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# **Combining principal component analysis and the evidential reasoning approach for healthcare quality assessment**

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## Abstract

Patient experience and satisfaction surveys have been adopted worldwide to evaluate healthcare quality. Nevertheless, national governments and the general public continue to search for optimal methods to assess healthcare quality from the patient's perspective. This study proposes a new hybrid method, which combines principal component analysis (PCA) and the evidential reasoning (ER) approach, for assessing patient satisfaction. PCA is utilized to transform correlated items into a few uncorrelated principal components (PCs). Then, the ER approach is employed to aggregate extracted PCs, which are considered as multiple attributes or criteria within the ER framework. To compare the performance of the proposed method with that of another assessment method, analytic hierarchy process (AHP) is employed to acquire the weight of each assessment item in the hierarchical assessment framework, and the ER approach is used to aggregate patient evaluation for each item. Compared with the combined AHP and ER approach, which relies on the respondents' subjective judgments to calculate criterion and subcriterion weights in the assessment framework, the proposed method is highly objective and completely based on survey data. This study contributes a novel and innovative hybrid method that can help hospital administrators obtain an objective and aggregated healthcare quality assessment based on patient experience.

**Keywords:** Healthcare quality assessment, patient experience and satisfaction, principal component analysis, analytic hierarchy process, the evidential reasoning approach

## 1. Background

Healthcare quality assessment has become a crucial topic of healthcare studies given that it will help ensure the proper allocation of limited healthcare resources in the face of continuously increasing healthcare demands and costs and standardize medical practice (Büyüközkan & Çifçi 2012, Büyüközkan et al 2011, Fragkiadakis et al 2016, Kong et al 2015, Lyratzopoulos et al 2011, Panagiotis et al 2016, Prior 2006). Patient experience is an important healthcare outcome, and surveys that measure patient experience and satisfaction are currently widely used to assess healthcare quality (Department of Health 2013, Jenkinson et al 2002, Jha et al 2008, Keller et al 2005, Kleefstra et al 2010, Vuković et al 2012). Governments and regulatory authorities in some countries now require hospitals to organize patient surveys at regular intervals (Jenkinson et al 2002). In the United States (US), some policy initiatives have attached financial incentives, such as directly linking patients' evaluations with doctors' financial rewards, to patient surveys (Rodriguez et al 2009). In the United Kingdom (UK), the Department of Health (2000) has launched a program of national surveys and has required every National Health Service (NHS) Trust to survey their patients annually. In Switzerland, the National Coordination and Information Office for Quality Improvement has recommended that a survey instrument be administered to hundreds of hospitals on an annual basis (Jenkinson et al 2002). In Australia, a national patient experience survey is conducted annually (Department of Health 2013). In China, the national government launched a new wave of healthcare reform in 2009 to reduce healthcare costs and improve healthcare quality and patient safety. To achieve these goals, the current healthcare strategy in China links the healthcare quality of hospitals

1 with the allocation of healthcare resources, such as government funding. The National  
2 Health and Family Planning Commission of China requires that a patient experience  
3 survey be an integral component of healthcare quality assessment.

4 A review of the literature shows that in different countries and regions, different  
5 questionnaires have been used to measure healthcare quality from different dimensions.

6 In the US, the Centers for Medicare and Medicaid Services has collaborated with the  
7 Agency for Healthcare Research and Quality to develop a standardized patient  
8 satisfaction questionnaire, the Consumer Assessment of Health Providers and Systems,  
9 for measuring the quality of inpatient hospital care (Goldstein et al 2005, Jha et al 2008).

10 In the UK, the Picker Patient Experience questionnaire is used to measure patients'  
11 experiences of inpatient care (Jenkinson et al 2003, Keller et al 2014). This  
12 questionnaire is given annually to survey the quality of inpatient care provided by all  
13 hospitals belonging to the NHS system. Moreover, since 2000, the Department of  
14 Health has required that the results of the survey must be reported in an annual patient  
15 prospectus. Until 2013, the Victoria Patient Satisfaction Monitor was the most widely  
16 used inpatient satisfaction questionnaire in Australia. This questionnaire has now been

17 replaced by the Victorian Health Experience Measurement Instrument (Department of  
18 Health 2013). In the Netherlands, eight academic hospitals have developed a Core  
19 Questionnaire for the Assessment of Patient Satisfaction (COPS) (Kleefstra et al 2010).

20 The Federation of Dutch Hospitals has accepted COPS as a standard instrument for  
21 measuring patient satisfaction. The main healthcare dimensions measured by the above  
22 questionnaires include: doctor–patient or nurse–patient communication; staff

1 responsiveness; environmental cleanliness and noise level; pain control or physical  
2 comfort; drug, admission, or discharge information communication; and overall  
3 satisfaction.

4 Different statistical methods have been employed to analyze survey data for patient  
5 experience. Spearman correlation analysis has been used to analyze the relationships  
6 between survey items and overall evaluation (Jenkinson et al 2002, Keller et al 2014).  
7 Cronbach's  $\alpha$  coefficient has been used to measure the internal consistency and  
8 reliability of questionnaires (Harris et al 1999, Keller et al 2005, Purcărea et al 2013,  
9 Vuković et al 2012). Exploratory and confirmatory factor analyses have been used to  
10 explore and validate the structure of the measured dimensions and items of  
11 questionnaires (Harris et al 1999, Keller et al 2014, Keller et al 2005). Regression  
12 models have been used to determine the impact of individual items on overall quality  
13 evaluation (Vuković et al 2012, Wong et al 2011). Multidimensional scaling has been  
14 used to identify similarities and dissimilarities among items in questionnaires (Vuković  
15 et al 2012), and principal component analysis (PCA) has been used to identify the main  
16 healthcare dimensions and their relationships with individual measured items from  
17 survey data (Purcărea et al 2013, Vuković et al 2012).

18 However, all the above statistical methods are for questionnaire validation or total-  
19 item relationship exploration, and advanced decision models that combine patient  
20 assessments or evaluations of different items or variables are needed to measure and  
21 evaluate overall healthcare quality. Driven by the need for the combined or integrated

1 assessment of overall healthcare quality, Behara et al. (2002) and Carlucci et al. (2013)  
2 used an artificial neural network (ANN) to model and obtain an overall evaluation from  
3 patient assessments of different healthcare dimensions. Büyüközkan et al. (2011)  
4 extended the traditional analytic hierarchy process (AHP) methodology to a fuzzy AHP  
5 to combine subjective and vague judgments of multiple healthcare quality indices or  
6 items. Büyüközkan and Çifçi (2012) combined a fuzzy AHP and a fuzzy technique for  
7 order of preference by similarity to ideal solution (TOPSIS) to aggregate patient  
8 assessments of multiple quality items. However, these combined assessment methods  
9 have their shortcomings. Specifically, an ANN contains nonlinear functions and is a  
10 black-box for users; these characteristics complicate its adoption by healthcare  
11 practitioners. Although the fuzzy AHP method extends the traditional AHP method to  
12 vague subjective judgments of multiple criteria and has the advantage of converting  
13 subjective judgments to numerical values, it contains the problem of rank reversal.  
14 Similar to the fuzzy AHP method, the fuzzy TOPSIS method has the advantage of  
15 handling fuzzy judgments of multiple criteria and the problem of rank reversal, which  
16 means that the ranking of alternatives may change when new alternatives are added. In  
17 our previous study (Kong et al 2015), we proposed using the evidential reasoning (ER)  
18 approach (Wang et al 2006, Xu 2012, Yang & Singh 1994) to combine objective quality  
19 indicators, subjective expert judgments, and patient feedback to provide an overall  
20 assessment of healthcare quality. The ER approach requires that the items measured or  
21 assessed in a questionnaire should be uncorrelated if their assessments are combined to  
22 obtain an overall quality assessment. In our previous study, we considered that patient

1 evaluations on four items—medical facilities, medical staff, medical processes, and  
2 medical outcomes in a hospital—are independent of each other. Thus, the ER approach  
3 is suitable for combining patient assessments of these four items. However, most patient  
4 experience surveys for measuring healthcare quality include dozens of items, and some  
5 items are correlated to some degree. In this situation, applying the ER approach directly  
6 to combine assessments of individual items to obtain an overall quality assessment is  
7 irrational.

8 In the present study, we propose combining PCA (Jolliffe 2002) and the ER  
9 approach to aggregate patient assessments of multiple correlated items for overall  
10 healthcare quality assessment. PCA helps transform original interrelated variables into  
11 a new set of uncorrelated variables, the new principal components (PCs). The weights  
12 of these PCs are then determined in accordance with the amount of variance that each  
13 PC accounts for in the dataset. The weighted uncorrelated PCs are then used as new  
14 quality criterion variables and are combined through the ER approach to obtain an  
15 overall healthcare quality assessment. Meanwhile, to compare the performance of the  
16 proposed method with that of another method, AHP is employed to acquire the weights  
17 of different healthcare quality dimensions and their corresponding survey items, and  
18 the ER approach is then used to aggregate the patient evaluation of each item.

19 The rest of this paper is structured as follows. The materials and methods used in  
20 this study are discussed in Section 2. The questionnaire is introduced in Section 2.1.  
21 The collected survey data are briefly discussed in Section 2.2. Brief introductions to



1 PCA, AHP, and the ER approach are provided in Sections 2.3, 2.4, and 2.5, respectively.  
2 The combined PCA and ER approach for the aggregation of patient assessments is  
3 introduced in Section 2.6. The combined AHP and ER approach for the aggregation of  
4 patient evaluations is described in Section 2.7. In addition to the characteristics of the  
5 survey data, the extracted PCs together with corresponding observable variables or  
6 items with significant component loadings, the weight of each extracted PC, the weights  
7 of different quality dimensions and corresponding survey items calculated via AHP,  
8 and the overall quality assessment results of both methods are presented in Section 3.  
9 Finally, a summary of this study and a discussion of the findings is provided in Section  
10 4.

## 11 **2. Materials and methods**

### 12 **2.1. Questionnaire**

13 We developed a questionnaire in reference to survey instruments for patient experience  
14 that have been used in the UK, the US, the Netherlands, and Australia. In addition to  
15 demographic information about the respondents, the questionnaire provides one overall  
16 rating of healthcare quality. It contains 25 items that measure healthcare quality from  
17 various aspects or dimensions, such as hospital environment, waiting time,  
18 communication with doctors, communication with nurses, care coordination, physical  
19 comfort, emotional support, respect for patient preferences, family and friend  
20 involvement, and drug information. For each item, typical five-point Likert-type scale  
21 responses (“very dissatisfied,” “dissatisfied,” “fair,” “satisfied,” and “very satisfied,”)  
22 were adopted. Occasionally, “not applicable” was recorded by the researchers if the

patients did not experience the problem associated with the question item. We coded “not applicable” responses as missing. For the overall rating of the healthcare quality, the satisfaction score of 0–10 was applied, where a score of 10 refers to the highest level of satisfaction.

## **2.2. Dataset**

Between August and September 2014, all patients at the point of discharge from one department of a top-tier teaching hospital affiliated with Peking University (hereafter referred to as Hospital A), Beijing, China, received questionnaires assessing the quality of the healthcare they received on the basis of on their in-hospital experiences. All questionnaires were completed anonymously, and one of our researchers helped respondents eliminate worries about the consequences of their responses and provided instructions on answering the questionnaires. A total of 213 surveys were collected from the hospital. We did not send questionnaires to patients who were unwilling to give us their responses or assessments of received healthcare.

We preprocessed the data from the 213 collected surveys as follows. First, if the response rate for an item was lower than 90%, we excluded the item from data analysis. Second, we excluded a patient’s survey data from the analysis if his or her responses to two or more items were “not applicable.” Third, we calculated the median value for each item and used the median value to replace the missing data of items retained for analysis. Fourth, we employed Spearman correlation analysis to explore the item-total relationship and excluded items with correlation coefficients with values less than 0.3.

After data preprocessing, we obtained 192 valid surveys with six deleted items.

### 2.3. PCA

PCA is a multivariate statistical approach commonly used to reduce the dimensions of a dataset that consists of interrelated single indicators or variables. It is a linear combination of variables that explains the variance structure of a matrix and reduces various data into a few PCs. It focuses on the use of a few PCs to reveal the internal structure among multiple observable variables that are uncorrelated with each other and allows the PCs to preserve the information embodied in original variables as much as possible.

Let  $x$  be a vector of  $p$  random variables, and the variances of  $p$  variables and structures of the covariances or correlations between  $p$  variables are considered of interest. Consider  $X$  is a  $(n \times p)$  matrix with  $n$  observations on  $p$  variables, and  $K$  is the covariance matrix of the random vector  $x$  with eigenvalues  $\lambda_1 \geq \lambda_2 \geq \dots \geq \lambda_p \geq 0$ , and eigenvectors  $\alpha_1, \alpha_2, \dots, \alpha_p$ . PCs are derived from the  $X$  matrix with the following linear functions  $\alpha'_j x$  ( $j = 1, 2, \dots, p$ ) of the elements of  $x$ , and the extracted PCs have maximum variance with constraints of  $\alpha'_j x$  being uncorrelated, i.e.,  $Cov[\alpha'_i x, \alpha'_j x] = 0, (i \neq j)$  (Jolliffe 2002, Park et al 2015). The mathematical framework of PCA is as follows:

$$Z_1 = \alpha'_1 x = \alpha_{11}x_1 + \alpha_{12}x_2 + \dots + \alpha_{1p}x_p = \sum_{j=1}^p \alpha_{1j}x_j \quad (1)$$

$$Z_2 = \alpha'_2 x = \alpha_{21}x_1 + \alpha_{22}x_2 + \dots + \alpha_{2p}x_p = \sum_{j=1}^p \alpha_{2j}x_j \quad (2)$$

$\vdots$

$$Z_p = \alpha'_p x = \alpha_{p1}x_1 + \alpha_{p2}x_2 + \dots + \alpha_{pp}x_p = \sum_{j=1}^p \alpha_{pj}x_j \quad (3)$$

$$1 \quad Var[Z_i] = \alpha_i' K \alpha_i, i = 1, 2, \dots, p \quad (4)$$

$$2 \quad Cov[Z_i, Z_j] = \alpha_i' K \alpha_j, i = 1, 2, \dots, p; j = 1, 2, \dots, p \quad (5)$$

3 where  $\alpha_j$  is a vector of  $p$  coefficients  $\alpha_{j1}, \alpha_{j2}, \dots, \alpha_{jp}$ , and  $\alpha_j$  is nothing but the  
4 eigenvector of covariance matrix  $K$  that corresponds to the  $j$ th largest eigenvalue  $\lambda_j$ .

5  $Z_i (i = 1, 2, \dots, p)$  represents PCs and “’” represents the transposition operation. The

6 first linear function  $\alpha_1' x$  finds the first PC,  $Z_1$ , that accounts for the maximal amount  
7 of total variance in the dataset. The second PC,  $Z_2$ , is uncorrelated with  $Z_1$  and

8 accounts for the maximal amount of variance in the dataset that is not accounted for by

9 the first component, such that at the  $k$ th stage, a linear function  $\alpha_k' x$  is found that has

10 maximum variance subject to being uncorrelated with  $\alpha_1' x, \alpha_2' x, \dots, \alpha_{k-1}' x$ . The  $k$ th

11 derived variable,  $\alpha_k' x$ , is the  $k$ th PC. Up to  $p$  PCs can be found but in general most of

12 the variation in  $x$  will be accounted for by  $m$  PCs where  $m \leq p$ . The elements in the

13 diagonal of the covariance matrix of the derived PCs are known as the eigenvalues

14  $\lambda_i (i = 1, 2, \dots, p)$  with  $\lambda_1 \geq \lambda_2 \geq \dots \geq \lambda_p \geq 0$ , which are the variance explained by

15 each PC and are constrained to decrease monotonically from the first PC to the last.

16 The coefficient  $\alpha_{ij} (i = 1, 2, \dots, p; j = 1, 2, \dots, p)$  is the element of the eigenvector and

17 is known as the loading or weight of the  $j$ th original variable for the  $i$ th PC (Jolliffe

18 2002). The importance or weight of each PC can be determined on the basis of the

19 amount of variance that it accounts for in the dataset.

20 After extracting PCs from the original dataset through linear transformation, we

21 need to understand the extracted PCs or determine which variables load significantly

22 on which component to retain only loadings that are statistically significant for each

PC. Thus, we have to identify which variable loadings are significant and which can be safely ignored for each component. Usually, rotating the extracted components can help identify the variables that load strongly on each component (Norman & Streiner 1998). Therefore, the value or score of the extracted PCs can be computed from original variables by multiplying the standardized values of variables by their corresponding weights or coefficients. Sometimes, the values of extracted PCs can be computed only from variables with significant loadings (Norman & Streiner 1998).

#### **2.4. AHP**

AHP was first developed in 1971 by Thomas Saaty (Saaty 1980). It is a multicriterion decision analysis method in which a complex, multicriterion problem is decomposed into multiple levels of hierarchy with the top level as the goal, intermediate levels as the criteria and subcriteria, and the lowest level offers alternatives; a hierarchal structure is thus formed for assessment (Saaty 1980). The relative importance of all criteria and subcriteria within each level of hierarchy is usually determined by expert judgment and calculated through pairwise comparisons (Saaty 2008).

The typical application of AHP includes four main stages. First, a hierarchy of criteria used for assessment needs to be developed. Second, a pairwise comparison survey is conducted to elicit the preferences of respondents. At this stage, a pairwise comparison matrix is formed where  $w_i/w_j$  measures the importance of criterion  $i$  relative to  $j$ . Typically, a nine-point scale is used where 1 means equal importance between two criteria, and 9 means the extreme importance of one criterion compared with another. Third, the consistency of respondents' judgments in pairwise

1 comparison is checked. Numerous methods, such as Eigenvalue method and geometric  
2 mean, are used to calculate the normalized weights of each criterion (Morgan 2017). In  
3 this study, we employed the Eigenvalue method for calculation. In the Eigenvalue  
4 method, a consistency ratio (CR) is employed to measure the consistency of individual  
5 responses, where 0 means perfect consistency in the responses given by an respondent  
6 and a CR value of 10% or less indicates that the pairwise comparison matrix is  
7 acceptable (Ishizaka et al 2010). Finally, the relative importance of each criterion in the  
8 hierarchy is calculated.

## 9 **2.5. The ER approach**

10 The ER approach (Xu 2012, Yang & Singh 1994, Yang & Xu 2002) was originally  
11 proposed to aid multiple attribute decision analysis (MADA) problems. It has the  
12 advantage of dealing with qualitative and quantitative attributes under uncertainty  
13 (Yang 2001, Yang & Xu 2002). It has been employed to aid medical decision-making,  
14 such as the assessment of clinical risk associated with cardiac chest pain (Kong et al  
15 2009, Kong et al 2012) and combined healthcare quality assessment(Kong et al 2015).

16 We assume  $N$  alternatives  $D_1, D_2, \dots, D_N$  exist that need to be assessed on the basis  
17 of  $L$  individual attributes or indicators  $A(A_1, A_2, \dots, A_L)$ , which are uncorrelated. The  
18  $j$ th attribute  $A_j (j = 1, 2, \dots, L)$  can either be qualitative or quantitative, and each  
19 attribute  $A_j$  can be assessed through a set of assessment grades  $H(H_1, H_2, \dots, H_M)$ ,  
20 which are assumed to be collectively exhaustive and mutually exclusive. Instead of  
21 using a certain score that represents an assessment grade to denote the evaluation of an  
22 alternative on an individual indicator in conventional MADA methods, a belief

1 distribution, such as  $\{(\beta_1, H_1), (\beta_2, H_2), \dots, (\beta_M, H_M)\}$ , can be used to express an  
 2 evaluation of an indicator that is distributed on a fixed set of assessment grades  $H$ .  
 3 Considering the relative importance or weight  $\omega_j (j = 1, 2, \dots, L)$  of each measured  
 4 attribute or indicator, a MADA problem can be modeled by the ER approach, as shown  
 5 in Fig. 1, where  $\beta_{tj} (t = 1, 2, \dots, M; j = 1, 2, \dots, L)$  is used to denote the degree of  
 6 belief in the  $t$ th assessment grade  $H_t$  for assessing the  $j$ th attribute  $A_j$ . The belief  
 7 degree can either be subjective if it quantifies a “personal belief” or objective if it is a  
 8 computed probability on the basis of recorded data.

---

9 INSERT FIGURE 1 HERE

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10 The core of the ER approach is the ER algorithm, which is used to aggregate the  
 11 distributed assessments of all attributes or indicators and generate a combined  
 12 assessment of an alternative. A brief introduction to the ER algorithm is provided below.

13 First of all, the degrees of belief  $\beta_{tj} (t = 1, 2, \dots, M; j = 1, 2, \dots, L)$  are  
 14 transformed into basic probability masses by combining the relative weights and the  
 15 degrees of belief using the following equations:

$$16 \quad m_{t,j} = w_j \beta_{tj}, t = 1, 2, \dots, M; j = 1, 2, \dots, L \quad (6)$$

$$17 \quad m_{H,j} = 1 - \sum_{t=1}^M m_{t,j} = 1 - w_j \sum_{t=1}^M \beta_{tj}, j = 1, 2, \dots, L \quad (7)$$

$$18 \quad \bar{m}_{H,j} = 1 - w_j, j = 1, 2, \dots, L \quad (8)$$

$$19 \quad \tilde{m}_{H,j} = w_j (1 - \sum_{t=1}^M \beta_{tj}), j = 1, 2, \dots, L \quad (9)$$

20 where  $m_{H,j} = \bar{m}_{H,j} + \tilde{m}_{H,j}$  for all  $j = 1, 2, \dots, L$  and  $\sum_{j=1}^L w_j = 1$ .  $m_{t,j}$  represents the  
 21 basic probability mass of an alternative being assessed to the assessment grade  $H_t$  on

1 attribute  $A_j$ . Note that the probability mass assigned to the grade set  $H$ ,  $m_{H,j}$ , which is  
 2 currently unassigned to any individual grades, is split into two parts:  $\bar{m}_{H,j}$  and  $\tilde{m}_{H,j}$ .  
 3  $\bar{m}_{H,j}$  is caused by the relative importance of the  $j$ th attribute  $A_j$  and  $\tilde{m}_{H,j}$  is caused  
 4 by the incompleteness of the  $j$ th attribute  $A_j$ .  $\bar{m}_{H,j}$  represents the contribution of other  
 5 attributes to assessing an alternative and is the proportion of beliefs that remain to be  
 6 assigned in accordance with the assessment of other attributes. In essence,  $\bar{m}_{H,j}$   
 7 provides a scope for conflict resolution in the presence of conflicting evidence.  $\tilde{m}_{H,j}$   
 8 will be zero if ignorance is absent from the assessment.

9 Subsequently, all the distributed assessments on  $L$  attributes or indicators are  
 10 aggregated to generate the combined degree of belief in each possible grade  $H_t$ . The  
 11 analytic format of the ER aggregation algorithm (Wang et al 2006) is as follows:

$$12 \quad m_t = k[\prod_{j=1}^L(m_{t,j} + \bar{m}_{H,j} + \tilde{m}_{H,j}) - \prod_{j=1}^L(\bar{m}_{H,j} + \tilde{m}_{H,j})], t = 1, 2, \dots, M \quad (10)$$

$$13 \quad \tilde{m}_H = k[\prod_{j=1}^L(\bar{m}_{H,j} + \tilde{m}_{H,j}) - \prod_{j=1}^L \bar{m}_{H,j}] \quad (11)$$

$$14 \quad \bar{m}_H = k[\prod_{j=1}^L \bar{m}_{H,j}] \quad (12)$$

$$15 \quad k = [\sum_{t=1}^M \prod_{j=1}^L(m_{t,j} + \bar{m}_{H,j} + \tilde{m}_{H,j}) - (M - 1) \prod_{j=1}^L(\bar{m}_{H,j} + \tilde{m}_{H,j})]^{-1} \quad (13)$$

$$16 \quad \beta_t = \frac{m_t}{1 - \bar{m}_H}, t = 1, 2, \dots, M \quad (14)$$

$$17 \quad \beta_H = \frac{\tilde{m}_H}{1 - \bar{m}_H} \quad (15)$$

18 where  $\beta_t$  and  $\beta_H$  represent the belief degrees of the aggregated assessment to which  
 19 an alternative is assessed to grade  $H_t$  and  $H$ , respectively, after combining the  
 20 distributed assessments on all indicators. The combined assessment of an alternative  
 21 can be denoted by  $S(y) = \{(H_t, \beta_t), t = 1, 2, \dots, M\}$ .  $\sum_{t=1}^M \beta_t + \beta_H = 1$  has been



proven (Yang & Xu 2002).

## **2.6. Combining PCA and the ER approach to assess healthcare quality**

As discussed in Sections 2.3 and 2.5, PCA has the advantage of transforming multiple interrelated indicators into a few uncorrelated PCs, and the ER approach has the advantage of combining the distributed assessments of multiple uncorrelated indicators under uncertainty. The combined PCA and ER approach can help rationally use collected survey data to provide an objective and aggregated healthcare quality assessment based on patient experience. The detailed procedures for combining PCA with the ER approach to assess the quality of healthcare provided by Hospital A are as follows:

First, numerical scores are used to replace the five-point Likert-type scales used in the survey. Specifically, a value of 1 is assigned to “very dissatisfied,” 2 to “dissatisfied,” 3 to “fair,” 4 to “satisfied,” and 5 to “very satisfied.” In this study, we obtained a numerical matrix  $A(192 \times 19)$  after excluding unqualified patient surveys, and each item  $a_{ij}(i = 1, 2, \dots, 192; j = 1, 2, \dots, 19)$  in the matrix ranges from 1 to 5.

Second, a preliminary statistical test, the Kaiser–Meyer–Olkin (KMO) index, accompanied by Bartlett’s test of Sphericity, should be employed to examine whether items in the survey dataset are interrelated. Moreover, the KMO test must have values higher than 0.5 and Bartlett’s test must be significant at a level lower than 0.05 (Purcărea et al 2013).

Third, if the survey dataset is suitable for PCA, PCA can be used to analyze the

1 dataset and derive the PCs that can be used as uncorrelated criterion variables for an  
2 aggregated quality assessment. We employed SPSS software to perform PCA. SPSS  
3 provides two options for performing PCA: “correlation matrix” and “covariance matrix.”  
4 The default setting is “correlation matrix,” and we usually use the default “correlation  
5 matrix” to perform PCA. Nevertheless, if the original dataset has been standardized,  
6 performing PCA with the “covariance matrix” will yield the same results as the  
7 “correlation matrix”.

8 Fourth, PCs are extracted from PCA. Generally, three methods are used to extract  
9 PCs. One method is based on the eigenvalue of each PC, and PCs with eigenvalues  
10 larger than 1 can be extracted as final PCs for subsequent analysis. One method is based  
11 on the researchers’ subjective judgments of the number of PCs that need to be extracted.  
12 Thus, a fixed number of PCs can be extracted. Another method to determine the number  
13 of PCs that can be extracted is based on the cumulative variance for which all extracted  
14 PCs can account for. In this method, a threshold value is set for the cumulative variance  
15 proportion, and the number of PCs can then be determined if the cumulative variance  
16 of combined PCs has reached this threshold value. In this study, we set the threshold  
17 value of the cumulative variance proportion at 70%.

18 Fifth, weights that correspond to the extracted PCs are calculated for later  
19 aggregation using the ER approach. In our case, we employed the eigenvalues that  
20 correspond to the extracted PCs to calculate the weight of each PC. Given that only a  
21 proportion of PCs have been extracted to represent all the original surveyed items, we

1 normalized the eigenvalues of the extracted PCs to obtain the weights of the  
 2 corresponding PCs for later assessment aggregation. Assuming that  $m$  PCs have been  
 3 extracted, and the corresponding eigenvalues are  $\lambda_i (i = 1, 2, \dots, m)$ , the weight  
 4 associated with each extracted PC is calculated using the following:

$$5 \quad w_i = \frac{\lambda_i}{\sum_{i=1}^m \lambda_i}, (i = 1, 2, \dots, m) \quad (16)$$

6 Sixth, variables that strongly load on each extracted PC are discovered, and the  
 7 assessments distributed on different evaluation grades for each PC are computed. The  
 8 identification of variables with significant loadings on a specific component is based  
 9 on the rotated component matrix generated by SPSS through PCA. Using the rotated  
 10 component matrix, we can identify the variables are interrelated and have strong  
 11 correlations with specific PCs. The distributed assessment of each PC is computed on  
 12 the basis of the component score coefficient matrix  $A(m * p)$  produced through PCA  
 13 and generated by SPSS, and the inner logic of the computation is described as in  
 14 equations (1), (2), (3), (4), and (5). The component score coefficient matrix  $A(m * p)$   
 15 contains  $m * p$  coefficients  $\alpha_{ij} (i = 1, 2, \dots, m; j = 1, 2, \dots, p)$  that represent the  
 16 weight or loading of the  $j$ th original variable for the  $i$ th extracted PC, where  $m$  is the  
 17 number of extracted PCs and  $p$  is the number of surveyed items in the dataset for  
 18 analysis. In this study, to compute the distributed assessment of each extracted PC, we  
 19 ignore variables without significant loadings on the PC and employ only variables that  
 20 load strongly on the PC. Thus, the weight  $w_{ik} (i = 1, 2, \dots, m; k = 1, 2, \dots, l)$  of the  $k$ th  
 21 variable that has significant loading on the  $i$ th PC can be calculated by normalizing the

1 corresponding coefficients of  $l$  variables, as displayed in the component score  
 2 coefficient matrix, where  $l$  is the number of all variables that have significant loadings  
 3 on the  $i$ th PC. The weight of the  $k$ th contributing variable for the  $i$ th PC is calculated  
 4 using the following:

$$5 \quad w_{ik} = \frac{\alpha_{ik}}{\sum_{k=1}^l \alpha_{ik}}, i = 1, 2, \dots, m; k = 1, 2, \dots, l \quad (17)$$

6 Note that  $\alpha_{ik}$  is always positive because we employ only variables with  
 7 significant loadings on each PC to compute the distributed assessment of the PC on  
 8 different grades.

9 We assume that the frequency distribution of the patient assessment of each  
 10 surveyed item on different evaluation grades is represented as  $\beta_{tj}(t = 1, 2, \dots, M; j =$   
 11  $1, 2, \dots, L)$ , where  $M$  is the number of evaluation grades,  $H_t(t = 1, 2, \dots, M)$ , which are  
 12 used to assess each item, and  $L$  is the number of items being assessed or surveyed. The  
 13 distributed assessment of each extracted PC,  $Z_i$ , on different evaluation grades,  
 14  $\beta_{Z_i,t}(i = 1, 2, \dots, m; t = 1, 2, \dots, M)$ , can be computed using the following:

$$15 \quad \beta_{Z_i,t} = \sum_{k=1}^l (w_{ik} * \beta_{tk}), t = 1, 2, \dots, M \quad (18)$$

16 where  $l$  is the number of all variables that have significant loadings on the  $i$ th PC,  $Z_i$ .

17 Finally, to aggregate the distributed assessments of extracted PCs to obtain an  
 18 aggregated healthcare quality assessment result  $\{(H_t, \beta_t), t = 1, 2, \dots, M\}$ , the ER  
 19 approach is employed on the basis of the weight of each extracted PC calculated in step

1 five using (16) and the distributed assessment of each PC computed in step six using  
2 (17) and (18).

### 3 **2.7. Combining AHP and the ER approach to assess healthcare quality**

4 As discussed in Section 2.4, AHP is a typical method used to calculate the relative  
5 importance of criteria in a hierarchy. Therefore, AHP can be used to calculate the  
6 weights of survey items and their corresponding quality dimensions instead of using  
7 the method discussed in Section 2.6 for PC and corresponding item weight calculation  
8 in PCA.

9 For convenience, we used the same patient satisfaction assessment framework as  
10 determined by PCA. We consider that one PC represents one quality dimension.  
11 Therefore, the number of extracted PCs represents the number of quality dimensions  
12 that were assessed in the survey. We then used AHP to calculate the relative importance  
13 of different quality dimensions and their corresponding survey items.

14 We invited six domain experts to provide their judgments about the importance of  
15 quality dimensions and corresponding items in the hierarchical framework. We built  
16 pairwise comparison matrix on the basis of the respondents' responses and used the  
17 Eigenvalue method to calculate the weight of those items at different levels in the  
18 assessment framework. We then averaged the weights calculated from the experts'  
19 responses if their pairwise comparisons pass the consistency check.

20 After determining the weight of each quality dimension and its corresponding  
21 survey item via AHP, we employed the ER approach to aggregate the assessment of

1 each item to obtain the overall quality assessment result.

### 2 **3. Results**

3 The characteristics of the studied survey data obtained after excluding unqualified  
4 surveys are shown in Table 1.

---

5 INSERT TABLE 1 HERE

---

6 After deleting items with a response rate lower than 90%, 19 items were retained  
7 in the dataset for analysis. The frequency of patients' evaluations of each item  
8 distributed on five-point Likert-type scales are described in Table 2.

---

9 INSERT TABLE 2 HERE

---

10 The KMO index for the studied survey dataset was 0.915 with a Bartlett's test  
11 significance of less than 0.001.

12 By using SPSS to perform PCA on the studied survey data, we obtained the results  
13 for the proportion of variance that is explained by each PC. We extracted seven PCs on  
14 the basis of the threshold value of 70% of the total variance that the combined PCs  
15 should account for in the dataset. The correlation between 19 items and the extracted  
16 seven PCs identified through PCA is shown in Table 3.

---

17 INSERT TABLE 3 HERE

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 INSERT TABLE 4 HERE
 

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2        The total variance explained by the seven extracted PCs is described in Table 4.

3        The normalized weights of the seven PCs were calculated using (16) on the basis of the

4        eigenvalues of the seven extracted PCs. These PCs have normalized weights of  $w_1 =$ 5        0.561,  $w_2 = 0.100$ ,  $w_3 = 0.084$ ,  $w_4 = 0.076$ ,  $w_5 = 0.066$ ,  $w_6 = 0.056$ , and  $w_7 = 0.056$ . The

6        rotated component matrix is shown in Table 5, where the rotated loadings of variables

7        that strongly load on each PC are shaded gray. The component score coefficient matrix

8        is shown in Table 6, where the coefficients of variables that strongly load on each PC

9        are also shaded gray. These variables are used to form the linear functions used to derive

10       the corresponding PCs.

11

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 INSERT TABLE 5 HERE
 

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 INSERT TABLE 6 HERE
 

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14        On the basis of the coefficients as presented in Table 6, we calculated the weights

15        of variables that load strongly on each PC using (17). The first PC (PC1) can be taken

16        as an example. From Tables 5 and 6, we can identify six variables that are significantly

17        correlated with PC1: Q5, Q6, Q8, Q9, Q10, and Q11. By normalizing their coefficients

18        for PC1, we can obtain the corresponding weights as  $w_{11} = 0.309 \div (0.309 + 0.189 +$ 19         $0.228 + 0.290 + 0.288 + 0.286) = 0.194$  (Q5),  $w_{12} = 0.119$  (Q6),  $w_{13} = 0.143$  (Q8),  $w_{14}$





1 dimensions are assessed in the survey. We consider the following seven quality  
2 dimensions on the basis of the characteristics of items assessed in each quality  
3 dimension: 1) doctor–patient or nurse–patient communication; 2) communication about  
4 illness; 3) hospital environment; 4) admission or discharge information; 5) waiting time;  
5 6) communication about drug or examinations; and 7) pain control or emotional support.  
6 We then employed AHP to generate the weights of the seven quality dimensions and  
7 their corresponding items.

8 We invited six experts to provide their preferences for the relative importance of  
9 each quality dimension and their corresponding items. In checking the consistency of  
10 the comparison matrix provided by each expert, we found that two experts' judgments  
11 are inconsistent. Therefore, we used only four experts' comparison matrix to calculate  
12 the weights of quality dimensions and their corresponding items. We used the  
13 Eigenvalue method to calculate each expert's results and averaged four experts' results  
14 to assign the final weights to each dimension and its corresponding items. The weights  
15 of the seven quality dimensions generated by AHP after averaging four experts'  
16 judgments are shown in Table 8, and the averaged weights of assessed items  
17 corresponding to each dimension are shown in Table 9.

---

18 INSERT TABLE 8 HERE

---

---

19  
20 INSERT TABLE 9 HERE

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1 Likewise, we employed IDS to aggregate the patient evaluation of each item on the  
2 basis of the weights of quality dimensions and corresponding items that we calculated  
3 through AHP. Fig. 4 shows the hierarchical assessment framework modelled by IDS in  
4 AHP method, and Fig. 5 shows the distributed assessments after aggregating all patients'  
5 evaluations based on the AHP hierarchical framework.

6 INSERT FIGURE 4 HERE

8 INSERT FIGURE 5 HERE

9 As the combined assessment result contains belief degrees distributed on different  
10 evaluation grades and is not straightforward enough to enable quality comparison  
11 between hospitals. Yang and Xu (2002) proposed the concept of expected utility to  
12 define a numerical value that is equivalent to the distributed assessment. For this  
13 purpose, the utilities of individual assessment grades need to be defined first. In our  
14 case, if we assign a quality score of 10 to “very satisfied,” 8 to “satisfied,” 6 to “fair,”  
15 4 to “dissatisfied,” and 2 to “very dissatisfied,” we can obtain a numerical quality score  
16 of Hospital A as  $10 \times 54.47\% + 8 \times 40.11\% + 6 \times 4.43\% + 4 \times 0.76\% + 2 \times 0.22\% =$   
17  $5.447 + 3.209 + 0.266 + 0.030 + 0.004 = 8.956$  through the combined method of PCA  
18 and ER. We can also obtain a quality score of 8.953 for Hospital A through the  
19 combined method of AHP and ER. If more than one hospital needs to be assessed, the  
20 numerical quality score generated for alternative hospitals can be employed to rank the

healthcare quality of different hospitals.

#### **4. Discussion and conclusions**

This study proposes a new hybrid method, which combines PCA and the ER approach, for the assessment of healthcare quality based on patient experience and satisfaction surveys. In this new hybrid method, PCA helps identify the structure of the relationship between interrelated items and to derive uncorrelated PCs. The structure of the relationship among different items can be identified on the basis of the extracted PCs, and the distributed assessments of the extracted PC can be computed from corresponding variables with significant loadings. In transforming the original variables to PCs, the weights of variables are taken into account on the basis of their loadings on corresponding PCs. The ER approach is then employed to aggregate the distributed assessments of extracted PCs to obtain an overall assessment of healthcare quality. The weight of each PC is considered in aggregation and determined by the variance that the corresponding PC accounts for in the dataset.

Combining the ER approach with PCA for the aggregated assessment of healthcare quality can enhance its capability to aid MADA problems with interrelated attributes or items. Using PCA to extract PCs can help transform interrelated items into uncorrelated PCs, which can then be used as multiple attributes or criteria to be aggregated by the ER approach. In contrast to the conventional component score computation in PCA that uses all available variables in linear functions, we employ only variables that have significant loadings on the corresponding PCs to transform the original interrelated variables to PCs. The weights of variables in transformation functions are determined

1 by their loadings on the PCs, i.e., their correlations with the corresponding PCs. This  
2 helps ensure that the distributed assessments on the extracted PCs are uncorrelated.

3 To compare the performance of the proposed method with that of another method,  
4 we also performed aggregated quality assessment through the combined AHP and ER  
5 approach. The quality assessment frameworks of the combined PCA and ER approach  
6 and of the combined AHP and ER approach are both derived from PCA. In the former  
7 method, the weight of each extracted PC and its corresponding items are all generated  
8 on the basis of collected data. By contrast, in the latter method, the relative importance  
9 of assessed items is calculated on the basis of the respondents' subjective judgments.  
10 These two different hybrid methods generated different aggregated distributed  
11 assessments (Fig. 3 and Fig 5) but similar overall quality scores (8.956 and 8.953).

12 Compared with the combined AHP and ER approach, the combined PCA and ER  
13 approach has the following advantages: it is completely based on survey data, and its  
14 result is completely objective and contains no subjective judgments . The use of AHP  
15 to calculate the weights of quality dimensions and corresponding items in the  
16 hierarchical framework has numerous disadvantages. First, an expert may have  
17 inconsistent judgments of pairwise comparison. Second, two experts may have  
18 completely different judgments for the same surveyed item set. Third, given that  
19 different experts have different opinions about healthcare quality, the weights of  
20 different dimensions and items calculated via AHP will certainly be different if different  
21 experts are surveyed. Therefore, if other experts are surveyed, we may obtain a different

1 overall quality assessment result through the combined AHP and ER method.

2 In the current healthcare environment, using patient experience and satisfaction  
3 surveys to evaluate healthcare quality is necessary and integral for overall healthcare  
4 assessment. The government and general public are searching for optimal methods to  
5 assess healthcare quality from a patient's perspective, and they try to link healthcare  
6 quality assessment results to resource allocation, such as government funding support.  
7 Healthcare consumers (patients) are very interested in the ranking of the healthcare  
8 quality of different hospitals, and the hospital's quality ranking will most certainly  
9 affect patients' healthcare service choices. The new hybrid method proposed in this  
10 study provides a pragmatic and objective approach to healthcare quality assessment by  
11 aggregating patient evaluations from different dimensions or perspectives. Although  
12 only one hospital was investigated in this study, this hybrid method is suitable for  
13 assessing numerous hospitals by using the same questionnaire. Moreover, it can help  
14 rank the healthcare provided by different hospitals on the basis of various quality  
15 dimensions.

16 To conclude, this study proposed a novel hybrid method that combines PCA and  
17 the ER approach. The method first identifies relationships among all surveyed items  
18 from collected survey data. It then transforms original interrelated items to uncorrelated  
19 PCs. Finally, it employs the ER approach to aggregate the distributed assessments of  
20 the extracted PCs. The proposed hybrid method is objective and completely based on  
21 survey datasets. It combines the advantages of PCA and the ER approach to provide a

novel and rational approach for assessing healthcare quality from the patient's perspective.

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### References

- Büyüközkan G, Çifçi G. 2012. A combined fuzzy AHP and fuzzy TOPSIS based strategic analysis of electronic service quality in healthcare industry. *Expert Systems with Applications* 39: 2341-54
- Büyüközkan G, Çifçi G, Güteryüz S. 2011. Strategic analysis of healthcare service quality using fuzzy AHP methodology. *Expert Systems with Applications* 38: 9407-24
- Behara RS, Fisher WW, Lemmink JGAM. 2002. Modelling and evaluating service quality measurement using neural networks. *International Journal of Operations & Production Management* 22: 1162-85
- Carlucci D, Renna P, Schiuma G. 2013. Evaluating service quality dimensions as antecedents to outpatient satisfaction using back propagation neural network. *Health Care Manage Science* 16: 37-44
- Department of Health. 2000. The NHS Plan. London: The Stationery Office
- Department of Health. 2013. Victorian health service performance monitoring framework. Victorian Government, Australia
- Fragkiadakis G, Doumpos M, Zopounidis C, Germain C. 2016. Operational and economic efficiency analysis of public hospitals in Greece. *Annals of Operations Research* 247: 787-806
- Goldstein E, Farquhar M, Crofton C, Darby C, Garfinkel S. 2005. Measuring hospital care from the patients' perspective: an overview of the CAHPS Hospital Survey development process. *Health Services Research* 40: 1977-95
- Harris LE, Swindle RW, Mungai SM, Weinberger M, Tierney WM. 1999. Measuring patient satisfaction for quality improvement. *Medical Care* 37: 1207-13
- Ishizaka A, Balkenbourg D, Kaplan T. 2010. Does AHP help us to make a choice? An experimental evaluation. *Journal of the Operational Research Society* 62: 1801-12
- Jenkinson C, Coulter A, Bruster S. 2002. The Picker Patient Experience Questionnaire: development and validation using data from in-patient surveys in five countries. *International Journal for Quality in Health Care* 14: 353-8
- Jenkinson C, Coulter A, Reeves R, Bruster S, Richards N. 2003. Properties of the Picker Patient Experience questionnaire in a randomized controlled trial of long versus short form survey instruments. *Journal Of Public Health Medicine* 25: 197-201
- Jha AK, Orav EJ, Zheng J, Epstein AM. 2008. Patients' perception of hospital care in the United States. *The New England Journal Of Medicine* 359: 1921-31
- Jolliffe IT. 2002. *Principal Component Analysis*. New York: Springer.
- Keller AC, Bergman MM, Heinzmann C, Todorov A, Weber H, Heberer M. 2014. The relationship between hospital patients' ratings of quality of care and communication. *Internal Journal for*

1           *Quality in Health Care* 26: 26-33

2   Keller S, O'Malley AJ, Hays RD, Matthew RA, Zaslavsky AM, et al. 2005. Methods used to streamline

3           the CAHPS Hospital Survey. *Health Services Research* 40: 2057-77

4   Kleefstra SM, Kool RB, Veldkamp CM, Winters-van der Meer AC, Mens MA, et al. 2010. A core

5           questionnaire for the assessment of patient satisfaction in academic hospitals in The Netherlands:

6           development and first results in a nationwide study. *Quality & Safety In Health Care* 19: e24

7   Kong GL, Xu D-L, Liu X, Yang J-B. 2009. Applying a belief rule-base inference methodology to a

8           guideline-based clinical decision support system. *Expert Systems* 26: 391-408

9   Kong GL, Xu D-L, Yang J-B, Ma XM. 2015. Combined medical quality assessment using the evidential

10          reasoning approach. *Expert Systems with Applications* 42: 5522-30

11   Kong GL, Xu DL, Body R, Yang JB, Mackway-Jones KRH, Carley S. 2012. A belief rule-based decision

12          support system for clinical risk assessment of cardiac chest pain. *European Journal of*

13          *Operational Research* 219: 564-73

14   Lyratzopoulos G, Elliott MN, Barbiere JM, Staetsky L, Paddison CA, et al. 2011. How can Health Care

15          Organizations be Reliably Compared?: Lessons From a National Survey of Patient Experience.

16          *Medical Care* 49: 724-33

17   Morgan R. 2017. An investigation of constraints upon fisheries diversification using the Analytic

18          Hierarchy Process (AHP). *Marine Policy* 86: 24-30

19   Norman GR, Streiner DL. 1998. *Biostatistics: the bare essentials*. Hamilton, Ontario B.C. Decker Inc.

20   Panagiotis M, Kostas K, Ioannis M. 2016. Factors affecting primary health care centers' economic and

21          production efficiency. *Annals of Operations Research* 247: 807-22

22   Park YS, Egilmez G, Kucukvar M. 2015. A novel life cycle-based principal component analysis

23          framework for eco-efficiency analysis: case of the United States manufacturing and

24          transportation nexus. *Journal of Cleaner Production* 92: 327-42

25   Prior D. 2006. Efficiency and total quality management in health care organizations: A dynamic frontier

26          approach. *Annals of Operations Research* 145: 281-99

27   Purcărea VL, Gheorghe IR, Petrescu CM. 2013. The assessment of perceived service quality of public

28          health care services in Romania using the SERVQUAL scale. *Procedia Economics and Finance*

29          6: 573-85

30   Rodriguez H, von Glahn T, Elliott M, Rogers W, Safran D. 2009. The Effect of Performance-Based

31          Financial Incentives on Improving Patient Care Experiences: A Statewide Evaluation. *Journal*

32          *Of General Internal Medicine* 24: 1281-88

33   Saaty TL. 1980. *The Analytic Hierarchy Process*. New York: McGraw-Hill.

34   Saaty TL. 2008. Decision making with the analytic hierarchy process *International Journal of Services*

35          *Sciences* 1: 83-98

36   Vuković M, Gvozdenović BS, Gajić T, Stamatović Gajić B, Jakovljević M, McCormick BP. 2012.

37          Validation of a patient satisfaction questionnaire in primary health care. *Public Health* 126: 710-

38          18

39   Wang YM, Yang JB, Xu DL. 2006. Environmental impact assessment using the evidential reasoning

40          approach. *European Journal of Operational Research* 174: 1885-913

41   Wong EL, Leung MC, Cheung AW, Yam CH, Yeoh EK, Griffiths S. 2011. A population-based survey

42          using PPE-15: relationship of care aspects to patient satisfaction in Hong Kong. *International*

43          *Journal for Quality in Health Care* 23: 390-6

44   Xu D-L. 2012. An introduction and survey of the evidential reasoning approach for multiple criteria

1           decision analysis. *Annals of Operations Research* 195: 163-87

2   Xu DL, McCarthy G, Yang JB. 2006. Intelligent decision system and its application in business

3           innovation self assessment. *Decision Support Systems* 42: 664-73

4   Yang JB. 2001. Rule and utility based evidential reasoning approach for multiple attribute decision

5           analysis under uncertainty. *European Journal of Operational Research* 131: 31-61

6   Yang JB, Singh MG. 1994. An evidential reasoning approach for multiple-attribute decision making with

7           uncertainty. *Systems, Man and Cybernetics, IEEE Transactions on* 24: 1-18

8   Yang JB, Xu DL. 2002. On the evidential reasoning algorithm for multiple attribute decision analysis

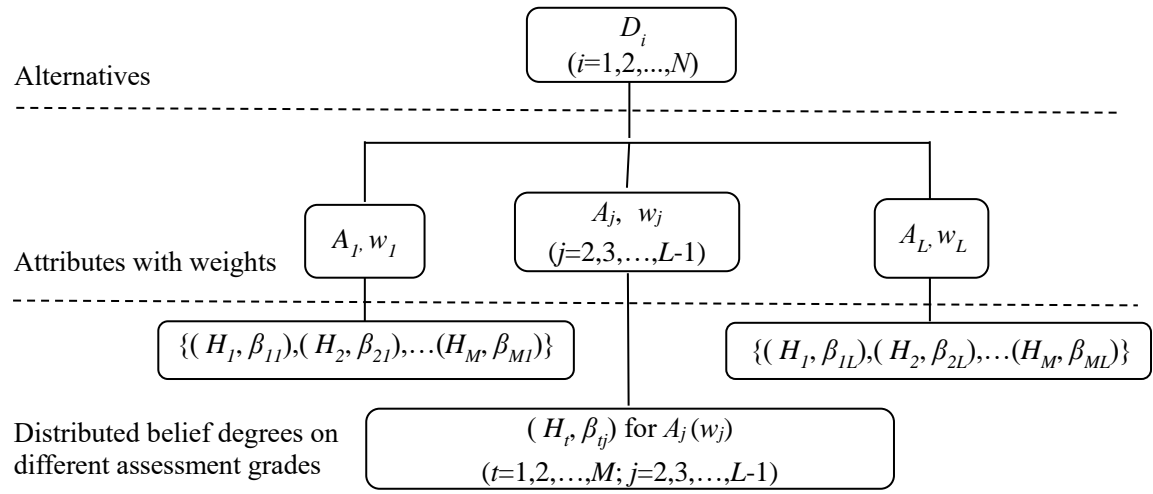
9           under uncertainty. *IEEE Transactions on Systems Man and Cybernetics Part A-Systems and*

10          *Humans* 32: 289-304

11



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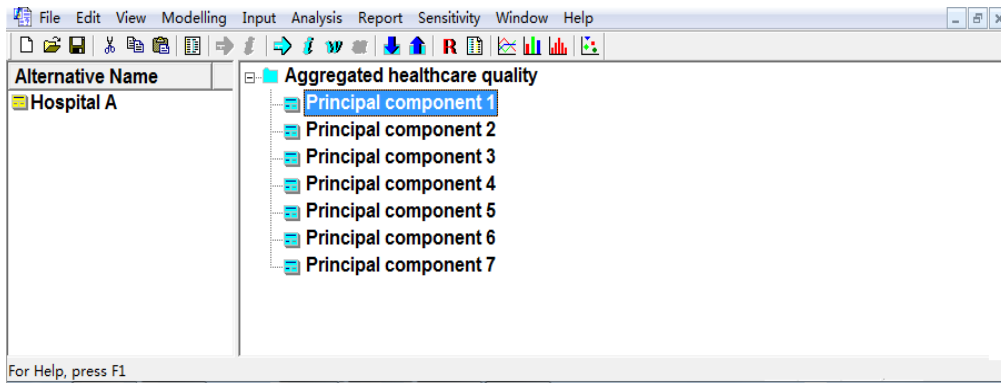
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3 **Fig. 1 A MADA problem modelled by the ER approach**

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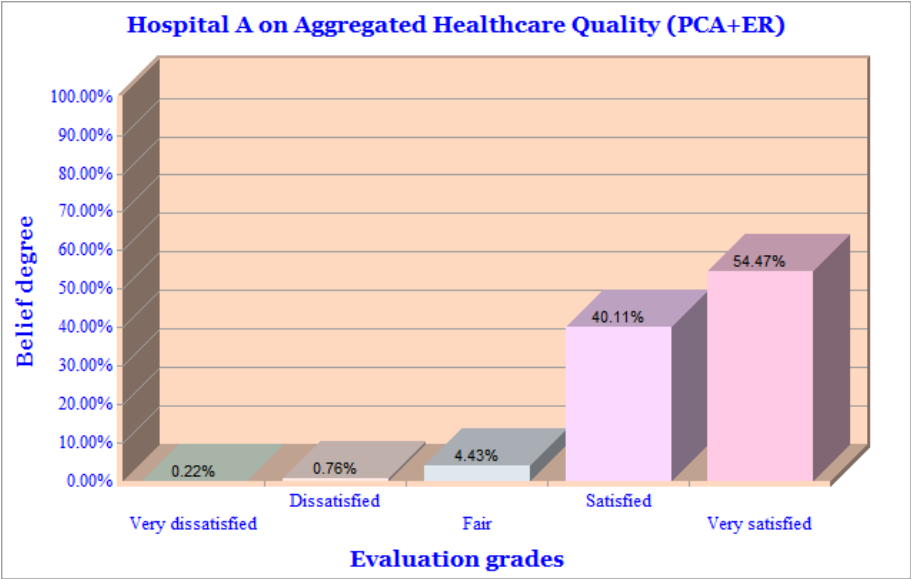
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8 **Fig. 2 The aggregated healthcare quality assessment problem modeled by IDS**

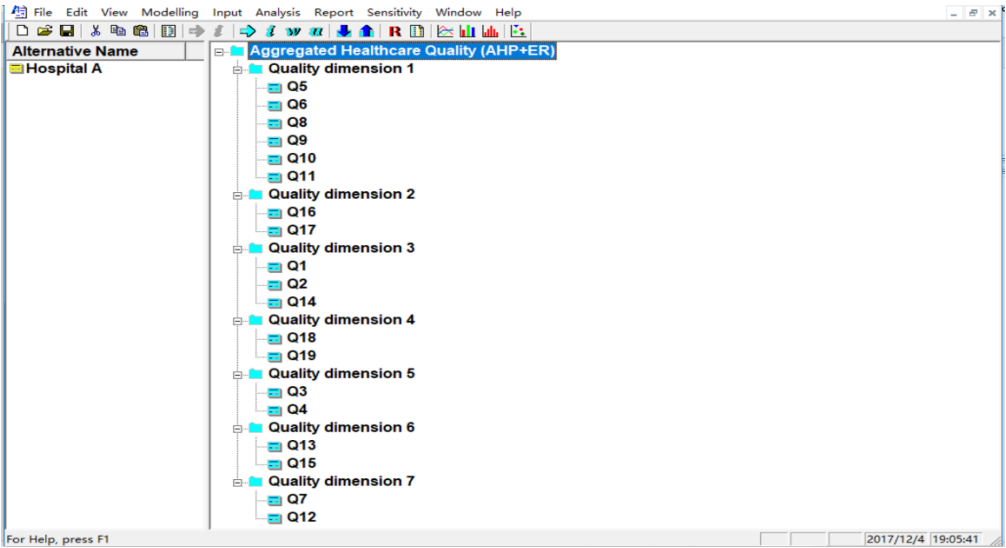
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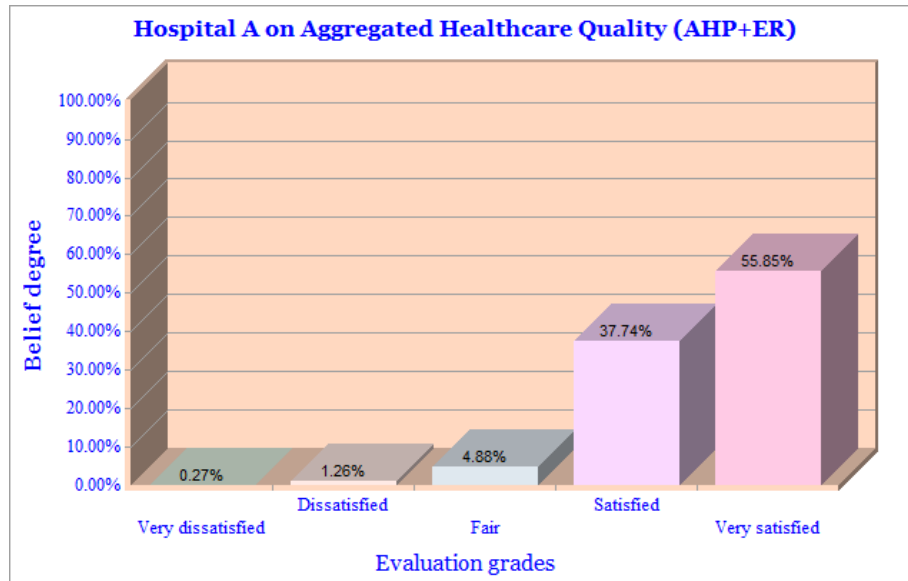
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**Fig. 3 The combined assessment result after aggregating assessments of the PCs**



**Fig. 4 The hierarchical assessment framework modeled by IDS**



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2 **Fig. 5 The combined assessment result after aggregating evaluation on each item**

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1    **Table 1 Characteristics of the studied survey data (N=192)**

<b>Variable</b>	<b>Subgroup</b>	<b>Number of patients (proportion)</b>
Gender	Male	82(42.7%)
	Female	110(57.3%)
Age (years old)	<=44	62(32.3%)
	45-59	43(22.4%)
	60-74	57(29.7%)
	>=75	30(15.6%)
Education background	Grade school or below	27(14.1%)
	Middle school	38(19.8%)
	High school or technical school	52(27.1%)
	College or above	75(39%)
Marital status	Married	149(77.6%)
	Widowed or divorced	21(10.9%)
	Single	22(11.5%)
Health condition	Bad	10(5.2%)
	Fair	75(39.1%)
	Good	61(31.8%)
	Excellent	30(15.6%)
	Data missing	16(8.3%)
Residential Address	Beijing	139(72.4%)
	Outside Beijing	53(27.6%)

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1 **Table 2 Frequency of patients' evaluations distributed on the five-point Likert-**  
2 **type scales**

	<b>1- Very dissatisfied</b>	<b>2- Dissatisfied</b>	<b>3- Fair</b>	<b>4- Satisfied</b>	<b>5- Very satisfied</b>
Q1	1.0%	1.6%	13.5%	57.3%	26.6%
Q2	1.6%	2.1%	7.3%	60.9%	28.1%
Q3	1.0%	4.2%	15.1%	51.0%	28.6%
Q4	1.0%	2.1%	14.1%	48.4%	34.4%
Q5	0	0.5%	1.6%	38.0%	59.9%
Q6	0	0.5%	2.6%	44.8%	52.1%
Q7	0.5%	3.1%	11.5%	49.0%	35.9%
Q8	0	0	2.6%	30.2%	67.2%
Q9	0	1.0%	7.3%	45.8%	45.8%
Q10	0	0.5%	3.6%	39.1%	56.8%
Q11	0	0	3.6%	43.8%	52.6%
Q12	0	1.0%	8.3%	63.5%	27.1%
Q13	0	0	9.4%	26.0%	64.6%
Q14	1.0%	1.0%	12.0%	57.3%	28.6%
Q15	0.5%	1.0%	4.7%	10.4%	83.3%
Q16	0	3.6%	5.2%	34.9%	56.3%
Q17	2.1%	3.6%	12.5%	46.4%	35.4%
Q18	1.0%	1.0%	3.1%	22.9%	71.9%
Q19	1.6%	1.0%	3.6%	13.0%	80.7%

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1 **Table 3 The correlation between the items and the extracted PCs**

Component	Items measured in the questionnaire
1	Q5. Doctors treated you with respect and dignity while you were in hospital. Q6. Doctors gave you answers you could understand when you had important questions to ask them. Q8. You had trust in your doctors. Q9. You could get help as soon as you wanted it after you pressed the call button. Q10. Nurses treated you with courtesy and respect. Q11. Nurses explained things in a way you could understand.
2	Q16. You and your family knew about details of your condition and treatment. Q17. Doctors explained test results clearly to you.
3	Q1. Cleanliness of your room and bathroom. Q2. Convenience of using personal item lockers. Q14. Other hospital staff (excluding doctors and nurses) treated you with courtesy and respect.
4	Q18. Hospital staff gave you and your family enough guidance on hospital admission.  Q19. Hospital staff gave you enough information about what symptoms or health problems to look out for after you were discharged, what activities you could and could not do, and how to take the medicine at home.
5	Q3. Time waiting to go to ward. Q4. Time waiting in ward for surgery to be performed.
6	Q13. Hospital staff did not bring you unexpected pain during medical examinations. Q15. You have been asked about your history of drug allergy and have been given enough information about the medicine, such as possible side-effects of the medicine, before giving you the medicine.
7	Q7. Doctors discussed with you when you had anxieties or fears about your condition or treatment. Q12. Your pain was well controlled.

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4 **Table 4 Total variance explained**

Component	Initial eigenvalues		
	Total	% of variance	Cumulative %
1	7.619	40.099	40.099
2	1.361	7.165	47.263
3	1.141	6.007	53.271
4	1.030	5.420	58.691
5	0.900	4.735	63.426
6	0.763	4.014	67.440
7	0.761	4.005	71.445

5

1    **Table 5 Rotated component matrix**

Item	Component						
	1	2	3	4	5	6	7
Q1	0.334	-0.012	0.689	0.210	0.140	0.072	-0.187
Q2	0.105	0.050	0.762	0.152	0.184	-0.061	0.240
Q3	0.162	0.211	0.259	0.025	0.721	-0.002	0.196
Q4	0.277	0.142	0.069	0.088	0.729	0.214	0.001
Q5	0.730	0.370	0.053	0.160	0.278	-0.009	-0.071
Q6	0.627	0.488	0.046	0.150	0.237	-0.010	0.183
Q7	0.289	0.445	0.094	0.362	0.151	-0.058	0.455
Q8	0.670	0.411	0.080	0.224	0.164	0.040	0.118
Q9	0.745	0.074	0.234	0.113	0.137	0.099	0.285
Q10	0.756	0.099	0.299	0.051	0.107	0.232	0.166
Q11	0.736	-0.006	0.292	0.129	0.108	0.224	0.197
Q12	0.357	0.132	0.125	0.104	0.143	0.207	0.709
Q13	0.437	0.307	0.047	0.221	0.004	0.487	-0.130
Q14	0.250	0.432	0.630	-0.116	-0.001	0.186	0.120
Q15	0.124	0.157	0.052	0.061	0.165	0.829	0.175
Q16	0.135	0.658	-0.042	0.181	0.316	0.224	0.202
Q17	0.206	0.705	0.218	0.155	0.105	0.184	0.005
Q18	0.191	0.213	0.179	0.727	-0.125	0.084	0.129
Q19	0.134	0.096	0.053	0.845	0.223	0.081	0.033

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1 **Table 6 Component score coefficient matrix**

Item	Component						
	1	2	3	4	5	6	7
Q1	0.029	-0.134	0.448	0.111	0.050	0.013	-
Q2	-0.188	-0.060	0.521	0.044	0.058	-	0.176
Q3	-0.139	-0.036	0.081	-	0.608	-	0.070
Q4	-0.023	-0.154	-0.083	-	0.646	0.115	-
Q5	0.309	0.109	-0.142	-	0.092	-	-
Q6	0.189	0.219	-0.140	-	0.006	-	0.011
Q7	-0.068	0.196	-0.055	0.134	-	-	0.403
Q8	0.228	0.139	-0.117	0.005	-	-	-
Q9	0.290	-0.195	-0.026	-	-	-	0.170
Q10	0.288	-0.160	0.035	-	-	0.092	0.013
Q11	0.286	-0.274	0.026	-	-	0.102	0.064
Q12	-0.019	-0.139	-0.062	-	-	0.094	0.753
Q13	0.111	0.082	-0.064	0.066	-	0.394	-
Q14	-0.111	0.340	0.431	-	-	0.066	-
Q15	-0.155	-0.102	-0.033	-	0.039	0.809	0.104
Q16	-0.179	0.410	-0.112	-	0.108	0.068	0.076
Q17	-0.132	0.534	0.112	-	-	0.024	-
Q18	-0.070	0.009	0.060	0.514	-	0.008	0.044
Q19	-0.099	-0.185	-0.058	0.653	0.162	0.020	-

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7 **Table 7 Distributed assessments of the seven extracted principal components**

Component	Belief degrees distributed on the five scales				
	1- Very dissatisfied	2- Dissatisfied	3- Fair	4- Satisfied	5- Very satisfied
1	0	0.45%	3.63%	40.35%	55.57%
2	1.18%	3.65%	9.33%	41.38%	44.47%
3	1.24%	1.60%	10.73%	58.65%	27.79%
4	1.33%	1.04%	3.42%	17.38%	76.83%
5	1.04%	3.09%	14.57%	49.70%	31.60%
6	0.35%	0.70%	6.22%	15.53%	77.19%
7	0.18%	1.77%	9.42%	58.46%	30.17%

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1     **Table 8 Weights of seven quality dimensions generated using AHP**

Quality dimension	Weight				
	Expert1	Expert2	Expert3	Expert4	Average
1- the doctor-patient or nurse-patient communication	0.060	0.263	0.209	0.237	0.192
2- communication about illness	0.327	0.036	0.355	0.138	0.214
3- hospital environment	0.026	0.155	0.037	0.045	0.066
4- admission or discharge information	0.135	0.056	0.051	0.122	0.091
5- waiting time	0.048	0.115	0.063	0.030	0.064
6- communication about medicines or examinations	0.284	0.061	0.061	0.238	0.161
7- pain control or emotional support	0.121	0.315	0.225	0.190	0.213

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1 **Table 9 Weights of items being assessed in the survey (generated using AHP)**

Dimension	Items measured in the questionnaire	Averaged weight
1	Q5. Doctors treated you with respect and dignity while you were in hospital.	0.308
	Q6. Doctors gave you answers you could understand when you had important questions to ask them.	0.221
	Q8. You had trust in your doctors.	0.220
	Q9. You could get help as soon as you wanted it after you pressed the call button.	0.108
	Q10. Nurses treated you with courtesy and respect.	0.094
	Q11. Nurses explained things in a way you could understand.	0.048
2	Q16. You and your family knew about details of your condition and treatment.	0.802
	Q17. Doctors explained test results clearly to you.	0.198
3	Q1. Cleanliness of your room and bathroom.	0.462
	Q2. Convenience of using personal item lockers.	0.260
	Q14. Other hospital staff (excluding doctors and nurses) treated you with courtesy and respect.	0.278
4	Q18. Hospital staff gave you and your family enough guidance on hospital admission.	0.500
	Q19. Hospital staff gave you enough information about what symptoms or health problems to look out for after you were discharged, what activities you could and could not do, and how to take the medicine at home.	0.500
5	Q3. Time waiting to go to ward.	0.792
	Q4. Time waiting in ward for surgery to be performed.	0.208
6	Q13. Hospital staff did not bring you unexpected pain during medical examinations.	0.333
	Q15. You have been asked about your history of drug allergy and have been given enough information about the medicine, such as possible side-effects of the medicine, before giving you the medicine.	0.667
7	Q7. Doctors discussed with you when you had anxieties or fears about your condition or treatment.	0.375
	Q12. Your pain was well controlled.	0.625

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