

# Analysis of workflow schedulers in simulated distributed environments

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#### **Abstract**

Task graphs provide a simple way to describe scientific workflows (sets of tasks with dependencies) that can be executed on both HPC clusters and in the cloud. An important aspect of executing such graphs is the used scheduling algorithm. Many scheduling heuristics have been proposed in existing works; nevertheless, they are often tested in oversimplified environments. We provide an extensible simulation environment designed for prototyping and benchmarking task schedulers, which contains implementations of various scheduling algorithms and is open-sourced, in order to be fully reproducible. We use this environment to perform a comprehensive analysis of workflow scheduling algorithms with a focus on quantifying the effect of scheduling challenges that have so far been mostly neglected, such as delays between scheduler invocations or partially unknown task durations. Our results indicate that network models used by many previous works might produce results that are off by an order of magnitude in comparison to a more realistic model. Additionally, we show that certain implementation details of scheduling algorithms which are often neglected can have a large effect on the scheduler's performance, and they should thus be described in great detail to enable proper evaluation.

**Keywords** Distributed computing  $\cdot$  DAG scheduling  $\cdot$  Task Scheduling  $\cdot$  Network models

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## 1 Introduction

Representing a computation by a directed task graph is a common programming model for defining programs for a distributed system or a parallel computer. The main advantage of such a program description is the possibility to capture parallelizable behaviour of an application while allowing to abstract the computation from specific architectures and computational resources. Task graphs are becoming one of the most popular ways of executing complex workflows on distributed systems (both cloud and high-performance clusters) and it is an active research idea to design both new task execution frameworks [4, 5, 31, 33, 37] and scheduling algorithms [13, 40, 43, 44].

Task graphs are used with various levels of task granularity. Fine-grained task graphs occur in the context of task-based programming models where tasks are usually short running fragments of code within a single program [18, 41]. In contrast, coarse-grained task graphs are used to represent complex workflows composed of a set of potentially long-running programs [3, 17, 28]. Although our benchmarks primarily focus on the latter category, the results are generalizable to a wider spectrum of task graph scheduling problems.

To execute a task graph as quickly as possible, it is crucial to produce a quality schedule that will distribute the computation amongst multiple nodes to achieve as much parallelization as possible, while also minimizing data transfers over the network. Yet, finding the optimal schedule for a task graph is NP-hard even for very restricted formulations (without transfer costs and resource management) [42]. Plenty of heuristics have been proposed to tackle this problem, ranging from list-based scheduling to genetic algorithms. Many surveys and comparisons of scheduling algorithms were published in [1, 21, 26, 44].

The primary objective of this paper is to analyze the behaviour of various scheduling heuristics and present the results in a verifiable and reproducible form. Most scheduler surveys assume an environment with an oversimplified communication and computation model. Some works use more complex communication models that attempt to simulate more realistic network behaviour [23, 30, 36, 38]. However, none of them deal with two important properties that inevitably arise during the actual execution of real world task graphs, namely that the scheduling itself takes time and that the duration of the individual tasks may not be known in advance to the scheduler. Also, to our best knowledge, no previous survey provides source codes of the implemented schedulers. One of the findings of our analysis is that various scheduler implementation details can have a large effect on the performance of the scheduling algorithm. Surveys that do not provide detailed scheduler source codes will thus be difficult to reproduce and verify.

It is not a goal of this paper to introduce new scheduling heuristics, rather it should provide guidance on which scheduler implementation details should be published and which benchmark properties should not be omitted in order to obtain reproducible results.

This work has the following goals to improve the current situation:



 Benchmark various scheduling algorithms in a complex communication and computation environment and provide the results in an open and reproducible form. This includes the task graphs, all source codes for schedulers and the simulation environment and also all benchmark scripts.

- Evaluate various simulated properties (such as network model or knowledge of task durations) to find out which have the largest effects on the performance of the individual schedulers.
- Provide an extensible simulation environment that facilitates prototyping and evaluation of task graph schedulers and network models.

This paper is structured as follows: We describe the problem of task graph scheduling in Sect. 2. Section 3 gives a brief overview of related works. Section 4 describes the simulation environment and implemented scheduling algorithms. Section 5 describes benchmark methodology and benchmarked task graphs. Section 6 contains benchmark results and discusses effects of the simulated properties. Lastly, we conclude in Sect. 7.

## 2 Problem statement

A *task graph* is an acyclic graph where nodes represent tasks and output data objects. Formally,  $TG = (\mathcal{T}, \mathcal{O}, \mathcal{A})$ , where  $\mathcal{T}$  is a set of tasks,  $\mathcal{O}$  is a set of data objects produced by tasks;  $\mathcal{T} \cap \mathcal{O} = \emptyset$ .  $\mathcal{A} = (\mathcal{T} \times \mathcal{O}) \cup (\mathcal{O} \times \mathcal{T})$  is a set of arcs between tasks and objects. Let  $t \in \mathcal{T}, o \in \mathcal{O}$ , then  $(t, o) \in \mathcal{A}$  means that a task t produces object o;  $(o, t) \in \mathcal{A}$  means that a data object o is an input for task t. We always assume that each object is produced by exactly one task  $(\forall o \in \mathcal{O} : |\mathcal{A} \cap (\mathcal{T} \times \{o\})| = 1)$ . For a task t, we call the set  $\{o \in \mathcal{O} \mid (o, t) \in \mathcal{A}\}$  inputs of task t and  $\{o \in \mathcal{O} \mid (t, o) \in \mathcal{A}\}$  outputs of task t. We also assume that  $(\mathcal{T} \cup \mathcal{O}, \mathcal{A})$  forms a finite directed acyclic graph.

Many works related to task graph scheduling assume that each task produces at most one output; however, in practice having multiple outcomes from a single task is a common requirement in workflows and is directly supported by some frameworks (e.g. Luigi, Rain²). Multiple outputs per task can be simply modeled in systems supporting only one output per task by introducing artificial tasks with zero execution times. Each such task takes an output and decomposes it into pieces. However, as we do not want to complicate scheduling by introducing dummy tasks that are actually not necessary to schedule, our simulation environment directly supports tasks with multiple outputs.

The task graph is executed on a set of *workers*, processes/machines that are able to execute tasks and produce their outputs. Let W denote the set of all workers. When a task t is finished on a worker w, all its output objects become immediately available at worker w. The worker w may send an object o to another

<sup>&</sup>lt;sup>2</sup> https://github.com/substantic/rain.



<sup>&</sup>lt;sup>1</sup> https://luigi.readthedocs.io/en/latest.

worker w' and make o available on w'. A task t can be executed on worker w only if all inputs of t are available at worker w. We assume that execution of each task is uninterruptible and non-replicable. We say that a task t is ready if all its inputs are already computed; a task t is enabled on w if t is ready and all its inputs are available on w.

The job of the scheduler is to assign tasks to workers, formally to produce a map  $S: \mathcal{T} \to \mathcal{W}$ . Static schedulers produce this map at the beginning of the computation and assign a worker to each task. Dynamic schedulers compose the map dynamically during the execution of the task graph. The goal of the scheduler is to create S such that it minimizes the makespan (the time it takes to finish all tasks in the graph).

A scheduler is allowed to change its decision and reschedule an already scheduled task to a different worker. A task reschedule may fail if the task is already running or if it has been already finished.

To align the simulation better with real-world task graph execution, we also include the following properties:

**Multi-core workers** Each worker may have multiple CPU cores; each task may require a number of CPU cores. The total number of cores required by simultaneously running tasks on a worker cannot exceed the total number of CPU cores of that worker. This reflects the fact that currently most of commodity and HPC processors have multiple CPU cores and software (represented by tasks) can utilize them.

**Communication model** In many previous scheduler surveys and theoretical papers, it is assumed that the transfer time of a data object depends only on the size of the object and not on the current network utilization [25, 39, 44, 46]. This is an unrealistic assumption about real computer networks, as the network speed is affected by the number of concurrently running downloads. Moreover, it is common that a real worker downloads more than one data object simultaneously, which further affects the transfer durations because the worker's bandwidth is shared.

We provide a more realistic network model that simulates full-duplex communication between workers where the total upload and download bandwidth of each worker is limited. The sharing of bandwidth between worker connections is modeled by the *max-min fairness model* [7]. Max-min fairness provides a bandwidth allocation for each worker. If we increase an allocation of any participant, than we necessarily decrease the allocation of some other participant with an equal or smaller allocation. When a download starts or finishes, the data flow between workers is recomputed immediately, thus we neglect the fact that it may take some time for the bandwidth to fully saturate.

To compare this model with previous results, we also include the *simple* model in our simulation environment. It corresponds to the above mentioned behaviour used in several previous works. In our experiments, we observe how the makespan changes in response to the used network model.

**Worker inner scheduler** Since each worker has to keep track of its running tasks, manage resources, and handle data object transfers, it becomes quite complex. In practice, the global scheduler cannot micromanage each worker because this approach could not scale to a larger number of workers. Therefore, we model a situation where each worker has its own inner scheduler. We call it *w-scheduler* and we reserve the word "scheduler" for the global scheduler that assigns tasks to workers.



The w-scheduler is not a subject of study in this work, hence we are going to fix one particular worker scheduler and execute all experiments with it. The implementation is inspired by the worker implementation used in HyperLoom [17] and Rain. It is described in Appendix 1.

**Minimal scheduling delay** Dynamic schedulers create task assignments continuously, based on the current situation. They could make a scheduling decision every time a task is finished; however, in practice there is often an upper bound on the number of scheduler invocations per second. It might be introduced artificially to reduce the scheduling overhead or it might be caused by a software or hardware limitation (e.g. messages with task changes cannot be received more often). We introduce *minimal scheduling delay* (MSD) that forces a minimal delay between two scheduler invocations.

**Information modes** In most works, it is expected that the scheduler is aware of the duration of all tasks and the sizes of all resulting data objects in advance. However, in practice this information may not be available. In many cases, it may not be clear for the author of the task graph how long will the tasks run or what will be the size of the resulting objects (e.g. even for an experienced data scientist, it may be hard to estimate how long will it take to train a machine learning model on a particular dataset with particular hyperparameters). Even if the task-graph author has precise knowledge of each task duration, it may be tedious to manually annotate each task individually. Therefore, we consider the following three modes of execution, which we call *imodes*:

- *exact*—scheduler has access to all task durations and object sizes for all elements in the task graph.
- *user*—for unfinished tasks, the scheduler has access only to a user-provided estimate of the task duration and its output sizes.
- *mean*—for unfinished tasks, the scheduler does not have any information about the duration or size of any graph element. However, the scheduler obtains the mean of the duration of all tasks and the mean of the size of all outputs.

Another possible scenario to consider could be a "blind" mode, where the scheduler does not know any durations nor sizes in advance. However, in this situation, the schedulers would be very sensitive to an initial estimate of the durations and sizes (namely the ratio between them, which influences decisions whether to move data objects between workers). This estimate strongly influences the early behaviour of dynamic schedulers and it is completely vital for static schedulers. To avoid exploring various estimated values that would have to be chosen almost arbitrarily, we propose to use the *mean* mode instead of the blind mode. We assume that if the scheduler knows nothing in advance, it could always monitor the durations and sizes of finished tasks gradually and such monitored values would converge to the mean. In practice, this would take some time, in our environment the schedulers know about the mean in advance. Nevertheless, we can often get a reasonable estimate of the mean durations based on previous executions of similar workflows.

For the *user* imode, we use values sampled from a random distribution that is specific to a subset of tasks or objects within the task graph that share similar properties



(e.g. in MapReduce, all map operations use the same distribution, all reduce operations use another distribution). Categorization of tasks into these subsets was done manually. This simulates a user that is able to categorize tasks and provide an estimate for each category.

In the experiments presented in this work, we aim to explore the behaviour of state of the art schedulers in a complex simulation environment that includes all of the aspects described above.

Beside the comparison of individual schedulers, we also want to measure how much does the used network model, information modes and minimal scheduling delays affect the individual schedulers. Many previous scheduler studies were performed in relatively simple environments without these effects. We want to analyze whether there is a significant difference between the performance of the standard heuristics when they are benchmarked in more realistic conditions.

## 3 Related work

Various workflow scheduling algorithms have been researched and implemented to date (e.g. HLFET [1], SCFET [27], DLS [34], LAST [6], MCP [45], ETF [19]). Number of publications overview and compare properties of these algorithms [26, 27, 44].

Numerous surveys on distributed workflow environments and their schedulers have been performed to categorize workflow environments based on their task allocation strategies, load balancing, and multi-tenancy behaviour [2, 22, 24, 29]. These are mostly focused on cloud scenarios and scheduling algorithms are not their main focus. They thus do not provide scheduler benchmarks.

Many works evaluate the algorithms using simplified environments with simple communication models and without considering *MSD* and *imode* effects. In [36] a complex network model with various network topologies was considered, but it only reports results on two scheduling algorithms. The [38] investigates the incorporation of contention awareness into task scheduling. In [30], performance impact of communication costs on static schedulers is studied.

All of these works use the assumption that task durations and data object sizes are known in advance (i.e. in our terminology they use the *exact* imode). As far as we know, there was no systematic study of MSD or imodes in the context of DAG scheduling.

Some of the popular distributed environment simulators such as Simgrid [14] or CloudSim [12] focus on deployment and provisioning infrastructures with low granularity of resource requirements, but do not directly consider scheduling task workflows with task dependencies. This problem has been assessed by various tools built on top of these two systems. DAGSim [23] only reports experimental results without providing the actual implementation which makes it difficult to extend the solution or reproduce the results. SimDAG [47] does not consider task resource requirements (e.g. number of cores) and also does not allow to define custom network models. WorkflowSim [16], ElasticSim [11], CloudSim4DWf [20] and Wrench [15] focus on simulating complex cloud scenarios, involving datacenter costs, multi-tenancy,



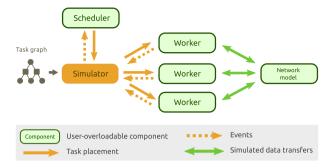


Fig. 1 Estee architecture

storage layers and other advanced factors. Even though their simulation environments are very advanced, their scheduling mostly operates on a different level of granularity, focusing on relatively coarse-grained cloud or cluster jobs. Scheduling a large number of fine-grained tasks is not their main focus and therefore it would be challenging to extend their schedulers with support for MSD or imodes.

## 4 Simulation environment

This section describes the simulation environment that we have implemented to analyse and compare various schedulers., benchmarked schedulers, network models and task graph sets.

#### 4.1 Simulation

We have implemented ESTEE,<sup>3</sup> a flexible open-source simulation environment that is designed for benchmarking and experimenting with task schedulers. The implementation is very open-ended and allows us to implement new schedulers, network models and workers easily. However, it also comes "battery-included" and provides implementations for all its components.

#### 4.2 Architecture

The architecture of ESTEE is depicted in Fig. 1. The central component is the *Simulator*, which controls the whole simulation and communicates with the scheduler and workers. The *Scheduler* reads events about finished tasks and returns allocations of tasks to workers. A *Worker* simulates the execution of assigned tasks and also the transfer of task outputs between workers. The communication between workers is handled by a network model that informs them about download completion.

<sup>&</sup>lt;sup>3</sup> https://github.com/it4innovations/estee.



Estee is written in Python to provide a high-degree of flexibility that facilitates rapid prototyping. Estee is an open-source project provided under MIT license.

## 4.3 Schedulers

We have implemented a set of schedulers inspired by classic scheduling heuristics. Originally these heuristics were mostly designed for environments with only one core per worker and one output per task; therefore, we had to slightly extend their implementation.

**blevel** Highest Level First with Estimated Times [1] (HLFET) is a basic list-based scheduling algorithm that prioritizes tasks based on their b-level. B-level of a task is the length of the longest path from the task to any leaf task (in our case the length of the path is computed using task durations, without data object sizes). The tasks are scheduled in a decreasing order based on their b-level.

**tlevel** Smallest Co-levels First with Estimated Times [27] is similar to HLFET, with the exception that the value computed for each task (t-level) is the length of the longest path from any source task to the given task. This value corresponds to the earliest time that the task can start. The tasks are scheduled in an increasing order based on their t-level.

**dls** Dynamic Level Scheduling [34] calculates a dynamic level for each task-worker pair. It is equal to the static b-level lessened by the earliest time that the task can start on a given worker (considering necessary data transfers). In each scheduling step, the task-worker pair that maximizes this value is selected.

mcp The Modified Critical Path [45] scheduler calculates the ALAP (as-late-as-possible) time for each task. This corresponds to the latest time the task can start without increasing the total schedule makespan. The tasks are then ordered by this value in an ascending order and scheduled to the worker that allows their earliest execution.

**etf** The ETF (Earliest Time First) scheduler [19] selects the task-worker pair that can start at the earliest time at each scheduling step. Ties are broken by a higher static b-level.

**genetic** This scheduler implementation uses a genetic algorithm to schedule tasks to workers. It uses the mutation and crossover operators described in [32]. Only valid schedules are considered, if no valid schedule can be found within a reasonable amount of iterations, a random schedule is generated instead.

ws Implementation of a simple work-stealing algorithm. The default policy is that each ready task is always assigned to a worker where it can be started with minimal transfer costs. The scheduler monitors the load of workers and when a worker starts to starve then a portion of tasks assigned to other workers is rescheduled to the starving worker.

We have also implemented several naive schedulers to serve as a baseline for scheduler comparisons.

**single** Scheduler that assigns all tasks to a single worker (it selects the worker with the most cores). The resulting schedule never induces any data transfers between workers.



**random** Static scheduler that schedules each task to a random worker.

All scheduler implementations use a random choice when an indistinguishable decision in the algorithm occurs, e.g. when more tasks have the same b-level in the case of *blevel*.

We have implemented the list based schedulers (*blevel*, *tlevel*, *dls*, *mcp*, *etf*) as closely as possible according to their description from the works that introduced them. These heuristics often schedule a task to a worker that allows the earliest start time of the task. However, the scheduler algorithms do not prescribe in detail how exactly should the scheduler find such worker, because the exact earliest start time often cannot be determined in advance due to unpredictable network contention. This implementation detail is crucial and should be included in the description of new scheduling algorithms.

For our implementation, we used a simple estimation of the earliest start time based on the currently running and already scheduled tasks of a worker and an estimated transfer cost based on uncontended network bandwidth.

In addition, we have also created extended versions of the *blevel*, *tlevel* and *mcp* schedulers to make them more compatible with the additional properties that are present in our simulation environment (e.g. multi-core workers, multi-core tasks, imodes). These modified versions use a worker selection heuristic that we call "greedy transfer" and they contain *-gt* suffix in their name in the benchmark results. We have not applied this heuristic to other schedulers, either because it could not be applied to them without changing their behaviour fundamentally or they already supported the mentioned properties.

The "greedy transfer" heuristic assigns the selected task to a worker that has a sufficient number of free cores on which the task may be executed and that requires the minimal data transfer (sum over all sizes of data objects that have to be transferred to that worker). It also adds support for clusters where some machines have a different number of cores than others. When a task t that needs c cores cannot be scheduled because of an insufficient number of free cores, the list scheduling continues by taking another task in the list instead of waiting for more free cores. This task will only consider workers that have less than c cores. This allows to schedule more tasks while it does not modify the priority of tasks because t cannot be scheduled on such workers anyway. Note that when all workers have the same number of cores, the behaviour is identical to ordinary list scheduling.

# 5 Benchmark description

This section describes task graphs that we have used to compare the performance of various scheduling algorithms and also cluster and scheduler configuration that we have used in our benchmarks.



## 5.1 Task graph datasets

We use three task graph sets including simple elementary graphs as well as real world inspired graphs to test the behaviour of schedulers in various situations. The first two sets are prepared by the authors, the third task graph set is derived from a set commonly used in other works. All graphs are published at [8]. Estee contains a task graph generator that can be used to generate graphs from the following categories with various parametrizations.

**elementary** contains trivial graph shapes, such as tasks with no dependencies or simple fork-join graphs. This set should test how the scheduler heuristics react to basic graph scenarios that frequently form parts of larger workflows.

**irw** is inspired by real world workflows, such as machine learning cross-validation or map-reduce.

**pegasus** is derived from graphs created by the Synthetic Workflow Generators [35]. The generated graphs correspond to the *montage*, *cybershake*, *epigenomics*, *ligo* and *sipht* workflows. We have extended the graphs with additional properties needed for testing imodes (notably expected task durations and data object sizes for the *user* imode).

The properties of all used graphs are summarized in Table 1. Each task in all described task graphs requires at most four cores.

### 5.2 Clusters

We have used the following cluster configurations (where  $w \times c$  means that the cluster has w workers and each worker has c cores):  $8 \times 4$ ,  $16 \times 4$ ,  $32 \times 4$ ,  $16 \times 8$ ,  $32 \times 16$ .

For simulating network connections, we use the *max-min fairness* and *simple* network models with bandwidths ranging from 32 MiB/s to 8 GiB/s. For experiments that do not focus on the network model (e.g. comparing imodes), we only use the *max-min* network model.

## 5.3 Scheduler settings

For evaluating the effect of MSD, we benchmark several MSD configurations. As a baseline we use a configuration with no delay (MSD is zero), i.e. the scheduling process is executed as soon as an event occurs. Beside the base case we have also measured delays of 0.1, 0.4, 1.6, and 6.4 seconds. In all these nonzero cases, we have also added a 50 milliseconds delay before sending the scheduler decision to workers to simulate the scheduler computation delay. For experiments that do not focus on MSD, we always use MSD of 0.1 seconds and 50 milliseconds delay.

For testing the effect of imodes, we benchmark schedulers with different information modes (exact, user, and mean) as defined in Sect. 2. For experiments that do not focus on imodes, we always use the *exact* imode.



Table 1 Task graph properties

II						
Graph	D	1#	0#	TS	LP	Description
plain1n	e	380	0	0.00	1	Independent tasks; normally distributed durations (Fig. 2a)
plain1e	မ	380	0	0.00	1	Independent tasks; exponentially distributed durations (Fig. 2a)
plain1cpus	မ	380	0	0.00	1	Independent tasks with varying core requirements (Fig. 2a)
triplets	e	330	220	17.19	3	Task triplets; middle task requires 4 cores (Fig. 2h)
merge_neighb.	ပ	214	107	10.36	2	Merge of adjacent task pairs (Fig. 2e)
merge_triplets	ပ	148	1111	10.77	2	Merge of task triplets (Fig. 2g)
merge_sm-big	မ	240	160	7.74	2	Merge of two results (0.5 MiB and 100 MiB data objects) (Fig. 2d)
fork1	o	300	100	71.6	2	Tasks with a pair of consumers each consuming the same output (Fig. 2b)
fork2	e	300	200	19.53	2	Tasks with a pair of consumers each consuming different output (Fig. 2c)
bigmerge	မ	321	320	31.25	2	Merge of a large number of tasks (variant of Fig. 2f)
duration_stairs	မ	380	0	0.00	1	Independent tasks; task durations range from 1 to 190 s (Fig. 2a)
size_stairs	e	191	190	17.53	2	1 producer 190 outputs / 190 consumers; sizes range from 1 to 190 MiB
splitters	ပ	255	255	32.25	∞	Binary tree of splitting tasks (Fig. 2j)
conflux	မ	255	255	31.88	∞	Merging task pairs (inverse of splitters) (Fig. 2k)
grid	ပ	361	361	45.12	37	Tasks organized in a 2D grid (i.e. splitters followed by conflux) (Fig. 2i)
fern	е	401	401	11.11	201	Long task sequence with side tasks (Fig. 21)
gridcat		401	401	115.71	4	Merge of pairs of 300 MiB files
Crossv		94	06	8.52	5	Cross validation
Crossvx		200	200	32.66	5	Several instances of cross validation
fastcrossv		94	06	8.52	5	Same as crossy but tasks are 50x shorter
mapreduce		321	25760	439.06	3	Map-reduce pattern
nestedcrossv		566	270	28.41	∞	Nested cross validation
montage	d	77	150	0.21	9	Montage workflow from Pegasus
cybershake	d	104	106	0.84	4	Cybershake workflow from Pegasus
epigenomics	d	204	305	1.36	∞	Epigenomics workflow from Pegasus
ligo	d	186	186	0.11	9	Ligo workflow from Pegasus



Table 1 (continued)	(1)					
Graph	D	L#	0#	TS	LP	Description
sipht	d	64	136	0.12	5	Sipht workflow from Pegasus
D = Dataset (e = elementary, i = path in the graph	elementary, i	= irw, p = pe	sgasus); #T = $\mathbb{N}$	vumber of tasks;	#O = Number	irw, p = pegasus); #T = Number of tasks; #O = Number of outputs; TS = Sum of all output object sizes (GiB); LP = longest oriented

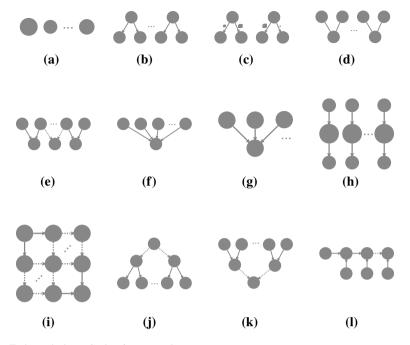


Fig. 2 Task graph shapes in the elementary data set

## 6 Evaluation

This section discusses results obtained by running the described benchmarks in our simulation environment. All obtained results are published at [9] including the generated charts for all configurations. Each particular configuration described in the previous section was executed 20 times, except for the *single* scheduler, which was executed only once, since it is deterministic. Unless specified otherwise, the experiments were performed with the default benchmark configuration (*max-min* netmodel, *exact* imode and 0.1s MSD).

Our benchmarks have produced large amounts of results. Below we discuss several noteworthy results, you can find more complete scheduler comparison results in the appendix.

**Random scheduler** Figure 3 shows simulated makespan lengths produced by the *random* scheduler and two other competitive schedulers, *blevel-gt* and the workstealing scheduler on selected graphs. While the random scheduler produces quite long makespans in certain cases (for example in the cross-validation graph), it is also surprisingly often quite competitive. Especially as the number of workers and the bandwidth increases, it can get even with other schedulers and sometimes even overcome them.

Similar results have also been observed in [10]. These results show that as the computational cluster and network transfer speed gets larger, scheduling decisions can become less important and other factors (like the runtime overhead of the task execution system) can start to dominate.



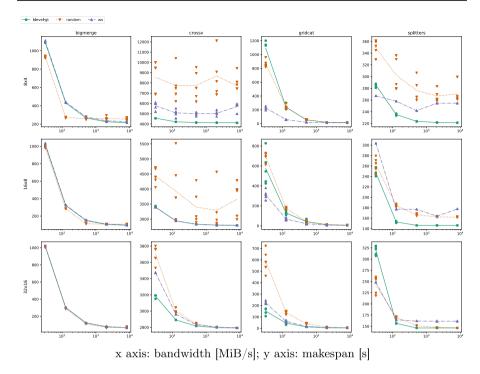


Fig. 3 Random scheduler performance

Worker selection strategy We have already explained in Sect. 4.3 that published scheduler algorithms do not always specify the exact implementation of worker selection. Yet as we can see in Fig. 4, this implementation detail is crucial. The worker selection strategy (which is the only thing that differentiates the schedulers with and without the -gt suffix) has a large effect on the produced schedule and thus the resulting makespan. Furthermore, it is evident that schedulers that use the "greedy transfer" selection strategy are highly correlated, which hints that in this case selecting the correct workers is more important than scheduling the order in which tasks will be executed.

**Network transfers** Figure 5 demonstrates that schedulers producing similar makespans may in fact generate vastly different amounts of network traffic. For example, for the *nestedcrossv* graph using the  $32 \times 16$  cluster, the work stealing scheduler transfers almost twice as much data than *blevel-gt*, yet it produces almost identical makespans.

**Network models** Figure 6 compares makespans between the *simple* and *max-min* network models on the IRW data set using the  $32 \times 4$  cluster for selected schedulers. The results are normalized with respect to the *simple* model. It is clear that results obtained by using the *simple* model often under-approximate the resulting makespan length. This is caused by the fact that network contention is not taken into account, which causes their transfer duration estimation to be overly optimistic. It is however interesting to note that in some cases the *simple* model over-approximates



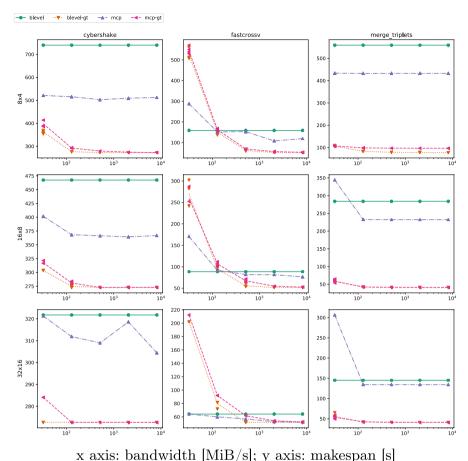


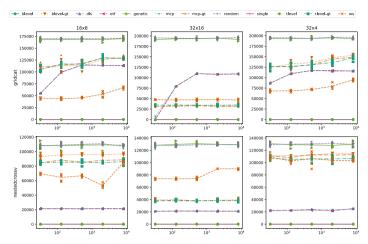
Fig. 4 Comparison of worker selection strategy

the makespan. Since most of the schedulers use heuristics, a faster network transfer does not necessarily lead to a shorter makespan.

On the IRW dataset, the differences vary based on the particular scheduler and task graph. Especially with slower bandwidths, the estimations produced by the two models can be an order of magnitude apart. Note that even small disparities are significant, since as shown in previous surveys [44] and in our provided results, the differences in produced makespans between existing scheduler heuristics are often very small and within a factor of two. As the bandwidth gets faster, the difference between the two models decreases, since network contention is lower and the *max-min* model starts to behave similarly to the *simple* model.

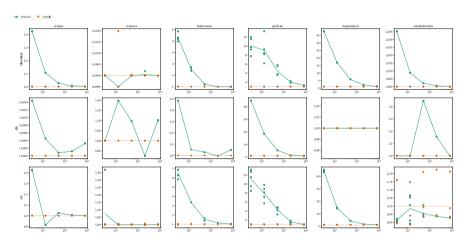
For the Pegasus data set, the results of both models are much more aligned. Differences on higher bandwidths are almost negligible. For slower bandwidths, the differences between the models are within a factor of two. Results for the Pegasus data set can be observed in Fig. 12 in the Appendix.





x axis: bandwidth [MiB/s]; left y axis: makespan [s], right y axis: sum of transferred data between all workers [MiB]

Fig. 5 Total transfers on IRW dataset



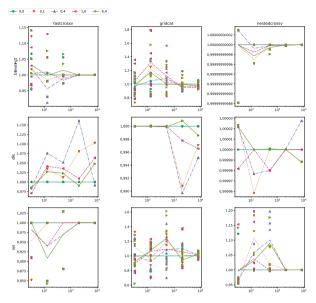
x axis: bandwidth [MiB/s]; y axis: makespan normalized to average of makespan of "simple" model

Fig. 6 Comparison of "max-min" and "simple" netmodel on IRW set; cluster 32 × 4

MSD Figure 7 shows the effect of MSD on the IRW data set using the  $32 \times 4$  cluster for selected schedulers. The results are normalized with respect to the case where MSD equals zero.

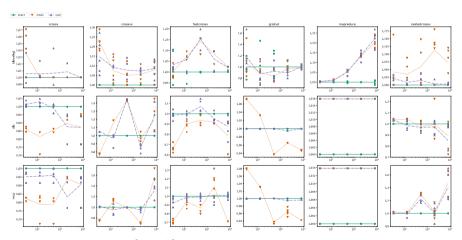
Our results show that the effect of MSD is relatively limited, especially when compared to the effect of the simulated network model. There seems to be no clear pattern as to whether decreasing MSD improves the makespan length consistently or not. It is however interesting to note that increasing MSD can actually improve





x axis: bandwidth [MiB/s]; y axis: makespan normalized to MSD 0.0 case

Fig. 7 Comparison of MSD on IRW subset; cluster  $32 \times 4$ 

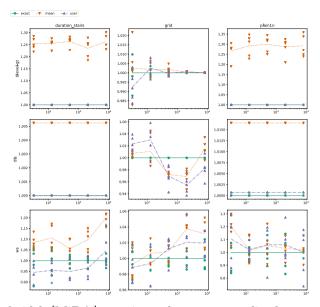


x axis: bandwidth [MiB/s]; y axis: makespan normalized to "exact" imode

Fig. 8 Comparison of imodes on IRW set; cluster  $32 \times 4$ 

the produced schedules (e.g. the *ws* scheduler on the *fastcrossv* graph). Increasing the delay between individual scheduling decisions introduces a "batching" effect. Even though the scheduler is allowed to make decisions less often, it has access to more accumulated events that happened in the meantime and it can thus potentially





x axis: bandwidth [MiB/s]; y axis: makespan normalized to exact average

Fig. 9 Comparison of imodes on three elementary graphs; cluster  $32 \times 4$ 

make a better decision. Using an artificial MSD in a real scheduler implementation can thus serve to improve the produced schedules, not just to reduce the scheduling overhead.

**Imodes** Figure 8 compares makespans between the imodes on the IRW data set using the 32 × 4 cluster for selected schedulers. The results are normalized with respect to the *exact* imode. The results show that the effect significantly depends on the particular scheduler. The effect of imodes seems to be more relevant than the effect of MSD, but in most cases it is still significantly smaller than the effect of the simulated netmodel. Since the *exact* imode provides the schedulers with the most accurate and complete information that they can get, it may be unintuitive why some schedulers actually perform better when presented with incomplete or inaccurate data (e.g. the *dls* scheduler on the *fastcrossv* graph). This is partially caused by the fact that all of the schedulers use heuristics, they can thus produce worse results even when presented with a more accurate input and vice versa.

Another reason is that with the *max-min* netmodel, the scheduler knows only a lower bound on the communication costs even if it knows the exact data size in advance. It has access to the network maximum bandwidth, but does not know the current and future network utilization, thus it only has a crude estimation of the real transfer duration.

Figure 9 shows the effect of imodes on three graphs from the elementary set. Imode effects are mainly visible for the *ws* and *blevel-gt* schedulers; for other schedulers, the effects are significantly smaller. The task graph *duration\_stairs* has tasks with several different durations, the duration estimates produced by the *mean* imode



will thus be fairly inaccurate. This is observable for the *blevel-gt* and *ws* schedulers, which produce up to 25% longer makespans when compared to the *exact* imode.

## 6.1 Validation

It is challenging to validate the performance of multiple task schedulers in real task execution frameworks. Schedulers of existing task frameworks are usually very deeply integrated and coupled to the surrounding system in order to be as performant as possible. It can thus be quite difficult, or even infeasible, to swap the scheduler for a different one. Task frameworks might also be fundamentally incompatible with some scheduling approaches. For example, workstealing schedulers perform a lot of complex communications amongst workers and the scheduler, and if the execution system does not support such communication patterns, implementing workstealing can amount to rewriting the whole system from scratch.

We have leveraged the approach from [10] and used its modified version of Dask [33] as a validation framework. In addition to its built-in workstealing scheduler, we have also implemented three simple scheduling algorithms into it (*blevel*, *tlevel* and *random*).

The absolute makespans of task graphs simulated by ESTEE and task graphs executed by some task framework cannot be directly compared, because the framework will always introduce runtime overheads and system noise that cannot be fully simulated. However, since one of the goals of this paper is to compare the relative performance of various schedulers, we have decided to compare the relative makespans normalized to a reference scheduler (*blevel*) to see if the ratios between the schedulers are similar when simulated and when executed.

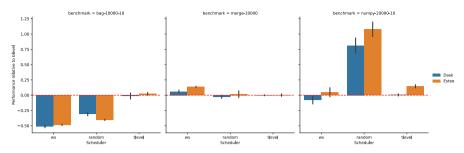
To ensure that we use the same task graphs for execution and simulation, we have executed several task graph benchmarks from [10] (you can find their description in that work) in Dask and generated execution traces. These traces were then used to reconstruct the execution times and output sizes of all tasks and this reconstructed task graph was then simulated in Estee. We have executed the task graphs with 24 workers on two nodes (one with the scheduler and the second one with the workers). Each task graph was executed and simulated three times.

The performance of each scheduler was normalized to the performance of the *blevel* scheduler within the same environment. The relative ratios were centered around zero by subtracting 1 from them, to focus on the relative differences. For example, if a task graph took 100s to execute in Dask with the *blevel* scheduler, but 110s with the *ws* scheduler, the ratio of the *ws* scheduler would be 0.1. If the simulation was perfect, the two columns for each scheduler would have the same height.

We have selected three interesting situations that can be seen in Fig. 10. Full results are in the Appendix in Fig. 13.

The first chart shows a situation where changing the scheduler resulted in large changes in makespans, and Estee was able to simulate these precisely. The second chart demonstrates a situation where all schedulers produce similar makespans, therefore in this case the scheduling algorithm does not seem to be that important. Estee also estimated that the differences between schedulers will be small. In the





x axis: scheduler; y axis: performance relative to blevel

Fig. 10 Scheduler performance relative to blevel in Dask and EsteE

third benchmark, ESTEE systematically overestimated the makespans of all three schedulers with respect to the reference scheduler. While the *ws* implementation in ESTEE was partly inspired by Dask, the scheduler behaviour is quite complex and in this case it was able to outperform the reference scheduler in a way that ESTEE wasn't able to simulate.

To summarize the average error, we took the relative makespans of individual schedulers w.r.t. the reference scheduler and calculated the difference between the executed and simulated relative makespan. The geometric mean of these differences is 0.0347, which suggests that the differences between the execution and simulation were relatively small, usually within a few percent.

## 7 Conclusion

We implemented a set of well known scheduling heuristics and prepared a dataset containing workflows of different types and scales. Based on those, we have conducted a series of fully reproducible benchmarks to analyze the influence of network models, information modes and minimal scheduling delays on the behaviour of the implemented schedulers.

Our results show that several implementation details of both the scheduling algorithms and the simulation environment must be clearly described and specified, otherwise the results might not be reproducible. We have shown that the complexity of the used network model may significantly affect the simulated workflow execution makespan. To our surprise, the effect of information modes has been relatively low for most of the benchmarked cases. It seems that for the benchmarked scheduling algorithms, it is relatively sufficient to know only rough estimates of task durations and data object sizes.

Lastly, we showed that various MSD values have a limited impact on the resulting makespan, but increasing the scheduling delay may in some cases improve the produced schedules.

Our results confirmed that it is important to consider the network behaviour when applying scheduling heuristics in real-world applications and that



it requires caution to refer to results that use simplified network models. We also encourage authors of scheduling algorithms to describe the worker selection strategy, possible delay between scheduler invocations, network model and other implementation details in utmost detail, to make scheduler benchmarks reproducible.

ESTEE, workflow datasets and scheduler implementations are open sourced, to make the results reproducible and extendable by the community. We believe that our results provide a comprehensive overview and comparison of workflow schedulers in various simulated conditions and that ESTEE has further potential to simplify the development and benchmarking of novel schedulers.

# **Appendix 1: W-scheduler**

This section contains description of the *w-scheduler*—worker inner scheduler. The (global) scheduler does not directly communicate with w-schedulers except by assigning tasks to workers. The assignment of task t may also contain two additional values: priority  $p_t$  and blocking  $b_t$ , such that  $b_t \le p_t$ . These values set priorities for downloading and task execution when more possible options are enabled at once for the w-scheduler.

Worker w starts to download an input  $o \in \mathcal{O}$  for a task  $t \in \mathcal{T}$  if t was assigned on w by the scheduler and o is not already on w. The download is started as soon as the task producing o is finished and there is a free download slot.

When more objects can be downloaded at once but there are not enough download slots, the downloads are prioritized based on the priority of tasks that need the object. When a task is not ready then its p is used, otherwise p is boosted by a constant. When more tasks need the same object, then the maximum priority is taken. Downloading is uninterruptible, once an object has started downloading, it is finished without interruption even when a download with a higher priority is enabled and the maximum number of concurrent downloads per worker is reached.

Download slots serve to limit simultaneous downloads. For the *max-min* network model, the worker is allowed to download at most four inputs at once, but at most two from the same worker. These particular numbers were observed as a reasonable compromise between parallel downloads and using bandwidth for higher priority tasks. For the *simple* model, we allow the worker to run arbitrarily many simultaneous downloads to make the model behave in a way that is similar to previous studies.

When a new task becomes enabled on a worker w or an execution of a task is finished, worker runs the following algorithm to decides if another task can be executed. We denote f as the a of free CPU cores (i.e. the total number of worker's cores minus the sum of core requirements of currently running tasks), E as a set of tasks that are enabled and non-running and X as a set of tasks from E which require more than f CPU cores. The worker picks a task t from  $E \setminus X$  with maximal priority such



that  $\forall t' \in X : p_t \leq b_{t'}$ . If such t exists, then t is started. This process is repeated until we cannot start another task this way.

## **Appendix 2: Benchmark results**

See Figs. 11, 12, 13.

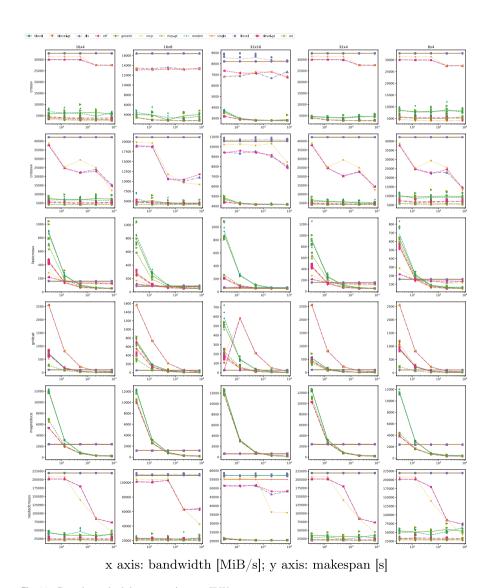
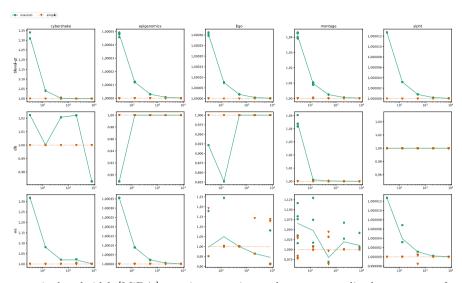


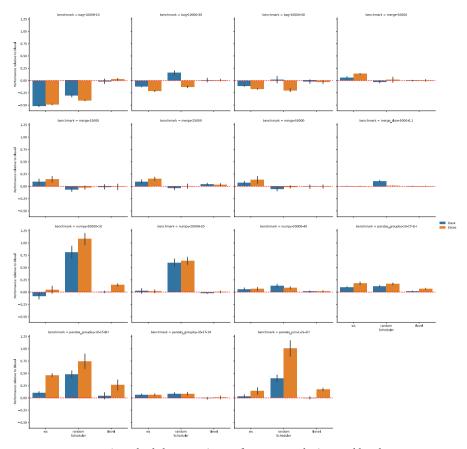
Fig. 11 Complete scheduler comparison on IRW set



x axis: bandwidth [MiB/s]; y axis: execution makespan normalized to average of makespan of "simple" model

Fig. 12 Comparison of "maxmin" and "simple" netmodel on Pegasus set; cluster 32 × 4





x axis: scheduler; y axis: performance relative to blevel

Fig. 13 Scheduler performance relative to blevel in Dask and ESTEE

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