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Christine Paulin-Mohring (Eds.)

Types for Proofs and Programs

International Workshop TYPES '96
Aussois, France, December 15-19, 1996
Selected Papers

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Preface

This book is made up of a selection of papers presented at the first annual workshop held under the auspices of the Esprit Working Group 21900 TYPES. It took place in Aussois, France, December 15-19, 1996. The workshop was attended by 89 people.

This volume is a follow-up to the proceedings of the workshops organised in 1993, 1994, and 1995 under the auspices of the Esprit Basic Research Action 6453 *Types for Proofs and Programs*. These proceedings were also published in the LNCS series, edited by Henk Barendregt and Tobias Nipkow (number 806, 1993), by Peter Dybjer, Bengt Nordström, and Jan Smith (number 996, 1994), and by Stefano Berardi and Mario Coppo (number 1158, 1995). The Esprit BRA 6453 was a continuation of the former Esprit Action 3245 *Logical Frameworks: Design, Implementation and Experiments*. The articles from the annual workshops organised under that action were edited by Gérard Huet and Gordon Plotkin in the books *Logical Frameworks* and *Logical Environments*, both published by Cambridge University Press.

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Selection

30 papers were submitted and fully reviewed. The final choice was made by the editors. We thank the following people who acted as referees.

Thorsten Altenkirch
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Benjamin Werner

July 1998

Eduardo Giménez and Christine Paulin
Editors

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