



1 ORIGINAL RESEARCH

2 **Anovel HEOMGA Approach for Class Imbalance Problem**  
3 **in the Application of Customer Churn Prediction**

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7 **Abstract**

8 Making class balance is essential when learning from highly skewed datasets; otherwise, a learner may classify all instances to  
9 a negative class, resulting in a high false-negative rate. As a result, a precise balancing strategy is required. Many researchers  
10 have investigated class imbalance using Machine Learning (ML) methods due to their powerful generalization performance  
11 and interpreting capabilities, comparing with random sampling techniques, to handle the problem of class imbalance in the  
12 preprocessing phase to facilitate learning process and improve performance results of learners. In this research, an effective  
13 method called HEOMGA is presented by combining Heterogeneous Euclidean-Overlap Metric (HEOM) and Genetic  
14 Algorithm (GA) for oversampling minority class. The HEOM is employed to define a fitness function for the GA. To assess  
15 the performance of the proposed HEOMGA method, three benchmark datasets from UCI repository in the domain of cus-  
16 tomer churn prediction are examined using three different ML learners and evaluated with three performance metrics. The  
17 experiment results show the effectiveness of the proposed method compared to some popular oversample methods, such as  
18 SMOTE, ADASYN, G SMOTE, and Gaussian oversampling methods. The HEOMGA method significantly outperformed  
19 the other oversampling methods in terms of recall, G mean, and AUC when the Wilcoxon signed-rank test is used.

20 **Keywords** Class imbalance problem · Genetic algorithm · HEOM · Oversampling · Classification

21 **Introduction**

22 The Telecom industry is evolving rapidly over time. In the  
23 same vein, the industry is facing severe revenue losses,  
24 because customers tend to leave a company and move to a  
25 competitor in the Telecom market (i.e., customer churn). The  
26 data of customers stored in such as Customer Relationship

Management (CRM) systems could be transformed into val- 27  
uable information with data mining and Machine Learning 28  
(ML) techniques. These techniques aid Telecom companies 29  
to formulate new policies, develop campaigns for existing 30  
clients, and figure out the main reasons behind customer 31  
churn. In this way, companies can easily observe their cus- 32  
tomer's behavior over time and manage them effectively. 33  
However, training learners with datasets which suffer from 34  
class imbalance distribution is an important and challenging 35  
problem in data mining and ML. 36

In recent years, the problem of imbalance class has been 37  
widely studied in the areas of ML. Typically, this problem 38  
occurs when the classes in a given dataset are unequally dis- 39  
tributed between the minority and majority classes. Without 40  
consideration of this problem, effective learning process by 41  
classification algorithms will be a challenge, since the main 42  
goal is the detection of minority classes [1]. Addressing this 43  
problem has attracted increased attention from the research 44  
community due to its importance in different applications; 45  
examples include malware detection [2], medical diagnosis 46  
domain [3], financial crisis prediction [4], and churn predic- 47  
tion [5]. Several studies carried out comparisons on random 48

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49 sampling techniques to handle the class imbalance problem  
 50 in the preprocessing phase. The results from these efforts  
 51 highlighted that these methods were useful before applying  
 52 classification algorithms [6, 7]. This is also confirmed by  
 53 the work of [8], when 26 datasets were used to investigate  
 54 the influence of class imbalance before and after balancing  
 55 the datasets. On the other hand, it was reported that random  
 56 sampling methods for class imbalance were shown not to be  
 57 useful in improving the performance of prediction results  
 58 [9, 10].

59 Balancing class is necessary when learning from highly  
 60 skewed datasets, because an imbalanced dataset could  
 61 result in classifying all the instances as negative, and hence  
 62 leads the learner to have a high false-negative rate [11, 12].  
 63 Therefore, a balancing strategy having better interpreting  
 64 capability is essential in the preprocessing phase to specify  
 65 churn customers. The cost is usually high when a learner  
 66 misclassifies the positive class instances, especially in churn  
 67 prediction. In this work, we propose a novel method based  
 68 on Heterogeneous Euclidean-Overlap Metric (HEOM) and  
 69 Genetic Algorithm (GA) to generate data points from the  
 70 existing minority ones rather than to use random methods.  
 71 This work proposes a data-level strategy for addressing the  
 72 class imbalance problem. The main objective of this work  
 73 is to investigate the suitability of the proposed method in  
 74 achieving optimal performance results and facilitating the  
 75 learning process by the learners from imbalance datasets.  
 76 A thorough empirical study was carried out which proves  
 77 the significant performance gains by the proposed method  
 78 compared to other popular oversampling algorithms.

79 The rest of the paper is organized as follows: Sec-  
 80 tion “Literature Review” reviews Synthetic Minority Over-  
 81 sampling Technique (SMOTE) and Adaptive Synthetic  
 82 Sampling Method (ADASYN) oversampling methods. Sec-  
 83 tion “Proposed Method” presents the proposed method. Sec-  
 84 tion “Experiment Design” describes the imbalance customer  
 85 churn datasets used to examine the proposed method, while  
 86 Sect. “Results and Discussion” provides the experiment  
 87 design used in this work. Section “Conclusion and Future  
 88 Work” presents the results and discussion of this research.  
 89 The final section concludes the paper along with future  
 90 work.

91 **Literature Review**

92 Research on synthesizing minority samples has been widely  
 93 studied to address the problem of class imbalance distribu-  
 94 tion at data level. The random sampling method is the  
 95 simplest way. Its main goal is to improve data quality in  
 96 the preprocessing phase before training classification algo-  
 97 rithms. Random sampling can be divided into two categor-  
 98 ies: random undersampling and random oversampling. In

the undersampling technique, the same samples belonging  
 to the same majority samples are removed from the dataset.  
 For example, 30% undersampling means that 30% of the  
 available majority instances are randomly removed from  
 the dataset. However, by removing significant instances,  
 this method may potentially lose valuable information. The  
 second category attempts to create a superset of the origi-  
 nal dataset. This can be achieved by replicating the minor-  
 ity instances from the existing dataset. The replication can  
 be done either randomly or using an intelligent method.  
 For example, 100% oversampling means that the minority  
 instances are replicated once in average. However, a draw-  
 back with this method is that creating additional instances  
 could have significant impacts on computational cost and  
 overfitting.

SMOTE is an advanced method of oversampling, and it  
 was developed by Chawla et al. [13]. This approach ran-  
 domly picks one data point from the  $k$  neighbors of a minor-  
 ity class sample and inserts a new synthetic minority class  
 sample on the line that connects the randomly chosen minor-  
 ity class sample and one of its  $k$  minority nearest neighbors,  
 belonging to minority class sample as illustrated in Fig. 1.

He et al. [14] proposed ADASYN to overcome the prob-  
 lem of class imbalance. It is an oversampling method that  
 was basically developed to reduce generating noise data  
 and the ambiguity along the decision boundaries produced  
 by SMOTE. The major difference between SMOTE and  
 ADASYN is in the generation of synthetic sample points for  
 minority data points. In ADASYN, the data points that are  
 harder to learn are more frequently presented by this method,  
 as shown in Fig. 2.

Recent developments of SMOTE and ADASYN, Bor-  
 derline-SMOTE [15], Safe-Level-SMOTE [16], and Local  
 Neighbourhood SMOTE [17] are some other extensions to  
 reduce generating noise data and the ambiguity along the  
 decision boundaries that are produced by SMOTE. These  
 extensions attempt to create data points from the minority  
 class that are close to the borderline between the two classes;

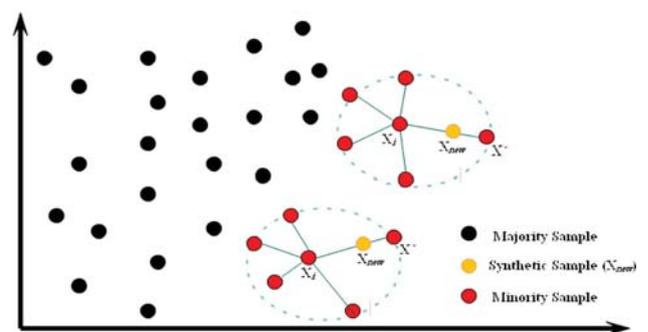


Fig. 1 Generation of synthetic samples using SMOTE, a randomly selected minority class sample and of its  $k=5$  nearest neighbors

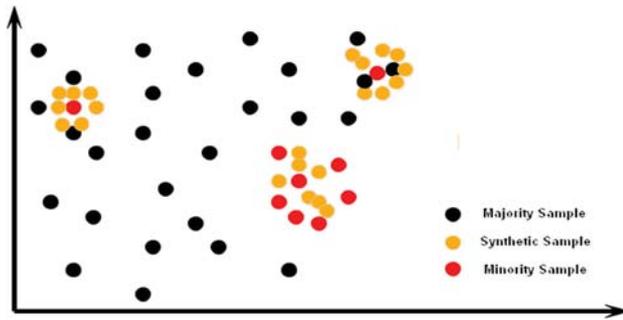


Fig. 2 Generation of synthetic samples using ADASYN

for example, ADASYN aimed at generating minority data samples based on their distribution. Barua et al. [18] recently proposed another recent technique for imbalanced data problem; named, Majority Weighted Minority Oversampling Technique (MWMOTE). This method has several functions, which include: (a) generate a useful synthetic class sample, (b) add weights to the selected sample based on their importance, and (c) use clustering approach to produce suitable synthetic minority class samples.

Zhu et al. [19] assessed the suitability of ADASYN, Borderline-SMOTE, Random oversampling, and SMOTE strategies for class imbalance in churn prediction using 11 datasets. The results recommended that suitable sampling strategies needed to be selected, and setting of class ratio had an impact on the model performance. In another work [20], the authors investigated six sampling techniques and their accounts on four customer churn datasets. These methods include Mega-trend Diffusion Function (MTDF), Synthetic Minority Oversampling Technique (SMOTE), Adaptive Synthetic Sampling approach (ADASYN), Couples Top-N Reverse k-Nearest Neighbor (TRkNN), Majority Weighted Minority Oversampling Technique (MWMOTE), and Immune centroids oversampling technique (ICOTE). Their empirical results demonstrated that MTDF performed better than the other oversampling methods they used in the study. Salunkhe et al. [21] proposed a hybrid data-level approach for handling class imbalance problems. The authors combined SMOTE and undersampling techniques to achieve better results. Their aim was to focus on the majority class's necessary data and avoid removing valuable information when using the undersampling technique before the model training stage. They achieved results better than the other techniques for class imbalance.

During the last decade, a worldwide range of studies has applied Genetic Algorithm (GA) for class imbalance problems [22–24]. In the approach of [25], GA with SMOTE was combined to perform oversampling and they used different sampling rates for different minority examples until reaching the desired oversampling rate. The results showed that the proposed method achieved better performance compared

to SMOTE. In another work, GenSample was proposed by [26]. They used the a GA method for oversampling minority class by taking into account the difficulty in the learning of an example and the improved performance caused by oversampling it. Their final results showed that better performance was achieved by the GenSample method compared to the traditional methods.

Distance-based algorithms are widely used for class imbalance problems to provide a numerical description of the similarity between two objects [27]. Several studies confirmed that improving the performances of distance metrics makes ML algorithms more accurate [28–30]. The aim of the research done by [31] is to improve the categorization process of the minority class by incorporating an idea of using dataset-specific distance function and choose the appropriate distance metric and k nearest-neighbor value among the five used distance metrics for five datasets. They concluded that there is no optimal distance metric for all the datasets.

Modifications can be made at the algorithm level by incorporating the cost of misclassifying minority samples or integrating one class learning algorithm. Bagging and boosting ensemble techniques can be used as cost-sensitive methods, where the classification outcome is some combination of multiple classifiers built on the dataset. Guo et al. [32] applied data boosting to improve the performance on hard samples that are difficult to classify. The algorithm-level method tries to adapt existing learning algorithms to strengthen their learning capability regarding the majority class. However, this approach requires a deep level of understanding related to the application domain and corresponding classifiers.

Hybrid methods are also used to conquer the problem of class imbalance recently. An ensemble of classifiers can be used at the algorithm level and different sampling methods and cost-sensitive learning methods can be hybridized at the data level. The authors in [33] incorporated oversampling and undersampling with an ensemble Support Vector Machine (SVM) to improve its prediction performance. Experimental results showed that better performance was achieved by SVM when the problem of class imbalance was contained by the use of oversampling and undersampling methods compared to other classifiers and SVM alone. Based on the conducted review, the first observation indicates that solving class imbalance at the data level seems to be the most viable and widely used option in practice to provide the learner with more robust training data.

## Proposed Method

### HEOM

There are a number of distance metrics that are designed and used for measuring similarity and dissimilarity among

226 samples within a given dataset. The use of these metrics  
 227 depends on the nature of a dataset's attributes, whether they  
 228 are numerical or only contain categorical attributes. For  
 229 example, Euclidean distance is the most widely used when  
 230 all the attributes are numerical. Another example, Hamming  
 231 Distance can be used when only have categorical attributes.  
 232 However, some other metrics were designed to handle nomi-  
 233 nal and categorical attributes, i.e., mixed or heterogeneous  
 234 data such as HEOM.

235 HEOM becomes more popular due to its simplicity and  
 236 efficiency in handling continuous and discrete attributes  
 237 independently [34–37].

238 Considering two input vectors,  $x$  and  $y$ , the HEOM dis-  
 239 tance can be calculated by

$$240 \quad d(x, y) = \sqrt{\sum_{i=1}^n d_i(x_i, y_i)^2}; \quad (1)$$

241  $d(x, y)$  is the distance between the two cases on its  $i$ th attri-  
 242 bute, where

$$243 \quad d(x, y) = \begin{cases} 1, & \text{if } x \text{ or } y \text{ is missing} \\ d_o(x, y), & \text{if } x \text{ and } y \text{ are discrete variables} \\ d_n(x, y), & \text{if } x \text{ and } y \text{ are continuous variables} \end{cases} \quad (2)$$

244 HEOM uses the overlap metric,  $d_o$ , for categorical  
 245 attributes

$$246 \quad d_o(x, y) = \begin{cases} 0, & \text{if } x = y \\ 1, & \text{otherwise} \end{cases} \quad (3)$$

247 The normalized Euclidean distance,  $d_n(x, y)$ , for continu-  
 248 ous attributes

$$249 \quad d_n(x, y) = \frac{|(x_i - y_i)|}{\max_a - \min_a} \quad (4)$$

254 **GA**

255 A GA searches for the global solution through an iterative  
 256 process; a new population is produced at each iteration,  
 257 which contains evolutions of individuals selected from the  
 258 previous iteration. The initial population is generally com-  
 259 posed of random solutions. The individuals are codified by  
 260 a data structure named chromosome. In the basic or standard  
 261 GA, the chromosomes are represented by a bit of string.  
 262 Each bit is also named, a gene that represents the presence  
 263 (value 1) or absence (value 0) of a specific characteristic in  
 264 the individual.

265 At each generation, the individuals have evaluated their  
 266 fitness to solve the problem. This evaluation is performed by  
 267 a fitness function, which decodes the information contained

268 in each individual chromosome into a measure of its quality.  
 269 The evaluation of a chromosome is done to test its "fitness"  
 270 as a solution. The fitness function plays a vital role of the  
 271 environment in natural evolution by rating individuals in  
 272 terms of their fitness. Selecting and formulating an appro-  
 273 priate fitness function are crucial to the efficient solution of  
 274 any given GA problem. In our case, selecting the optimal  
 275 samples (data points) in the initial population, which are  
 276 the minority class, is set to HEOM. After evaluation, some  
 277 individuals in the population are selected for reproduction,  
 278 producing descendants, which will form a new population.  
 279 This selection must privilege the fittest individuals, accord-  
 280 ing to the natural selection principles.

281 In the reproduction of the selected individuals, their char-  
 282 acteristics or genes are combined to obtain two descendants.  
 283 This combination process is performed with the application  
 284 of the crossover operator, which is a binary operator applied  
 285 to two individuals. These individuals are named parents,  
 286 and their chromosomes are combined to produce two new  
 287 individuals, named offspring. For the bit-string representa-  
 288 tion, a common crossover operator is a one-point crossover.  
 289 A second genetic operator usually applied is the mutation,  
 290 which enforces a genetic variability in the new solutions.  
 291 The boundary mutation alters genes from the individuals  
 292 generated in the crossover step.

293 The procedures of population generation, evaluation of its  
 294 individuals, selection, and application of the genetic opera-  
 295 tors are iterated, forming the basis of the GAs. Depending  
 296 on the initial population, the GA may produce distinct solu-  
 297 tions to the same problem. Therefore, the GA is usually run  
 298 several times with different initial populations, and to stop  
 299 the GA, other criteria can be used. For example, the GA may  
 300 be when a maximum number of generations are reached.

301 **HEOMGA Method**

302 HEOM measures the distance of a minority data point to  
 303 all other minority data points in a population, which is the  
 304 square root of their summation to produce the fitness scores  
 305 for those data points in the population. HEOM acts as a fit-  
 306 ness function for measuring similarity (distance) between  
 307 the individuals (data points) in a population which contains  
 308 all minority class samples in the training dataset to decide to  
 309 use which data points. The two data points with smallest fit-  
 310 ness scores produced from HEOM are selected as parents for  
 311 mating, and then, the GA variants (crossover and mutation)  
 312 are applied to produce offspring within the same iteration.  
 313 Based on the three genetic operators and the evaluations,  
 314 the better new populations of a candidate after the specified  
 315 number of generations (e.g., number of generations = 5), the  
 316 best solution (a newly generated data point) is formed and  
 317 appended to the initial population. To start the next iteration,  
 318 two data points with the smaller fitness scores in the updated

319 population are selected as parents by returning the corre- 332  
 320 sponding distance to each data point in the initial popula- 333  
 321 tion in addition to the appended data points from the dis- 334  
 322 tances list produced in the previous iteration. The role of crossover 335  
 323 and mutation operators then begins. This procedure will be 336  
 324 repeated until the minority data points in the current popula- 337  
 325 tion are equal to the number of majority data points in the 338  
 326 original data set. Finally, to avoid the generation of newly 339  
 327 duplicated data points, the algorithm will check and delete 340  
 328 any duplicated ones. Figure 3 depicts the proposed method 341  
 329 process.

330 SMOTE and ADASYN generate noise samples that 342  
 331 have penetrated in the majority class region, resulting in 343  
 344

an increase in overlapping. These noise samples are less 332  
 useful, because they do not add any new information to 333  
 the imbalance datasets, and they may lead to overfitting. 334  
 It was confirmed that using the Euclidean distance metric 335  
 that SMOTE and ADASYN use to measure the distance 336  
 between two objects introduces some issues regarding 337  
 imbalanced data and performance problems regarding 338  
 computation or approximation of the square root [33]. 339  
 Most datasets have both nominal and categorical attrib- 340  
 utes, and the major weakness of the Euclidean distance is 341  
 that when some attributes have a large range of values as 342  
 opposed to the remaining attributes, they may influence a 343  
 bigger impact on the computed distance, while attributes 344

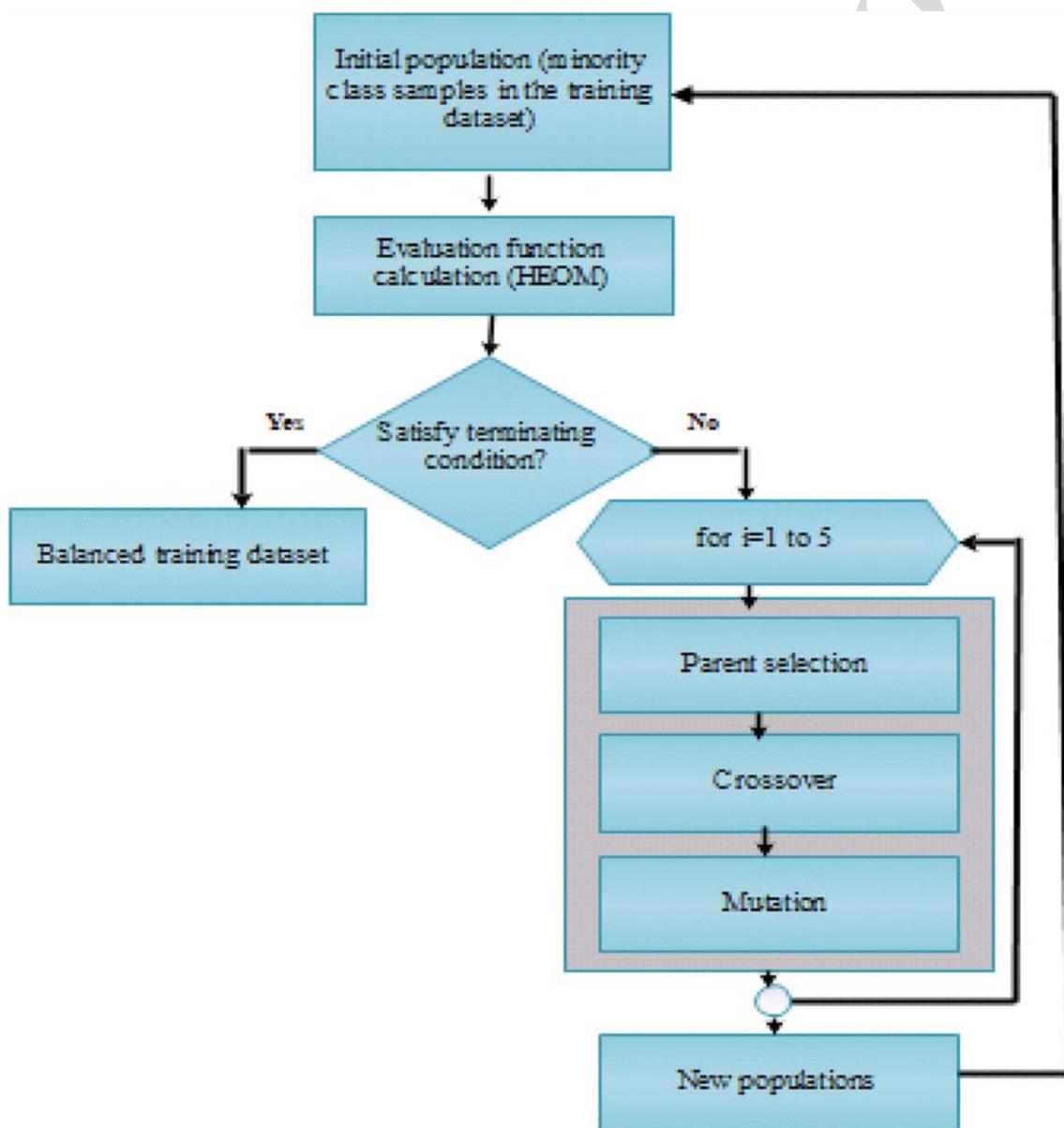


Fig. 3 Basic structure of the HEOMGA method

Author Proof

345 with a lower range of values will have a lesser impact on  
 346 the results.

347 In the proposed method, all the minority data points  
 348 are selected as the initial population, and the HEOM finds  
 349 the distance between them by calculating the square root  
 350 of their summation to produce the final fitness scores. In  
 351 HEOM, normalized Euclidean distance is used for numeric  
 352 features, and the overlap distance for categorical features  
 353 is employed to find the distance between two instances  $x_1$   
 354 and  $x_2$  as provided in Eqs. (3 and 4). Applying the HEOM  
 355 distance metric allows better handling of nominal and cat-  
 356 egorical attributes in accordance with the dataset nature.  
 357 In addition, HEOM will help obtain better representation  
 358 capability for minority data points and will enable us to  
 359 appropriately select the data points that will be used as  
 360 input for mating in the GA.

361 Crossover and mutation operators in the GA realize  
 362 on the search exploration and exploitation, respectively.  
 363 Exploration is the ability to create diversity in the popu-  
 364 lation by exploring the search space, while exploitation  
 365 is the reduction of diversity by focusing on individuals  
 366 with higher fitness scores. Therefore, the newly generated  
 367 synthetic data points will be produced in a safe region  
 368 within the boundaries of the minority data points that are  
 369 selected by the HEOM. As shown in Fig. 4, overlapping  
 370 and overfitting problems will be somehow alleviated by  
 371 causing the distance ( $d$ ) between the generation area (the  
 372 pink dotted oval) and the decision boundary to be larger  
 373 and spread the newly generated data points far from the  
 374 majority space (Table 1).

375 The use of crossover and mutation operators assists in  
 376 improving the learning process by providing rich informa-  
 377 tion about the newly generated data points, since they are  
 378 inherited from the original data points, as shown in Fig. 5.  
 379 This will make the learning process by a given learner  
 380 easier. Finally, the HEOMGA will check and delete any  
 381 duplicated data points during the generation process to  
 382 avoid the generation of newly repeated samples.

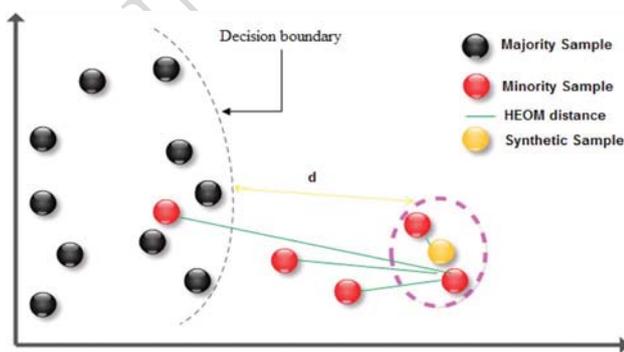


Fig. 4 An example of how can HEOMGA avoid overlapping

## Experiment Design 383

### Datasets 384

385 A set of publicly available datasets for customer churn pre-  
 386 diction are used in this work. Table 2 gives the details for  
 387 each dataset. Evaluation of data mining and ML methods  
 388 on publically available datasets offers different advantages  
 389 [38]

- In terms of comparability of results, ranking methods,  
 and evaluation of existing methods with new techniques 390
- Study the impact of the data and their characteristics  
 on the performance of a technique 391
- Using available datasets provide insight into the effect  
 of each phase of the followed methodology. 392

### Baseline Approaches and Learners 397

398 To examine the capability of the methods, three different  
 399 learners are used: Decision Trees (DTs i.e., C4.5 algo-  
 400 rithm), Bagging, and SVM with radial basis function ker-  
 401 nel ( $SVM_{rbf}$ ), due to their popularity with classification  
 402 problems and their sensitivity to imbalance datasets. The  
 403 DTs rely on greedy-search heuristics that checks one vari-  
 404 able at a time [39], and therefore, it can attain a high level  
 405 of accuracy by predicting the majority class, particularly  
 406 if the majority class constitutes most of the dataset.

407 An SVM learner tries to find the hyper plane splitting  
 408 instances of two classes based on the largest distance  
 409 between them. It is useful mainly due to its capability to  
 410 work in high feature space, since the learner can map com-  
 411 plex nonlinear relationships between input and output with  
 412 relatively high accuracy [40]. SVM with a radial basis  
 413 function ( $SVM_{rbf}$ ) kernel is used. Bagging is an ensem-  
 414 ble learning learner, which has proved the ability to han-  
 415 dle class imbalance problems effectively. The number of  
 416 the nearest neighbors ( $K$ ) parameter in both SMOTE and  
 417 ADASYN was set to 5 [41].

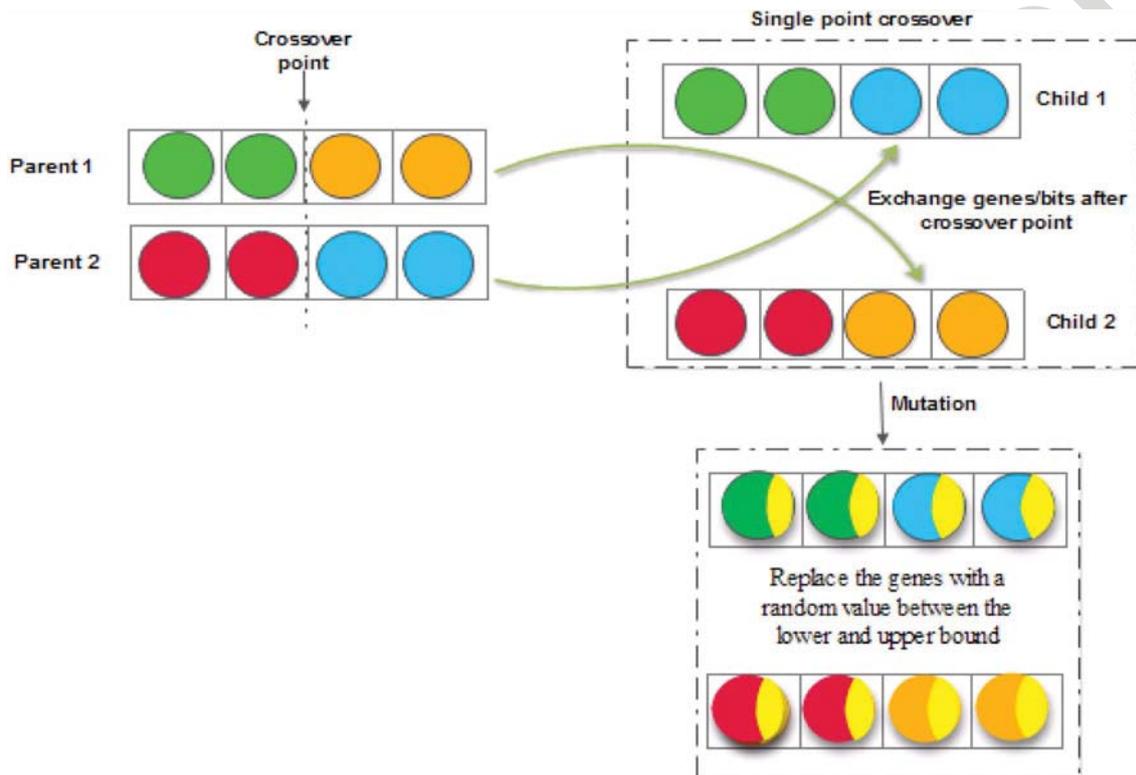
418 Tenfold cross-validation is used to avoid picking par-  
 419 ticular parts that are for training and testing. The number  
 420 of  $k$  was adjusted to 10; the data were split into ten parts;  
 421 the procedure starts by splitting the dataset into 90% for  
 422 training and 10% for testing. To finalize the process, the  
 423 procedure was repeated ten times to allow each part of  
 424 data being as testing data, and finally, the average results  
 425 are considered for the used datasets on the ten partitions.  
 426 Min–Max method is applied to transform training data-  
 427 sets into the range of 0 to  $-1$ , which means that all the

Author Proof

**Table 1** Description of imbalanced datasets characteristics

| Dataset source                               | Number of samples | Number of attributes | Minority (%) | Majority (%) | Imbalanced ratio |
|--|-------------------|----------------------|--------------|--------------|------------------|
| <sup>a</sup> Real world dataset <sup>a</sup> | 3333              | 21                   | 14.49        | 85.51        | 5.90             |
| <sup>b</sup> Real world dataset <sup>b</sup> | 7043              | 21                   | 26.54        | 73.46        | 2.77             |
| <sup>c</sup> Real world dataset <sup>c</sup> | 100,000           | 50                   | 49.56        | 50.43        | 1.02             |

<sup>a</sup><http://www.sgi.com/tech/mlc/db/>  
<sup>b</sup><https://www.ibm.com/analytics/us/en/>  
<sup>c</sup><https://www.kaggle.com/abhinav89/telecom-customer/data>



**Fig. 5** GA operators' processes

**Table 2** Confusion matrix for two-class problem

|                               | Actual          |                     |
|-------------------------------|-----------------|---------------------|
|                               | Churn customers | Non-churn customers |
| Predicted churn customers     | TP              | FP                  |
| Predicted non-churn customers | FN              | TN                  |

428 values of numeric range of a feature are reduced to a scale  
 429 between 0 and - 1 range. All the experiments are imple-  
 430 mented using Python scikit-learn and the DTs SVM<sub>rbf</sub>  
 431 and bagging learners are constructed based on the use of

default parameters on Windows 7 with 2 Duo CPU running 432  
 on 3.13 GHz PC with 44.25 GB RAM. 433

**Evaluation Metrics** 434

To assess learners' results, a confusion matrix was employed 435  
 to count: True Positive (TP) and True Negative (TN) denote 436  
 the number of positive and negative examples that are clas- 437  
 sified correctly, while False Negative (FN) and False Posi- 438  
 tive (FP) represent a number of misclassified positive and 439  
 negative examples, respectively. Table 2 shows a confusion 440  
 matrix of a two-class problem. The first column of the table 441  
 is the actual class label of the examples, and the first row 442  
 presents their predicted class label. 443

444 The Recall is the True-Positive rate, which refers to the  
 445 percentage of positive instances correctly predicted as posi-  
 446 tive class instances

447 
$$\text{Recall} = \frac{TP}{TP + FN} \tag{5}$$

448

449 **Geometric Mean (G mean)**

450 Gmean is a good indicator that can be used to assess the  
 451 overall performance for a given learner, because it combines  
 452 the learner’s accuracy on the positive class and negative  
 453 class samples. Therefore, a large value of this measure indi-  
 454 cates that the learner performs well on both classes' samples

455 
$$\text{Gmean} = \sqrt{\frac{TP}{TP + FN} \times \frac{TN}{TN + FP}} \tag{6}$$

456

457 **Area Under Curve (AUC)**

458 Receiver-Operating Curve (ROC) is usually known as AUC.  
 459 The ROC graph plots true-positive rates versus false-posi-  
 460 tive rates. Learners can be selected based on their trade-  
 461 off between true positives and false positives. Rather than  
 462 visually comparing curves, the ROC metric aggregates the  
 463 performance of classification methods into a single number,  
 464 which makes it easier to compare the overall performance of  
 465 different learners. This metric can also be applied to evaluate  
 466 learning from imbalanced data. The bigger the AUC indi-  
 467 cates, the better the generalization of the methods. The AUC  
 468 can be determined as follows:

469 
$$\text{AUC} = \frac{\left(1 + \frac{TP}{TP + FN} - \frac{FP}{FP + TN}\right)}{2} \tag{7}$$

470

471 The above evaluation metrics can reasonably evaluate  
 472 the learning process from imbalanced datasets, since their  
 473 formulae are relative to the rare class, which is in our case  
 474 the churn class. These measurements are used to evaluate  
 475 the proposed method and its effectiveness to overcome class  
 476 imbalance.

477 **Results and Discussion**

478 The performance of three learners without using any balanc-  
 479 ing method (i.e., 0% balancing) and the results of the pro-  
 480 posed method against SMOTE, ADASYN, G-SMOTE [42],  
 481 and Gaussian method [43] were applied over three customer  
 482 churn datasets to study the impact of different balancing  
 483 technique on the evaluation measures used in this work. The  
 484 results are summarized in Tables 3, 4, and 5.

**Table 3** DTs results based on the evaluation metrics for all the data-sets

| Dataset   | Method          | Recall       | G mean       | AUC          |
|-----------|-----------------|--------------|--------------|--------------|
| Dataset 1 | 0% balancing    | 0.780        | 0.852        | 0.856        |
|           | SMOTE           | 0.741        | 0.798        | 0.833        |
|           | ADASYN          | 0.725        | 0.802        | 0.812        |
|           | Proposed method | <b>0.926</b> | <b>0.944</b> | <b>0.944</b> |
|           | G-SMOTE         | 0.758        | 0.841        | 0.847        |
| Dataset 2 | 0% balancing    | 0.481        | 0.626        | 0.648        |
|           | SMOTE           | 0.559        | 0.659        | 0.684        |
|           | ADASYN          | 0.500        | 0.635        | 0.673        |
|           | Proposed method | <b>0.816</b> | <b>0.816</b> | <b>0.818</b> |
|           | G-SMOTE         | 0.609        | 0.716        | 0.789        |
| Dataset 3 | 0% balancing    | 0.522        | 0.523        | 0.523        |
|           | SMOTE           | 0.466        | 0.544        | 0.551        |
|           | ADASYN          | 0.464        | 0.540        | 0.546        |
|           | Proposed method | <b>0.523</b> | <b>0.552</b> | <b>0.554</b> |
|           | G-SMOTE         | 0.473        | 0.536        | 0.541        |
|           | Gaussian method | 0.478        | 0.539        | 0.543        |

The best result of each dataset is emphasized in bold

**Table 4** SVM results based on the evaluation metrics for all the data-sets

| Dataset   | Method          | Recall       | G mean       | AUC          |
|-----------|-----------------|--------------|--------------|--------------|
| Dataset 1 | 0% balancing    | 0.219        | 0.466        | 0.724        |
|           | SMOTE           | 0.814        | 0.816        | 0.817        |
|           | ADASYN          | 0.676        | 0.739        | 0.739        |
|           | Proposed method | <b>0.845</b> | <b>0.919</b> | <b>0.919</b> |
|           | G-SMOTE         | <b>0.845</b> | <b>0.919</b> | 0.918        |
| Dataset 2 | 0% balancing    | 0.484        | 0.662        | 0.734        |
|           | SMOTE           | 0.674        | 0.740        | 0.752        |
|           | ADASYN          | 0.636        | 0.725        | 0.738        |
|           | Proposed method | <b>0.815</b> | <b>0.846</b> | <b>0.847</b> |
|           | G SMOTE         | 0.681        | 0.748        | 0.748        |
| Dataset 3 | 0% balancing    | 0.443        | 0.537        | 0.547        |
|           | SMOTE           | 0.395        | 0.524        | 0.545        |
|           | ADASYN          | 0.402        | 0.535        | 0.544        |
|           | Proposed method | <b>0.502</b> | <b>0.557</b> | <b>0.560</b> |
|           | G SMOTE         | 0.500        | 0.529        | 0.530        |
|           | Gaussian method | 0.498        | 0.551        | 0.553        |

The best result of each dataset is emphasized in bold

485 Tables 3, 4, 5 show that HEOMGA performs better  
 486 than 0% balancing, SMOTE, ANDSYN, G SMOTE, and  
 487 Gaussian method in term of Recall for all the used datasets.

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**Table 5** Bagging results based on the evaluation metrics for all the datasets

| Dataset   | Method          | Recall       | G mean       | AUC          |
|-----------|-----------------|--------------|--------------|--------------|
| Dataset 1 | 0% balancing    | 0.137        | 0.371        | 0.591        |
|           | SMOTE           | 0.131        | 0.362        | 0.581        |
|           | ADASYN          | 0.098        | 0.313        | 0.545        |
|           | Proposed method | <b>0.875</b> | <b>0.934</b> | <b>0.934</b> |
|           | G SMOTE         | 0.762        | 0.862        | 0.876        |
|           | Gaussian method | 0.867        | 0.927        | 0.928        |
| Dataset 2 | 0% balancing    | 0.455        | 0.646        | 0.794        |
|           | SMOTE           | 0.724        | 0.745        | 0.786        |
|           | ADASYN          | 0.534        | 0.680        | 0.733        |
|           | Proposed method | <b>0.776</b> | <b>0.849</b> | <b>0.853</b> |
|           | G SMOTE         | 0.554        | 0.678        | 0.796        |
|           | Gaussian method | 0.651        | 0.801        | 0.802        |
| Dataset 3 | 0% balancing    | 0.418        | 0.521        | 0.533        |
|           | SMOTE           | 0.416        | 0.513        | 0.524        |
|           | ADASYN          | 0.413        | 0.512        | 0.523        |
|           | Proposed method | <b>0.480</b> | <b>0.537</b> | <b>0.540</b> |
|           | G SMOTE         | 0.428        | 0.529        | 0.538        |
|           | Gaussian method | 0.437        | 0.523        | 0.539        |

The best result of each dataset is emphasized in bold

488 Therefore, an improvement in the churn rate is achieved by  
 489 the proposed methods among the other used oversampling  
 490 methods.

491 The bigger the AUC and G mean indicate the better the  
 492 generalization of the methods. Empirical experiment results  
 493 indicated that the proposed method outperforms the tested  
 494 oversampling methods in terms of G mean and AUC for  
 495 the datasets. The proposed method for the three datasets  
 496 obtained the best G mean and AUC values compared to  
 497 other methods. This can be explained by the fact that the  
 498 use of the proposed method provides rich information to  
 499 the learners, which in turn improve prediction results and  
 500 the learning process.

501 The receiver-operating characteristic (ROC) graph cal-  
 502 culates the learner performance by changing the DTs' con-  
 503 fidence level, SVM<sub>rbf</sub>, and Bagging scores to get distinct  
 504 values of TP<sub>rate</sub> and FP<sub>rate</sub>, as shown in Figs. 6, 7, and 8.

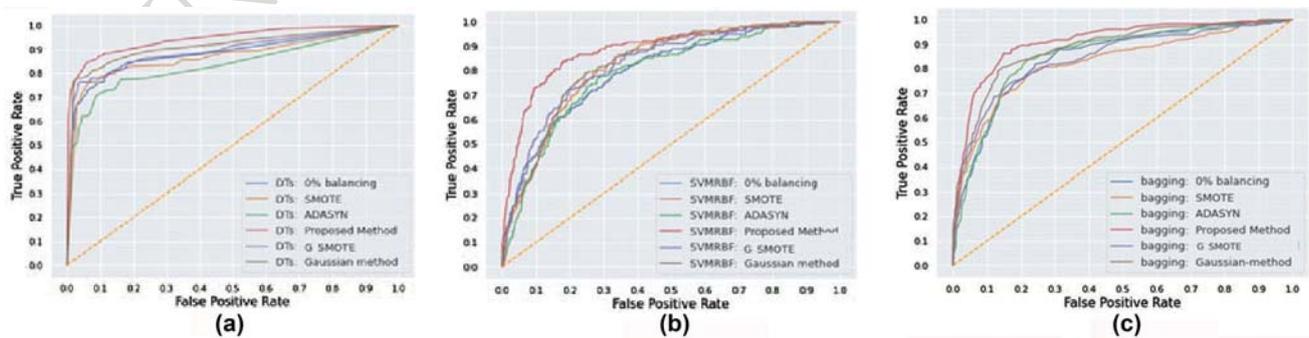
505 The lines of the proposed method in Figs. 6, 7, and 8  
 506 is closer to the left-hand border and the top border com-  
 507 pared to 0% balancing, SMOTE, ANDSYN, G SMOTE, and  
 508 Gaussian method. This indicates that the proposed method  
 509 offers the finest results among the other methods for class  
 510 imbalance problems in the application of customer churn  
 511 prediction.

512 For further check the statistical significance of the pro-  
 513 posed method and whether it significantly outperforming  
 514 the other used oversampling algorithms in terms of Recall,  
 515 G mean, and AUC, Wilcoxon signed-rank test [44] is per-  
 516 formed. The results of the test are provided in Tables 6, 7  
 517 and 8. The test's confidence level is set 0.05, given the null  
 518 hypothesis that the learners' performance varies significantly  
 519 across the various algorithms and evaluation metrics with  
 520 the proposed method as a control algorithm.

521 The test results in terms of Recall, G mean, and AUC  
 522 are given in Tables 6, 7 and 8 to validate the proposed  
 523 method significantly outperforms 0% balancing, SMOTE,  
 524 ADASYN, G SMOTE, and Gaussian method.

## 525 Conclusion and Future Work

526 This work proposes an effective preprocessing approach,  
 527 called HEOMGA, to overcome class imbalance issues and  
 528 assist the learners in improving their generalization capac-  
 529 ity and performance. This work has conducted a set of  
 530 experiments on publicly available customer churn predic-  
 531 tion datasets to assess the performance of the proposed  
 532 method. Experimental results showed the efficiency of the  
 533 proposed method as compared to the other tested over-  
 534 sampling methods. Moreover, the proposed HEOMGA  
 535 method significantly outperformed the other oversampling



**Fig. 6** ROC curve comparison among 0% balancing, SMOTE, ANDSYN, proposed method, G SMOTE, and Gaussian method for dataset 1 using **a** DTs, **b** SVM<sub>rbf</sub>, and **c** Bagging

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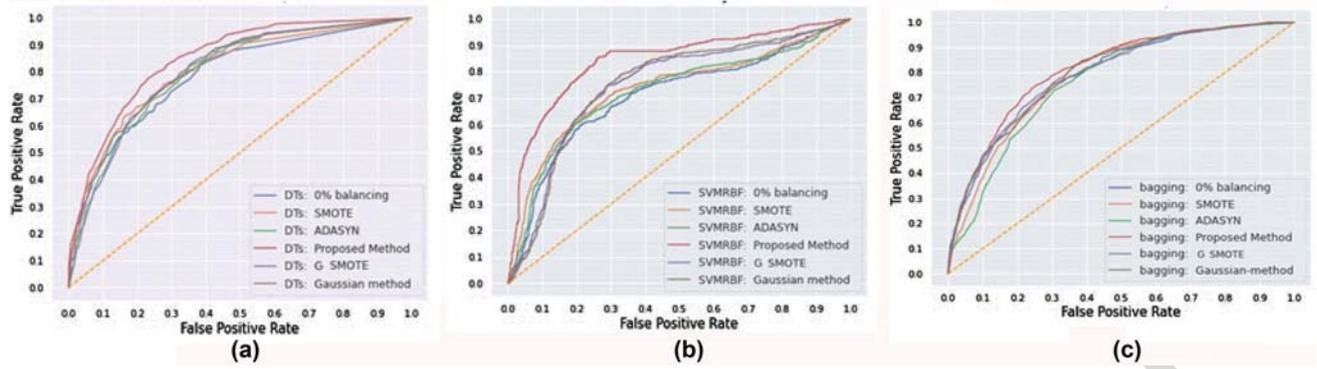


Fig. 7 ROC curve comparison among 0% balancing, SMOTE, ANDSYN, proposed method, G SMOTE, and Gaussian method for dataset 2 using a DTs, b SVM<sub>rbf</sub>, and c Bagging

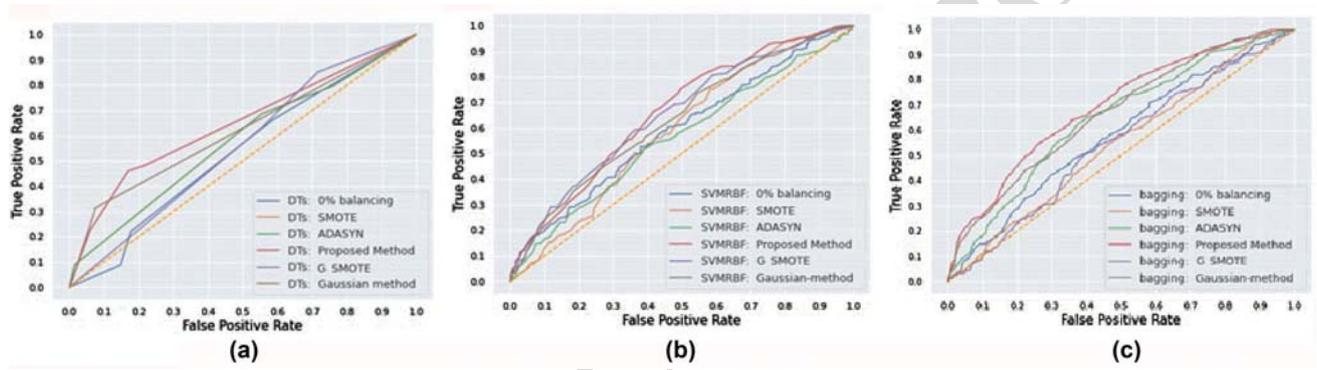


Fig. 8 ROC curve comparison among 0% balancing, SMOTE, ANDSYN, proposed method, G SMOTE, and Gaussian method for dataset 3 using a DTs, b SVM<sub>rbf</sub>, and c Bagging

Table 6 Wilcoxon signed-rank test evaluation results based on Recall

| Comparison                          | <i>p</i> value | <i>W</i> value | Mean difference | <i>R</i> <sup>+</sup> | <i>R</i> <sup>-</sup> | <i>Z</i> -value | Mean ( <i>W</i> ) | Std ( <i>W</i> ) | Significance |
|-------------------------------------|----------------|----------------|-----------------|-----------------------|-----------------------|-----------------|-------------------|------------------|--------------|
| Proposed method vs. 0% balancing    | 0.05           | 10             | 0.50            | 455                   | 10                    | -4.5765         | 232.5             | 48.62            | +            |
| Proposed method vs. SMOTE           | 0.05           | 1              | -0.10           | 464                   | 1                     | 4.7616          | 232.5             | 48.62            | +            |
| Proposed method vs. ADASYN          | 0.05           | 0              | 0.04            | 465                   | 0                     | -4.7821         | 232.5             | 48.62            | +            |
| Proposed method vs. G-SMOTE         | 0.05           | 0              | -0.13           | 435                   | 0                     | -4.703          | 217.5             | 46.25            | +            |
| Proposed method vs. Gaussian Method | 0.05           | 0              | -0.13           | 406                   | 0                     | -4.6226         | 203               | 43.91            | +            |

*R*<sup>+</sup> is the sum of ranks for the datasets in which the first method outperforms the second and *R*<sup>-</sup> is the sum of ranks of the opposite, Std is standard deviation (*W*), and + refers to significance at 0.05 level

536 methods in terms of Recall, G mean, and AUC based on  
 537 the Wilcoxon signed-rank test analysis. In the future, it  
 538 would be interesting to see the results of the proposed  
 539 HEOMGA in conjunction with applying feature selection

540 methods. Another research direction can be to test other  
 541 distance metrics to tackle the class imbalance, and finally,  
 542 another line of future research would be to try to tackle  
 543 class overlap situations.

**Table 7** Wilcoxon signed-rank test evaluation results based on G mean

| Comparison                          | <i>p</i> value | <i>W</i> value | Mean difference | $R^+$ | $R^-$ | <i>Z</i> -value | Mean ( <i>W</i> ) | Std ( <i>W</i> ) | Significance |
|-------------------------------------|----------------|----------------|-----------------|-------|-------|-----------------|-------------------|------------------|--------------|
| Proposed method vs. 0% balancing    | 0.05           | 0              | 0.3             | 465   | 0     | -4.7821         | 232.5             | 48.62            | +            |
| Proposed method vs. SMOTE           | 0.05           | 1              | -0.05           | 464   | 1     | -4.7616         | 232.5             | 48.62            | +            |
| Proposed method vs. ADASYN          | 0.05           | 1              | 0.03            | 464   | 1     | -4.7616         | 232.5             | 48.62            | +            |
| Proposed method vs. G-SMOTE         | 0.05           | 8.5            | -0.15           | 426.5 | 8.5   | -4.5192         | 217.5             | 46.25            | +            |
| Proposed method vs. Gaussian Method | 0.05           | 20             | -0.14           | 445   | 20    | -4.3708         | 232.5             | 48.62            | +            |

$R^+$  is the sum of ranks for the datasets in which the first method outperforms the second and  $R^-$  is the sum of ranks of the opposite, Std is standard deviation (*W*), and + refers to significance at 0.05 level

**Table 8** Wilcoxon signed-rank test evaluation results based on AUC

| Comparison                          | <i>p</i> value | <i>W</i> value | Mean difference | $R^+$ | $R^-$ | <i>Z</i> -value | Mean ( <i>W</i> ) | Std ( <i>W</i> ) | Significance |
|-------------------------------------|----------------|----------------|-----------------|-------|-------|-----------------|-------------------|------------------|--------------|
| Proposed method vs. 0% balancing    | 0.05           | 0              | 0.05            | 465   | 0     | -4.7821         | 232.5             | 48.62            | +            |
| Proposed method vs. SMOTE           | 0.05           | 0              | -0.04           | 465   | 0     | -4.7821         | 232.5             | 48.62            | +            |
| Proposed method vs. ADASYN          | 0.05           | 0              | 0.04            | 465   | 0     | -4.7821         | 232.5             | 48.62            | +            |
| Proposed method vs. G-SMOTE         | 0.05           | 0              | -0.15           | 435   | 0     | -4.703          | 217.5             | 46.25            | +            |
| Proposed method vs. Gaussian Method | 0.05           | 0              | -0.14           | 435   | 0     | -4.703          | 217.5             | 46.25            | +            |

$R^+$  is the sum of ranks for the datasets in which the first method outperforms the second and  $R^-$  is the sum of ranks of the opposite, Std is standard deviation (*W*), and + refers to significance at 0.05 level

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548 **References**

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