **Early(II)**, **EarlyMiddle**, **Middle**, **MidLate**, and **Late**.

The two bands of columns with blue bars in Figure 8 identify genes of which the promoters contain a putative URS1 or MSE regulatory sequence, respectively. The degree to which the sequence matches the consensus for each of these regulatory elements is indicated by the brightness of the bar: the best matches are represented by the bright blue bars that appear to be concentrated towards the left of each band, the less stringent matches cause the darker blue bars more visible towards the right. The most stringent match for the URS1 site is 5'-TCGGCGGCTDW-3', and the least stringent is 5'-GGCGGC-3'. The most stringent match for the MSE site is 5'-HDVKNACAAAAD-3', and the least stringent is 5'-DNCRCAAAWD-3'.

Figure 5 of [15] shows that the upstream sequences relative to the genes in the clusters **Metabolic**, **Early(I)**, and **Early(II)** contain several occurrences of the regulatory element URS1, while the ones in the clusters **EarlyMiddle** and **Middle** contain many MSE sites. We report here results regarding the analysis of the cluster **Early(I)** with the objective to expose the URS1 site. We also report a less satisfactory analysis of the cluster **Middle**.

### 6.3 The Early(I) cluster

The cluster **Early(I)** contains 36 genes, namely RTS2, MEK1, NDJ1, MNE1, EHD2, DBP1, IPL1, VPS30, UGA3, PCH2, SEO1, CIT2, SCC2, KIP3, RAD51, IME4, ZIP1, DMC1, RAD54, HFM1, LEU1, PAD1, ATP10, CIK1, FKH1, HOP1, SPS19, KIN2, ECM17, RPM2, CCP1, BAT1, IME2, SPO13, RED1, SMT4. We extracted the upstream region of 600 base pairs (allowing overlaps with other ORFs) using the tool developed by VanHelden *et al.* [49].

Table 6 shows the trees produced by VERBUMCULUS on the family of 36 upstream regions and annotated with the scores  $z_2$ ,  $z_3$ ,  $z_4$ ,  $z_8$  and  $z_9$ , maximum length 6 bps. Only patterns with a score higher than 4.0 (in absolute value) are shown. For comparison purposes, Table 7 lists a few most notable words along with their statistics. In [15] it is reported that 43% of the upstream regions of the genes in the cluster **Early(I)** have a core URS1 motif, while we found only 33%. However, the expected number of **GGCGGC** is so small that the reported occurrences of this word have to be considered surprising by any measure, whether in terms of total number of occurrences or number of sequences containing it.

Observe that the words in the  $z_2$ -tree of Table 6 are not independent. Instead, prefixes of some words are suffixes of others, which suggests that their occurrences might be correlated. We used sequence alignment (see, e.g. [7]) to “assemble” short sequences in longer sequences (see Tables 8-10). As seen in this example, the alignment step can be used to partially overcome the limitation of VERBUMCULUS to discover exact motifs.

Table 8 shows an alignment produced by using four such overlapping words from the tree. The consensus of the alignment **TCGGCGGCA** exactly matches two motifs in the Transcription Element Search System (TESS/TRANSFAC) database [51, 50], namely Y\$HSP70\_02 and Y\$SSA1\_01. This pattern contains the core **GGCGGC**, mentioned repeatedly in [15].

Next, we used four more motifs from the tree to build another alignment (see Table 9). The consensus **TGCGCGGCT** matches one motif in TESS, Y\$G3PDH\_01, that is already known in the literature [33].

Finally, we chose five motifs from the tree and build the multiple alignment of Table 10. The consensus **TAGCCGCGGA** exactly matches five motifs in TESS, namely Y\$CAR1\_02, Y\$CAR2\_01, Y\$MES1\_01, Y\$SPO13\_01, Y\$TOP1\_01. For example, Y\$SPO13\_01 is known to be a key regulatory of nitrogen repression and meiotic development [46]. However, the authors of [15] did not report the finding of this regulatory element.

In conclusion, VERBUMCULUS not only succeeded in identifying the regulatory elements we were looking for, but also found some other interesting new patterns in the cluster that were possibly overlooked. At the same time, in the  $z_2$ -tree of Table 6 there were also patterns such as **CTTTTC**, **AAAAAA**, and **ACCGGC**. The former two have been detected as elements in scaffold/matrix attachment regions (MARs) of eukaryotic genomes [1, 47]. MARs are basic components for high level genome compaction and organization, therefore are highly frequent in genomic sequences [21, 9]. In addition, biological experiments have shown that they anchor genomic sequences to proteinaceous nuclear matrix and affect gene expression [45, 35, 9]. For the latter pattern, we have not found any biological significance yet.

We went on producing a few more suffix trees annotated with other scores. Table 6 shows the tree decorated with scores  $z_3$ ,  $z_4$ ,  $z_8$  and  $z_9$ . Some remarks are in order. The  $z_3$  and  $z_4$  trees are quite similar except for the following: the tree for  $z_3$  enhances **GCCGCC**, **TTTTT** while the tree for  $z_4$  does not. Vice versa, the tree for  $z_4$  emphasizes **TA** as being under-represented, a phenomenon that is missed in the tree annotated with  $z_3$ .

The word **GGCGGC** appears again in both  $z_3$ - and  $z_4$ -trees. However, in the case of  $z_3$  the pattern



$w$	<i>occurrences</i>		<i>sequences</i>	
	$E(w)$	$f(w)$	$E_c(w)$	$c(w)$
AAAAAA	26.44	109	25.74	22
TTTTTT	29.38	110	27.63	25
GGCGGC	1.15	25	1.51	12
TAGCCG	2.43	9	2.11	9

Table 7: Explicit statistics for some most devious words (in term of number of occurrences and/or number of sequences containing at least one occurrence) in the 36 sequences that form cluster Early(I). The individual symbol probabilities are .31 for A and T and .18 for G and C

C	G	G	C	G	G	-
g	G	G	C	G	G	-
-	G	G	C	G	G	-
-	G	G	C	G	G	C
C	G	G	C	G	G	C

Table 8: Alignment of four highly overlapping words picked from the  $z_2$ -tree of Table 6

G	g	G	C	G	G	-	-	-
G	C	G	C	G	c	-	-	-
-	-	G	C	G	G	C	T	-
-	-	-	C	G	G	C	T	A
G	C	G	C	G	G	C	T	A

Table 9: Alignment of four other highly overlapping words picked from the tree of  $z_2$ -tree of Table 6

A	G	C	C	G	C	-	-	-
-	G	C	C	G	C	-	G	-
-	G	C	C	G	C	C	-	-
-	-	C	C	G	C	g	G	-
-	-	C	C	G	g	C	-	A
A	G	C	C	G	C	C	G	A

Table 10: Alignment of five other highly overlapping words picked from the  $z_2$ -tree of Table 6

GGCGGC is no more the highest scoring one. GGCGGC ranks fifth after AAAAAA, AAAAA, AAAA, AAA. In fact, as one would expect, the approximation of the variance used in  $z_3$  does affect in particular the scores of highly periodic words.

It is somewhat surprising that the families of words  $A^+$  and  $T^+$  appear as strongly marked in the tree under  $z_4$ . The pervasive over-representation of AAA, TTT, TAT, ATA have been reported by Nussinov [37], Brendel *et al.* [12] and Leung *et al.* [31]. They correspond to the highly occurring 'A box' (AATAAAYAAA) and 'T box' (TTWTWTTWTT) binding sites of MARs across different species [22, 1, 35, 9, 47]. In any case, it is comforting to see that the word GGCGGC is still the highest scoring motif in the tree.

The  $z_8$ - and  $z_9$ -trees pertain both to scores defined in terms of sequence families. It is interesting to compare the tree for the score  $z_8$  with the tree for  $z_2$ . The tree for  $z_8$  exposes GCCGTG, TAGCCG, CGCCGA, CCGGCG and AGGACC while the tree annotated with  $z_2$  does not. Vice versa, the tree for  $z_2$  shows GCGCGC, GGCGG, CTTTTC and AAAAAA. The fact that these trees are very similar seems to suggest that, under our conditions, words that occur at least once in unexpectedly many sequences in a family might be spotted just by looking for words with a high occurrence score in the family as a whole. The function  $z_9$  (defined as in WORDUP) happens to assign a high score the two motifs GGCGGC and GCGGCT. Surprisingly, it exposes at least two words present in the tree for the score  $z_2$  but not appearing in the tree for  $z_8$ , namely, GGCGG and CTTTTC.

We also analyzed the dataset replacing the underlying model with a Markov chain. We produced five trees assuming models of order  $M = 0, \dots, 4$ . Order  $M = 0$  corresponds to the i.i.d. model, whereas higher orders  $M > 0$  assumes that the source is generating symbols with a probability distribution which depends on the  $M$  preceding symbols. Figure 11 shows the trees computed by VERBUMCULUS using a common score and parameters. To clarify the differences we produced another figure where we removed the tree, we connected common words with a red line, and we circled in green the singletons. We observe that for  $M = 0, 1, 2$  there is some general agreement: in particular the word GGCGGC consistently achieves the highest score. However, for the order 3 we are left only with one word (AGGACC) that does not appear anywhere else. If we had lowered the threshold to 3, GGCGGC would have appeared among other other fifteen words. The fourth order tree contains the prefix GGCGG, although other three unknown words scores a little higher. This phenomenon can be expected, since we train our model on the sequences themselves. As the size of the model grows its capability of prediction grows as well. Therefore there are less and less surprising words. In order to get roughly the same amount of nodes in the trees, we should have lowered the threshold as  $M$  increases.

## 6.4 The Middle cluster

We describe tests conducted with VERBUMCULUS on other cluster in the same dataset from [15]. This will show that when the core of consensus is not a fixed pattern, but admits instead multi-valued positions, then it becomes more difficult to find by our method.

The cluster **Middle** is composed by 63 genes, namely: STE5, PBP2, MRPL37, APC11, YSW1, UBC1, EK11, CDC10, SPS2, SPS1, SPR6, GPI8, CDC26, CDH1, ISC10, CLB6, SUT1, HXT10, PES4, SPR28, CDC20, GNP1, SPR3, YCK3, FET5, CDA2, CDA1, SPS18, CDC5, REV7, PIG1, NMT1, MIP6, SPO20, CNM67, YCK2, SUR4, TEP1, RNH70, BNR1, CDC3, KAR1, CWP1, HYM1, ORC1, NDT80, SPO12, FUS2, ORC3, APC9, CDC16, SSP1, PCT1, STO1, BBP1, MUD13, AUT1, HXT14, SPS4, UBC11, SPR1, HST1, ECM23, SSP2.

The family of upstream sequences should display frequent occurrences of the MSE sites ranging from HDVKNACAAAAAD (most stringent, appearing in 7 sequences) to DNCRCAAAWD (least stringent,

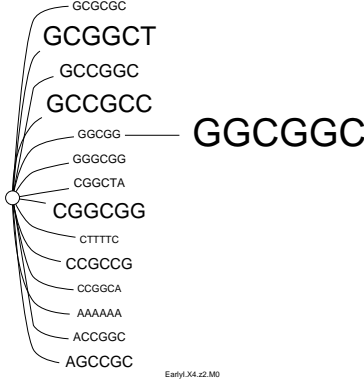
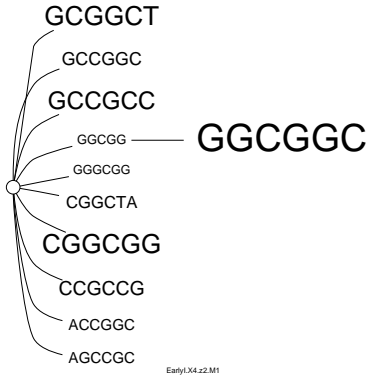
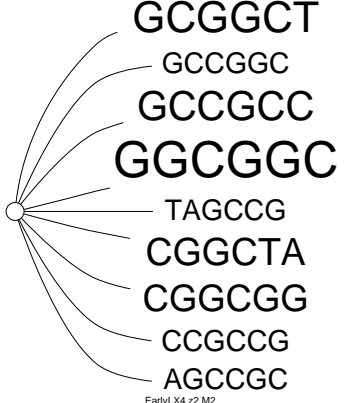

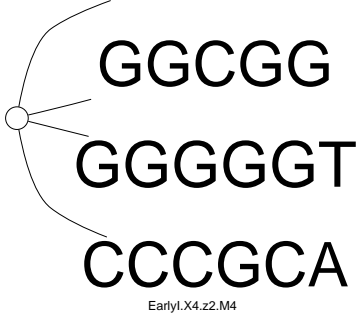
$M$	VERBUMCULUS	$M$	VERBUMCULUS
0	 <p>GGCGGC</p> <p>EarlyI.X4.z2.M0</p>	1	 <p>GGCGGC</p> <p>EarlyI.X4.z2.M1</p>
2	 <p>GGCGGC</p> <p>EarlyI.X4.z2.M2</p>	3	 <p>AGGACC</p> <p>EarlyI.X4.z2.M3</p>
4	 <p>GGCGG</p> <p>EarlyI.X4.z2.M4</p>		

Table 11: Early(I) cluster, score  $z_2$ , threshold 4.0,  $M$  is the order of the Markov chain

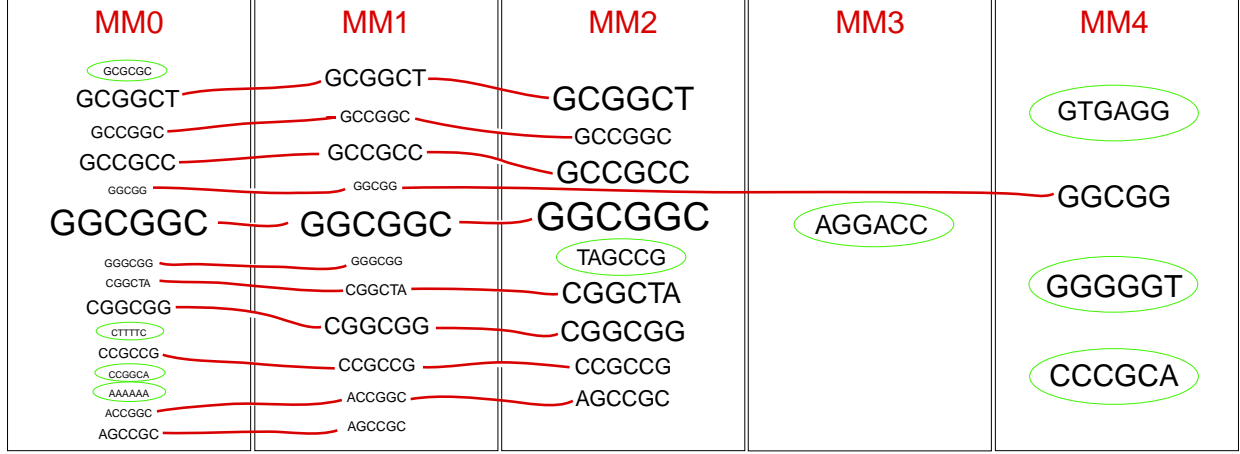


Figure 9: The collection of words from Figure 11. Identical words are connected with lines, while singleton words are circled

$w$	<i>occurrences</i>		<i>sequences</i>	
	$E(w)$	$f(w)$	$E_c(w)$	$c(w)$
CAAA	242.76	349	62.37	63
CTTT	197.31	346	60.82	62
TTTT	350.02	884	62.65	63
CACAAA	14.11	40	16.09	37
TTTTTT	19.82	78	30.42	46

Table 12: Statistics for some notable words of the cluster **Middle** (63 sequences)

appearing in 31 sequences). The complication for VERBUMCULUS is that these patterns are not fixed strings but rather regular expression, however trivial: for example **N** is a wildcard denoting any letter in the set **A, C, G, T**, whereas **R** can be substituted only with a purine (**A** or **G**), **Y** with a pyrimidine (**C** or **T**), etc.

We would like to isolate the core **CAAA** or, even better, **CACAAA** from the upstream regions relative to the genes in the cluster **Middle**. Six sequences share another prominent motif, namely **CWBYSCCTTT**.

Unfortunately, it seems difficult to catch **CACAAA** in **Middle**. The  $z_2$ -tree in Table 13 shows the 15 words with highest  $z_2$  score: **CACAAA** does not show up among them. We have to lower the threshold on that score to 5.0 before we can see **CACAAA**, but this has the simultaneous effect of raising the tree size to almost 100 nodes. The same happens when we look for **CAAA** (see Table 13-right). However, at least **CTTT** pops up now among the highest scoring motifs. Table 12 shows the statistics of these and other notable words.

We used other scores to see if we could get **CACAAA** somewhere. Table 13 shows the  $z_4$ -tree for the cluster **Middle** that suffers again from the presence of the family of words **A<sup>+</sup>** and **T<sup>+</sup>**, but no **CACAAA**. It also shows the  $z_8$ -tree, but again no **CACAAA**. Finally, a surprise. The  $z_9$ -tree shows **CACAAA** in the high scoring patterns.



Score	$T$	VERBUMCULUS	Score	$T$	VERBUMCULUS
$z_2$	7.0	<p>Mid.600bps.z2.L6.X7</p>	$z_2$	3.0	<p>Mid.600bps.z2.L4.X3</p>
$z_4$	10.0	<p>Mid.600bps.z4.L6.X10</p>	$z_8$	6.0	<p>Mid.600bps.z8.L6.X6</p>
$z_9$	12.0	<p>Mid.600bps.z9.L6.X12</p>			

## 7 Conclusion

This paper describes a genome-wise searching system for over- or under-represented nucleotide motifs, called VERBUMCULUS. The main advantages brought about by this tool are speed, low memory requirements and visualization capabilities. This rests on the core structure of the algorithm, which takes advantage of strong properties at the intersection of statistics, pattern matching and combinatorics on words. As a result, the facility at the outset can detect over- or under-represented patterns in linear time and space for most of the scores in use. An array of experimental tests, ranging from simulations on synthetic data to the discovery of regulatory elements on the upstream regions of a set of genes of the yeast, was used to demonstrate the strengths as well as some limitations of the tool.

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