## Lecture Notes in Computer Science

Edited by G. Goos and J. Hartmanis

386

J.E. Pin (Ed.)

# Formal Properties of Finite Automata and Applications

LITP Spring School on Theoretical Computer Science Ramatuelle, France, May 23–27, 1988 Proceedings



Springer-Verlag

Berlin Heidelberg New York London Paris Tokyo Hong Kong

### **Editorial Board**

D. Barstow W. Brauer P. Brinch Hansen D. Gries D. Luckham C. Moler A. Pnueli G. Seegmüller J. Stoer N. Wirth

### Editor

J.E. Pin Université Paris VI et CNRS LITP, Tour 55-65, 4 place Jussieu F-75252 Paris Cedex 05, France

CR Subject Classification (1987): F.1, F.4.3, G.2

ISBN 3-540-51631-X Springer-Verlag Berlin Heidelberg New York ISBN 0-387-51631-X Springer-Verlag New York Berlin Heidelberg

This work is subject to copyright. All rights are reserved, whether the whole or part of the material is concerned, specifically the rights of translation, reprinting, re-use of illustrations, recitation, broadcasting, reproduction on microfilms or in other ways, and storage in data banks. Duplication of this publication or parts thereof is only permitted under the provisions of the German Copyright Law of September 9, 1965, in its version of June 24, 1985, and a copyright fee must always be paid. Violations fall under the prosecution act of the German Copyright Law.

© Springer-Verlag Berlin Heidelberg 1989 Printed in Germany

Printing and binding: Druckhaus Beltz, Hemsbach/Bergstr. 2145/3140-543210 – Printed on acid-free paper

### Foreword

This volume contains the proceedings of the sixteenth Spring School of Theoretical Computer Science (Ecole de Printemps d'Informatique Théorique) organized jointly by the LITP (Paris), the ENSEEITH, the LSI (Toulouse) and the "Association d'Informatique Théorique", with the support of the Centre National de la Recherche Scientifique (CNRS) and of the Programme de Recherches Coordonnées (PRC) Mathématiques et Informatique.

This Spring School is a yearly meeting whose subject and location change every year. It usually consists partly of tutorial introductions and general surveys and partly of more specialized lectures. The list of the past Spring Schools is as follows (with the name of the organizers):

- 1. Langages Algébriques, Bonascre, 1973, J.P. Crestin et M. Nivat.
- 2. Complexité des algorithmes, Ile de Berder, 1974, P. Flajolet.
- 3. Monoïdes syntactiques, Vic sur Cère, 1975, J.F. Perrot.
- 4. Sémantique des langages de programmation, Molines en Queyrac, 1976, M. Nivat.
- 5. Séries Formelles, Vieux-Boucau les Bains, 1977, J. Berstel.
- 6. Lambda Calcul, La Châtre, 1978, B. Robinet.
- 7. Théorie des Codes, Jougne, 1979, D. Perrin.
- 8. Parallélisme, Colleville, 1980, G. Roucairol.
- 9. Langages Algébriques, Murol, 1981, L. Boasson.
- 10. Compilation, Barèges, 1982, L. Nolin.
- 11. Algorithmique, Ile de Ré, 1983, M. Fontet.
- 12. Automates et Mots Infinis, Le Mont Dore, 1984, D. Perrin.
- 13. Logique Combinatoire et λ-calcul, Val d'Ajol, 1985, G. Cousineau et P.L. Curien.
- 14. Réseaux d'Automates, Argelès-sur-Mer, 1986, Ch. Choffrut.
- 15. Linguistique et Informatique, Ile d'Oléron, 1987, M. Gross et D. Perrin.

The proceedings of the last four Spring Schools have been published in English in this series (LNCS 192, 242, 316, 377).

The subject of the sixteenth School is the theory of finite automata and its applications. However two important parts of this theory are not treated in this volume, because they were already the subject of two earlier Spring Schools: "Automata on infinite words" (Spring School 1984) and "Automata Networks" (Spring School 1986).

The proceedings have been divided into three sections. The first section is devoted to the mathematical foundations of the theory of automata. The first paper of this section, by J. Berstel, is a survey of the theory of finite automata which contains many interesting examples. The paper by H. Straubing is an introduction to the wreath product and the decomposition techniques for finite automata. M.P. Schützenberger's paper deserves special mention. Professor Schützenberger was not able to attend the Spring School, but he was kind enough to prepare this article on rational functions, which was read by D. Perrin at the Spring School. The next two articles, by myself and J.C. Birget, concern some useful tools of the theory: relational morphisms and transductions in my article, and two-way finite automata in Birget's article. The paper by I. Simon is a survey on factorization forests, a concept that covers most of the "Ramseyan type" properties used in the theory of automata.

The second section deals with famous problems of the theory of automata. The first paper, by K. Hashiguchi, gives the main ideas of his recent algorithm for determining the starheight of a given rational language. The second paper, by J. Meakin, presents some recent advances on word problems. The paper by W. Thomas shows the connections between automata and quantifier hierarchies in logic. P. Weil gives a survey on the difficult problems connected with the concatenation product, including some very recent results. The last two papers of this section are directly related to semigroup theory. A. de Luca and S. Varricchio give some new finiteness conditions for semigroups, and J. Almeida presents a new approach on equations defining varieties of finite semigroups.

Some applications of finite automata are presented in the last section. Algorithms on strings using automata are analyzed by M. Crochemore. G. Rauzy and A. Restivo show the applications of finite automata to number theory and to the theory of codes, respectively. A. Straubing and D. Thérien present their recent work on computational complexity based on finite automata. The last two papers, by I. Guessarian and D. Vergamini, are devoted to the application of automata to the modeling of distributed systems.

Finally, I would like to thank my co-organizers Colette Ravinet and Patrick Sallé. Both spent a lot of time organizing this Spring School. Special mention is due to Colette Ravinet who

discovered the beautiful Centre Léo Lagrange in Ramatuelle. The managers and employees of the Centre deserve special mention for their kindness and for providing us with delicious "anchoyades" and perpetual sun. Finally, I would like to thank the local council of Ramatuelle for their reception.

Paris, May 1989

Jean-Eric Pin

## Contents

Mathematical foundations of the theory of automata1
Finite automata and rational languages. An introduction
The wreath product and its applications
Décomposition polynomiale des fonctions rationnelles (English summary)25  M.P. Schützenberger
Relational morphisms, transductions and operations on languages
Basic techniques for two-way finite automata
Properties of factorization forests
Problems related to the theory of automata73
Relative star height, star height and finite automata with distance functions74 <i>K. Hashiguchi</i>
Automata and the word problem
Automata and quantifier hierarchies
Concatenation product: a survey
A finiteness condition for semigroups
Equations for pseudovarieties

Applications of the theory of automata165
Algorithms and automata
Numbers and automata
Codes and Automata
Finite automata and computational complexity
A characterization of fair computations of finite state SCCS processes
Verification of distributed systems: an experiment
<b>Author Index</b>