



System Level Power Optimization of Digital Audio Back End for Hearing Aids

Pracny, Peter; Jørgensen, Ivan Harald Holger; Bruun, Erik

Published in:
Circuits, Systems and Signal Processing

Link to article, DOI:
[10.1007/s00034-016-0419-z](https://doi.org/10.1007/s00034-016-0419-z)

Publication date:
2017

Document Version
Peer reviewed version

[Link back to DTU Orbit](#)

Citation (APA):
Pracny, P., Jørgensen, I. H. H., & Bruun, E. (2017). System Level Power Optimization of Digital Audio Back End for Hearing Aids. *Circuits, Systems and Signal Processing*, 36(6), 2441–2458. <https://doi.org/10.1007/s00034-016-0419-z>

General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

Circuits, Systems, and Signal Processing

System Level Power Optimization of Digital Audio Back End for Hearing Aids

--Manuscript Draft--

Manuscript Number:	CSSP-D-15-00692R3
Full Title:	System Level Power Optimization of Digital Audio Back End for Hearing Aids
Article Type:	Original Research
Keywords:	audio; hearing aid; low voltage; Low power; Digital; system level; power optimization; interpolation filter; sigma-delta modulator; digital-to-analog converter; Class D; power amplifier; figure-of-merit.
Corresponding Author:	Peter Pracny, Ph.D. InvenSense Inc. Bratislava, SLOVAKIA
Corresponding Author Secondary Information:	
Corresponding Author's Institution:	InvenSense Inc.
Corresponding Author's Secondary Institution:	
First Author:	Peter Pracny, Ph.D.
First Author Secondary Information:	
Order of Authors:	Peter Pracny, Ph.D. Ivan Harald Holger Jørgensen Erik Bruun
Order of Authors Secondary Information:	
Funding Information:	
Abstract:	<p>Abstract—This work deals with power optimization of the audio processing back end for hearing aids - the interpolation filter (IF), the sigma-delta (SD) modulator and the Class D power amplifier (PA) as a whole. Specifications are derived and insight into the tradeoffs involved is used to optimize the interpolation filter and the SD modulator on the system level so that the switching frequency of the Class D PA - the main power consumer in the back end - is minimized. A figure-of-merit (FOM) which allows judging the power consumption of the digital part of the back end early in the design process is used to track the hardware and power demands as the tradeoffs of the system level parameters are investigated. The result is the digital part of the back end optimized with respect to power which provides audio performance comparable to state-of-the-art. A combination of system level parameters leading to the lowest switching frequency of the Class D power amplifier reported in literature for the SD modulator-based back end is derived using this approach.</p>
Response to Reviewers:	<p>This submission is the final version of our manuscript. According to the instructions for authors and the email from the editor the following changes were done:</p> <ul style="list-style-type: none"> - the order of the references was changed to alphabetic order. - footnote with contact information of all authors was added on the first page <p>Thank you.</p>

System Level Power Optimization of Digital Audio Back End for Hearing Aids

Peter Pracný, Ivan H. H. Jørgensen, and Erik Bruun

Abstract—This work deals with power optimization of the audio processing back end for hearing aids - the interpolation filter (IF), the sigma-delta ($\Sigma\Delta$) modulator and the Class D power amplifier (PA) as a whole. Specifications are derived and insight into the tradeoffs involved is used to optimize the interpolation filter and the $\Sigma\Delta$ modulator on the system level so that the switching frequency of the Class D PA – the main power consumer in the back end – is minimized. A figure-of-merit (FOM) which allows judging the power consumption of the digital part of the back end early in the design process is used to track the hardware and power demands as the tradeoffs of the system level parameters are investigated. The result is the digital part of the back end optimized with respect to power which provides audio performance comparable to state-of-the-art. A combination of system level parameters leading to the lowest switching frequency of the Class D power amplifier reported in literature for the $\Sigma\Delta$ modulator-based back end is derived using this approach.

Index Terms—audio, hearing aid, low voltage, low power, digital, system level, power optimization, interpolation filter, $\Sigma\Delta$ modulator, digital-to-analog converter, Class D, power amplifier, figure-of-merit.

1. Introduction

High audio quality, longer operation time and small device size are parameters demanded in hearing aids today. Optimum balance between the design parameters in every part of a hearing aid device is therefore of vital importance, making the power consumption one of the crucial requirements for the design. This is also the case for the audio signal processing path which requires a digital-to-analog conversion and a power amplifier at the back end to drive the speaker (see Fig.1). In order to ensure high efficiency in the output stage, it is normally operated in class D mode by using a push-pull configuration (basically two large inverters) controlled by two 1-bit signals [1,4,6,12,16,17]. Apart from having a high efficiency, this also eliminates problems with device matching compared to using a Class AB output stage as in [14,26,30]. The Class D output stage is usually implemented as an H-bridge (schematic in Fig.1 is simplified, showing single ended operation). Compared to [14,26,30] which use Class AB power stage, the Class D allows to perform all the signal processing before the output

Peter Pracný, Bieloruská 13, 82106 Bratislava, Slovak Rep., peter.pracny@outlook.com

Ivan H. H. Jørgensen, Dept. Electrical Engineering, Tech. Univ. of Denmark, Kgs. Lyngby, Denmark, ihhj@elektro.dtu.dk

Erik Bruun, Dept. Electrical Engineering, Tech. Univ. of Denmark, Kgs. Lyngby, Denmark, eb@elektro.dtu.dk

1 filter in digital domain. Digital design provides the advantage of low voltage, low
2 power and cost effective implementation and scales down with integrated circuit
3 (IC) technologies of today.
4

5 As the output stage operates using a single bit input, the resolution of the
6 input signal (16 bits) must be converted to a 1-bit signal. A wide spread solution
7 to this is using oversampled noise shaping modulators, also called $\Sigma\Delta$ modulators
8 [1,12,16,17]. These modulators trade off the number of bits versus sampling
9 frequency by suppressing the quantization noise at low frequencies at the expense
10 of a drastic increase in high frequency noise. The high frequency noise is in this
11 application filtered in the speaker (and placed outside the audible frequencies).
12 Due to the oversampling nature of the oversampled $\Sigma\Delta$ modulator, an
13 interpolation filter (IF) is needed prior to the modulator. The purpose of the
14 interpolation filter is to upscale the sampling frequency of the incoming signal
15 from f_{sin} to a new signal with a sampling rate ($OSR \times f_{sin}$) that equals the sampling
16 rate of the $\Sigma\Delta$ modulator. Basically, the interpolation filter is simply a filter which
17 ensures that extra sampling points (interpolation points) are added to the input
18 signal without deteriorating the quality of the signal. However, the complexity of
19 the interpolation filter depends on the upscaled sampling rate and thus the power
20 consumption of the interpolation filter must be taken into account when
21 evaluating the performance of the entire output stage. This will be treated in this
22 paper. When using a multibit $\Sigma\Delta$ modulator, a digital pulse width modulation
23 (DPWM) block that turns the $\Sigma\Delta$ signal into a symmetrical 1 bit pulse width
24 modulation is needed.
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42

43 This paper deals with the power optimization of the system in Fig. 1 and
44 provides an overview of results obtained during a PhD study presented in [18].
45 The paper summarizes and elaborates the partial conclusions derived during the
46 course of the PhD project. In Section 2, the design specifications and the figure-
47 of-merit for the $\Sigma\Delta$ modulator and the interpolation filter are discussed. The
48 figure-of-merit is used to judge the power consumption of the digital part early in
49 the design process. In Section 3, an initial design is described. This design is used
50 as the starting point for the optimization described in this section. Various
51 approaches to optimize the initial $\Sigma\Delta$ modulator design are investigated using the
52 tradeoffs of basic system level parameters and summarized. The resulting designs
53 are then compared using the figure-of-merit which is introduced in section 2. A
54
55
56
57
58
59
60
61
62
63
64
65

1 trendline for the digital part of the system of Fig. 1 is derived based on the
2 summary of results in Section 4, and a comparison with other state-of-the-art
3 works in this topic is presented. In the conclusion of Section 5, it is discussed
4 which approach leads to optimized audio back end with respect to power
5 consumption.
6
7
8
9

10 **2. Design Specifications and Figure-of-merit**

11
12
13 A thorough discussion on hearing aid audio back end system specification
14 and the $\Sigma\Delta$ modulator is provided in [19]. Taking into account that a hearing aid is
15 intended for people with hearing problems, the bandwidth (BW) of the audio
16 signal is a tradeoff between ensuring sufficient sound quality and the limited
17 power available and is normally around 10 kHz. While it is possible to design a
18 hearing aid with a signal bandwidth of 4 kHz to keep the current consumption
19 even lower and still ensure some speech intelligibility, the bandwidth of BW = 10
20 kHz ensures good speech intelligibility as well as good localization of sound
21 sources. In order to fulfill the Nyquist criterion, the input sampling frequency $f_{s_{in}}$
22 must be larger than $2 \times BW = 20$ kHz. As the bandwidth for the hearing aid
23 application is half of the bandwidth in high fidelity audio, the sampling frequency
24 at the input of the system for this design was chosen to be half of the standard
25 high fidelity audio sampling frequency $44.1 \text{ kHz}/2 = 22.05 \text{ kHz}$. Also, in this work
26 ideal 16 bit quantization of the input signal to the back end system is assumed.
27 This results in the signal-to-quantization-noise ratio SQNR = 98 dB. The input
28 signal of the back end is then up-sampled using a multistage IF and passed to the
29 $\Sigma\Delta$ modulator [15,24,27].
30
31
32
33
34
35
36
37
38
39
40
41
42
43

44
45 Investigating the hearing aids in the market today does not bring much
46 information about the requirements for the electronics as this is considered
47 confidential information. However, from [1] and [6] the peak signal-to-noise-ratio
48 varies between 70 dB and 92dB, and in this work, the target is a signal-to-noise-
49 and-distortion ratio (SNDR) of 90 dB at the total output. The IF and the $\Sigma\Delta$
50 modulator are designed to keep the quality of the audio signal close to SNDR = 98
51 dB so that a margin of approximately 8 dB is left for the performance reduction
52 introduced by the output stage. Higher order $\Sigma\Delta$ -modulators inherently become
53 unstable when the input exceeds a certain signal amplitude. This amplitude is
54 called the maximum stable amplitude (MSA) and varies for all $\Sigma\Delta$ -modulators
55
56
57
58
59
60
61
62
63
64
65

depending on the design. Therefore, the higher the MSA, the more the requirement for the noise can be relaxed to achieve a certain SNR. However, when the MSA approaches full scale, the quantization noise tends to increase drastically for $\Sigma\Delta$ -modulators, yielding a very poor SNR, and thus a design requirement of an MSA as close to -1 dBFS as possible is chosen as a compromise. A maximum system clock frequency was initially specified by a hearing aid company to be 5.6 MHz but as the work in this paper shows significant improvements can be achieved by exceeding this number.

Both the IF and the $\Sigma\Delta$ modulator are digital designs in this work. A digital $\Sigma\Delta$ modulator can be looked at as a digital filter with two transfer functions: a signal transfer function (STF) and a noise transfer function (NTF). Hence, a figure of merit (FOM) developed for digital filters [2,28,35] can be applied. In this work, the FOM is used to judge the complexity of the IF and the $\Sigma\Delta$ modulator by counting the number and complexity of adders [11, 20-23]. This leads to

$$FOM = (\sum_i b_i \times OSR_i) / 64 \quad (1)$$

where i is the number of adders in the block of interest, b_i is the number of bits used in individual adders and OSR_i is the oversampling used for the individual adders. The factor of 64 in (1) is included since this is the OSR for the $\Sigma\Delta$ modulator in the first design presented in this paper and thus we normalized the FOM to this. In the case of the $\Sigma\Delta$ modulator block, OSR_i is the same for all the adders. Since this FOM accounts for the majority of the cells needed to implement the IF and the $\Sigma\Delta$ modulator, it is roughly proportional to the power consumption of the design and is a valuable tool when choosing between designs in an early design phase. The lower the FOM, the less hardware and power demanding the design is. There are more precise figures of merit for $\Sigma\Delta$ modulators used in other works [27]. However, these figures of merit can be used only after the design has been completed and possibly measured. The advantage of the figure of merit of (1) is that it makes it possible to decide early in the design process whether or not an optimization approach is reasonable. The above mentioned specifications and FOM will be used in this work for comparison when optimizing the back end system. For the sake of comparison, all the FOMs in this work are normalized to $64 \times f_{s_{in}} = 64 \times 22.05 \text{ kHz} = 1.4 \text{ MHz}$, the sampling rate used for the first design presented in section 3.

3. Optimization

A simplified general schematic for all the $\Sigma\Delta$ modulators in this work is shown in Fig. 2. The basic cascade of resonators with feedback (CRFB) structure is used. This converter type has been chosen for two reasons. First, the order can be scaled arbitrarily simply by adding more feedback loops. Second, as the study focuses on the system level design parameters (sampling rate, modulator order, etc.), only one topology is treated to limit the study. There are other architectures also suited for digital implementation, such as MASH [32], using the bus splitting and frequency masking methods to save hardware and current consumption [7,33,34]. Since this work covers the initial design phase, it discusses simple tradeoffs of system level parameters to arrive at a conclusion of how the choice of these parameters affects the hardware and power demands of the system. Inclusion of the above mentioned advanced design techniques would introduce complexity and make the effect of a simple parameter tradeoff less readable. For this reason, the $\Sigma\Delta$ modulator architecture is kept to be the basic CRFB. The advanced design techniques can be introduced at a later phase in a project. Moreover, feedback (FB) can be used around the whole back end to improve the performance, but in this case an analog-to-digital converter (ADC) has to be included in the FB, and the system is not fully digital. In this case, the FOM of (1) would become more complex to account for the hardware and power consumption of the analog blocks. Such investigation is left as future work.

A model using fixed-point arithmetic was designed and simulated in Matlab for all the $\Sigma\Delta$ modulator and IF designs of this work. The coefficients of these designs can be found in [18]. Since all the designs have the same SQNR performance at the output and the fixed-point model performs computations exactly as a VHDL code does (there is one-to-one correspondence of the output bit stream of the Matlab model and the VHDL code), the fixed-point model can be used for judging the complexity of the design with the FOM.

Typical state-of-the-art designs use a combination of system level parameters as shown in Table 1 [5,8,13,31]. The starting point for the $\Sigma\Delta$ modulator design in this work was to design a modulator using a low number of bits at the output and a maximum sampling rate of 5.6Mhz. This resulted in a 3rd order modulator with an oversampling ratio $OSR = 64$ and a 3 bit quantizer [19].

The maximum modulator NTF gain is $H_{\text{inf}} = 1.5$ as advised in [27]. Since the $\Sigma\Delta$ modulator of the initial design works with $\text{OSR} = 64$, the IF has to increase the input sampling frequency $f_{s_{\text{in}}}$ by a factor of 64. To reduce the hardware demands and power consumption, the state-of-the-art DAC designs implement the IF as a multi stage filter [15,24,27]. The IF that is used for the initial $\Sigma\Delta$ modulator design consists of 4 stages and is shown in Fig. 3. In order to investigate the impact of the first stage of the interpolation filter on the FOM there are two versions of the initial design. The details of the first version are provided in [19] and [24]. This design uses an FIR filter as the first stage of the IF and it turns out that the FOM is too high for a hearing aid application. The second version with an IIR filter as the first stage of the IF [11] is inspired by [25,29,36] and is denoted in Table 2 and 3 as the ‘Initial design’.

Rather than using the suggestion in [27] that the IF should suppress the frequency images below the $\Sigma\Delta$ modulator NTF, this work uses suppression of around 60 dB for the closest image in the frequency spectrum. This is sufficient to reach the hearing threshold of a normal hearing person to make sure the image is not hearable [24] and [10].

Normally, plots such as the one shown in Fig. 4 are used to understand the system level parameter tradeoffs and their impact on peak SQNR performance [27]. Fig. 4 shows the peak SQNR of the $\Sigma\Delta$ modulator plotted as a function of the OSR parameter for modulator orders of $M = 1$ to 8. For the case of the ‘Initial design’, the peak SQNR = 106 dB. Since peak SQNR = 98 dB is sufficient according to the specification, the margin left is used for coarse coefficient quantization to reduce the FOM [20]. The resulting peak SQNR of the modulator is then 98 dB.

For hearing aid application, the power consumption is a critical parameter. But the information about the power consumption is not included in plots such as Fig. 4. Therefore, the tradeoffs of the system level parameters and the power consumption will be investigated in the following sections of this article. To optimize the ‘Initial design’ with respect to power, various approaches were investigated in this work:

3.1 $\Sigma\Delta$ Modulator Order versus OSR tradeoff

The idea behind the optimization of the $\Sigma\Delta$ modulator and the entire back end compared to the initial design (order = 3, OSR = 64, 3bit, max. NTF gain = 1.5) is to decrease the OSR of the modulator from 64 to 32 and increase its order from 3 to 6. This keeps the ideal peak SQNR = 106 dB so that coefficients can again be coarsely quantized and give resulting SQNR = 98 dB after coefficient quantization with low FOM [20]. By performing these changes in the $\Sigma\Delta$ modulator, the aim is to reduce the switching frequency of the Class D output stage [3] and the DPWM block by 50% as this frequency is the same as the operating frequency of the $\Sigma\Delta$ modulator (see Fig. 1). With the Class D output stage being the main power consumer in the back end system due to switching losses of the output transistors, this will result in considerable power savings. Moreover, these changes will have positive impact on the IF too as oversampling by 32 only is needed compared to oversampling by 64 in the initial design. This saves part of the last stage, performing oversampling by a factor of 2 in the IF of the initial design. Using the FOM of (1), a FOM = 86.8 is calculated for the whole IF, out of which FOM = 36 goes for the part that will be saved by this optimization. This is a reduction in power consumption by more than 40% in the IF. With savings in the PA and the IF, the only block of the back end system that remains to be investigated to see whether or not this optimization approach is reasonable is the $\Sigma\Delta$ modulator. This investigation was performed in [20]. Taking the Matlab fixed-point models and calculating the FOM according to (1) gives the data and FOM in Table 2 and 3, clearly showing that the FOM of the 6th order modulator with OSR = 32 compared to 3rd order modulator with OSR = 64 of the initial design remains approximately the same after the back end system optimization. This can be predicted by looking at Fig. 2. The OSR of the 6th order modulator is halved compared to the 3rd order modulator but the area is doubled. To have lower power consumption in the Class D output stage and have larger area of the $\Sigma\Delta$ modulator is a reasonable tradeoff since the $\Sigma\Delta$ modulator is implemented using only digital standard cells and thus easily scales with technology. The same cannot be said about the Class D output stage. The current consumption of the back end can be calculated as the sum of the currents needed in each block:

$$I_{total} = I_{int} + I_{SDM} + I_{DPWM} + I_{dr} \quad (2)$$

where I_{int} is the current needed in the IF, I_{SDM} is the current of the $\Sigma\Delta$ modulator, I_{DPWM} is the current of the DPWM block and I_{dr} is the current of the Class D PA. It was found that I_{dr} and I_{DPWM} will be reduced by 50% and I_{int} by 41.5% by the optimization. Comparing the ‘Section 3.1’ design with the ‘Initial design’ in Table 3, it can be seen that I_{SDM} will remain approximately the same. Thus, in total there are considerable power savings achieved by this optimization approach.

3.2 Very High Order Modulators

The same optimization approach as in Section 3.1 is used again. Again, the OSR of the $\Sigma\Delta$ modulator is halved and the order is doubled compared to the $\Sigma\Delta$ modulator of Section 3.1 (order = 6, OSR = 32, 3bits) while the audio quality is kept within the specification. Thus the OSR is $32/2 = 16$ and the order is $6 \times 2 = 12$.

To reach the required SQNR at the modulator output and for stability reasons, the number of bits in the quantizer has to be increased from 3 bits to 5 bits. Again, a model using fixed-point arithmetic was built and simulated in Matlab. A comparison with the previous design iterations is shown in Table 2 and Table 3. Table 3 shows that the FOM of the 12th order $\Sigma\Delta$ modulator design is much higher than the FOM of previous design iterations. The reasons are described in detail in [18]. The trade-off between modulator order and OSR is shown graphically in Fig. 5 assuming a $\Sigma\Delta$ modulator with 3 or 5 bits quantization.

In conclusion, further attempts to continue with the approach of trading higher modulator order for lower OSR result in higher FOM. This leads the optimization of the DAC away from the optimum design and parameter choice. The idea of trading lower OSR for higher modulator order to obtain better FOM has its limits and a different approach has to be tried in further optimization steps.

3.3 Using Interpolation Factor of 3

The DAC can be optimized with respect to power by reducing the OSR of the $\Sigma\Delta$ modulator. If the OSR is restricted to be a factor of integer power of two, the only option is to reduce the OSR from 32 down to 16. Such an optimization would reduce the switching frequency of the Class D PA by 50% and thus save 50% of power compared to the design of Section 3.1. Moreover, the power

consumption of the DPWM block would also be reduced by 50% as its operating frequency f_{DPWM} depends directly on OSR (see Fig. 1). Power consumption would also be saved in the IF because the part of the last stage that increases the frequency from $16 \times f_{sin}$ to $32 \times f_{sin}$ would not be needed. Table 2 shows that this stage has the highest FOM of all stages for the design of Section 3.1 because it operates at highest frequency and thus consumes the largest amount of power in the IF. The only block of the DAC that remains to be investigated is the $\Sigma\Delta$ modulator. This has been done in [22-23], and the investigation shows that in order to achieve the necessary performance of SQNR and MSA, the maximum gain of NTF, H_{inf} , of the $\Sigma\Delta$ modulator must be increased significantly above the recommendations in [27].

Alternatively, the OSR can be selected to 24 as a compromise between the values of 32 and 16. The resulting $\Sigma\Delta$ modulator design is included in Table 3. In order to achieve $OSR = 24$, one of the stages of the IF has to perform sample rate increase by a factor of 3. In [22-23], two cases are investigated. The sampling frequency increase by a factor of 3 can be performed either by the first stage of the IF or by the last stage of the IF. The IF options investigated in [22-23] are summarized in Table 4. Table 4 shows that a lower FOM is achieved if the sampling frequency increase is implemented with the first stage as an IIR filter. Further improvement of the FOM of the IF without significantly compromising the performance can be achieved by implementing the second stage of the IF as a CIC (Cascaded Integrator Comb) filter instead of IIR. The IF option with the lowest FOM is then included in Table 3 for total FOM comparison.

3.4 Increasing the Number of Quantizer Bits

With a higher number of bits, the OSR may be further reduced without compromising the peak SQNR. Also, Section 3.3 shows that increase of the maximum NTF gain of the $\Sigma\Delta$ modulator should be investigated as a way to achieve better performance. In this section, these two approaches are combined in order to reduce the OSR of the $\Sigma\Delta$ modulator while keeping its order, peak SQNR and MSA. The maximum clock frequency is defined by the DPWM block to be

$$f_{DPWM} = 2^Q \times OSR \times f_{sin} \quad (3)$$

For the design of Section 3.1, this results in $f_{sDPWM} = 2^3 \times 32 \times 22.05 \text{ kHz} = 5.65 \text{ MHz}$. The same maximum system frequency can be obtained if the number of bits in the $\Sigma\Delta$ modulator quantizer is increased to 5 and the OSR is decreased to 8. In this case, $f_{DPWM} = 2^Q \times \text{OSR} \times f_{s_{in}} = 2^5 \times 8 \times 22.05 \text{ kHz} = 5.65 \text{ MHz}$. Thus, the power consumption of the DPWM block remains unchanged by such change. Again, since the switching frequency of the Class D stage is the same as the operating frequency of the $\Sigma\Delta$ modulator (see Fig. 1), it would be reduced by 75% compared to the design of Section 3.1 (order = 6, OSR = 32, 3 bit). To have lower power consumption in the Class D output stage and have more bits in the quantizer of the $\Sigma\Delta$ modulator is a reasonable tradeoff since the $\Sigma\Delta$ modulator is completely digital.

However, a 6th order modulator with OSR = 8 and a 5 bit quantizer does not provide the required peak SQNR = 98 dB at the output of the modulator if maximum NTF gain $H_{inf} = 1.5$ is used as recommended in [27]. As in section 3.3, maximum NTF gain H_{inf} can be increased to obtain the required peak SQNR performance [21]. A detailed investigation in [21] shows that a maximum NTF gain $H_{inf} = 5$ is sufficient to achieve the required SQNR, and further increase of this parameter decreases MSA of the $\Sigma\Delta$ modulator below the specification of -1.2 dBFS. Thus, $H_{inf} = 5$ is chosen for this design.

With this modification, the operating frequency of the $\Sigma\Delta$ modulator and thus the switching frequency of the Class D output stage is reduced by a factor of 8 compared to the initial design (order = 3, OSR = 64, 3 bits) and by a factor of 4 compared to the design of Section 3.1 (order = 6, OSR = 32, 3 bits). This will result in considerable power savings. Again, these changes will have a positive impact on the IF too as only an oversampling by 8 is needed compared to oversampling by 64 in [8, 13, 31] and by 32 in Section 3.1. This saves the entire last stage in the IF operating at high frequency. Using the FOM of (1) for the IF of the ‘Initial design’ and Section 3.1 results in FOM = 86.8 and FOM = 51 respectively (see Table 2). After the reduction of OSR down to 8, the FOM of the IF is 16.3. This is an improvement of hardware/power saving by more than 80% in the IF compared to the ‘Initial design’ and by more than 65% compared to the design of Section 3.1. With the same maximum clock frequency of the DPWM block as in Section 3.1, and with power savings in the IF and in the Class D output stage, also the $\Sigma\Delta$ modulator must be investigated. This investigation was

performed in [21], and the result is included as the $\Sigma\Delta$ FOM in Table 3. From this, a reduction of the current consumption of the $\Sigma\Delta$ modulator of more than 60% is estimated. Thus, in (2), I_{int} , I_{SDM} and I_{dr} are reduced substantially, resulting in considerable power savings from the proposed optimization approach.

3.5 Relaxing the Specification for Maximum Clock Frequency

In Section 3.1, the Class D PA has been identified as the main power consumer in the back end system. The switching frequency (and thus the power consumption) of the PA directly depends on the OSR of the $\Sigma\Delta$ modulator. Therefore, it makes sense to reduce the OSR in order to save power. In a state-of-the-art work on hearing aid audio back end design, [1] and [9], the Class D PA switching frequency is as low as 96 kHz. In order to achieve such a low Class D PA switching frequency, a hybrid PWM- $\Sigma\Delta$ modulator is used. The disadvantage is that without a clock doubler [1], this back end requires 24 MHz system clock. In this section, it is shown that if the maximum clock frequency specification of 5.6 MHz given in Section 2 is relaxed, the $\Sigma\Delta$ modulator and IF can be designed for $OSR = 4$ with $Q = 8$ bits in the quantizer and still deliver $SQNR = 98$ dB at the $\Sigma\Delta$ modulator output and $MSA = -1$ dBFS. With this specification, (3) results in $f_{SDPWM} = 2^8 \times 4 \times 22.05 \text{ kHz} = 22.6 \text{ MHz}$. Using the same design approach as in Section 3.4 and [21], the maximum NTF gain is found by the simulation to be $H_{inf} = 20$. Thus, the $\Sigma\Delta$ modulator uses order = 6, $OSR = 4$ and 8 bits in the quantizer. This results in switching frequency of the PA of $f_{SPA} = OSR \times f_{sin} = 4 \times 22.05 \text{ kHz} = 88.2 \text{ kHz}$, which, to the best knowledge of the authors, is the lowest switching frequency of a Class D PA reported in the literature for a digital audio back end.

The disadvantage of this design is that a maximum NTF gain of $H_{inf} = 20$ allows high frequency content at the input of the $\Sigma\Delta$ modulator quantizer which limits the amplitude at the output of the $\Sigma\Delta$ modulator and thus the power that can be delivered to the load (e.g. the STF DC gain of the $\Sigma\Delta$ modulator drops to -2.3 dB [18]). However, the same problem would be experienced in [1].

Again, a model using fixed-point arithmetic was built and simulated in Matlab. The FOM of the $\Sigma\Delta$ modulator is 36.4 and the FOM of the IF is 11.8. With $OSR = 4$ and an 8 bit quantizer in the $\Sigma\Delta$ modulator, the operating frequency of the DPWM block is 22.6 MHz. Moreover, with an 8 bit quantizer, the DPWM block becomes complex, and for a poor design, it might consume more power

than the Class D PA itself [9]. An ASIC implementation is needed to properly measure the power consumption of the DPWM block and the Class D PA and arrive at a proper conclusion which of these two blocks would be the main power consumer. Still, the tradeoff of higher number of bits in the quantizer for a lower OSR is of interest as, unlike the Class D PA, the digital blocks of the back end (the IF, the $\Sigma\Delta$ modulator and the DPWM block) scale with technology.

The results of section 3.3 to 3.5 show that a trade-off between OSR and number of bits can be made with a significant effect on the FOM. This is also illustrated in Fig. 6.

The real penalty is the -2.3 dB DC gain of the $\Sigma\Delta$ modulator STF which limits the amount of signal power that can be delivered to the load. This problem is solved by including the feedforward coefficients in the $\Sigma\Delta$ modulator to have $STF = 1$ (e.g. 0 dB). The feedforward coefficients require additional adders, but, unlike in Section 3.2, with $OSR = 4$, these adders do not increase the FOM significantly due to the low sampling frequency. Further investigation is left as future work.

3.6 Comparison to State-of-the-art

The design developed in Section 3.5 is compared with other state-of-the-art designs for hearing aid back ends in Table 4. In the end, the aim of all the digital modulator types for Class D PA mentioned in this work is to provide a 1 bit (or 1.5 bit) signal to drive the Class D PA. Ten years back, designers and researchers argued whether to use a pulse width modulation (PWM) to obtain the 1 bit signal or a pulse density modulation (PDM) (e.g. 1 bit $\Sigma\Delta$ modulator). It can be concluded that the state-of-the-art development and research of the past decade show that optimization of both - the PWM modulator and the PDM modulator - leads to a similar result. This result is one of the types of hybrid between $\Sigma\Delta$ modulation and PWM modulation such as this work ($\Sigma\Delta$ modulator combined with DPWM stage) or [1].

One of the disadvantages of the $\Sigma\Delta$ modulation when compared to PWM, often mentioned in the state-of-the-art is the high switching frequency of the Class D PA [1, 3,9]. Table 6 shows that the design proposed in this work is an example that a back end based on digital $\Sigma\Delta$ modulator can be designed with Class D PA

switching frequency comparable (or even lower) than a back end based on digital PWM.

4. Conclusion

The design of a digital audio back end is a task with a considerable number of design variables. An optimization at system level has been investigated in order to determine the optimum configuration of the interpolation filter and the $\Sigma\Delta$ modulator while achieving minimal power consumption for a system. The optimization is performed at system level, and the power consumption is estimated by considering the number and complexity of adders in combination with the clock frequencies for the digital pulse width modulator and the Class D output stage.

For the $\Sigma\Delta$ modulator, a cascade of resonators with feedback (CRFB) is assumed. It is found that both the order of the modulator, the oversampling ratio and the number of bits in the quantizer influence the overall power consumption significantly. This is partly due to the power consumption of the modulator itself, but occurs also because the number of bits and the sampling rate greatly influence the complexity of the interpolation filter. An optimum configuration is found to be a 6th order modulator with an oversampling ratio of 4 and 8 bits in the quantizer. This configuration requires a maximum system clock frequency of 22.6 MHz and results in a switching frequency for the digital output stage of only 88.2 kHz. Also, the interpolation filter becomes very simple. If such a high frequency system clock is not available, a higher oversampling ratio and a lower number of bits in the quantizer is required.

[1] V. Adrian, J. S. Chang, and B. Gwee, "A low-voltage micropower digital Class D amplifier modulator for hearing aids," *IEEE Trans. Circuits and Systems I: Regular Papers*, vol. 56, no. 2, pp. 337-349, Feb. 2009.

[2] V. I. Anzova, J. Yli-Kaakinen, and T. Saramäki, "An algorithm for the design of multiplierless IIR filters as a parallel connection of two all-pass filters," in *Proc. IEEE Asia Pacific Conf. on Circuits and Systems (APCCAS)*, Dec. 2006, pp. 744-747.

[3] M. Berkhout and L. Dooper, "Class D audio amplifiers in mobile applications," *IEEE Trans. Circuits and Systems I: Regular Papers*, vol. 57, no. 5, pp. 992-1002, May 2010.

[4] D. Cartasegna, P. Malcovati, L. Crespi, K. Lee and A. Baschiroto, "A design methodology for high-order class-D audio amplifiers," *Analog Integrated Circuits and Signal Processing*, vol. 78, issue 3, pp 785-798, March 2014.

- [5] R. Cellier, E. Allier, C. Crippa, R. Bassoli, A. Nagari, G. Pillonnet, and N. Abouchi, "A fully differential digital input Class D with EMI spreading method for mobile application," in *Proc. AES 37th International Conference*, Aug. 2009, pp. 1-8.
- [6] C. Chen, J. Fan, X. Hu and Y. Hei, "A Low Power, High Performance Analog Front-End Circuit for 1 V Digital Hearing Aid SoC," *Circuits, Systems, and Signal Processing*, vol. 34, issue 5, pp 1391-1404, May 2015.
- [7] B. Fitzgibbon, M. P. Kennedy, and F. Maloberti, "A novel implementation of dithered digital Delta-Sigma modulators via bus-splitting," in *Proc. IEEE Int. Symposium on Circuits and Systems (ISCAS)*, pp. 1363-1366, May 2011.
- [8] T. Forzley and R. Mason, "A scalable Class D audio amplifier for low power applications," in *Proc. AES 37th International Conference*, Aug. 2009, pp. 1-8.
- [9] B. Gwee, J. S. Chang, and V. Adrian, "A micropower low-distortion digital Class D amplifier based on an algorithmic pulsewidth modulator," *IEEE Trans. Circuits and Systems I: Regular Papers*, vol. 52, no. 10, pp. 2007-2022, Oct. 2005.
- [10] S. Hougaard, O. Jensen, M. Kristensen, C. Ludvigsen, J. Petersen, and P. Weis, *Sound & Hearing*, Widex A/S, 2007
- [11] I. H. H. Jørgensen, P. Pracný, and E. Bruun, "Hardware efficient implementation of half-band IIR Filter for interpolation and decimation," *IEEE Trans. Circuits and Systems II: Express Briefs*, vol. 60, no. 12, pp. 892-896, Dec. 2013.
- [12] C. H. Kao, W. P. Lin and W. C. Chen, "High efficiency and low distortion switching power amplifier for hearing aids," *Proc. IEE Circuits, Devices and Systems*, vol. 153, no. 2, pp. 143-147, Feb. 2006.
- [13] S. Kim, N. Cho, S. Song, and H. Yoo, "A 0.9 V 96 μ W fully operational digital hearing aid chip," *IEEE J. Solid-State Circuits*, vol. 42, no. 11, pp. 2432-2440, Nov. 2007.
- [14] K. Lee, Q. Meng, T. Sugimoto, K. Hamashita, K. Takasuka, S. Takeuchi, U. Moon, and G. C. Temes, "A 0.8 V, 2.6 mW, 88 dB dual-channel audio Delta-Sigma D/A converter with headphone driver" *IEEE J. Solid-State Circuits*, vol. 44, no. 3, pp. 916-927, March 2009.
- [15] R. G. Lyons, *Understanding Digital Signal Processing*, 3rd ed. Upper Saddle River, NJ: Prentice Hall, 2011.
- [16] J. Noh, D. Lee, J.-G. Jo, and C. Yoo, "A Class D amplifier with pulse code modulated (PCM) digital input for digital hearing aid," *IEEE J. Solid-State Circuits*, vol. 48, no. 2, pp. 465-472, Feb. 2013.
- [17] D. E. S. Piovani, M. C. Schneider, and C. G. Montoro, "Design of a low power CMOS Class D amplifier for hearing aids," in *Proc. Circuits and Systems for Medical and Environmental Workshop (CASME)*, Dec. 2010, pp. 1-4.
- [18] P. Pracný, *Design considerations for a digital audio Class D output stage with emphasis on hearing aid application*, PhD thesis, Department of Electrical Engineering, Technical University of Denmark, 2013. [Online]. Available: http://orbit.dtu.dk/fedora/objects/orbit:124638/datastreams/file_2df0e70f-eedc-4b27-95ab-87e8817c6f72/content, accessed August 2015.

- [19] P. Pracný and E. Bruun, "ΣΔ modulator system-level considerations for hearing-aid audio Class-D output stage application," in *Proc. 2012 8th Conf. on Ph.D. Research in Microelectronics and Electronics (PRIME)*, Jun. 2012, pp. 1-4.
- [20] P. Pracný, I. H. H. Jørgensen, and E. Bruun, "System-level optimization of a DAC for hearing-aid audio Class D output stage," in *Proc. 4th Doctoral Conference on Computing, Electrical and Industrial Systems (DoCEIS)*, Apr. 2013, pp. 647-654.
- [21] P. Pracný, I. H. H. Jørgensen, and E. Bruun, "System-level power optimization for a ΣΔ D/A converter for hearing-aid application," in *Proc. 2013 9th Conf. on Ph.D. Research in Microelectronics and Electronics (PRIME)*, Jun. 2013, pp. 1-4.
- [22] P. Pracný, I. H. H. Jørgensen, and E. Bruun, "Interpolation by a prime factor other than 2 in low-voltage low-power ΣΔ DAC," in *Proc. 31st NORCHIP Conf.*, Nov. 2013, pp. 1-6.
- [23] P. Pracný, I. H. H. Jørgensen, and E. Bruun, "Interpolating by a factor of 3 in low-voltage low-power ΣΔ DAC," *Analog Integrated Circuits and Signal Processing*, vol. 80, no. 3, pp. 375-385, Sep. 2014.
- [24] P. Pracný, P. M. Llimós, and E. Bruun, "Interpolation filter design for hearing-aid audio class-D output stage application," in *Proc. 19th IEEE Int. Conf. on Electronics, Circuits, and Systems (ICECS)*, Dec. 2012, pp. 364-367.
- [25] M. Renfors and T. Saramaki, "Recursive N-th band digital filters - Part I: Design and properties," *IEEE Trans. Circuits and Systems*, vol. 34, no. 1, pp. 24-39, Jan. 1987.
- [26] J. Roh, S. Byun, Y. Choi, H. Roh, Y. Kim, and J. Kwon, "A 0.9-V 60-μW 1-bit fourth-order Delta-Sigma modulator with 83-dB dynamic range," *IEEE J. Solid-State Circuits*, vol. 43, no. 2, pp. 361-370, Feb. 2008.
- [27] R. Schreier, G. C. Temes, *Understanding Delta-Sigma Data Converters*, Piscataway, NJ: Wiley-IEEE Press, 2004.
- [28] G. Stoyanov, Z. Nikolova, K. Ivanova, and V. Anzova, "Design and realization of efficient IIR digital filter structures based on sensitivity minimizations," in *Proc. 8th Int. Conf. on Telecommunications in Modern Satellite, Cable and Broadcasting Services*, Sep. 2007, pp. 299-308.
- [29] R. A. Valenzuela and A. G. Constantinides, "Digital signal processing schemes for efficient interpolation and decimation," *IEE Proceedings G*, vol. 130, no. 6, pp. 225-235, Dec. 1983.
- [30] K. Wong, K. Lei, S. U, and R. P. Martins, "A 1-V 90dB DR audio stereo DAC with embedding eadphone driver," in *Proc. IEEE Asia Pacific Conference Circuits and Systems (APCCAS)*, Nov. 2008, pp. 1160-1163.
- [31] X. Yao, L. Liu, D. Li, L. Chen, and Z. Wang, "A 90dB DR audio delta-sigma DAC with headphone driver for hearing aid," in *Proc. 3rd International Congress on Image and Signal Processing (CISP)*, Oct. 2010, pp. 2890-2893.
- [32] Z. Ye and M. P. Kennedy, "Reduced complexity MASH delta-sigma modulator," *IEEE Trans. Circuits and Systems II: Express Briefs*, vol. 54, no. 8, pp 725-729, Aug. 2007.
- [33] Z. Ye and M. P. Kennedy, "Hardware reduction in digital Delta-Sigma modulators via error masking - part I: MASH DDSM," *IEEE Trans. Circuits and Systems I: Regular Papers*, vol. 56, no. 4, pp. 714-726, Apr. 2009.

- [34] Z. Ye and M. P. Kennedy, "Hardware reduction in digital Delta-Sigma modulators via error masking - part II: SQ-DDSM," *IEEE Trans. Circuits and Systems II: Regular Papers*, vol. 56, no. 2, pp. 112-116, Feb. 2009.
- [35] J. Yli-Kaakinen and T. Saramaki, "A systematic algorithm for designing multiplierless computationally efficient recursive decimators and interpolators," in *Int. Symp. on Image and Signal Processing and Analysis (ISPA)*, Sep. 2005, pp. 167-172.
- [36] J. Yli-Kaakinen and T. Saramaki, "A systematic algorithm for the design of lattice wave digital filters with short-coefficient wordlength," *IEEE Trans. Circuits and Systems I: Regular Papers*, vol. 54, no. 8, pp. 1838-1851, Aug. 2007.

Fig. 1. Block schematic of a back end used in hearing aid audio application.

Fig. 2. Simplified schematic of N-th order CRFB $\Sigma\Delta$ modulator with Q bit quantizer (in the case of this schematic, N is an odd number. In general, N can be an odd or an even number. In the case N is an even number, the 'g' coefficient would be wrapped around the 1st and 2nd stage of the modulator).

Fig. 3. Multi-stage IF with 4 stages performing sample-rate increase by 64.

Fig. 4. Peak SQNR of the 3 bit $\Sigma\Delta$ modulator output signal as a function of OSR for modulator orders 1 to 8.

Fig. 5. Trading lower OSR for higher order of the $\Sigma\Delta$ modulator. The $\Sigma\Delta$ modulator gives the larger contribution to the combined FOM (blue plot), especially at high $\Sigma\Delta$ modulator orders. The optimum when trading lower OSR for higher order of the $\Sigma\Delta$ modulator is order = 6 and OSR = 32.

Fig. 6. Trading lower OSR for higher number of bits in the $\Sigma\Delta$ modulator quantizer and higher maximum NTF gain.

Table 1. State-of-the-art hearing-aid audio DAC designs and DACs intended for mobile phones using Class D power amplifier.

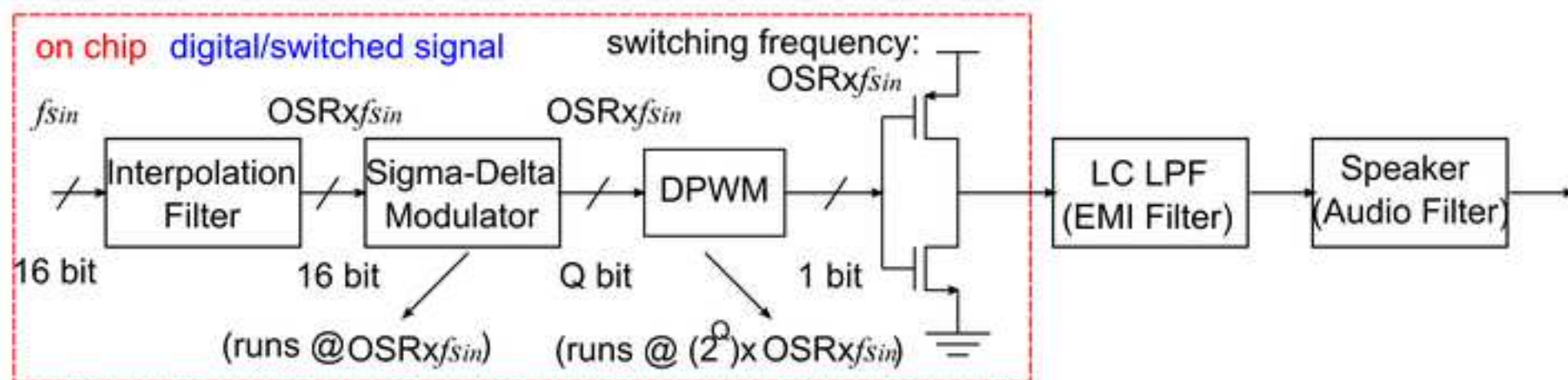
Table 2. IF FOM comparison

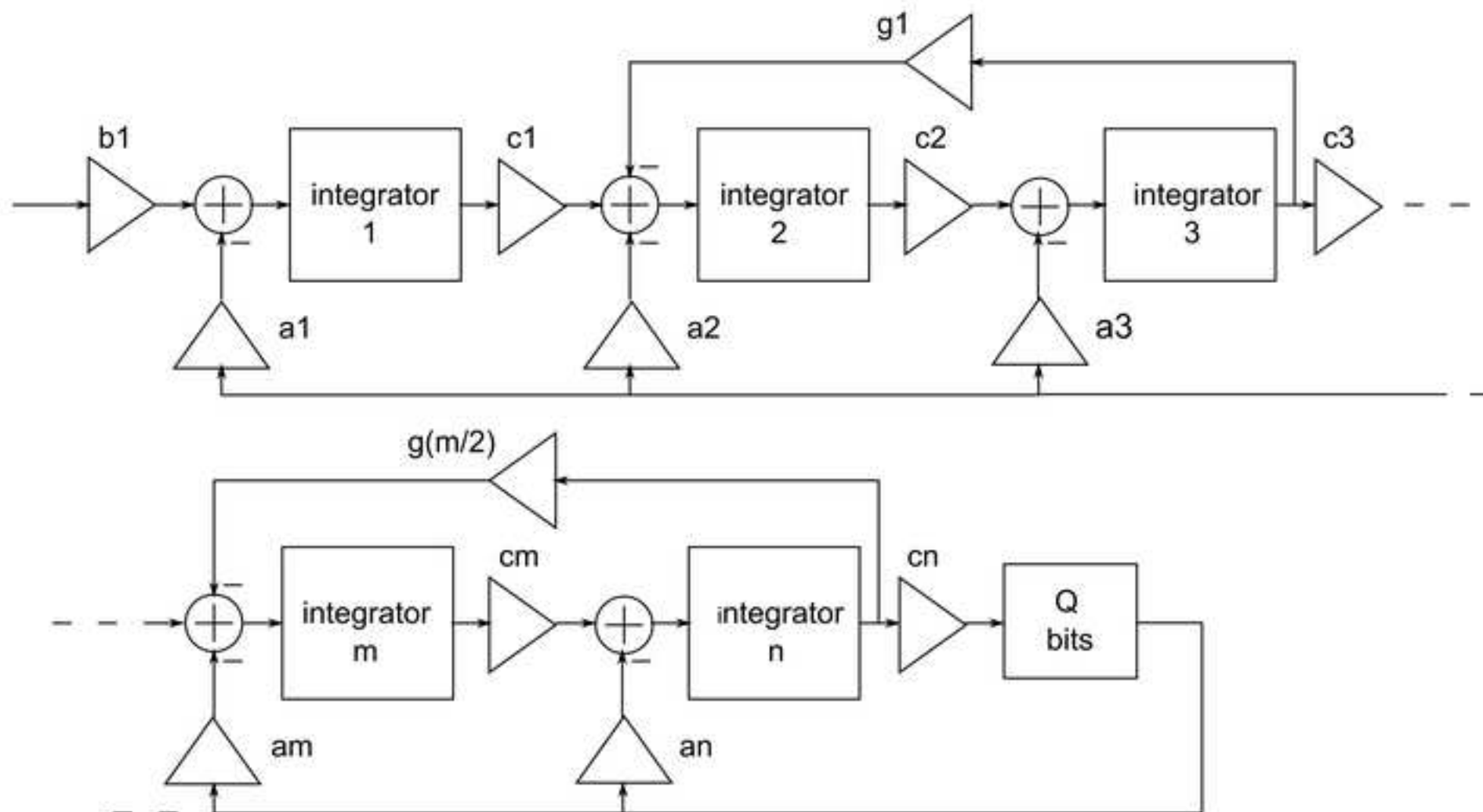
Table 3. Back end design comparison including all the blocks of the system, with completed design in Matlab.

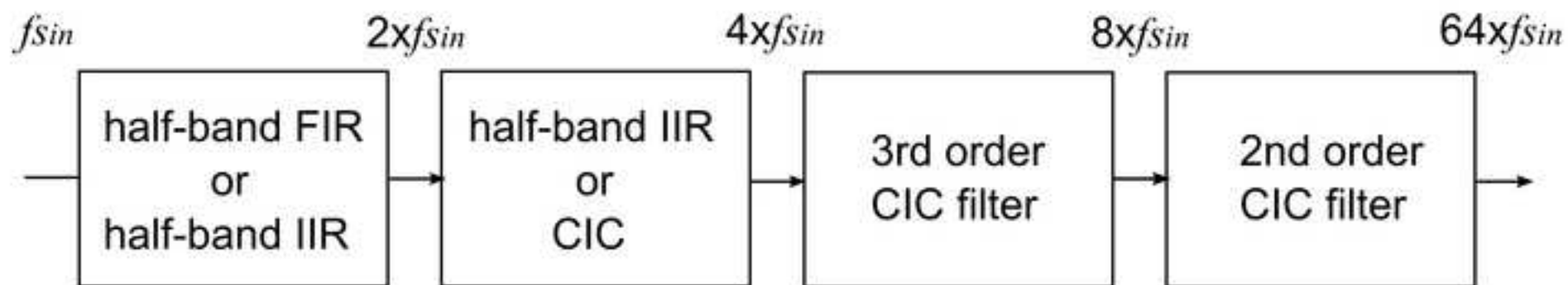
Table 4. IFs using a stage performing interpolation by a factor of 3.

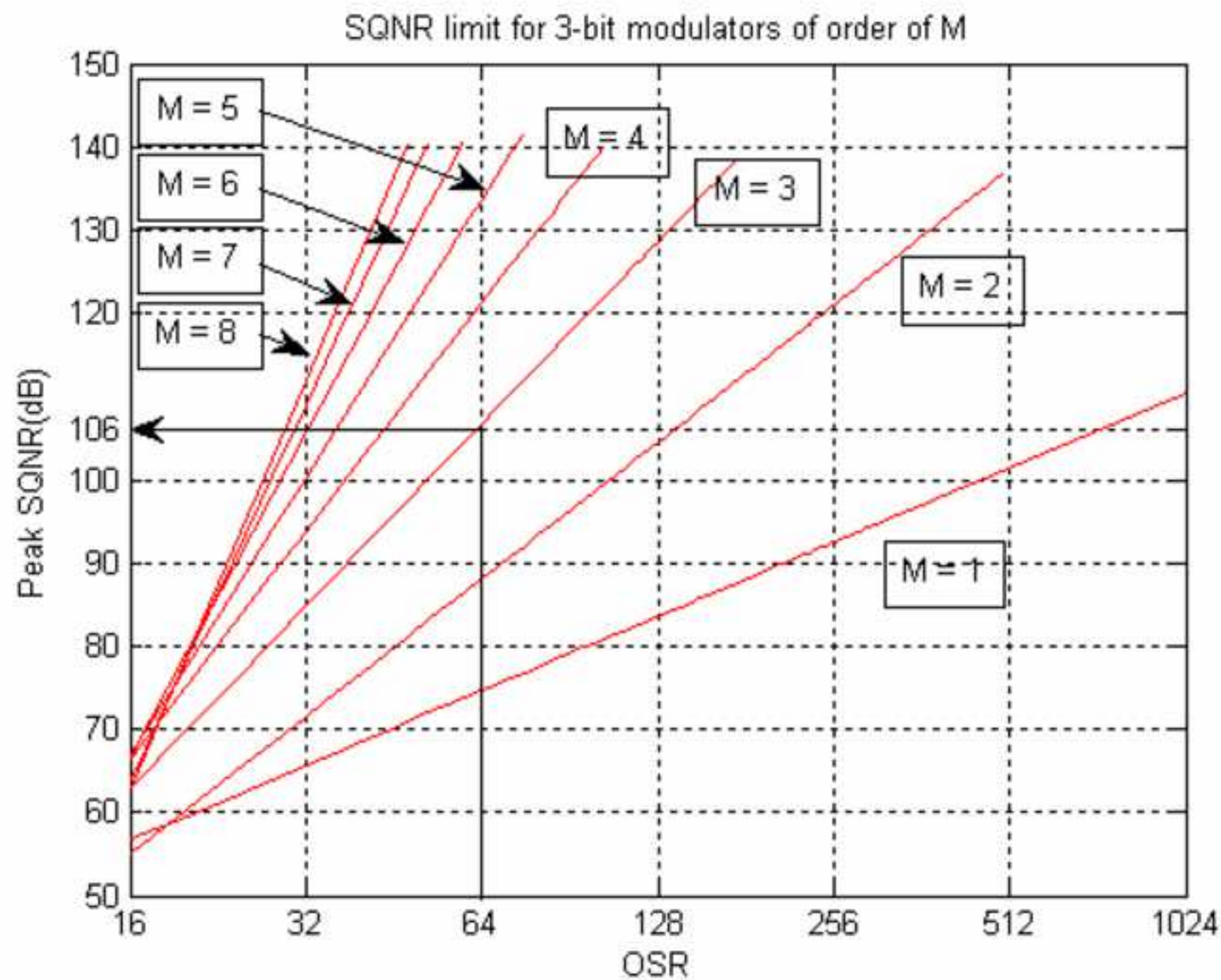
Table 5. Maximum clock defined by the DPWM block

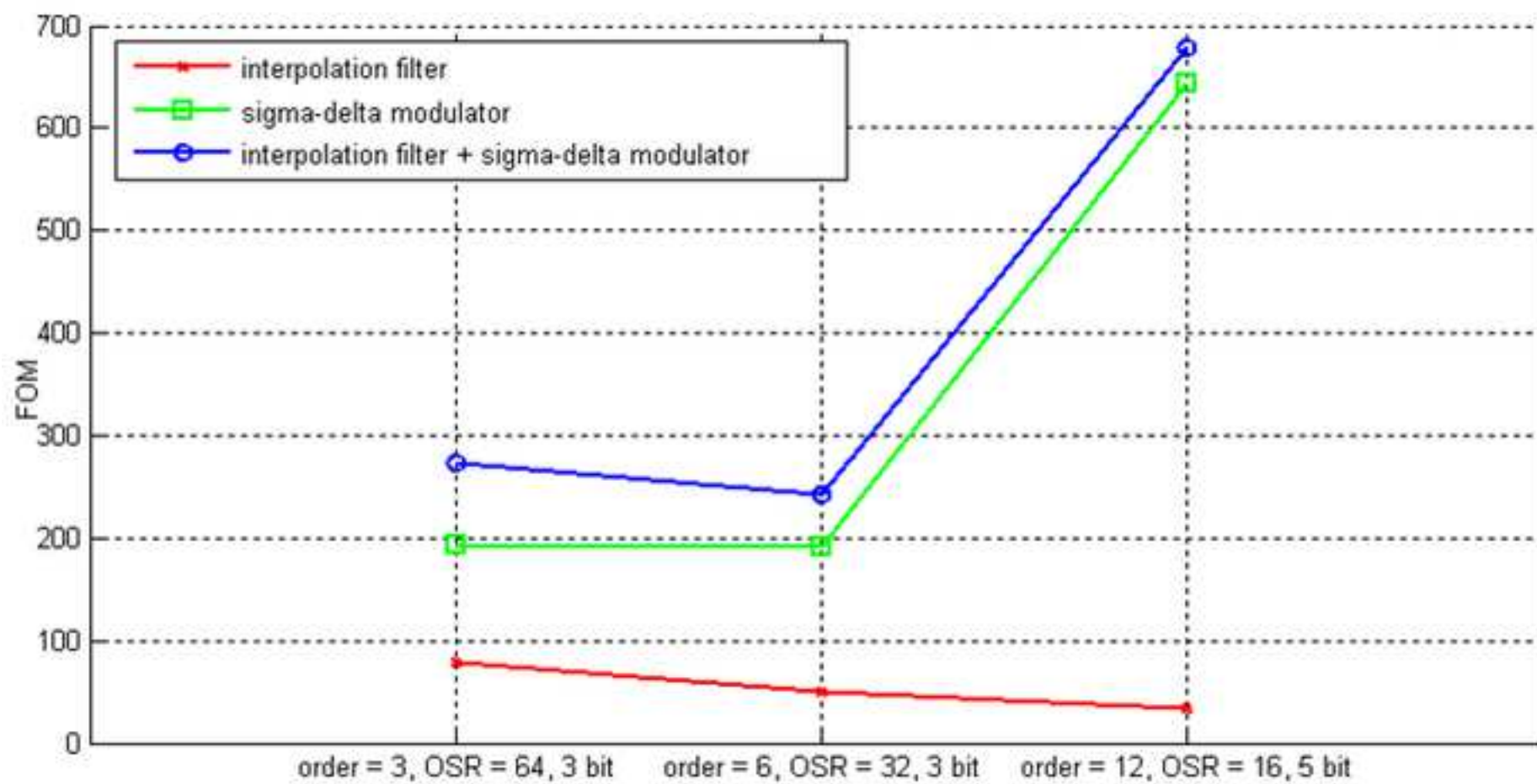
Table 6. Comparison of state-of-the-art hearing aid back end designs.











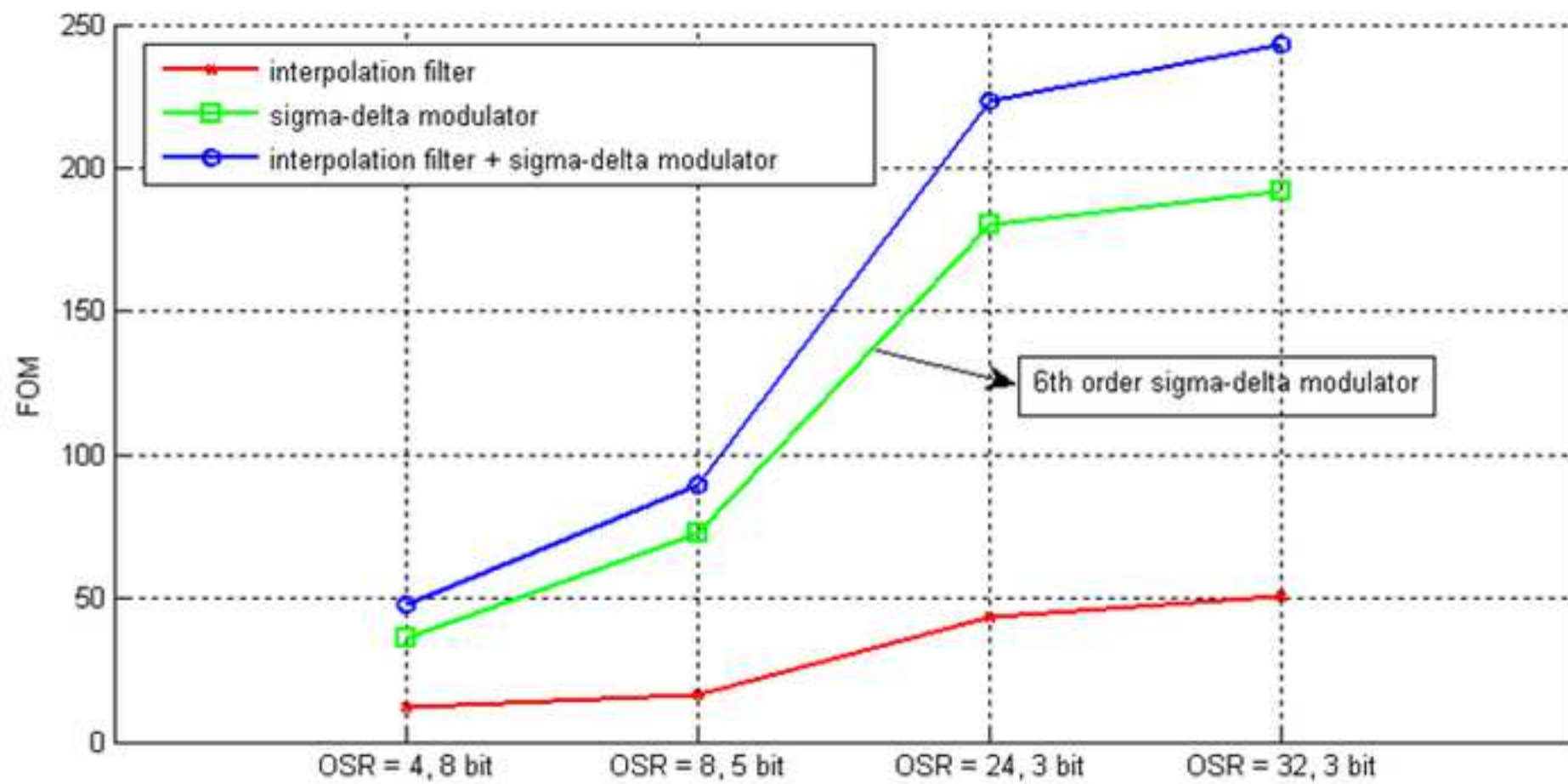


Table 1.

[Ref.] 'year	Application	Vdd [V]	Input signal		Modulator				System output	
			Bits	fs_{in} [kHz]	OSR	Order	Bits	SNDR [dB]	PA	SNDR [dB]
[13] '07	Hearing aid	0.9	16	32	64	4	1	N/A	onchip	79
[8] '09	Mobile phone	1.2	16	44.1	64	3	3	106.7	offchip	90
[5] '09	Mobile phone	3.6	24	48	48	3	7	122	onchip	N/A
[31] '10	Hearing aid	1.8	16	22.05	64	4	1	105.7	onchip	85.6

Table 2.

$\Sigma\Delta$ Modulator	Order = 3, OSR = 64, 3bit (Initial design)				Order = 6, OSR = 32, 3 bit (Section 3A)				Order = 12, OSR = 16, 5 bit (Section 3B)			
	Filter	OSRin	OSR	FOM	Filter	OSRin	OSR	FOM	Filter	OSRin	OSR	FOM
IF stage 1	IIR	fs_{in}	2	9.5	IIR	fs_{in}	2	9.5	IIR	fs_{in}	2	9.5
IF stage 2	IIR	$2 \times fs_{in}$	2	7.2	IIR	$2 \times fs_{in}$	2	7.2	IIR	$2 \times fs_{in}$	2	7.2
IF stage 3	CIC	$4 \times fs_{in}$	2	8.6	CIC	$4 \times fs_{in}$	2	8.6	CIC	$4 \times fs_{in}$	2	8.6
IF stage 4	CIC	$8 \times fs_{in}$	8	61.5	CIC	$8 \times fs_{in}$	4	25.5	CIC	$8 \times fs_{in}$	2	9
IF total			64	86.8			32	51			16	34.3

$\Sigma\Delta$ Modulator	Order = 6, OSR = 24, 3bit (Section 3C)				Order = 6, OSR = 8, 5 bit (Section 3D)				Order = 6, OSR = 4, 8 bit (Section 3E)			
	Filter	OSRin	OSR	FOM	Filter	OSRin	OSR	FOM	Filter	OSRin	OSR	FOM
IF stage 1	IIR	fs_{in}	3	19.9	IIR	fs_{in}	2	9.5	IIR	fs_{in}	2	9.5
IF stage 2	CIC	$3 \times fs_{in}$	2	3.4	CIC	$2 \times fs_{in}$	2	2.3	CIC	$2 \times fs_{in}$	2	2.3
IF stage 3	CIC	$6 \times fs_{in}$	2	6.7	CIC	$4 \times fs_{in}$	2	4.5	-	-	-	-
IF stage 4	CIC	$12 \times fs_{in}$	2	13.5	-	-	-	-	-	-	-	-
IF total			24	43.5			8	16.3			4	11.8

Table 3.

Design		Initial design	Section 3.1	Section 3.2	Section 3.3	Section 3.4	Section 3.5
$\Sigma\Delta$ Modulator	Order	3	6	12	6	6	6
	OSR	64	32	16	24	8	4
	Quantizer bits	3	3	5	3	5	8
	Max. NTF gain	1.5	1.5	1.5	1.7	5	20
	MSA	-0.5 dBFS	-0.9 dBFS	-1 dBFS	-1.2 dBFS	-1.2 dBFS	-0.1 dBFS
	SNDR @ MSA	98.2 dB	96 dB	97.7 dB	99.3 dB	98.7 dB	98.4 dB
	STF DC gain	-0.16 dB	-0.81 dB	0.61 dB	-0.84 dB	-0.65 dB	0 dB
	Feedforward coeffs.	no	no	yes	no	no	no
	$\Sigma\Delta$ FOM	193	192	644	180	73	36.4
Interpolation filter (IF)	SNDR @ MSA	97.7 dB	101.2 dB	101.2 dB	97.4 dB	98.7 dB	98.2 dB
	pass-band ripple	0.5 dB	0.5 dB	0.5 dB	0.6 dB	0.6 dB	0.6 dB
	1st stage FOM	9.5	9.5	9.5	19.9	9.5	9.5
	2nd stage FOM	7.2	7.2	7.2	3.4	2.3	2.3
	3rd stage FOM	8.6	8.6	8.6	6.7	4.5	-
	4th stage FOM	61.5	25.5	8.3	13.5	-	-
	IF total FOM	86.8	51	33.6	43.5	16.3	11.8
	Total FOM (IF + $\Sigma\Delta$)	273	243	677.6	223.5	89.3	48.2
DPWM clock freq.		11.3 MHz	5.6 MHz	11.3 MHz	4.2 MHz	5.6 MHz	22.6 MHz
PA switching freq.		1.4 MHz	706 kHz	353 kHz	529 kHz	176 kHz	88.2 kHz

Table 4.

$\Sigma\Delta$ Modulator	order = 6, OSR = 24, 3 bit (Section 3.3)				order = 6, OSR = 24, 3 bit (Section 3.3)				order = 6, OSR = 24, 3 bit (Section 3.3)			
	(a)				(b)				(c)			
	Filter	OSRin	OSR	FOM	Filter	OSRin	OSR	FOM	Filter	OSRin	OSR	FOM
IF stage 1	IIR	fs_{in}	2	9.5	IIR	fs_{in}	3	19.9	IIR	fs_{in}	3	19.9
IF stage 2	IIR	$2 \times fs_{in}$	2	7.2	IIR	$3 \times fs_{in}$	2	10.8	CIC	$3 \times fs_{in}$	2	3.4
IF stage 3	CIC	$4 \times fs_{in}$	2	4.5	CIC	$6 \times fs_{in}$	2	6.7	CIC	$6 \times fs_{in}$	2	6.7
IF stage 4	CIC	$8 \times fs_{in}$	3	53	CIC	$12 \times fs_{in}$	2	13.5	CIC	$12 \times fs_{in}$	2	13.5
IF total			24	74			24	51			24	43.5

Table 5.

Design	$\Sigma\Delta$ Modulator		DPWM clock ($\text{OSR} \times 2^Q \times 22.05 \text{ kHz}$)
	OSR	Q bits	
Section 3.1	32	3	5.6 MHz
Section 3.4	8	5	5.6 MHz

Table 6.

[Ref] 'year	Analog / Digital	Modulator	BW/ $f_{s_{in}}$ [kHz]	$\Sigma\Delta$ modulator			System clock	Class D freq.	FB
				order	OSR	bits			
[9] '05	Digital	PWM	4/48	-	-	-	100 MHz	96 kHz	no
[12] '06	Analog	PWM	-	-	-	-	-	75 kHz	no
[13] '07	Digital	$\Sigma\Delta$	4/32	4	16	1	2 MHz	2 MHz	no
[1] '09	Digital	$\Sigma\Delta$ +PWM	8/48	3	2	8	24.6 MHz	96 kHz	no
[17] '10	Analog	PWM	-	-	-	-	-	200 kHz	no
[31] '10	Digital	$\Sigma\Delta$	10/22.05	4	64	1	1.28 MHz	1.28 MHz	no
[16] '13	Analog +Digital	$\Sigma\Delta$	-	6	-	3 level	5 MHz	5 MHz	yes
this work	Digital	$\Sigma\Delta$ +PWM	10/22.05	6	4	8	22.6 MHz	88.2 kHz	no