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**MATHEMATICAL MORPHOLOGY  
AND ITS  
APPLICATIONS TO  
IMAGE AND  
SIGNAL PROCESSING**

# **Computational Imaging and Vision**

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# MATHEMATICAL MORPHOLOGY AND ITS APPLICATIONS TO IMAGE AND SIGNAL PROCESSING

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# Preface

It has been seven years since the first International Symposium on Mathematical Morphology (ISMM) took place in Barcelona, Spain, in May 1993. Since then, meetings were also held in Fontainebleau, France (September 1994), Atlanta, Georgia (May 1996), and Amsterdam, The Netherlands (June 1998). This volume contains an up-to-date sampling of international scientific work on Mathematical Morphology that was presented during the fifth ISMM, held at the Xerox Palo Alto Research Center (PARC), in Palo Alto, California, June 26–29, 2000.

We would like to thank all members of the program committee for their invaluable work in reviewing the submitted papers. A blind review process was used, whereby each paper was reviewed by two to four committee members. This resulted in the acceptance of the 45 papers included in this volume. The tight schedule the ISMM chairs were working with required that committee members review up to ten papers in four weeks, a Herculean effort on their part. We are deeply appreciative of their commitment to making this conference a success.

We are also thankful to Jeanette Figueroa for her amazingly efficient help with all aspects of the organization. The conference would not have been the same without her. We would also like to thank Ulisses Braga-Neto and Sinan Batman who handled the rather difficult task of identifying important keywords used to build the subject index at the end of this volume. Finally, we gratefully acknowledge the financial and logistical support provided by Xerox Corporation.

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