

Preprints are preliminary reports that have not undergone peer review. They should not be considered conclusive, used to inform clinical practice, or referenced by the media as validated information.

Temporal word embedding with predictive capability

Ahnaf Farhan (▲ afarhan@miners.utep.edu) The University of Texas at El Paso
Roberto Camacho Barranco The University of Texas at El Paso
Monika Akbar The University of Texas at El Paso
M. Shahriar Hossain The University of Texas at El Paso

Research Article

Keywords: word embedding, dynamic embeddings, temporal embeddings, neural network

Posted Date: December 3rd, 2022

DOI: https://doi.org/10.21203/rs.3.rs-2322214/v1

License: (c) This work is licensed under a Creative Commons Attribution 4.0 International License. Read Full License

Additional Declarations: No competing interests reported.

Version of Record: A version of this preprint was published at Knowledge and Information Systems on July 13th, 2023. See the published version at https://doi.org/10.1007/s10115-023-01920-8.

1	Temporal word embedding with predictive		
2	capability		
3	Ahnaf Farhan ^{1*†} , Roberto Camacho Barranco ^{1†} , Monika Akbar ¹ and M. Shahriar Hossain ^{1*}		
 ^{1*}Department of Computer Science, The University of Texas Paso, 500 W University Ave, El Paso, 79968, Texas, US 			
7 8	*Corresponding author(s). E-mail(s): afarhan@miners.utep.edu; mhossain@utep.edu;		
9 10	Contributing authors: rcamachobarranco@miners.utep.edu; makbar@utep.edu;		
11	[†] These authors contributed equally to this work.		

Abstract

12

Semantics in natural language processing is largely dependent on contex-13 tual relationships between words and entities in a document collection. 14 The context of a word may evolve. For example, the word "apple" 15 currently has two contexts – a fruit and a technology company. The 16 changes in the context of words or entities in text data such as sci-17 entific publications, and news articles can help us understand the 18 evolution of innovation or events of interest. In this work, we present 19 a new diffusion-based temporal word embedding model that can cap-20 ture short and long-term changes in the semantics of entities in different 21 domains. Our model captures how the context of each entity shifts 22 over time. Existing temporal word embeddings capture semantic evo-23 lution at a discrete/granular level, aiming to study how a language 24 developed over a long period. Unlike existing temporal embedding meth-25 ods, our approach provides temporally smooth embeddings, facilitating 26 prediction and trend analysis better than those of existing models. Exten-27 sive evaluations demonstrate that our proposed temporal embedding 28 model performs better in sense-making and predicting relationships 29 between entities in the future compared to other existing models. 30

Keywords: word embedding, dynamic embeddings, temporal embeddings,
 neural network

³³ 1 Introduction

Text data available over the internet have grown exponentially in the past 34 decade. There are ample techniques to transform an unstructured text collection 35 into a structured representation allowing us to apply conventional data mining 36 and machine learning algorithms for analytical purposes. An issue with the 37 conventional approach to representing unstructured data is that the contextual 39 changes in the meanings of words as the language evolves are not considered in 39 the models. That is, conventional representation models do not consider text 40 publications as evolving streams of data. 41

The contextual evolution of a word plays a vital role in its contemporary 42 semantics. For example, the context of the word *Cloud* changed over time in 43 the last two decades. The word, Cloud, in news articles, reflected its connection 44 with weather-related terms in the beginning. From 2008 to 2012, the word 45 *cloud* started to reflect the context of web-based storage, such as Dropbox and 46 Google drive. Slowly, from 2016 the word *cloud* started to reflect cloud-based 47 computing services, such as Amazon Web Service (AWS), Microsoft Azure, and 48 Google Cloud Platform, as the services became more affordable and popular. 49 Figure 1 demonstrates that the nearest neighbors of the word *cloud* changed 50

⁵¹ over the years for a news dataset. Taking all these changes in the neighborhood of *cloud*, how can we predict its neighborhood in the coming years?

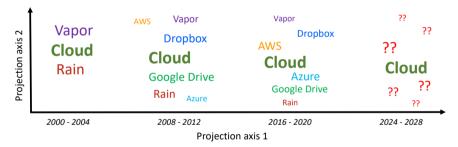


Fig. 1 The nearest neighbors of the word cloud over time.

52

To serve a larger set of analytic needs – including the prediction of a mathematical space that words may represent in the future – modern unstructured data representation techniques are slowly drifting toward the analysis of temporal aspects of text [1–3]. Nevertheless, the ability to represent unstructured text with a temporal context is still in its infancy. In this paper, we present a temporal embedding model for representing text data in a structured way based on the temporal context.

Our observation from timestamped text collections indicates that new concepts and events do not spike on one day and disappear on the next, rather concepts and events evolve over time. For example, the concept of COVID started to rise at a fast rate in February and March of 2020, but the topic

started several months before that. Similarly, the topic of Russia's Ukraine 64 invasion did not occur in one day. In unstructured text representations, discrete 65 timestamps do not help much to reflect the rise and fall of entities well. The 66 appearance of a new entity in one timestamp needs to be diffused earlier than 67 when it appeared first, to reflect a smooth transition to capture evolution. 68 However, not all words and entities evolve, and there can be some words that 69 appear suddenly and then disappear quickly. The scope of this paper is limited 70 to words and entities that evolve over time, with time units of around months 71 or years. 72

To provide a smooth transition for evolving words in their representations, in one of our previous research efforts, we presented the issue of capturing the evolution of concepts using a diffusion-based time-reflective representation [4]. *Diffusion* of a word, in [4], was reflected by smoothly incorporating its effect across timestamps, before and after it appears. This time-reflective representation enabled the tracking of the meaning of every word in terms of their neighborhood and captured changes in context over time.

One of the challenges of [4] was that each word vector had a length equal 80 to the number of documents in the corpus (See Section 4.1.1), which is not 81 practical for analyzing a corpus containing thousands of documents. Moreover, 82 since the vectors generated for the words were directly dependent on the 83 documents where those words appeared, vectors for the same words in the 84 future cannot be extrapolated (because the future documents are yet to be seen 85 and not features of this representation). That means the model did not generate 86 embeddings with prediction capability. To address these challenges, in the 87 current paper, we construct a contextual low-dimensional temporal 88 embedding space that mimics this high-dimensional representation 89 while maintaining the essential diffusion information contained in 90 the vectors. We introduce a neural-network-based framework that generates 91 low dimensional temporal word embeddings while optimizing for multiple 92 key objectives. 93

Word embeddings are low-dimensional vector space models obtained by 94 training a neural network using contextual information from a large text corpus. 95 There are several variants of word embeddings with different features, such 96 as word2vec [5, 6], GloVe [7], and BERT [8]. These embedding techniques do 97 not explicitly address dynamic changes in context. The few existing efforts 98 [3, 9–11] to generate dynamic low-dimensional language representations fail to 99 integrate the concept of temporal diffusion into language models effectively. 100 Moreover, these existing models cannot simultaneously capture both the short-101 term and long-term drifts in the meaning of words. As a result, sharply trending 102 concepts, such as COVID-19 (coronavirus disease 2019), cannot be modeled in 103 the embedding space when long-term drifts are considered. On the other hand, 104 long-range effects – such as the change in the meaning of the word cloud – are 105 not captured when these algorithms take only short-term drifts into account. 106 Moreover, the existing models only have limited capability to generate dynamic 107 embeddings that can be used for predicting future embeddings. 108

The diffusion-based temporal word embedding model that we propose in 100 this paper is able to capture both short-term and long-term in the corpus. It 110 incorporates diffusion into the modeling by integrating the time dimension 111 smoothly into the model's objective function. The temporal embeddings are 112 generated for all words in all timestamps in a connected space, and hence the 113 vectors can be used to predict embeddings of words in the future, unlike other 114 existing temporal or dynamic embedding techniques. In this paper, we use 115 the phrase temporal word embeddings and dynamic word embeddings 116 interchangeably. 117

The experimental results in Section 5 show that the proposed method performs significantly better than the state-of-the-art temporal embedding models [3, 11, 12] in capturing both short-term and long-term changes in word semantics. Additionally, our model provides embeddings to facilitate more meaningful predictions for the future context of a word.

¹²³ The contributions of this paper are summarized as follows:

- This paper describes a neural network model that generates low-dimensional dynamic embeddings from high-dimensional time-reflective feature vectors without degrading the quality of word vectors.
- Our proposed model creates a homogeneous embedding space for all timestamps in the data so that each word's temporal embedding can be seen as a multi-variate signal, which conventional signal prediction algorithms can leverage to predict embeddings in a future timestamp.
- We introduced a diffusion mechanism in the objective function in order to smooth the embeddings for better prediction capability.
- We compare the new model with regular temporal co-occurrence-based, dynamic-embedding-based, and time-masking transformer-based models on the task of semantic change detection.
- In this paper, we introduce the application of predicting a future embedding
 space for an existing timestamped document collection.

¹³⁸ 2 Related Work

This section provides a detailed review of the literature on the various aspects
of our research work in order to put our contributions in perspective. The
related works presented here are divided into two subsections, describing two
different tasks: the generation of temporal embeddings and the prediction of a
future embedding space.

¹⁴⁴ 2.1 Generation of temporal embeddings

Semantic evolution: Meanings of words in a language change over time depending on their use [13, 14]. Temporal syntactic and semantic shifts are called *diachronic changes* [1]. Several probabilistic approaches tackle the problem of modeling the temporal evolution of a vocabulary by converting a set of timestamped documents into a latent variable model [15–18]. Other approaches ¹⁵⁰ model diachronic changes using Parts of Speech features [19] or using graphs ¹⁵¹ where the edges between nodes (that represent words) are stronger based ¹⁵² on context information [20]. However, tracking semantic evolution is not ¹⁵³ possible using these techniques because they do not generate language models.

Language Models: The state-of-the-art technique for language modeling 154 is word2vec, introduced by Mikolov et al. [5, 6]. This method generates a 155 static language model where every word is represented as a vector (also called 156 embedding) by training a neural network to mimic the contextual patterns 157 observed in a text corpus. There are several variants of this method which 158 include probabilistic approaches [21] as well as matrix-factorization-based 159 techniques such as GloVe [7]. A major challenge with *static* representations is 160 that they do not incorporate any temporal information that can be used for 161 tracking semantic evolution. Our work focuses on incorporating the temporal 162 dimension of text data into text embedding models so that evolution of a vector 163 space over time can be studied. 164

Static to dynamic embeddings: A proposed solution to tracking seman-165 tic evolution is to obtain a *static* representation for each timestamp in a corpus 166 and then artificially couple these embeddings over time using regression or sim-167 ilar methods [1, 3, 12, 22]. However, this approach has several drawbacks. First, 168 it requires having a significant number of occurrences for all words at all times. 169 which is usually not the case since words can gain popularity or appear at 170 different times. Second, the artificial coupling of embeddings across timestamps 171 can introduce artifacts in the model that may lead to wrong conclusions. A 172 potential solution to the sparsity problem is introduced by Camacho et al. [4], 173 which leverages diffusion theory [23] to generate a robust temporal representa-174 tion. The technique uses a temporal tf-idf representation in which the model 175 changes size with the number of documents and as a result, is not extensible. 176

Joint training of temporal embeddings: The drawbacks of using *static* 177 word embedding models to generate temporal representations have led to the 178 development of new techniques that can train the embeddings for different 179 timestamps jointly. The models use filters or regularization terms to connect the 180 embeddings over time. Yao et al. [10] propose to generate a co-occurrence-based 181 matrix and factorize it to generate temporal embeddings. The embeddings 182 over timestamps are aligned using a regularization term. Rudolph et al. [11] 183 apply Kalman filtering to exponential family embeddings to generate temporal 184 representations. Bamler et al. [9] use similar filtering but apply it to embeddings 185 using a probabilistic variant of *word2vec*. According to Bamler et al. [9], using a 186 probabilistic method makes the model less sensitive to noise. All these methods 187 focus primarily on capturing long-term semantic shifts, while our goal is to be 188 able to capture both long and short-term shifts. 189

¹⁹⁰ 2.2 Prediction of a future embedding space

Prediction using linear transformation: Several researchers have focused
 on studying multi-dimensional time-series prediction [24–27] using methods such
 as linear regression and accounting for temporal effects such as seasonality [25].

[28] discussed linear, homogenous, and heterogenous transformation of 194 embeddings with timestamps for estimating embeddings for future timestamps. 195 Linear transformation learns a mapping between embeddings of two consecutive 196 timestamps. Homogenous transformation learns a mapping between stacked 197 embeddings of timestamp 1 to (T-1) and stacked embeddings of timestamp 2 198 to (T). In heterogeneous transformation, instead of stacking the embeddings 199 from all the timestamps, it learns weight matrices for mapping embeddings 200 from all pairs of consecutive timestamps and uses various smoothing functions 201 to combine the weight matrices. However, the embedding vectors for each 202 timestamp are learned separately, which means the embedding vectors at 203 each timestamp are static. Some other studies [29], [30] also leverage linear 204 transformations of embedding vectors in order to predict embeddings in the 205 future timestamps [29] first train a dynamic embedding model then create a 206 time-context vector to predict estimated embeddings for the next timestamp 207 through the linear transformation of embeddings of the present timestamp. 208

However, these models are not well-suited for the prediction of highdimensional non-linear phenomena, which is the case of semantic evolution.

Prediction using non-linear modeling: Our generated temporal embedding is a nonlinear sequence of signals. Therefore, our prediction of a future
embedding space from existing time series data requires sequence modeling
that can handle nonlinearity.

To model non-linear phenomena, several neural-network-based sequence 215 modeling techniques have been introduced recently [31-34]. In this paper, we 216 leverage state-of-the-art techniques in terms of sequence modeling, such as (1)217 the Long Short Term Memory (LSTM) [31] and (2) Gated Recurrent Units 218 (GRU) [32] recurrent neural networks (RNNs). We also explore the effect of 219 adding an attention mechanism [33] to both LSTM- and GRU-based RNNs, 220 which allows the network to focus on the most important elements of the 221 sequence. Finally, we evaluate the non-recurrent attention-based Transformer 222 model [34] which, in contrast to RNNs, can be trained in parallel. 223

²²⁴ 3 Problem Description

In this paper, we focus on timestamped text corpora, such as collections of scientific publications, or news articles, that have publication dates. Let $\mathcal{D} = \{d_1, d_2, \ldots, d_{|\mathcal{D}|}\}$ be a corpus of $|\mathcal{D}|$ documents and $\mathcal{W} = \{w_1, w_2, \ldots, w_{|\mathcal{W}|}\}$ be the set of $|\mathcal{W}|$ entities (names, places, scientific terms) extracted from the text corpus \mathcal{D} . We consider each of the entities a word.

Each document d contains words from the vocabulary $(\mathcal{W}_d \subset \mathcal{W})$ in the same order as they appear in the original document of d. Every document $d \in \mathcal{D}$ is labeled with a timestamp $t_d \in \mathcal{T}$, where \mathcal{T} is the ordered set of timestamps. The goal of this paper is two-fold.

• Task 1: Constructing a low-dimensional temporal embedding space, with predictive capability: The first task is to obtain a temporal word embedding model \mathcal{U} from corpus \mathcal{D} . For every timestamp $t \in \mathcal{T}$, we seek to obtain a vector representation u_{it} for every word $w_i \in \mathcal{W}$. The word embeddings \mathcal{U} are represented as a 3-dimensional matrix of size $|\mathcal{W}| \times |\mathcal{T}| \times |u|$ where |u| is a user-given constant that indicates the size of each vector. We use the shorthand U_i to describe the 2-dimensional matrix of size $|\mathcal{T}| \times |u|$ that represents word $w_i \in \mathcal{W}$ over all the timestamps.

• Task 2: Predicting a future embedding space: The second task is associated with predicting a future embedding space. We aim to train a model for which $\mathcal{P}(\mathbb{U}^{t_a:t_b}) \approx \mathbb{U}^{t_{b+1}}$, i.e., a model that takes as input the temporal embedding vectors for every word between t_a and t_b timestamps and predicts as output embedding vectors for every word in the vocabulary for timestamp t_{b+1} . The output of \mathcal{P} can be used to forecast the future contexts of the words in the vocabulary.

249 4 Methodology

This section is divided into two subsections describing the two tasks: temporal embedding generation and prediction of a future embedding space, as outlined in the problem description.

²⁵³ 4.1 Construction of a temporal embedding space

To construct a temporal embedding space that can be used for the prediction of 254 future embedding space, we design an objective function that satisfies several 255 crucial aspects in terms of similarity between words, weights reflecting relevance 256 between contextual words, temporal diffusion of amplitudes of words, and 257 connecting embedding spaces of different timestamps. We use a shallow neural 258 network to accommodate the embedding generation with a complex objective 259 function that models a temporally-driven training dataset. The training data 260 generation and each component of the objective function are explained below. 261

4.1.1 Training data for generating low-dimensional temporal embeddings

To construct the training dataset for generating low-dimensional temporal embeddings, we use the diffusion-based time reflecting representation from our previous research efforts [4]. In this subsection, we first summarize the steps of generating a diffusion-based time-reflecting representation, constructed over a high-dimensional space and not having predictive capacity. Afterward, we discuss the process of creating training data.

As part of our previous research [4], we compute the frequency of words appearing in the documents over time to track the semantic evolution of the words. In our earlier research, we observed that the distribution of the frequency of a word over time was severely irregular, in particular for words or noun phrases that suddenly appeared at a particular timestamp or that are used sporadically. A frequency distribution that is inconsistent or uneven with time does not help capture trends because an evolving trend is considered a slower process compared to a sporadic one. Our idea of evolving trends is based on a social science concept known as the diffusion theory [23].

Based on *diffusion theory* [23], which refers to the change of the distributional 279 patterns of a phenomenon over time, the meaning of a word and, consequently, 280 its vector representation, diffuses over time. In [4], to smooth the word vectors 281 over time based on the diffusion theory, we assumed that every document is 282 present in every timestamp but with a higher probability for the timestamps 283 closer to when the document was initially published. We used a Gaussian filter 284 to diffuse the contribution of the document smoothly before and after the 285 publication date of the document. The Gaussian filter used a sliding window, 286 going from the first to the last timestamp. The contribution of a document d287 increased the closer its timestamp t_d was to the current timestamp t. The tf-idf 288 weight of a word was modified at each timestamp with Equation (1) to generate 289 a time-reflective representation, which is referred to as temporal tf-idf [4]. 290

$$\hat{w}(w,d,t_d,t,\varsigma) = \left(\frac{1}{\sqrt{2\pi\varsigma^2}}e^{-\frac{(t_d-t)^2}{2\varsigma^2}}\right) \cdot \left(\frac{\left(1 + \log(f_{w,d})(\log\frac{|\mathcal{D}|}{\lambda_w})\right)}{\sum_{w'\in\mathcal{W}_d}\left((1 + \log(f_{w',d})(\log\frac{|\mathcal{D}|}{\lambda_{w'}})\right)^2\right)}\right)$$
(1)

Here, \hat{w} is the weighted tf-idf value at timestamp t for the word $w \in \mathcal{W}$ in document $d \in \mathcal{D}$, which was published at timestamp t_d . The term $f_{w,d}$ represents the term frequency of word w in document d, λ_w is the number of documents that contain word w, and \mathcal{W}_d is the set of words that appear in document d. The standard deviation of the Gaussian distribution function is represented by ς , and is set by the user.

In order to construct a training dataset for the current paper, using the 297 temporal tf-idf representation of Eq. 1, we compute the cosine dissimilarity 298 (1.0-cosine similarity) between every pair of words and store these as a dis-299 tance/dissimilarity matrix Δ , where each element can be addressed as $\delta_{iit} \in \Delta$. 300 This distance/dissimilarity matrix Δ becomes the training data for the expected 301 distance/dissimilarity between a particular pair of words $(w_i, w_j) \in \mathcal{W}$ at time 302 $t \in \mathcal{T}$. We use the notation δ_{ij} to represent a vector of size $|\mathcal{T}|$ with the tempo-303 ral tf-idf-based cosine dissimilarity between $(w_i, w_j) \in \mathcal{W}$ for all the timestamps. 304 The cosine dissimilarities are later used in the output layer of our proposed 305 neural network. 306

4.1.2 Simplistic embedding model optimizing for similarity only

One of our objectives is to obtain a low-dimensional word embedding model \mathcal{U} such that computing the cosine dissimilarity between the word vectors results in a distance matrix that closely resembles Δ . Equation (2) formulates this objective as ϑ . In this case, we are optimizing the vectors in \mathcal{U} to minimize the difference between the cosine dissimilarity of each pair of word vectors for every timestamp and the cosine dissimilarity from temporal tf-idf model in $_{315}$ Δ (Eq. (1)). The minimization of the difference will ensure that our model $_{316}$ captures the same similarity as the temporal tf-idf model, but ours will provide $_{317}$ low-dimensional contextual vectors.

In this paper, the term dist(A, B) refers to the cosine dissimilarity between 318 vectors A and B. The cosine dissimilarity between a pair of word vectors is 319 bounded between [0, 1]. A cosine dissimilarity of 0 between two word vectors 320 means that both words share the same context, while a cosine dissimilarity of 321 1 means that the vectors are completely orthogonal, thus they do not share 322 contextual similarities. The variable α is introduced as a scaling factor to avoid 323 numerical stability issues with values close to zero. The simplest form of our 324 objective function, incorporating only the similarity aspects, is as follows. 325

$$\vartheta_1(\mathcal{U}) = \sum_{i=1}^{|\mathcal{W}|} \sum_{j=1}^{|\mathcal{W}|} \sum_{t=1}^{|\mathcal{T}|} \left(\alpha \cdot dist(u_{it}, u_{jt}) - \alpha \cdot \delta_{ijt} \right)^2 \tag{2}$$

4.1.3 Weighing relevance: Giving more importance to the neighborhood of each word

In our work, we focus on the task of studying the semantic evolution of a word 328 based on changes to its context. Thus, it is more important that our word 329 embedding model correctly captures the *relevant* neighborhood of a word. We 330 empirically discovered that each word has a small number of *relevant* neighbors. 331 That is, each word shares context with a small number of words. To take 332 this into account in the objective function, we introduce a penalty when the 333 temporal tf-idf-based cosine dissimilarity δ_{ijt} is small, ensuring that our word 334 embedding model captures the *relevant* context accurately. 335

$$\vartheta_2(\mathcal{U}) = \sum_{i=1}^{|\mathcal{W}|} \sum_{j=1}^{|\mathcal{U}|} \sum_{t=1}^{|\mathcal{T}|} (\alpha \cdot dist(u_{it}, u_{jt}) - \alpha \cdot \delta_{ijt})^2 \cdot e^{-\beta \delta_{ijt}}$$
(3)

where β is a scaling parameter to increase/decrease the importance given to 336 the samples with a smaller distance. Notice that $e^{-\beta \delta_{ijt}}$ in Eq. (3) imposes a 337 higher penalty to examples with smaller baseline distances. The penalty is less 338 when the dissimilarity from the temporal tf-idf model is large (that is a lesser 339 penalty for contextually similar words). Equation (3) supports the phenomenon 340 that, for a specific word, most of the words in the vocabulary are at a relatively 341 large distance. The large distances need not be a part of the penalty because 342 the objective function is only concerned about neighbors that appear in the 343 vicinity for the temporal tf-idf model. 344

345 4.1.4 Temporal diffusion filter

In connection with the diffusion theory [23] (introduced earlier with frequencybased training data generation in Section 4.1.1), we assume that the meaning of a word, and consequently its vector representation, diffuses (or drifts) over time. Thus, our model should generate word embeddings that evolve smoothly over time. To introduce this concept in our objective function, we model the
 effect of every word vector in all timestamps to some degree.

We use a Gaussian filter (Eq. (4)) to *diffuse* the contribution of each vector smoothly before and after the timestamp of the current sample. The filter uses a sliding window, going from the first to the last timestamp. σ is a user-settable parameter representing the standard deviation of the Gaussian distribution. A large value of σ means that the diffusion of word vectors is slow over time. A small standard deviation allows for capturing short-term changes in meaning.

$$\gamma(t,\sigma) = \left\langle \left(\frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(t_i-t)^2}{2\sigma^2}}\right) \text{ with } t_i = 1, \dots, |\mathcal{T}| \right\rangle$$
(4)

Equation (5) presents the updated objective ϑ_3 which includes the temporal diffusion of the word embeddings.

$$\vartheta_3(\mathcal{U}) = \sum_{i=1}^{|\mathcal{W}|} \sum_{j=1}^{|\mathcal{W}|} \sum_{t=1}^{|\mathcal{T}|} \left(\alpha \cdot dist(\gamma(t,\sigma)U_i,\gamma(t,\sigma)U_j) - \alpha \cdot \delta_{ijt} \right)^2 \cdot e^{-\beta\delta_{ijt}}$$
(5)

4.1.5 Smoothness penalty: Creating a homogeneous temporal embedding space

The second important goal that our word embedding model should achieve is to be spatially smooth over time. Continuous or smooth temporal embeddings are those where the distance (e.g., Manhattan or Euclidean) between two vectors of the same word for consecutive timestamps is small. Equation (6) captures the expected behavior by penalizing significant spatial changes.

$$\varepsilon_{1a}(\mathcal{U}) = \sum_{i=1}^{|\mathcal{W}|} \sum_{t=1}^{|\mathcal{T}|-1} ||u_{it+1}, u_{it}||_2$$
(6)

The main issue with this expression is that by forcing consecutive vectors to be very close together, we might be losing important information when the vectors drift apart in the original data. Thus, we introduce weights, ω_{ϑ} , and ω_{ε} to control the effect of each objective. The final objective function takes the form of Eq. (7).

$$\mathcal{F}_a(\mathcal{U}) = \vartheta_3(\mathcal{U})^{\omega_\vartheta} \varepsilon_1(\mathcal{U})^{\omega_\varepsilon} \tag{7}$$

An alternative form would be:

$$\mathcal{F}_b(\mathcal{U}) = \omega_\vartheta \log \vartheta_3(\mathcal{U}) + \omega_\varepsilon \log \varepsilon_1(\mathcal{U}) \tag{8}$$

or

$$\mathcal{F}_{c}(\mathcal{U}) = \omega_{\vartheta}\vartheta_{3}(\mathcal{U}) + \omega_{\varepsilon}\varepsilon_{1}(\mathcal{U}) \tag{9}$$

4.1.6 Implementation 362

We implemented a neural network-based model using Tensorflow to generate 363 our low-dimensional temporal word embeddings. An overall view of the 364 architecture of our neural network is shown in figure 2. The goal of the neural 365 network is to minimize Eq. (7). The embeddings for all words in all timestamps 366 are generated in the hidden layer. We initialize the weights in the hidden layer 367 in the range [0, 1]. The data used for training the model contains three inputs 368 (one-hot encoding of a pair of words for which the cosine dissimilarity is known, 369 and the timestamp) and one target value (cosine dissimilarity). The inputs 370 are the indices for two random words w_{it} and w_{jt} , at timestamp t. The target 371 value is the expected cosine dissimilarity between w_{it} and w_{it} , obtained using 372 the temporal tf-idf representations of Eq. (1). 373

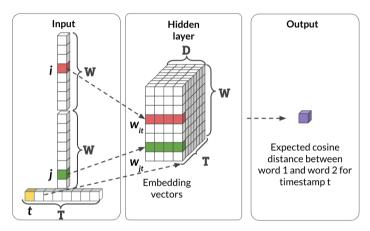


Fig. 2 The proposed neural network architecture for temporal embedding generation in the hidden laver.

4.2 Sequential model predicting a future embedding space: 374

In this subsection, we explain how to extrapolate the generated temporal 375 embeddings to build an embedding space for a future timestamp. 376

For predicting a future embedding space, we leverage state-of-the-art tech-377 niques in terms of sequence modeling, such as (1) the Long Short Term Memory 378 (LSTM) [31] and (2) Gated Recurrent Units (GRU) [32] recurrent neural net-379 works (RNNs). We also explore the effect of adding an attention mechanism [33] 380 to both LSTM- and GRU-based RNNs, which allows the network to focus on the 381 most important elements of the sequence. Finally, we evaluate the non-recurrent 382 attention-based *Transformer* model [34] which, in contrast to RNNs, can be 383 trained in parallel. The following subsections provide a detailed description of 384

the four sequential models we used for predicting future embeddings. 385

386 4.2.1 LSTM model structure

Most of the progress in RNN-based sequence modeling has been oriented towards 387 machine translation, which uses an encoder-decoder architecture [32, 33, 35]. 388 The objective of the encoder part of the network is to *summarize* the input 380 data as state vectors. The state vectors pass to the decoder layer, which is in 390 charge of generating the outputs that best fit the input state. In the particular 391 case of machine translation, a complete sentence such as "I love you" would be 392 transformed into a single vector by the encoder, and then a decoder trained to 393 generate text in Spanish would output "Te amo". 30/

In our case, we only focus on the encoder part of the model, since our primary goal is to train the RNN in such a way that we can predict the next element in the sequence. Each element of the sequence is a word embedding for timestamp t, or, more generally, a fixed-size vector.

Figure 3 illustrates the structure of the LSTM-based network we use for 399 word embedding prediction. In this particular diagram, we are using three 400 LSTM cells. This means that we predict the embedding vector for the next 401 timestamp using the word embeddings of the previous three timestamps. The 402 number of LSTM cells, or *sequence length*, is a user-defined parameter. The 403 dense layer before the predicted embeddings is required because the output 404 layer of the LSTM is always between -1 and 1 due to the tanh activation of 405 the hidden state. 406

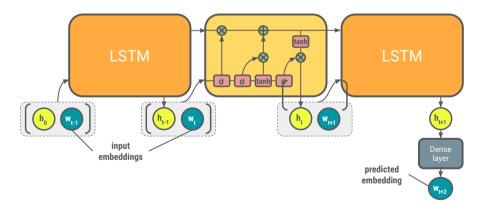


Fig. 3 Structure of the LSTM-based network used for word embedding prediction.

407 4.2.2 GRU model structure

Figure 4 illustrates the structure of the GRU-based network used to model the evolution of our temporal word embeddings. In this particular diagram, we are using two GRU cells, but the user-defined *sequence length* parameter can be used to change this number. This model also requires a dense layer before the predicted embeddings layer because of the tanh activation function in the GRU cell structure.

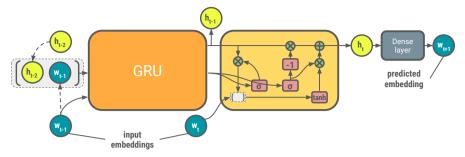


Fig. 4 Structure of the GRU-based network used for word embedding prediction.

414 4.2.3 Attention-based model structure

Figure 5 illustrates a generic version of an attention-based network with RNNs.

⁴¹⁶ In our experiments, we replace the generic RNNs with LSTM and GRU cells.

⁴¹⁷ The α values in the figure refer to the *attention weights*. The diagram shows

⁴¹⁸ only one line going from one RNN to the next, but as we have explained in

the LSTM section, it is possible to have more than one state passed from one

- ⁴²⁰ cell to the next. Similar to the LSTM- and GRU-based networks, it is possible ⁴²¹ to change the training sequence length, which is set to 5 in this example for
- ⁴²¹ to change the training sequence length, which is set to 5 in this example for illustrative purposes.

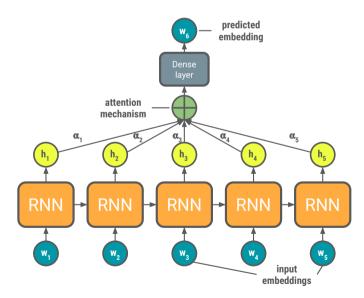


Fig. 5 Structure of the attention-based networks [33] used for word embedding prediction, with LSTM and GRU cells instead of vanilla RNNs.

423 4.2.4 Transformer-based approach

The sequential nature of the different versions of RNNs prohibits parallel training. The *Transformer* model [34] gets rid of the recurrence part of the previous networks and relies completely on a self-attention mechanism. This model allows for parallel training, and it is also good at learning long-term dependencies. Furthermore, distant elements can affect each other without running into the vanishing gradients issue [34].

The *Transfomer* model uses a stack of self-attention layers to handle sequential inputs. The idea of self-attention is to be able to generate a compressed representation of a sequence by studying (or *attending* to) different positions of the input. The original *Transformer* has an encoder-decoder architecture, but as in the previous cases, we only use the encoder portion of the model.

Figure 6 presents a diagram of the resulting network, which consists of a stack of encoder layers, a positional encoding element, and the inputs and outputs. Each encoder layer contains:

- A multi-head attention element, which is the most important (and complex)
 element of the encoder.
- A feed-forward dense network, which consists of a dense layer with a ReLU
 activation function followed by a regular dense layer.
- A normalization of the sum of the residual connection and the output of
 each of the previous two elements. This is introduced to avoid the vanishing
 gradients issue.

The positional encoding is required to give the model information about the temporal dimension of the input word embedding vectors. There are different positional encoding functions, but we use the one presented by Vaswani et

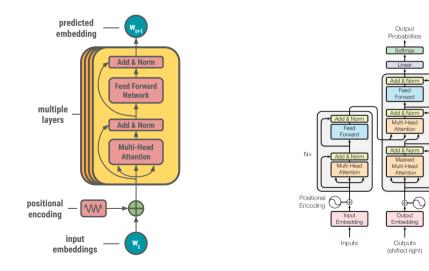


Fig. 6 Structure of the network used for word embedding prediction using only the encoder layer from the Transformer architecture [34].

⁴⁴⁸ al. [34], which consists of a vector of sine-cosine pairs at each position that ⁴⁴⁹ rotate at different frequencies.

450 5 Experimental Results

⁴⁵¹ We performed experiments using multiple datasets: a synthetic dataset, PubMed ⁴⁵² Pandemic dataset, PubMed COVID dataset, NyTimes news dataset, and the ⁴⁵³ National Vulnerability dataset. Experimental analysis is conducted using these ⁴⁵⁴ datasets to evaluate the stages of problems described in the problem description, ⁴⁵⁵ namely (1) the generation of temporal embeddings and (2) the prediction of ⁴⁵⁶ future embedding space. Based on these two stages, we present our experimental ⁴⁵⁷ results in subsections 5.1 and 5.2.

458 The datasets that we used in this section are outlined in table 1.

Data	Documents	Span	# Timestamps
Synthetic Data	10,000	-	10
PubMed(Pandemic) 2	328,908	2000-2020	21
PubMed(COVID) ¹	374,883	Jan 2020-May 2022	29
PubMed(CANCER) ²	613,949	1998-2018	21
NyTimes ²	812,857	1990-2018	29
NyTimes (President) ²	769,214	1990-2022	32
NyTimes (Russia-Ukraine) 2	4,957	Jan 2020-Dec 2021	24
NVD ²	165,552	1999-2021	23

Table 1Datasets used for our experiments.

Note: The PubMed(Pandemic), PubMed(Cancer), NyTimes, and NVD dataset files are available in Kaggle link² below.

We generated the synthetic dataset consisting of 10,000 words and ten
timestamps. For this dataset, we already know the 10-nearest neighbors of each
word in every timestamp. Neighborhoods of larger sizes will contain random
words starting at the 11th nearest neighbor.

The **PubMed pandemic dataset**, contains **328,908** abstracts of *pandemic* and epidemic-related biomedical publications. The abstracts were published between years 2000 to 2020. **The PubMed COVID** dataset contains **374,883** abstracts of biomedical papers related to COVID-19, published between 2020-2022. The corpus was collected from Kaggle COVID19 Open Research Dataset Challenge [36]. The **PubMed CANCER** consists of 21 years of data with **613,949** abstracts that contain the keyword cancer.

The New York Times corpus contains 812,857 news articles that were
published over 29 years. We collected Russia-Ukraine related news from
NYTimes that contains 50,000 news articles published between years 2020
to 2021. The NVD dataset includes 165,552 bulletins published in the last 20
years.

The named entities from the **NYTimes** and **NVD** dataset are extracted using *spaCy*'s Named Entity Recognition (NER) model [37], and We extracted the biomedical entities for the **PubMed** abstracts using *scispaCy*'s Biomedical Named Entity Recognition [38].

The analysis of the PubMed and NVD datasets was limited to the top3,000 entities based on their term frequency-inverse document frequency (tf-idf)
weights, while the analysis of the New York Times corpus was limited to the
top-5,000 words, based on their tf-idf weights.

483 5.1 Experiments on the generated temporal embeddings

We evaluate our temporal word embedding method by comparing its performance with that of a regular tf-idf model, the temporal tf-idf model [4], dynamic Bernoulli embeddings [11], temporal word embeddings with a compass (TWEC) [12], and tempoBert [3]. In all our experiments, we used an **embedding size of 64**.

We seek to answer the following questions through experiments and casestudies.

- 491 1. What is the effect of introducing different penalty terms in our objective
 492 function? (Section 5.1.1)
- 493 2. How well do the models perform in terms of capturing the neighborhood of
 494 entities over time, compared to the temporal tf-idf? (Section 5.1.2)
- ⁴⁹⁵ 3. How well do the models perform in terms of capturing changes in the
- neighborhood over time in the respective embedding spaces? (Section 5.1.3)
 497 4. How well does our algorithm track the quick evolution of a specific entity,
 498 such as *COVID*, compared to other methods? (Section 5.1.4)
- ⁴⁹⁹ 5. How well does our algorithm capture the semantic evolution of a general ⁵⁰⁰ term, such as *pandemic*, compared to other methods? (Section 5.1.5)

501 5.1.1 Effect of penalty terms

In this experiment, we study the effect of the different versions of our objective function on the quality of the temporal word embedding model, focusing on the task of tracking semantic evolution. The versions under this study correspond to ϑ_1 (2), ϑ_2 (3), ϑ_3 (5), \mathcal{F}_a (7), \mathcal{F}_b (8), and \mathcal{F}_c (9). We quantify the quality of the resulting vectors with two different metrics: similarity and continuity.

The similarity is measured as the number of intersections between the word neighborhoods obtained using the temporal tf-idf model and each of the different versions of our objective function. The goal of the similarity evaluation is to quantify how well our model mimics the temporal tf-idf model. It must be noted that we did not expect to have a perfect match in the neighborhoods of words since the temporal tf-idf model representation does not take into account latent contextual relationships between words.

The continuity is measured using the average, maximum, and minimum mean squared errors (MSE) across consecutive timestamps for the word vectors obtained using the different versions of our objective function.

Figure 7 shows the results for the similarity evaluation with the synthetic 517 dataset described at the beginning of Section 5. The objective function labeled 518 as \mathcal{F}_a on the figure performs significantly better than the other formulations. 519 If we discard \mathcal{F}_b and \mathcal{F}_c , it is possible to see how the similarity improves with 520 the progression in which we developed our objective function. Furthermore, 521 taking into account that only the top-10 nearest neighbors are known and set as 522 accurate in the synthetic data and the rest of the neighbors are random, having 523 an average of 8 intersections means that our model can correctly capture the 524 semantic evolution of the synthetic dataset. 525

Evaluating continuity is required to ensure that there is a smooth transition 526 between timestamps for the vectors of the same word. A high average or 527 minimum MSE value indicates that there is a significant movement of the 528 word vectors over time in the embedding space. However, a small maximum 529 MSE value would mean that the word embeddings are not following the trends 530 observed in the temporal tf-idf model-based training. Thus, the best model is 531 one that has high similarity with the temporal tf-idf model while maintaining 532 a low MSE value. 533

Figure 8 shows the results for the continuity evaluation. In this case, F_c has a continuity of 0.0, which, in conjunction with the similarity results, indicates that this objective function produces static, unusable vectors. The second smallest average MSE value is obtained with \mathcal{F}_a , which also showed the best performance in terms of similarity. Thus, the **final objective function** is \mathcal{F}_a (Eq. (7)), and we confirm that the smoothness penalty (Eq. (6)) has a positive effect both on the similarity and continuity results.

541 5.1.2 Capability to capture content neighborhood

A major purpose of any temporal or dynamic word representation modeling is
to capture content similarity over time. We compare three models – TWEC,
Dynamic Bernoulli embeddings, and our temporal word embedding – with
Temporal tf-idf [4] in Figure 9, using PubMed (pandemic) dataset. We use

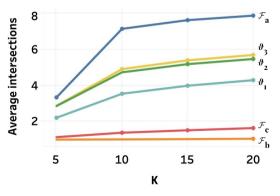


Fig. 7 Average number of intersections per timestamp for different neighborhood sizes (k) between the neighborhoods obtained with the baseline method and those obtained using the different versions of our objective function (embedding size = 64).

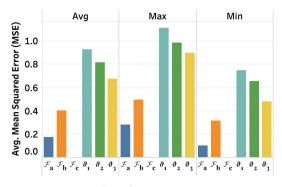


Fig. 8 Average mean squared error (MSE) for different versions of our objective function. The average MSE is computed from obtaining the squared difference between vectors for the same word for every pair of consecutive timestamps (embedding size = 64).

temporal tf-idf [4] for this comparison because it models content smoothly over 546 time. Each line in the figure represents average set-based Jaccard similarity 547 between the 10-nearest neighbors of 1000 randomly selected entities using 548 temporal tf-idf and the 10-nearest neighbors of the same entities using one of the 549 three models. Figure 9 demonstrates that our embedding model and TWEC have 550 closer similarity with temporal tf-idf than Bernoulli embeddings. Additionally, 551 our model has greater similarity with the neighborhood of temporal tf-idf in 552 the earlier timestamps, compared to both TWEC and Bernoulli embeddings. 553 Bernoulli embeddings over different timestamps do not change much to capture 554 the evolution of words. This resulted in an almost horizontal line for Bernoulli 555 embeddings in figure 9. 556

⁵⁵⁷ Our model smoothly spreads word influence using diffusion over the years. ⁵⁵⁸ As a result, our embedding model performs significantly better than other ⁵⁵⁹ methods, even when the vocabulary is smaller in the earlier timestamps.

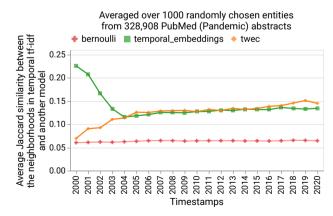


Fig. 9 Jaccard similarity in the neighborhoods between temporal tf-df [4] and each of the three models – TWEC, Bernoulli embeddings, and our temporal word embedding model. (PubMed (pandemic) dataset. Embedding size = 64.)

550 5.1.3 Capability to detect changes in neighborhood

An objective of a temporal embedding technique is to capture changes in 561 the neighborhood of each word over time. The ability to capture changes 562 allows us to study the evolution of concepts. This subsection provides an 563 experiment to investigate how much change occurs from one year to another in 564 the neighborhood using different models. We quantify the change in terms of set-565 based Jaccard dissimilarity (1.0-Jaccard similarity) between the neighborhood 566 of a word in the current year and the neighborhood of the same word in the 567 previous year. Average Jaccard dissimilarity over many words in a certain year 568 for a model gives an overall idea of how much the model can detect changes in 569 the neighborhood. 570

Figure 10 demonstrates average Jaccard dissimilarity (change) at each year for five different models – our temporal embedding model, Bernoulli embeddings, TWEC, and vanilla tf-idf computed independently at each year, and temporal tfidf using 1000 randomly selected entities from the PubMed (pandemic) dataset. The plot shows that our temporal embedding model detects more changes in terms of average Jaccard dissimilarity compared to other models.

The Bernoulli embeddings capture the least amount of changes. Based on 577 further investigation (not covered in this paper), we noticed that Bernoulli 578 embeddings rarely capture any changes. These embeddings capture only a 579 few long-term changes, whereas our temporal embedding model significantly 580 captures both long-term and short-term changes. TWEC captures more changes 581 than Bernoulli and temporal tf-idf, but lesser changes than the vanilla tf-idf. 582 Our temporal word embedding performs even better than the vanilla tf-idf. 583 Contextual changes are best-captured using our temporal embedding because 584 the objective function of our model spreads the effect of each word smoothly 585 from the current year to other years. As a result, our model captures changes, in 586

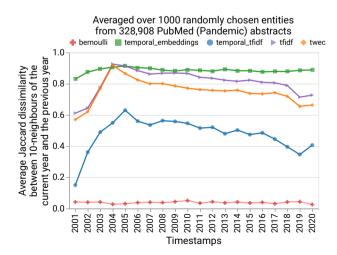


Fig. 10 Comparison of average Jaccard dissimilarity (change) between 10-neighbors of the current year and the previous year.

terms of average Jaccard dissimilarity, better than regular tf-idf and temporal
 tf-idf models.

⁵⁸⁹ Our model is clearly superior in terms of the ability to capture changes. In ⁵⁹⁰ subsection 5.1.4, we explain how the superiority in the detection of changes in ⁵⁹¹ the neighborhood helps in analyzing evolving concepts, such as *COVID-19*.

⁵⁹² 5.1.4 Analyzing the neighborhood of COVID-19

In this experiment, we analyze the changes in the neighborhood of the word 593 COVID in the PubMed (COVID) dataset. Figure 11 presents how the simi-594 larities between the entity COVID and some of its nearest neighbors-China, 595 epidemic, pandemic, and patients- change over time using (a) TWEC model, 596 (b) Bernoulli embeddings, (c) temporal tf-idf, and (d) our temporal embed-597 ding model. The data contains ranges of two-weeks from January to July of 598 2020. From August 2020, COVID-19 was considered a pandemic – which is a 599 global outbreak rather than a local epidemic [39]. In figure 11, we observe that 600 (figure 11 (c)) temporal tf-idf and (figure 11 (d)) our temporal embedding can 601 detect the rising trends of *pandemic* and falling trends of the word *epidemic*. 602 This observation matches our known knowledge regarding COVID-19. TWEC 603 (figure 11 (a)) is able to track this to some degree but with zigzag-patterns in the 604 trends. Bernoulli embeddings (figure 11 (b)) give higher similarity for *pandemic* 605 than *epidemic* with the word *COVID*, which is correct in July but the timeline 606 does not demonstrate any rising and falling trends of the words *pandemic* and 607 epidemic, as they should based on our knowledge about COVID-19. 608

Our temporal embedding model (figure 11 (d)) demonstrates that the word 609 China had high similarity with COVID in the beginning. The similarity started 610 to fall by the end of March. According to our model, starting at the end of 611 March, the word *epidemic* started to exhibit lesser similarity with *COVID* and 612 the word *pandemic* started to show higher similarity. The temporal tf-idf model 613 (figure 11 (c)) demonstrates a similar trend. The trends resemble our common 614 knowledge regarding the COVID-19 pandemic. Also, TWEC (figure 11 (a)) 615 has an overall downward trend for the word *China*, but with zigzag movements 616 over the timeline. Bernoulli embeddings (figure 11 (b)) do not demonstrate any 617 change and capture a static similarity for the entire timeline. We noticed that 618 the underlying vectors in Bernoulli embeddings change, but the neighbors of 619 a word do not change much. That indicates that the changes in the vectors 620 generated by Bernoulli embeddings might be the result of some scaling effect 621 rather than changes due to the reformation of the neighborhood. 622

We know that the number of COVID-infected *patients* increased over the months of 2020. Our temporal embedding model (as well as the temporal tf-idf) captures the rising-similarity of the word *patients* in the context of *COVID* quite smoothly (figure 11 (d)). TWEC also has an upward trend which is less smooth. However, the Bernoulli embeddings do not demonstrate any changes in the similarity between the words *patients* and *COVID*.

This experiment demonstrates that our temporal embedding model captures the short-term changes in content (as shown by temporal tf-idf) while also

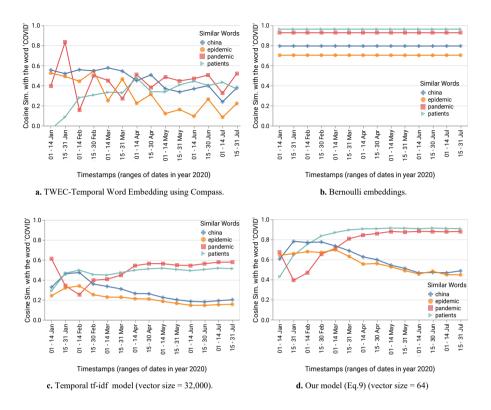


Fig. 11 Evolution of the word *COVID* in PubMed COVID-19-related abstracts published in 2020 using four different models – TWEC, Bernoulli embeddings, temporal tf-idf, and our temporal embedding model. *Cosine similarity* is used to compute the similarity between the vectors of the word *COVID* and any other word.

capturing the context that we can track smoothly to study the evolution of a
concept, such as *COVID*. In contrast, Bernoulli embeddings construct a context
that is intractable in terms of similarity. TWEC provides noisy patterns that
are difficult to interpret.

5.1.5 Analysis of the the word Pandemic

With the rise of the COVID-19 pandemic, it has become essential to study how biomedical scientists have dealt with a pandemic in the past years. Such an analysis requires a model that can capture long term changes. In this experiment, we attempt to track the closest term to the word *pandemic* in each year of the PubMed (pandemic) dataset, which spans biomedical abstracts from 2000 to 2020.

Each line of figure 12 plots the similarity of the top nearest-neighbor of the word *pandemic* in each year. The five lines represent similarities using five different models – Bernoulli embeddings, our temporal embedding model, temporal tf-idf, vanilla tf-idf, and TWEC. Notice that our temporal embedding

model demonstrates peak similarities in 2009/2010 and in 2020, when H1N1 646 influenza (swine flu) and COVID-19, respectively became prominent. This 647 signal from our temporal embedding model reflects the fact that the worst 648 pandemics in the last 20 years are the H1N1 influenza in 2009 [40] and COVID-649 19 in 2020 [41]. Note that other words like *concerns* in 2004 and *public* in 2015 650 are detected as the top nearest neighbors, which are not highly similar to the 651 word *pandemic*. This indicates that no entities appeared too close to the word 652 *pandemic* in those years. 653

TWEC captures influenza and H1N1 in the middle of the timeline but fails 654 to capture COVID-related keywords in 2020 as the closest entity to pandemic. 655 In figure 12, the Bernoulli model can pick up *coronavirus* as the nearest neighbor 656 of *pandemic* but it was not able to pick up influenza in its trend. Moreover, 657 coronovirus appears in all the years as the top nearest neighbor of pandemic 658 which is not correct because the fact is that the coronavirus spread started in 659 2019 and became a pandemic in 2020 [41]. Temporal tf-idf and vanilla tf-idf 660 were able to pick up coronavirus/COVID. Temporal tf-idf and vanilla tf-idf 661 were also able to pick up influenza subtype H1N1 (swine flu) but the respective 662 similarities were not high. 663

Based on the experiment presented in this subsection, our temporal embedding model has the ability to separate highly contextual words (such as H1N1 and COVID) of a concept (such as *pandemic*) via similarity-peaks. Our model

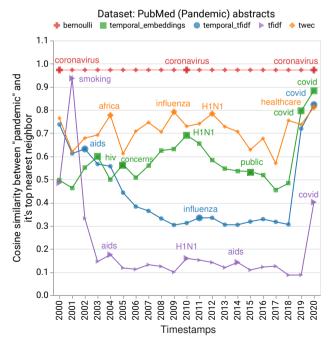


Fig. 12 Cosine similarity of the top nearest neighbor of *pandemic* in each year using all methods. Nearest neighbors are written with selected peaks. Our temporal embedding method provides better context for *pandemic*. Embedding size = 64.

helps in determining prominent neighbors of a concept in the past. Our vectors
are able to construct a peak for a prominent nearest neighbor because our
method models diffusion. That is, a concept that appears today affects the
past and the future to some extent, regardless of whether the concept directly
appears in the contents or not.

⁶⁷² 5.1.6 Comparison with BERT temporal embedding

Based on recent literature, there is a surge in applications using Bidirectional 673 Encoder Representations from Transformers (BERT). BERT provides vectors 674 for each appearance of words. The vectors of the same word appearing in the 675 same timestamp can be used to create a word embedding vector for that word 676 in that timestamp, leading to temporal word embeddings. TempoBert model [3] 677 is such a mechanism. In the TempoBert model, the timestamps are added at 678 the start and end of each sentence as a means of training text data for differ-679 ent timestamps. The BERT-generated embeddings are clustered for semantic 680 evolution. In our experiment here, we use a variant of TempoBert, referred to 681 as temporal BERT, which does not cluster vectors but rather calculates the 682 arithmetic mean of embedding vectors of a word at each timestamp to generate 683 one vector for one word at each timestamp. 684

A drawback of the BERT-based model is its excessive computation time 685 compared to other embedding models due to the complex structure of the deep 686 learning model. Therefore, for this experimental analysis, we downsample the 687 corpus to 10% of articles per month to ease the computation for BERT. The 688 corpus for this experiment includes 10% of Pubmed COVID-related articles 689 (between Jan 2020 – May 2022) and 10% of NYTimes Russia-Ukraine-related 690 articles (over 24 months between Jan 2020 - Dec 2021). In this section, we 691 examine, how the neighborhood of the words COVID and UKRAINE changes 692 over time using the word embeddings generated by temporal BERT and our 693 temporal embedding model. 694

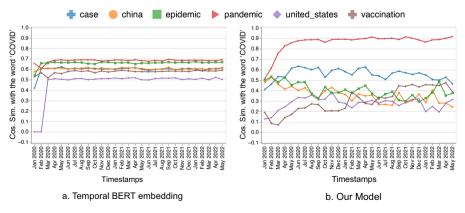


Fig. 13 Cosine similarity of the embedding of "COVID" with neighbor words at the different timestamp. [Temporal BERT vs Our Model]

Figure 13 presents the cosine similarity of embeddings of the word "COVID" 605 with its neighboring words at different timestamps. The plot on the left (a) is 696 generated by using embeddings from temporal BERT, and the plot on the right 697 (b) is generated by using our temporal embedding model. In figure 13(b), we 698 observe that at the beginning of the month of January 2020, the words "case", 699 "china", "epidemic", and "pandemic" are the closest neighbors of the word 700 "COVID". Then, over time, the similarities of the words "china" and "epidemic" 701 with "COVID" decreases while the similarities of the words "pandemic", "united 702 states", and "vaccination", with COVID increase. The changing neighborhood 703 of "COVID" reflects how "COVID" spreads throughout the world over time, 704 starting from china and eventually becoming the world's most widespread 705 pandemic. Further, vaccination programs were initiated at the beginning of 2021. 706 Our model captures these trends well, as reflected in the plot of figure 13(b). 707 The plot on the left (figure 13(a)), on the other hand, provides mostly straight 708 lines and fails to capture such changes in the neighborhood of "COVID". 709

Another experimental result in figure 14 presents the cosine similarity of 710 embeddings of the word "UKRAINE" with its neighboring words at different 711 timestamps. Based on our known knowledge from the news, Russia invaded 712 Ukrainian territory in February 2022 [42]. As part of our experiment, we trained 713 both the temporal BERT and our model with news data collected prior to the 714 invasion. The embeddings generated by our model (Figure 14 (b)) shows that 715 the similarities between each of the words "cold war", "invasion", and "Russia" 716 with the word "UKRAINE" increased at the end of the year 2021, which is 717 prior to the actual invasion. The temporal BERT, however, failed to detect any 718 changes in the neighborhood of the word "Ukraine". This analysis indicates 719 that the embeddings generated by our model have better prediction capability 720 compared to the temporal BERT embedding model. 721

Temporal BERT does not perform well due to the fact that complex deep neural network models require extensive training on large datasets. In order to train a BERT model from scratch, it is recommended to use billions of sentences,

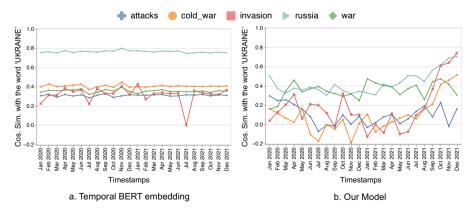


Fig. 14 Cosine similarity of the embedding of "UKRAINE" with neighbor words at the different timestamp. [Temporal BERT vs Our Model]

which is sometimes not available for a specific domain. In our experiment related
to COVID (figure 13), we used a pre-trained BERT model (clinical-bert [43]
and fine-tuned it with our data. For the Russia-Ukraine-related experiment
(figure 14), we used bert-small [44, 45]), which is later fine-tuned by the smaller
dataset. In these experiments, we find that despite fine-tuning the BERT model,
it fails to capture the temporal evolution of words. Our model performs well
even with small datasets, requiring lesser training samples.

732 5.1.7 Stacking cosine similarities

A streamgraph is a stacked area chart widely used in concept visualization [46]. In this subsection, we provide an analysis of the entity *president* using a streamgraph using the New York Times dataset. Cosine similarities of the nearest neighbors of the entity *president* are stacked in the streamgraph of figure 15.

We observe how the entities *Obama* and *Trump* started to get closer to 738 president only a few years before their presidency. Biden started to get closer 739 to *president* in the year 2008 when he became the vice president. The cosine 740 similarity between the word *Biden* and the word *president* increased in 2020, 741 which matches with the actual event that Biden won the presidential election in 742 2020. We also observe the particular cases of political families, such as the Bush, 743 and *Clinton* families, that have been relevant to the presidential elections for 744 the last four decades. General entities – such as White House, and United States 745 - relevant to the entity *president* do not change much in similarity (the width 746

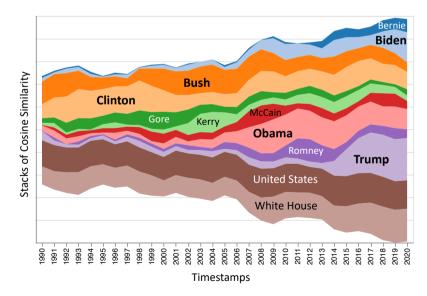


Fig. 15 Streamgraph of the word *President* using the New York Times corpus. The width of each of the bands represent cosine similarity of each word with the word *President*. The word vectors at different timestamps are generated using our temporal word embedding model (embedding size = 64).

of each of the bands) but remain nearest neighbors at all times. This indicates 747 the consistency of the words White House, and United States in relation to the 748 word *president*. Other entities, on the other hand, appear and disappear over 749 time based on their relevance to the word president. For example, Gore and 750 Kerry were presidential candidates in the years 2000 and 2004, respectively. 751 Their cosine similarity with the word *president* increased during those years. 752 The results of this experiment demonstrate that our temporal embedding 753 model effectively captures the trends of a historical concept. Additionally, the 754 changes in the cosine similarity of the words are smooth, indicating that the 755 embeddings are changing smoothly over time and that they are well suited 756 for extrapolating into future timestamps for predicting the future state of 757 the embeddings. Subsection 5.2.3 discusses experiments related to predicted 758 embeddings of the word *president*. 759

⁷⁶⁰ 5.1.8 Sensitivity analysis for hyperparameters

In this experiment, we evaluate the effect of performing a sweep of different values for (a) the embedding size, (b) the exponential factor β , (c) the scale factor α , (d) the temporal diffusion filter standard deviation σ , (e) the smoothness penalty factor ω_{ϵ} , and (f) the learning rate of our model. We use the average number of intersections per timestamp between the neighborhoods obtained using our method and those generated using the temporal tf-idf method as our accuracy metric.

Figure 16 presents the effect of changing the parameters of interest on the accuracy of our model. The results show that the embedding size, the scale

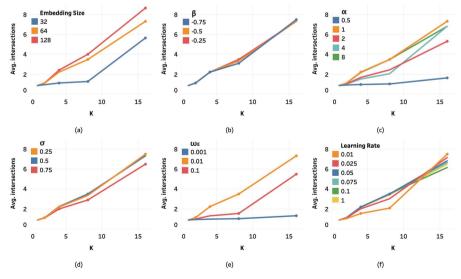


Fig. 16 Average number of intersections per timestamp between the neighborhoods obtained with temporal tf-idf [4] and our temporal embedding model for the NVD data with changing (a)embedding size, (b) β , (c) α , (d) σ , (e) ω_{ϵ} , and (f) learning rate.

factor (α), and the smoothness penalty factor (ω_{ϵ}) have significant effects on the accuracy of neighborhood-detection. Figure 16 only presents the results obtained using the NVD dataset. We performed similar analyses for the other datasets, which resulted in similar findings.

Figure 16 (a) shows that using an embedding size of 128 resulted in slightly 774 better performance than a size of 64. However, this slight improvement does 775 not justify the significant increase in training time and computational/storage 776 complexity. Training time increased from ~ 18 hours to ~ 50 hours per 777 experiment in a GPU-enabled cluster when we increase the embedding size from 778 64 to 128. Therefore, we decided to keep an embedding size of 64. The selection 779 of all the parameters in a neural network with a complex cost function like 780 ours is a "big data" challenge. After many different iterations, we discovered 781 that the size of 64 provides reasonably meaningful results in reasonable run 782 times with the available resources. 783

⁷⁸⁴ 5.2 Experiments on prediction capability

In this section, we evaluate the selected time-series modeling techniques to
generate temporal word embedding predictions. We perform the experiments
on three different datasets: (1) PubMed abstracts [47], (2) New York Times
articles, and (3) National Vulnerability Database (NVD) bulletins [48].

The temporal word embeddings used as baseline data were generated using the method presented in section 4. We split the embeddings for each dataset into training and test datasets based on their timestamps. The word embeddings of the first X years out of $|\mathcal{T}|$ are the training data. The generated models were tested using the word vectors for the last $|\mathcal{T}| - X$ years, which are not part of the training data. The X parameter is user-defined.

We evaluate the performance of the time-series modeling techniques using 795 two different metrics: (1) average mean squared error (MSE) between the pre-796 dicted and the actual word vectors, and (2) neighborhood similarity (explained 797 next). We define *neighborhood similarity* as the average of the average number 798 of intersections between the neighborhoods generated using the actual word 799 embeddings and those generated using the predicted word embeddings, divided 800 by the neighborhood size k where $k \in [1, 2, 4, 8, 16]$. The neighborhood similar-801 ity is computed only for the test data timestamps. We formalize the concept of 802 neighborhood similarity as follows: 803

neighborhood similarity($\mathcal{N}_a, \mathcal{N}_b$) =

$$\sum_{w \in \mathcal{W}} \sum_{k \in [1,2,4,8,16]} \sum_{t \in \mathcal{T}_{\text{test}}} \frac{\mathcal{N}_a(w,t,k) \cap \mathcal{N}_b(w,t,k)}{k}$$

where $\mathcal{N}_a(w, t, k)$ returns the k nearest neighbors of word w at time t obtained from word embeddings generated using method a.

⁸⁰⁶ In this section, we seek to answer the following questions.

- ⁸⁰⁷ 1. Which sequence modeling technique is most well-suited to predict future
 ⁸⁰⁸ word embeddings? (Section 5.2.1)
- 2. How sensitive is the selected time-series modeling technique to changes in
 the hyperparameters? (Section 5.2.2)
- 3. How well does our algorithm predict the evolution of a specific term?
 (Section 5.2.3)

5.2.1 Model selection for prediction

The main goal of this experiment is to identify the sequence modeling technique that has the best performance in terms of predicting the semantic evolution of the given corpora. First, we identify the best hyperparameters by performing a sensitivity analysis for (1) LSTM, (2) GRU, (3) LSTM with attention, (4) GRU with attention, and (5) the Transformer model. Section 5.2.2 describes this sensitivity analysis in more detail.

For each model, we generate predicted word embeddings for every timestamp of the test dataset. We use the neighborhood similarity metric to measure the performance of each model.

Figures 17 and 18 present a comparison, for each dataset, between the best versions of each sequence modeling technique. Figure 17 presents the results in terms of the neighborhood similarity, while Figure 18 shows the effect of changing the neighborhood size K on the average number of intersections between the baseline and the predicted embeddings.

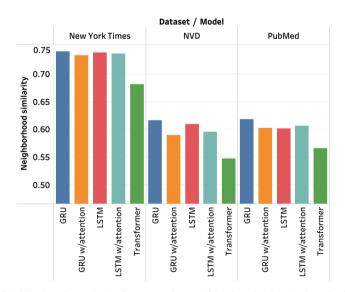


Fig. 17 Neighborhood similarity between the neighborhoods obtained with the baseline temporal embedding method (Eq. 7) and neighborhoods obtained using the predict-next technique with different sequential models for the NVD, PubMed and New York Times datasets, using dynamic values of K.

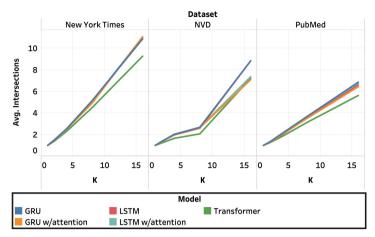


Fig. 18 Average number of intersections for different neighborhood size k per timestamp between the neighborhoods obtained with the baseline temporal embedding method (Eq. 7) and neighborhoods obtained using the predict-next technique with different sequential models for the NVD, PubMed and New York Times datasets (embedding size = 64), using dynamic values of K.

The results show that the GRU and LSTM-based networks outperform the 828 more complex sequential models in all datasets. For both GRU and LSTM, 829 the inclusion of the attention mechanism did not result in better performance. 830 This is because the attention mechanism is explicitly designed to model long 831 sequences [34], but our text-based embeddings have a limited number of times-832 tamps, resulting in a small temporal sequence. There fore GRU and LSTM 833 without the attention mechanism are more appropriate for predicting future 834 embeddings. 835

⁸³⁶ 5.2.2 Sensitivity analysis

In this section, we present the effect of performing a sweep of the hyperpa-837 rameters on the GRU-based sequential model. We performed similar analyses 838 for the other variants, but, for brevity, we only present the results obtained 839 with the best model. The evaluated parameters are (a) the batch size, (b) the 840 fraction of timestamps used for training, (c) the input sequence length, (d) 841 the number of encoder units for the neural network, (e) the optimizer, and (f) 842 the learning rate. We use the neighborhood similarity metric to quantify the 843 performance of each parameter combination. 844

Figure 19 presents the effect of changing the batch size (Figure 19(a)) and the fraction of timestamps used for the training/test split (Figure 19(b)) on neighborhood similarity. Based on the plots, it appears that changing the batch size does not have a significant effect on neighborhood similarity. Meanwhile, changing the train-test size has little effect on neighborhood similarity.

Figure 20 (a) presents the effect of changing the input sequence length on neighborhood similarity. This plot reveals that using an input consisting of the word embeddings for two or more timestamps results in a slightly better performance. Figure 20 (b) shows that changing the number of encoder units for the neural network has a negligible effect on the neighborhood similarity.

The plots of figures 19 and 20 indicate that the generation of neighborhoods of words from predicted embeddings is not sensitive to batch size, training/test split, input sequence size, and the number of encoder units, in general.

Figure 21 presents the effect of changing the optimizer and learning rate on neighborhood similarity. It is important to note that for these plots, a learning rate of 0.0 on the x-axis actually represents the neighborhood similarity obtained using the dynamic learning rate presented by Vaswani et al. [34]. The results clearly exhibit downward or upward trends with increasing learning rates. This is an indication that the neighborhood similarity is sensitive to the

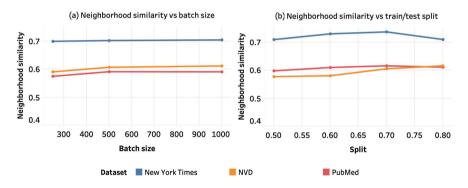


Fig. 19 Neighborhood similarity between the neighborhoods obtained with the baseline temporal embedding method (Eq. 7) and the neighborhoods obtained using the predict-next techniques with different sequential models for the NVD, PubMed and New York Times datasets, using dynamic values of K, while changing (a) the batch size and (b) the fraction of timestamps used for training.

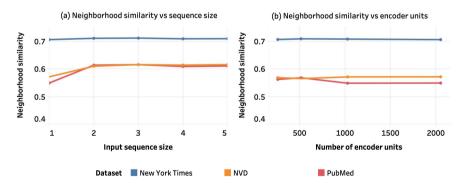


Fig. 20 Neighborhood similarity between the neighborhoods obtained with the baseline temporal embedding method (Eq. 7) and the neighborhoods obtained using the predicted embeddings with different sequential models for the NVD, PubMed and New York Times datasets, using dynamic values of K, while changing (a) the input sequence size and (b) the number of encoder units.

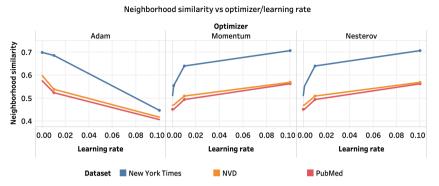


Fig. 21 Neighborhood similarity between the neighborhoods obtained with the baseline temporal embedding method (Eq. 7) and neighborhoods obtained using the predicted embeddings with different sequential models for the NVD, PubMed and New York Times datasets, with different optimizers and learning rates. The learning rate of 0.0 represents the dynamic learning rate presented by Vaswani et al. [34].

learning rate and hence the model requires tuning with different learning rate
 values to make sure the optimizer does not get stuck in local minima.

5.2.3 Case study and trend analysis

In this section, we perform a qualitative analysis of the performance of the 867 predicted temporal word embeddings on the task of tracking semantic evolution. 868 In this subsection, we report prediction results using LSTM. Similar results are 869 observed using GRU. We used New York Time data for two case studies – how 870 well do the predicted embeddings (1) relevant to the word war represent our 871 knowledge about contemporary political tension between different countries, 872 and (2) capture entities in the US political domain while studying the word 873 president. 874

Figure 22(a) contains cosine similarity of the nearest neighbors of the word 875 war. Relevant nearest neighbors - "Russia", "Ukraine", "ISIS", "Syria", and 876 "Taliban" – were selected from the predicted embedding for the year 2022. 877 Embeddings from previous years were used for training the LSTM. Figure 22(a)878 shows that the embeddings of the words "Syria" and "ISIS" were two words 879 most similar to the embedding of *war* in the beginning. Their similarity 880 with *war* gradually declined. The prediction for the year 2022 demonstrates 881 the continuous decline of "Syria" and "ISIS" from the word *war*. The word 882 "Taliban" became more similar to the word war between 2017 and 2020. The 883 U.S. and the Taliban peace deal occurred in 2020 [49]. The Taliban took over 884 the Afghan government in 2021 [50]. The prediction for 2022 reflects the end 885 of a long-lasting "war" by showing that the similarity of the word "Taliban" 886 and *war* will be lesser. 887

The similarities of the words "Russia" and "Ukraine" with *war* were declining through 2017-2020 but started to rise between 2020 and 2021. The predicted embeddings in the year 2022 show that "Russia" becomes the topmost

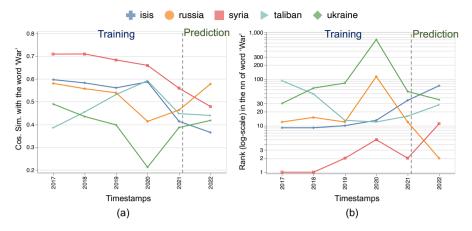


Fig. 22 Evolution of the neighborhood of the term *war* in the NYTimes dataset where the embeddings of words at timestamp 2022 is extrapolated using LSTM (a) cosine similarity between the embedding of the word *war* and relevant word embeddings at different timestamps. (b) Rank (position) of relevant words in the nearest neighborhood of the word *war* at different timestamps.

⁸⁹¹ nearest neighbor of *war*. Simultaneously, the similarity between "Ukraine" and ⁸⁹² *war* is predicted to increase in 2022.

Figure 22(b) shows the ranks of the same nearest neighbors of the word 893 war. The smaller the rank value more similar a neighbor is to the word war. 894 The vertical axis is in logarithmic scale for better visualization. Similar trends 895 as figure 22(a) are observed in figure 22(b). For example, 'Russia' and "Ukraine" 896 both are coming closer in rank to the word **war**, which is reflected as a falling 897 pattern in figure 22(b). Also, it is noticeable that the prediction of 'Syria' for 898 2022 has an upward direction indicating that 'Syria" is shifting away from the 899 word war. On the other hand, the downward direction of "Russia" in the 2022 900 prediction supports our known knowledge that "Russia" moved closer to war. 901 For the second case study, our word of interest is **President**. We selected 902 some relevant words - "Obama", "Trump", "Biden", "Bernie", "Democrats", 903 and "Republicans" - which have been closely associated with the word President 904 based on our knowledge of US politics of the past decade. We used embeddings 905 from 2011 to 2020 for training and extrapolated the embeddings of 2021. 906

In figure 23(a), we observe that the embedding of the word "Obama" is the 907 most similar to the embedding of *President* in the year 2011. In the year 2016, 908 the embedding of the word "Trump" gains more similarity to the word President 909 as "Trump" was elected as the new president of the United States. On the other 910 hand, the similarity of the words "Biden" and "Bernie" started to increase in 911 the year 2018 as they were competing for the presidential candidate for the 912 election in the year 2020. The predicted embeddings in the year 2021 show that 913 the similarity of the embedding of the word "Biden" increases substantially, 914 and it becomes the second top closest neighbor between all the relevant words 915 in this study. Figure 23(b) shows that the position of "Biden" in the nearest 916

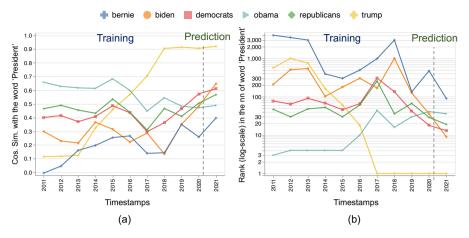


Fig. 23 Evolution of the neighborhood of the term *President* in the NYTimes dataset where the embeddings of words at timestamp 2021 is extrapolated using LSTM (a) cosine similarity between the embedding of the word *President* and relevant word embeddings at different timestamps. (b) Rank (position) of relevant words in the nearest neighborhood of the word *President* at different timestamps.

neighbors of *President* dropped significantly from 1000 to 9 in the last 3 years,
indicating that "Biden" quickly moved closer to the word *President*.

These case studies demonstrate that the predicted embeddings using an 919 LSTM-based prediction model can capture the trend in the training data and 920 provide well-explainable relationships between entities in a predicted embedding 921 space of a future timestamp. The performance of forecasting the embeddings 922 depends heavily on the ability of temporal embeddings to capture trends. In 923 section 5.1, we demonstrate that the state-of-the-art models cannot capture 924 changes in the context of words and cannot produce smooth transitions of word 925 similarity over time. While our temporal embedding model can capture the 926 change in the context and produce a smooth transition of embeddings, thus 927 performs well when extrapolated into the future embedding space. 928

929 6 Conclusions

This paper introduces a new technique to generate low-dimensional temporal 930 word embeddings for timestamped documents and predict a future embedding 931 space. We compare our temporal word embedding technique with other state-932 of-the-art techniques. Our temporal embeddings reflect a representation that: 933 (1) can track changes observed within a short period, (2) provides a smooth 934 evolution of the word vectors over a continuous temporal vector space, (3) uses 935 the concept of *diffusion* to capture trends better than the existing models, (4)936 is low-dimensional, and (5) performs well in capturing future neighborhoods of 937 words. Unlike previous dynamic embedding models, our proposed model creates 938 a homogeneous space over every timestamp of the embeddings. As a result, 939 the generated vectors of timestamps perform well in the prediction of a future 940

embedding space using conventional predictive models. The future direction
of our research is to automate hyperparameter tuning and study temporal
embedding models for images to learn text-image joint temporal embeddings.

₉₄₄ Statements and Declarations

Financial & Non-financial interests: The authors have no relevant financial or non-financial interests to disclose. All authors certify that they have no affiliations with or involvement in any organization or entity with any financial interest or non-financial interest in the subject matter or materials discussed in this manuscript. The authors have no financial or proprietary interests in any material discussed in this article.

• Conflicts of interest: The authors have no conflicts of interest to declare that are relevant to the content of this article.

953 **References**

- [1] Hamilton, W.L., Leskovec, J., Jurafsky, D.: Diachronic Word Embeddings Reveal Statistical Laws of Semantic Change. In: Proceedings of ACL, vol. 1, pp. 1489–1501. Association for Computational Linguistics, Berlin, Germany (2016). https://doi.org/10.18653/v1/P16-1141
- [2] Tang, X.: A State-of-the-Art of Semantic Change Computation. Natural Language Engineering, 1–28 (2018). https://doi.org/10.1017/ S1351324918000220
- [3] Rosin, G.D., Guy, I., Radinsky, K.: Time masking for temporal language
 models. In: Proceedings of the Fifteenth ACM International Conference
 on Web Search and Data Mining, pp. 833–841. Association for Computing
 Machinery, New York, NY, USA (2022). https://doi.org/10.1145/3488560.
 3498529
- Barranco, R.C., Dos Santos, R.F., Hossain, M.S., Akbar, M.: Tracking the
 evolution of words with time-reflective text representations. In: 2018 IEEE
 International Conference on Big Data (Big Data), pp. 2088–2097. IEEE,
 Seattle, WA, USA (2018). https://doi.org/10.1109/BigData.2018.8621902
- [5] Mikolov, T., Sutskever, I., Chen, K., Corrado, G., Dean, J.: Distributed representations of words and phrases and their compositionality. In: Proceedings of the 26th International Conference on Neural Information Processing Systems - Volume 2, pp. 3111–3119. Curran Associates Inc., Red Hook, NY, USA (2013)
- [6] Mikolov, T., Chen, K., Corrado, G., Dean, J.: Efficient estimation of word representations in vector space. CoRR abs/1301.3781 (2013). https: //doi.org/10.48550/arXiv.1301.3781

 Pennington, J., Socher, R., Manning, C.D.: Glove: Global vectors for word representation. In: Empirical Methods in Natural Language Processing (EMNLP), pp. 1532–1543 (2014). https://doi.org/10.3115/v1/D14-1162

[8] Devlin, J., Chang, M.-W., Lee, K., Toutanova, K.: BERT: Pre-training of deep bidirectional transformers for language understanding. In: Proceedings of the 2019 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, Volume 1 (Long and Short Papers), pp. 4171–4186. Association for Computational Linguistics, Minneapolis, Minnesota (2019). https: //doi.org/10.18653/v1/N19-1423

- [9] Bamler, R., Mandt, S.: Dynamic word embeddings. In: Precup, D., Teh,
 Y.W. (eds.) Proceedings of the 34th International Conference on Machine
 Learning. Proceedings of Machine Learning Research, vol. 70, pp. 380–389
 (2017)
- Yao, Z., Sun, Y., Ding, W., Rao, N., Xiong, H.: Dynamic word embeddings for evolving semantic discovery. In: Proceedings of the Eleventh ACM International Conference on Web Search and Data Mining, pp. 673–681. Association for Computing Machinery, New York, NY, USA (2018). https: //doi.org/10.1145/3159652.3159703
- [11] Rudolph, M., Blei, D.: Dynamic Embeddings for Language Evolution. In: Proceedings of the 2018 World Wide Web Conference, pp. 1003–1011.
 International World Wide Web Conferences Steering Committee, Republic and Canton of Geneva, CHE (2018). https://doi.org/10.1145/3178876.
 3185999
- [12] Di Carlo, V., Bianchi, F., Palmonari, M.: Training temporal word embeddings with a compass. Proceedings of the AAAI Conference on Artificial Intelligence 33(01), 6326–6334 (2019). https://doi.org/10.1609/aaai.v33i01.
 33016326
- [13] Aitchison, J.: Language Change: Progress or Decay?, 4th edn. Cambridge
 University Press, Cambridge (1981)
- [14] Yule, G.: The Study of Language, 6th edn. Cambridge University Press,
 Cambridge (2016). https://doi.org/10.1017/CBO9781316594131
- [15] Radinsky, K., Davidovich, S., Markovitch, S.: Learning causality for news
 events prediction. In: Proceedings of the 21st International Conference
 on World Wide Web, pp. 909–918. Association for Computing Machinery,
 New York, NY, USA (2012). https://doi.org/10.1145/2187836.2187958
- [16] Yogatama, D., Wang, C., Routledge, B.R., Smith, N.A., Xing, E.: Dynamic
 language models for streaming text. Transactions of the Association for

- Computational Linguistics **2**, 181–192 (2014). https://doi.org/10.1162/ tacl_a_00175
- [17] Tang, X., Qu, W., Chen, X.: Semantic change computation: A successive approach. In: Behavior and Social Computing, pp. 68–81. Springer, Cham (2013). https://doi.org/10.1007/978-3-319-04048-6_7
- [18] Naim, S.M., Boedihardjo, A.P., Hossain, M.S.: A scalable model for tracking topical evolution in large document collections. In: IEEE BigData, pp. 726-735 (2017). https://doi.org/10.1109/BigData.2017.8257988
- [19] Mihalcea, R., Nastase, V.: Word epoch disambiguation: Finding how words change over time. In: Proceedings of the 50th Annual Meeting of the Association for Computational Linguistics (Volume 2: Short Papers), pp. 259–263. Association for Computational Linguistics, Jeju Island, Korea (2012). https://aclanthology.org/P12-2051
- [20] Mitra, S., Mitra, R., Maity, S., Riedl, M., Biemann, C., Goyal, P., Mukherjee, A.: An automatic approach to identify word sense changes in text media
 across timescales. Natural Language Engineering 21, 773–798 (2015)
- [21] Barkan, O.: Bayesian neural word embedding. In: Proceedings of the Thirty-First AAAI Conference on Artificial Intelligence, pp. 3135–3143
 (2017)
- [22] Rosin, G.D., Adar, E., Radinsky, K.: Learning Word Relatedness over Time. In: Proceedings of the 2017 Conference on Empirical Methods in Natural Language Processing, pp. 1168–1178. Association for Computational Linguistics, Copenhagen, Denmark (2017). https://doi.org/10.
 18653/v1/D17-1121
- [23] Angulo, J., Pederneiras, C., Ebner, W., Kimura, E., Megale, P.: Concepts of diffusion theory and a graphic approach to the description of the epidemic flow of contagious disease. Public Health Rep **95**(5), 478–485 (1980)
- [24] McGovern, A., Rosendahl, D.H., Brown, R.A., Droegemeier, K.K.: Identifying predictive multi-dimensional time series motifs: an application to
 severe weather prediction. Data Mining and Knowledge Discovery 22(1-2),
 232-258 (2011)
- [25] Matsubara, Y., Sakurai, Y., Faloutsos, C.: AutoPlait: Automatic Mining of Co-evolving Time Sequences. In: Proceedings of the 2014 ACM SIGMOD International Conference on Management of Data, pp. 193–204. ACM, New York, NY, USA (2014). https://doi.org/10.1145/2588555.2588556
- [26] Yu, H.-F., Rao, N., Dhillon, I.S.: High-dimensional Time Series Prediction
 with Missing Values. arXiv (2015). https://doi.org/10.48550/ARXIV.1509.

- 1053 08333
- [27] Yu, H.-F., Rao, N., Dhillon, I.S.: Temporal regularized matrix factorization for high-dimensional time series prediction. In: Proceedings of the 30th International Conference on Neural Information Processing Systems.
 NIPS'16, pp. 847–855. Curran Associates Inc., Red Hook, NY, USA (2016)
- [28] Saha, T.K., Williams, T., Hasan, M.A., Joty, S., Varberg, N.K.: Models
 for Capturing Temporal Smoothness in Evolving Networks for Learning
 Latent Representation of Nodes. arXiv (2018). https://doi.org/10.48550/
 ARXIV.1804.05816
- [29] Kumar, S., Zhang, X., Leskovec, J.: Predicting dynamic embedding trajectory in temporal interaction networks. In: Proceedings of the 25th ACM
 SIGKDD International Conference on Knowledge Discovery & Data Mining, pp. 1269–1278. Association for Computing Machinery, New York, NY, USA (2019). https://doi.org/10.1145/3292500.3330895
- [30] Kutuzov, A.: Distributional word embeddings in modeling diachronic
 semantic change. PhD thesis, University of Oslo (2020). http://urn.nb.no/
 URN:NBN:no-84130
- [31] Hochreiter, S., Schmidhuber, J.: Long short-term memory. Neural Computation 9(8), 1735–1780 (1997). https://doi.org/10.1162/neco.1997.9.8.
 1735
- [32] Cho, K., van Merriënboer, B., Gulcehre, C., Bahdanau, D., Bougares,
 F., Schwenk, H., Bengio, Y.: Learning phrase representations using RNN
 encoder-decoder for statistical machine translation, 1724–1734 (2014).
 https://doi.org/10.3115/v1/D14-1179
- [33] Bahdanau, D., Cho, K., Bengio, Y.: Neural Machine Translation by Jointly Learning to Align and Translate. arXiv:1409.0473 [cs, stat] (2014). https: //doi.org/10.48550/ARXIV.1409.0473
- [34] Vaswani, A., Shazeer, N., Parmar, N., Uszkoreit, J., Jones, L., Gomez,
 A.N., Kaiser, L., Polosukhin, I.: Attention is all you need. In: Advances in
 Neural Information Processing Systems, pp. 6000–6010. Curran Associates
 Inc., Red Hook, NY, USA (2017)
- [35] Sutskever, I., Vinyals, O., Le, Q.V.: Sequence to sequence learning with
 neural networks, pp. 3104–3112. MIT Press, Cambridge, MA, USA (2014)
- [36] Wang, L.L., Lo, K., Chandrasekhar, Y., Reas, R., Yang, J., Burdick, D.,
 Eide, D., Funk, K., Katsis, Y., Kinney, R.M., Li, Y., Liu, Z., Merrill, W.,
 Mooney, P., Murdick, D.A., Rishi, D., Sheehan, J., Shen, Z., Stilson, B.,
 Wade, A.D., Wang, K., Wang, N.X.R., Wilhelm, C., Xie, B., Raymond,

D.M., Weld, D.S., Etzioni, O., Kohlmeier, S.: CORD-19: The COVID-19
 Open Research Dataset. Association for Computational Linguistics, Online
 (2020). https://aclanthology.org/2020.nlpcovid19-acl.1

[37] Montani, I., Honnibal, M., Honnibal, M., Landeghem, S.V., Boyd, A.,
Peters, H., McCann, P.O., jim geovedi, O'Regan, J., Samsonov, M., Altinok,
D., Orosz, G., de Kok, D., Kristiansen, S.L., Bournhonesque, R., Kannan,
M., Miranda, L., Baumgartner, P., Edward, Bot, E., Hudson, R., Roman,
Fiedler, L., Mitsch, R., Daniels, R., Howard, G., Phatthiyaphaibun, W.,
Tamura, Y., Bozek, S.: explosion/spaCy: v3.4.3: Extended Typer support
and bug fixes. Zenodo (2022). https://doi.org/10.5281/zenodo.7310816

[38] Neumann, M., King, D., Beltagy, I., Ammar, W.: ScispaCy: Fast and robust models for biomedical natural language processing. In: Proceedings of the 18th BioNLP Workshop and Shared Task, pp. 319–327. Association for Computational Linguistics, Florence, Italy (2019). https://doi.org/10.
18653/v1/W19-5034

- [39] Steffens, I.: A hundred days into the coronavirus disease (COVID-19)
 pandemic. Euro Surveill. 25(14) (2020)
- [40] Sullivan, S.J., Jacobson, R.M., Dowdle, W.R., Poland, G.A.: 2009 H1N1
 influenza. Mayo Clin. Proc. 85(1), 64–76 (2010)

 [41] Cucinotta, D., Vanelli, M.: Who declares covid-19 a pandemic. Acta biomedica : Atenei Parmensis 91(1), 157–160 (2020). https://doi.org/10.
 23750/abm.v91i1.9397

- [42] Tosun, O.K., Eshraghi, A.: Corporate decisions in times of war: Evidence
 from the russia-ukraine conflict. Finance Research Letters 48, 102920
 (2022). https://doi.org/10.1016/j.frl.2022.102920
- [43] Alsentzer, E., Murphy, J., Boag, W., Weng, W.-H., Jindi, D., Naumann,
 T., McDermott, M.: Publicly available clinical BERT embeddings. In:
 Proceedings of the 2nd Clinical Natural Language Processing Workshop, pp.
 72–78. Association for Computational Linguistics, Minneapolis, Minnesota,
 USA (2019). https://doi.org/10.18653/v1/W19-1909
- [44] Bhargava, P., Drozd, A., Rogers, A.: Generalization in NLI: Ways (Not) To
 Go Beyond Simple Heuristics. Association for Computational Linguistics,
 Online and Punta Cana, Dominican Republic (2021). https://doi.org/10.
 18653/v1/2021.insights-1.18

[45] Turc, I., Chang, M., Lee, K., Toutanova, K.: Well-read students learn better: The impact of student initialization on knowledge distillation. CoRR abs/1908.08962 (2019). https://doi.org/10.48550/arXiv.1908.08962

- [46] Byron, L., Wattenberg, M.: Stacked graphs geometry & aesthetics. IEEE
 Transactions on Visualization and Computer Graphics 14(6), 1245–1252
 (2008). https://doi.org/10.1109/TVCG.2008.166
- [47] PubMed. U.S. National Library of Medicine, Bethesda, Maryland. https://pubmed.ncbi.nlm.nih.gov/
- [48] Booth, H., Rike, D., Witte, G.A.: The National Vulnerability Database
 (NVD): Overview. NIST Pubs, National Institute of Standards
 and Technology (December 2013). https://www.nist.gov/publications/
 national-vulnerability-database-nvd-overview
- [49] Verma, R.: US-Taliban peace deal and regional powers as potential spoilers:
 Iran as a case study. International Politics 59(2), 260–279 (2022). https:
 //doi.org/10.1057/s41311-021-00302-7
- ¹¹³⁹ [50] Boni, F.: Afghanistan 2021: Us withdrawal, the taliban return and regional ¹¹⁴⁰ geopolitics. Asia Maior **XXXII**, 375–391 (2022)