

COVID-19 pandemic, predictions and control in Saudi Arabia using SIR-F and age-structured SEIR model

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Abstract

COVID-19 has affected every individual physically or physiologically, leading to substantial impacts on how they perceive and respond to the pandemic's danger. Due to the lack of vaccines or effective medicines to cure the infection, an urgent control measure is required to prevent the continued spread of COVID-19. This can be achieved using advanced computing, such as artificial intelligence (AI), machine learning (ML), deep learning (DL), cloud computing, and edge computing. To control the exponential spread of the novel virus, it is crucial for countries to contain and mitigate interventions. To prevent exponential growth, several control measures have been applied in the Kingdom of Saudi Arabia to mitigate the COVID-19 epidemic. As the pandemic has been spreading globally for more than a year, an ample amount of data is available for researchers to predict and forecast the effect of the pandemic in the near future. This article interprets the effects of COVID-19 using the Susceptible-Infected-Recovered (SIR-F) while F-stands for 'Fatal with confirmation,' age-structured SEIR (Susceptible Exposed Infectious Removed) and machine learning for smart health care and the well-being of citizens of Saudi Arabia. Additionally, it examines the different control measure scenarios produced by the modified SEIR model. The evolution of the simulation results shows that the interventions are vital to flatten the virus spread curve, which can delay the peak and decrease the fatality rate.

Keywords COVID-19 \cdot Control measurements \cdot Interventions \cdot Mathematical SIR \cdot SIR-F \cdot SEIR \cdot Critical cases

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1 Introduction

In past decades, numerous diseases have emerged in different geographical regions in the world, such as *Ebola, Zika virus, Nipah virus, and coronavirus* [1]. In December 2019, a novel coronavirus (COVID-19) emerged from the Coronaviridae family in Wuhan, China [2–4].

However, COVID-19 is of zoonotic origin, but it spread via human-to human transmission, and there has been a steady increase in the number of confirmed cases globally. It is clear that the infection transmission rate of this virus is higher than that of other viruses.

Recent studies suggest that COVID-19 is first transmitted from animals, such as bats, to humans. It was previously reported that a group of patients who tested positive for COVID-19 were associated with the seafood market in Wuhan, South China. Later, the virus quickly spread throughout the country and then subsequently to other countries. COVID-19 poses a significant threat to public health.

Looking at the severity of the breakout and the potential of its spread globally, the WHO declared a global health emergency in early January 2020; later, in the month of March 2020, it was declared a pandemic.

1.1 COVID-19 in the Kingdom of Saudi Arabia

Coronavirus has been associated with significant disease outbreaks in East Asia and the Middle East in the past 2 decades. Middle East Respiratory Syndrome coronavirus (MERS-CoV) was first reported in Saudi Arabia in September 2012 [5]. The mortality rate of MERS was approximately 37.1%, and many patients experience mild-to-severe acute respiratory syndrome conditions that required hospitalization [6].

The recently emerged severe acute respiratory system-related coronavirus-2 (SARS-CoV-2) is the causes of the current pandemic, and many efforts have been made to control the virus.

The first case of COVID-19 in Saudi Arabia was reported on March 2, 2020, in the eastern region area named Qatif. The patient was a female returning from Iraq. Later, on March 4, various prevention measures were taken by the Ministry of Health (e.g., suspension of Umrah, tourism, suspension of international flights to a number of countries, suspension of domestic flights, partial curfew for 21 days, Makkah, Madinah lockdown) to control the pandemic. Despite these restrictions, Saudi Arabia has the highest number of COVID-19 cases compared with the other Gulf countries.

According to the Saudi Press Agency, during the first wave of the COVID-19 pandemic, it has infected more than 333,193 individuals up to 27th September 2020, with 11,505 active cases in Saudi Arabia [7]. According to the Ministry of Health of Saudi Arabia, the total number of recovered cases recorded on September 27, 2020, was 317,005, with a total of 198 cities, towns, and villages reporting cases.

The Ministry of Health reported a second wave of the COVID-19 pandemic on September 29, 2020. The total number of cases recorded as of June 04, 2021, was 455,418, with a total of 438,206 recoveries (a recovery rate of 98%), and the total number of deaths was 7424 [8].

The main aim of this paper is to study the spread of the virus in Saudi Arabia based on realistic data collection and published reports. The article focuses on the time series model based on the SIR-F and age-structured SEIR model with the total number of increases in confirmed cases, recoveries, and deceased cases.

The paper is organized as follows: the SIR-F model is introduced by taking the classic SIR model with customized ODE, and its various aspects are discussed. Additionally, we presented the results of the age-structured SEIR model and our analysis of the effect of the pandemic in Saudi Arabia. This article concludes with the outcomes of our analysis and its connections to the evidence with the collected data.

2 Literature review

2.1 Basic SIR-F Model

A generalized SIR-F model is numerically implemented and customized with the ordinary differential equation (ODE) derived from the basic SIR model. In the basic SIR model, the total population is considered to have the possibility of susceptibility to the virus (S), infection (I) and recovery (R). Susceptible individuals were subtracted from the total population of virus carriers (confirmed by testing). In the SIR-F model, we assume that some patients might have died before going to the hospital or before testing positive. The infection rate, β , represents the velocity of the disease in the population. The transition state from S to I is always stochastic, and the model is defined as follows:

$$S \to^{\beta I} S^* \to^{\alpha_1} F,$$

$$S^* \to^{1-\alpha_1} I \to^{\gamma} R,$$

$$I \to^{\alpha_2} F$$
(1)

where S = Susceptible, S^* is confirmed cases, I = Infected, R = Recovered, F = Deaths.

 α_1 is the mortality rate of S^* , α_2 is the mortality rate after the individual is affected [1/min], β =Effective constant rate [1/min], and γ =Recovery rate [1/min].

2.2 Non-dimensional SIR-F model

The ordinary differential equation of the SIR-F model is given as

$$\frac{dx}{dt} = -\rho xy
\frac{dy}{dt} = \rho(1 - \theta)xy - (\sigma + \kappa)y
\frac{dz}{dt} = \sigma y
\frac{dw}{dt} = \rho\theta xy + \kappa y$$
(2)

where N is the total population, and R_0 is the contact rate at which new infections are caused when contacted with the others.

$$R_0 = \rho(1-\theta)(\sigma+\kappa)^{-1} = \beta(1-\alpha_1)(\gamma+\alpha_2)^{-1}$$

$$\frac{\rho}{\sigma} = R_0 > 1$$
(3)

If R_0 is more than 1, it means that there is a high possibility of outbreak in the future, and if R_0 is less than or equal to 1, then there is no epidemic, and the virus will die without affecting a large number of populations.

3 Proposed model: age-structured SEIR model

3.1 Basic SEIR model

The model is described with the transmission rate parameters shown in Fig. 1.

Furthermore, suppose that:

 μ is the equal birth and death rate,

 $1/\alpha$ is the mean latent period for the disease,

 $1/\gamma$ is the mean infectious period, and the contact rate is β .

This can be described by the ordinary differential equation (ODE) [9].

$$\frac{dS}{dt} = \mu - \beta(t)SI - \mu S$$

$$\frac{dE}{dt} = \beta(t)SI - (\mu + \alpha)E$$

$$\frac{dI}{dt} = \alpha E - (\mu + \gamma)I$$
(4)

where $\beta = \beta_0 = constant$, and R_0 is defined as

$$R_0 = \frac{\beta_0 \alpha}{(\mu + \alpha)(\mu + \gamma)} \tag{5}$$



Fig. 1 Basic SEIR Model

Individuals who become infected may experience an average R_0 secondary infection while they are infectious.

3.2 The modified SEIR model

We assumed the model to be a closed system by considering the total population of Saudi Arabia to be 34,218,169, according to KAPSARC [10], including 21,103,198 Saudi citizens and 13,114,97 residents.

A group of populations are delineated by age classes with parameter *a*, which allows for a variable transition rate based on their age. The ODE is modified as follows [11]:

$$\frac{dS_{a}(t)}{dt} = -N^{-1}\beta_{a}(t)S_{a}(t)\sum_{b}I_{b}(t)
\frac{dE_{a}^{1}(t)}{dt} = N^{-1}\beta_{a}(t)S_{a}(t)\sum_{b}I_{b}(t) - 3E_{a}^{1}(t)/t_{1}
\frac{dE_{a}^{2}(t)}{dt} = 3E_{a}^{1}(t)/t_{1} - 3E_{a}^{2}(t)/t_{1}
\frac{dE_{a}^{3}(t)}{dt} = 3E_{a}^{2}(t)/t_{1} - 3E_{a}^{3}(t)/t_{1}
\frac{dI_{a}(t)}{dt} = 3E_{a}^{3}(t)/t_{1} - I_{a}(t)/t_{i}
\frac{dH_{a}(t)}{dt} = (1 - m_{a})I_{a}(t)/t_{i} + (1 - f_{a})C_{a}(t)/t_{c} - H_{a}(t)/t_{h}
\frac{dC_{a}(t)}{dt} = c_{a}H_{a}(t)/t_{h} - C_{a}(t)/t_{c}
\frac{dR_{a}(t)}{dt} = c_{a}H_{a}(t)/t_{h} - (1 - c_{a})H_{a}(t)/t_{h}
\frac{dD_{a}(t)}{dt} = \frac{f_{a}C_{a}(t)}{t_{c}} + p_{a}H_{a}(t)/t_{h}$$
(6)

Susceptible individuals [S] become infected via contact with an infected individual.

Exposed individuals [E] progress toward a symptomatic state at an average time $t_{l.}$

Infected individuals [I] get infected with an average of R_0 secondary infections, with time t_i , the infected individual either get hospitalized or recovered.

Hospitalized individuals [H] either recover or the situation of the individual worsens to a critical state with time t_h . The individual then progresses to either critically ill individuals in the ICU or infection leads to death.

Critical individuals [C] progress toward ICU usage; they either return to the hospital state [H] and die[D] on a time scale of t_c .

Recovered individuals [R] cannot get infected again once recovered.



Fig. 2 The modified SEIR model

The parameters of the modified SEIR model (Fig. 2) fall into four categories [11].

- 1. A time-dependent infection rate $\beta(t)$
- 2. Time scale of different transitions t_l (time from infection to infectiousness), t_i (time either get recovers or falls severely ill), t_h (time infected individual get recover or deteriorates into critical state), and t_c (time an individual remains critically ill or stabilize)
- 3. Age-specific parameters m_a (individual mildly infected or asymptomatic), c_a (individual in critical state), p_a (fraction of severe cases progressing toward palliative care) and f_a (fraction of critical cases that are fatal)
- 4. If the number of individuals exceeds the capacity of the ICU, the individual will be placed in an overflow category. Patients in this category give priority to the younger group to progress them toward a recovery state.

The transmission rate $\beta_a(t)$ is given by:

$$\beta_a(t) = R_0 \zeta_a M(t) \left(1 + \varepsilon \cos\left(2\pi \left(t - t_{\max}\right)\right) \right) / t_i \tag{7}$$

where ζ_a is the degree where the age groups are isolated from the rest of the individuals, M(t) is the time of mitigation measure, ε is the amplitude of seasonal variation in transmission, and t_{max} is the time at which the transmission rate is peak.

3.3 Parameter estimations

The parameters are estimated from the cumulative number of cases and the fatalities reported [11]. Since COVID-19 has more severe impacts on the elderly population, age is an important determinant of the overall burden on the health care system. Several studies have attempted to estimate the infectious transmission rate with different security measures, such as social distancing and infection control.

S.No	Age_first	Age_last	Period_of_Life	School	Office	Others	Age	Population	Portion
0	0	2	Nursery	3	0	0	2	1,797,741	0.053055
1	3	5	Nursery school	4	0	1	5	1,786,702	0.052729
2	6	10	Elementary school	5	0	1	10	2,869,228	0.084677
3	11	13	Middle school	5	0	1	13	1,549,188	0.045720
4	14	18	High school	6	0	1	18	2,304,784	0.068019
5	19	25	University/work	3	3	1	25	3,477,278	0.102622
6	26	35	Work	0	6	1	35	6,503,090	0.191920
7	36	45	Work	0	5	1	45	6,834,007	0.201686
8	46	55	Work	0	5	1	55	4,187,502	0.123582
9	56	65	Work	0	5	1	65	1,894,782	0.055919
10	66	75	Retired	0	0	4	75	460,193	0.013581
11	76	85	Retired	0	0	3	85	181,034	0.005343
12	86	95	Retired	0	0	2	95	38,890	0.001148

 Table 1
 Population pyramid collected from the World Bank Databank

Table 2 Population parameters	Parameter	Value	
	Age distribution	Saudi Arabia	
	Case counts (Confirmed and death cases)	Saudi Arabia	
	Number of hospital beds	70,815	
	Number of available ICU beds	6515	
	Cases imported into community per day	0.1	
	Number of cases at the start of the simulation	14,735	
	Total population	34,218,169	

3.4 Population

We used the World Bank Databank datasets [12] to create the population pyramid of Saudi Arabia, as shown in Table 1. It demonstrates the general population pyramid across different age groups employing the real population pyramid.We used the World Bank Databank datasets [12] to create the population pyramid of Saudi Arabia, as shown in Table 1. It demonstrates the general population pyramid across different age groups employing the real population pyramid.

The exploratory population parameters of COVID-19 for KSA are summarized in Table 2, and the epidemiological parameters are summarized in Table 3.

Table 3 Epidemiology parameters	Parameter	Value	
•	Average time in regular ward (days)	7	
	Average time in ICU ward	14	
	Infectious period	3	
	Latency	3	
	Increase in death rate when ICU are overcrowded	2	
	Seasonal peak in transmissibility	June, July 2020	
	R_0 at the beginning of the outbreak	1.7–2	
	Seasonal variation in transmissibility	0	

Intervention Sequence	From	То	Reduction of transmission
Intervention 0	Mar 09, 2020	Apr 16, 2020	1-1%
Intervention 1	Apr 16, 2020	May 21, 2020	24.9-29.1%
Intervention 2	May 21, 2020	Jun 11, 2020	15.1-16.9%
Intervention 3	Jun 11, 2020	Jul 02, 2020	32.7-39.3%
Intervention 4	Jul 02, 2020	Jul 29, 2020	39.7-48.3%
Intervention 5	Jul 29, 2020	Aug 19, 2020	31.8-38.2%%
Intervention 6	Aug 19, 2020	Sep 22, 2020	37–45%
Intervention 7	Sep 22, 2020	Oct 13, 2020	30.9-37.1%
Intervention 8	Oct 13, 2020	Nov 03, 2020	29.2-34.8%
Intervention 9	Nov 03, 2020	Dec 07, 2020	38.8-47.2%
Intervention 10	Dec 07, 2020	Jan 01, 2021	34.4-41.6%
Intervention 11	Jan 01, 2021	Feb 01, 2021	16-18%
Intervention 12	Feb 01, 2021	Mar 14, 2021	29.2-34.8%
Intervention 13	Mar 14, 2021	Apr 17, 2021	20.5-23.5%
Intervention 14	Apr 17, 2021	June 20, 2021	30.9-37.1%

 Table 4
 Intervention with transmission rate

3.5 Epidemiology

3.5.1 Mitigation

The study considered various control measures and intervention strategies, such as quarantine, social distancing, school and university closures, travel suspension, prohibition of social gatherings and complete lockdown. Each intervention was measured over time and compared with the baseline scenario to reduce the impact of the pandemic. Scenarios are compared with the number of confirmed cases, growth rate, peak time, and total deaths. Table 4 demonstrates the interventions starting from the first cases reported in the KSA until June 20, 2021, with a total of 15 runs.

3.6 Results

By introducing the interventions, the cumulative number of infected cases and the number of deaths were reduced, which helped decrease the effects of the epidemic by flattening the curve and decreasing the number of infected cases (Fig. 3).

A model [11] was developed to estimate the epidemiological parameters for the 9 different age groups, as shown in Table 5 and Fig. 3. When applied to the KSA epidemic, the model estimates that the virus had an R_0 value between 1.7 and 2.

Table 5 demonstrates the distribution of age groups, which shows that individuals fall into each group when infected. The columns are summarized based on the severity informed by the epidemiological and clinical observations from China, Spain, Switzerland, and Italy.

Figure 4 estimates the evolution of the KSA epidemic under the scenario where the security measures are relaxed for the younger group but kept the same within the older group. The evolution of the epidemic predicted that most deaths occurred in the older age group, even though the percentage of infections was predicted to be higher in the younger age group.

3.6.1 Discussion

Considering the rising number of cases and deaths in the Kingdom of Saudi Arabia, several interventions have been introduced by the government, such as social distancing, prohibiting social gatherings with no more than twenty individuals, temporary bans on dine in restaurants and international travel bans. The SIR-F model is improved by closure and lockdown to investigate the effect of interventions with the closure of educational institutions and the market. Forecasting and uncertainty have been proposed to be integral parts of the decision-making process [13].

Regarding the implementation of an intervention, the effect was predicted for the spread of virus with a simulation run of 700 days starting from the date when the first case was recorded [14]. The study analyzed the virus peak and size of the pandemic in the Kingdom and estimated that the virus would be under control by the end of June 2021, as shown in Fig. 5 [14].

The study verifies that the infection curve decreased in April 2021 and that the pandemic period will end in April 2022. Additionally, Fig. 6 shows that $\rho(rho)$ for the fifth phase is decreasing but is far from the end of the epidemic [14].

In our present study, we focused on close observation of interventions by categorizing the individuals into different age groups. To control the spread of the virus, we need to keep the effective reproduction number below one. We have proposed a modified SEIR model to observe overflow in (C/O) situations to monitor the infection rate closely and to avoid overflows in the ICU by observing infections in different age groups. Table 5 demonstrates that the effect of the virus on the elderly age group with the highest fatal percentage

Age group	Age distribution	Confirmed % of total	Severe % of Confirmed	Pallia- tive % of severe	Critical % of severe	Fatal % of criti- cal	Fatal % of all infec- tions
0–9	5,956,215	5	1	0	5	10	0
10–19	4,860,281	5	3	0	10	10	0
20–29	5,354,763	10	3	0	10	10	0
30–39	6,980,363	15	3	0	15	10	0.01
40-49	6,408,790	20	6	0	20	10	0.02
50–59	3,216,573	20	10	0	25	20	0.1
60–69	1,373,521	25	25	5	30	30	0.88
70–79	493,856	20	35	10	25	40	2.1
80+	169,509	40	50	20	15	40	5.2

Table 5 Age group infected distribution



Fig. 3 Infection growth

rate of infections was very high compared with the other age groups. Since the virus has a more severe effect on elderly individuals, plans and policies for intervention strategies can be developed, encompassing early detection through surveillance and diagnosis. In response to the increase in the number of daily cases and to control the pandemic, Saudi Arabia launched the COVID-19 vaccination drive on December 17, 2020, after the Saudi Food and Drug Authority (SFDA) approved the registration of the Pfizer-BioNTech vaccine. During



Fig. 4 Confirmed case distribution in different age groups



Fig. 5 Predicted number of cases with closure and lockdown using the SIR-F model for 700 days

the campaign, elderly individuals over the age of 65, those suffering from chronic diseases, and front-line health workers were given priority. The second vaccination phase began on February 18, 2021. The second vaccine, Oxford-AstraZeneca, was approved by the Saudi Food and Drug Authority (SFDA) and made available for all Saudi citizens and expatriates. Free vaccine shorts were distributed throughout the kingdom. The Ministry of Health announced on May 30, 2021, that 40% of the Kingdom's population had received at least one



dose of a COVID-19 vaccine administered across 587 vaccination centers [15]. The government of Saudi Arabia aims to complete the vaccination campaign drive before the end of 2021. As a result, future research can analyze a further decrease in the infection rate, a decrease in the parameter $\rho(rho)$ [14], and the mitigation of the pandemic at an earlier date.

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