Static output-feedback control under information structure constraints

J. Rubió-Massegú^{a,*}, J. M. Rossell^a, H. R. Karimi^b, F. Palacios-Quiñonero^a

^aDepartment of Applied Mathematics III, Universitat Politècnica de Catalunya (UPC), 08242-Manresa, Barcelona, Spain ^bDepartment of Engineering, University of Agder, Faculty of Engineering and Science, N-4898 Grimstad, Norway

Abstract

An important challenge in the static output-feedback control context is to provide an isolated gain matrix possessing a zero-nonzero structure, mainly in problems presenting information structure constraints. Although some previous works have contributed some relevant results to this issue, a fully satisfactory solution has not yet been achieved up to now. In this note, by using a Linear Matrix Inequality approach and based on previous results given in the literature, we present an efficient methodology which permits to obtain an isolated static output-feedback gain matrix having, simultaneously, a zero-nonzero structure imposed a priori.

Keywords: Information structure constraints, output-feedback control, LMIs.

1. Introduction

Nowadays, robust state-feedback controllers for a wide class of systems containing disturbances, nonlinearities, uncertainties and delays are usually obtained by solving convex optimization problems with Linear Matrix Inequality (LMI) constraints (Boyd, Ghaoui, Feron, and Balakrishnan, 1994). Moreover, for problems involving a structured set of subsystems with restricted information exchange, this LMI approach also allows to impose special zero-nonzero structures on the LMI variables in order to produce a control matrix whose structure is in accordance with the information structure constraints of the system.

A serious drawback in practical implementation of statefeedback controllers is that a full knowledge of the state vector is rarely available. In the static output-feedback approach, the goal is to find a controller that computes the vector of control actions directly from the vector of observed variables, which usually are linear combinations of the states. The main difficulty to attain this goal is that, following the usual LMI approach, an implicit relation results and, in general, the outputfeedback gain matrix, namely K, cannot be directly isolated. A relevant contribution to this problem can be found in the works by Zečević and Šiljak (2004, 2008, 2010), where several explicit expressions for K are provided. However, in order to obtain a zero-nonzero structure, it would be desirable to have a simpler expression for K, since this would help to make the structural constraints on the LMI variables less restrictive and, therefore, to supply more degrees of freedom to achieve a proper solution of the LMIs involved in the process.

In the present paper, based on some simplifications of the gain matrices used in the previous works, we obtain an effective LMI formulation to design static output-feedback controllers similar to the existing one for the state-feedback problem. Moreover, by exploiting this similarity, a strategy to obtain structured output gain matrices is provided. Due to its generality, conceptual simplicity and ease of implementation, the proposed strategy can be a significant tool to be considered in a wide variety of control problems involving a partial knowledge of the state variables and constrained information exchange.

The rest of the paper is organized as follows. Section 2 presents the problem statement. In Section 3, the matrices used in Zečević and Šiljak (2004, 2008, 2010) are transformed in such a way that the output gain matrix takes a similar form to that of the state gain matrix. Section 4 is devoted to developing a strategy to compute the output gain matrices. In Section 5, an academic numerical example to illustrate the effectiveness of the proposed methodology is presented and, finally, conclusions are drown in Section 6.

2. Problem statement

Consider an LMI which depends on a symmetric positive-definite $n \times n$ matrix X, an $m \times n$ matrix Y, and possibly other matrix variables or scalars. Since the LMI may contain both positive-definite and positive semi-definite terms, we write it in a compact form as

$$F(X, Y, z) > 0$$
, $G(X, Y, z) \ge 0$, $X > 0$, (1)

where z is the vector containing the scalars and the entries of the matrix variables distinct from X and Y. This kind of LMI appears in a large amount of control problems in the context of static state-feedback on both discrete and continuous time, where the state gain matrix, namely \tilde{K} , is explicitly given by $\tilde{K} = YX^{-1}$ (see Boyd et al. (1994), or the more recent works by Amato et al. (2010); Chen and Wang (2012); Dhawan and Kar (2011); Du et al. (2011); Huang and Mao (2009); Liu et al.

 $^{^{\}dot{\bowtie}}$ This work was supported in part by the Spanish Ministry of Economy and Competitiveness under Grant DPI2011-25567-C02 and by the Norwegian Center of Offshore Wind Energy (NORCOWE) under Grant 193821/S60 from the Research Council of Norway (RCN).

^{*}Corresponding author. Tel.: +34 93 8777251, fax: +34 93 8777202 *Email addresses: josep.rubio@upc.edu (J. Rubió-Massegú), josep.maria.rossell@upc.edu (J. M. Rossell), hamid.r.karimi@uia.no (H. R. Karimi), francisco.palacios@upc.edu (F. Palacios-Quiñonero)

(2011); Oishi and Fujioka (2010); Wang et al. (2010); Wang and Shen (2011) and references therein).

In static output-feedback control problems, the state gain matrix factors as the product $\tilde{K} = KC$, where C is a given $q \times n$ full row-rank matrix with q < n, and K is the output gain matrix with dimensions $m \times q$. Consequently, when an output gain matrix K is required, the following problem arises:

Problem 1. Find a solution of the LMI given in (1) such that the product YX^{-1} factors as

$$YX^{-1} = KC, (2)$$

where K is a matrix with dimensions $m \times q$.

To solve this problem, Zečević and Šiljak (2004, 2008, 2010) considered matrices of the form

$$X = \rho X_0 + Q X_Q Q^T + U X_C U^T,$$

$$Y = Y_C U^T,$$
(3)

where $\rho > 0$ is an LMI variable, X_Q, X_C, Y_C are matrix variables with X_Q, X_C symmetric, and X_0, Q, U are constant matrices satisfying $X_0C^T = U$, CQ = 0, with X_0 symmetric. The authors proved that if X and $\rho X_0 + Q X_Q Q^T$ are nonsingular matrices, then $Y X^{-1} = K C$ with

$$K = \rho^{-1} Y_C \left[I - U^T S R \right], \tag{4}$$

where I is an identity matrix, and

$$S = \left[\rho X_0 + Q X_Q Q^T\right]^{-1} U X_C, \quad R = \left[I + U^T S\right]^{-1}. \quad (5)$$

Observe that the expression for K given in (4), although explicit, is so intricate that imposing additional conditions on this matrix, as a given zero-nonzero structure, might demand severe structural constraints on the matrix variables X_Q, X_C, Y_C , which might lead to poor solutions of the LMI (1) or even infeasibility.

In this paper, by means of a convenient change of the matrix variables in (3), we simplify equations (4) and (5) so that K takes the form $K = Y_R X_R^{-1}$, where Y_R, X_R are new matrix variables. This simple expression for K is analogous to that obtained for the state gain matrix $\tilde{K} = YX^{-1}$, consequently the usual strategy used to produce structured state gain matrices can be employed to obtain structured output gain matrices. This will result in a conceptually simple and easy-to-implement method for output-feedback controller design under information structure constraints.

3. Preliminary results

The purpose of this section is to express the matrices X, Y in (3) in a more appropriate way. In the sequel, Q is an $n \times (n-q)$ matrix such that its columns are a basis of Ker(C), X_0 is a given symmetric $n \times n$ matrix and $U = X_0C^T$.

Since $CU = CX_0C^T$, CU is symmetric. Moreover, for the LMI (1) to be feasible with matrices of the form (3), it is necessary to assume that CU is invertible. To prove this, let X be as in (3) and suppose that X > 0. From CQ = 0 and $CX_0C^T = CU$, it follows that

$$0 < CXC^{T} = \rho CU + CUX_{C}U^{T}C^{T} = CU\left[\rho I + X_{C}U^{T}C^{T}\right],$$
 (6) and, consequently, CU is invertible.

Theorem 1. The matrices X, Y given in (3) can be written in the form $X = Q\tilde{X}_QQ^T + R\tilde{X}_RR^T$, $Y = \tilde{Y}_RR^T$, where $\tilde{X}_Q, \tilde{X}_R, \tilde{Y}_R$ are matrices of appropriate dimensions with \tilde{X}_Q, \tilde{X}_R symmetric, and R is given by $R = U(CU)^{-1}$.

We can observe that matrix R in the statement satisfies the matrix identity CR = I. To prove Theorem 1, first we need a technical lemma which explicitly solves the homogeneous equation $C\bar{X} = 0$ with \bar{X} symmetric.

Lemma 1. For a given $n \times n$ symmetric matrix \bar{X} , the following two conditions are equivalent: (a) $C\bar{X} = 0$, (b) $\bar{X} = QX_QQ^T$, where X_Q is a symmetric matrix. Moreover, if (a) and (b) are satisfied, then (b) holds with $X_Q = Q^{\dagger}\bar{X}(Q^{\dagger})^T$, where Q^{\dagger} is the Moore-Penrose pseudoinverse of Q, i.e. $Q^{\dagger} = (Q^TQ)^{-1}Q^T$.

PROOF. Clearly (b) implies (a). Suppose (a) holds and let X_Q be the matrix $X_Q = Q^{\dagger} \bar{X} (Q^{\dagger})^T$. From (a), we have $\bar{X} = QS$ for an $(n-q) \times n$ matrix S. Then, $QQ^{\dagger} \bar{X} = QQ^{\dagger} QS = QS = \bar{X}$ and $QX_QQ^T = QQ^{\dagger} \bar{X} (Q^{\dagger})^T Q^T = \bar{X} (Q^{\dagger})^T Q^T = (QQ^{\dagger} \bar{X})^T = \bar{X}^T = \bar{X}$, concluding the proof of Lemma 1.

PROOF (Proof of Theorem 1). Consider the matrices

$$\begin{split} \tilde{X}_C &= CUX_CCU + \rho CU, \\ \tilde{X}_Q &= X_Q + \rho M_0, \\ \tilde{Y}_C &= Y_CCU, \end{split} \tag{7}$$

where M_0 is given by $M_0 = Q^{\dagger} \left[X_0 - U(CU)^{-1} U^T \right] (Q^{\dagger})^T$. Taking into account that $X_0 C^T = U$, which implies $CX_0 = U^T$, we have $C[X_0 - U(CU)^{-1} U^T] = 0$. By Lemma 1, we get

$$QM_0Q^T = X_0 - U(CU)^{-1}U^T. (8)$$

From (3), (7) and (8), and after some elementary manipulations, it is easy to see that

which is the form given in the statement with $\tilde{X}_R = \tilde{X}_C$, $\tilde{Y}_R = \tilde{Y}_C$ and $R = U(CU)^{-1}$. This completes the proof.

4. Output-feedback controller design

In this section, a useful methodology to get an isolated outputfeedback control gain matrix possessing, simultaneously, a preassigned zero-nonzero structure, is developed.

Denote $X_Q = \tilde{X}_Q$, $X_R = \tilde{X}_R$, and $Y_R = \tilde{Y}_R$ in Theorem 1. Then, we have

$$X = QX_QQ^T + RX_RR^T, Y = Y_RR^T,$$
 (10)

where X_Q and X_R are $(n-q) \times (n-q)$ and $q \times q$ symmetric matrices, respectively, and Y_R is an $m \times q$ matrix. In (10), Q is an $n \times (n-q)$ matrix whose columns are a basis of Ker(C), and R is a given $n \times q$ matrix such that CR = I (R is a right inverse of C). Notice that R can be parameterized as

$$R = C^{\dagger} + QL, \tag{11}$$

where L is an $(n-q) \times q$ matrix and C^{\dagger} is the Moore-Penrose pseudoinverse of C, which is explicitly given by $C^{\dagger} = C^T (CC^T)^{-1}$. Indeed, $C(C^{\dagger} + QL) = I$, and if CR = I then $C(R - C^{\dagger}) = 0$. Hence, $R = C^{\dagger} + QL$ for an $(n-q) \times q$ matrix L.

In terms of the new matrix variables, the gain matrix obtained from expressions (4) and (5) takes a very simple form, as shown in the following theorem.

Theorem 2. Suppose that X in (10) is nonsingular. Then, X_R is nonsingular and $YX^{-1} = KC$ with $K = Y_RX_R^{-1}$.

PROOF. Pre-multiplying the first equation in (10) by C, and taking into account that CQ = 0 and CR = I, it follows that $CX = X_R R^T$. Since X is nonsingular, CX has rank q. Therefore, X_R has rank q and X_R is nonsingular since X_R is a $q \times q$ square matrix. Moreover,

$$Y = Y_R R^T = Y_R X_R^{-1} X_R R^T = Y_R X_R^{-1} C X. (12)$$

Post-multiplying both sides of (12) by X^{-1} , we get $YX^{-1} = KC$ with $K = Y_R X_R^{-1}$, and the proof is concluded.

We can now summarize the controller design in the following steps:

- Step 1. Choose an $(n-q)\times q$ matrix L and compute $R=C^{\dagger}+QL$.
- Step 2. Substitute the matrices X, Y given in (10) into the LMI (1). The new LMI has X_O , X_R , Y_R , and z as variables.
- Step 3. Find a solution (X_Q, X_R, Y_R, z) of this LMI, when it is feasible, and compute the matrices X, Y given in (10). Then, the triplet (X, Y, z) is a solution of (1) satisfying $YX^{-1} = KC$, where $K = Y_RX_R^{-1}$.

Observe that the expression obtained for the gain matrix $K = Y_R X_R^{-1}$ allows to impose a preassigned structure on K by taking X_R and Y_R in the usual way, that is, X_R as a block-diagonal matrix and Y_R with the zero-nonzero structure desired for K. For example, if we are interested in obtaining a gain matrix of the form

$$K = \begin{bmatrix} K_{11} & K_{12} & 0\\ 0 & 0 & K_{23}\\ K_{31} & 0 & K_{33} \end{bmatrix}, \tag{13}$$

then we take

$$X_{R} = \begin{bmatrix} X_{1} & 0 & 0 \\ 0 & X_{2} & 0 \\ 0 & 0 & X_{3} \end{bmatrix}, Y_{R} = \begin{bmatrix} Y_{11} & Y_{12} & 0 \\ 0 & 0 & Y_{23} \\ Y_{31} & 0 & Y_{33} \end{bmatrix}, (14)$$

in order to achieve the desired structure on the gain matrix K. It is worth noting that X_Q is a *full* matrix, and that the blocks of X_R and Y_R might contain a very large number of free entries, specially in large-scale systems.

Remark 1. (i) It should be noted that following this strategy, the number of free LMI variables is greater than or equal to the number of free LMI variables that are obtained using the strategies proposed in Zečević and Šiljak (2010), which are based on employing the expressions (3), (4) and (5), while constraining the values of the matrices X_O, X_C, Y_C .

- (ii) The proposed strategy depends on the choice of L, which plays a similar role to the matrix X_0 in (3) but with smaller dimensions. This has the advantage that less parameters have to be previously chosen.
- (iii) For the problem of stabilizing a continuous linear time-invariant system with a nonlinear term, some heuristic choices for L can be deduced from the (heuristic) choices for X_0 in Zečević and Šiljak (2010) and the relationship between L and X_0 , that can be easily obtained from (11) (which yields $L = Q^{\dagger}R$) and the equations $R = U(CU)^{-1}$, $U = X_0C^T$.

In view of Remark 1, the proposed methodology appears to be suitable for large-scale systems. The next proposition allows us to reduce the dimensionality of the term $X = QX_QQ^T + RX_RR^T > 0$, which appears in the LMI of Step 2.

Proposition 1. The matrix inequality $\left[QX_QQ^T + RX_RR^T\right] > 0$ is equivalent to $X_Q > 0$ and $X_R > 0$.

PROOF. We have

$$QX_{Q}Q^{T} + RX_{R}R^{T} = \begin{bmatrix} Q & R \end{bmatrix} \begin{bmatrix} X_{Q} & 0 \\ 0 & X_{R} \end{bmatrix} \begin{bmatrix} Q & R \end{bmatrix}^{T}. (15)$$

The $n \times n$ matrix $P = [Q \ R]$ is nonsingular, because if Qu + Rv = 0, where u and v are vectors of appropriate dimensions, then 0 = C[Qu + Rv] = CRv = v and, therefore, v = 0. This implies that Qu = 0, hence u = v = 0. Now, from (15) we have that $[QX_QQ^T + RX_RR^T] > 0$ if and only if $diag[X_Q, X_R] > 0$, which is equivalent to $X_Q > 0$ and $X_R > 0$.

To end this section, we deal with optimization problems of the form

$$\begin{cases}
\text{Minimize } h(X, Y, z) \\
\text{subject to the LMI (1) and the constraint (2)}
\end{cases}$$
(16)

where the objective function h is assumed to be linear. We can associate to this non-convex problem an LMI optimization problem:

$$\begin{cases} \text{Minimize } h(X, Y, z) \\ \text{subject to the LMI (1), } X, Y \text{ as in (10)} \end{cases}$$
 (17)

where the optimization variables are X_Q , X_R , Y_R and z. Clearly, an optimal solution of the convex problem (17) is not necessarily an optimal solution of (16), but it minimizes the objective function on a set that satisfies all the constraints in (16). In particular, the constraint (2) is satisfied with $K = Y_R X_R^{-1}$. Obviously, solving (17) with an appropriate structure on the matrices X_R , Y_R , a preassigned zero-nonzero structure on the gain matrix K can also be achieved.

5. Numerical example

In this section, the effectiveness of the proposed methodology is illustrated by means of an academic example. A practical application of the theoretical results presented in this paper in the field of *Structural Vibration Control* can be found in Rubió-Massegú et al. (2012).

5.1. An H_{∞} control approach

The standard H_{∞} control procedure for continuous linear time-invariant systems with static state-feedback control involves solution of the following LMI (Boyd et al., 1994):

$$\begin{bmatrix} AX + XA^{T} + BY + Y^{T}B^{T} + \gamma^{-2}B_{w}B_{w}^{T} & * \\ C_{z}X + D_{z}Y & -I \end{bmatrix} < 0, \quad (18)$$

where the unknowns X > 0, Y, and the constant matrices A, B, B_w , C_z , D_z , are of appropriate dimensions, $\gamma > 0$ is a scalar parameter which bounds the H_∞ -norm of the system (induced L^2 gain), and (*) denotes the symmetric entry. The corresponding state-feedback gain matrix is then given by $\tilde{K} = YX^{-1}$. Introducing the parameter $\eta = \gamma^{-2}$, the smallest value of γ under static output-feedback can be achieved by solving the following optimization problem:

$$\begin{cases}
\text{Maximize } \eta \\
\text{subject to } X > 0, \ \eta > 0, \ \text{LMI (18)} \text{ and constraint (2)}
\end{cases}$$
(19)

which has the form given in (16). The matrix values are

$$A = \begin{bmatrix} -4 & 0 & -2 & 0 & 0 \\ 0 & -2 & 0 & 2 & 0 \\ 0 & 0 & -2 & 0 & -1 \\ 0 & -2 & 0 & -1 & 0 \\ 3 & 0 & -2 & 0 & -1 \end{bmatrix}, \quad B = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad B_w = \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix},$$

$$C = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}, \quad C_z = \begin{bmatrix} I_5 \\ 0_{3\times5} \end{bmatrix}, \quad D_z = \begin{bmatrix} 0_{5\times3} \\ I_3 \end{bmatrix}.$$

$$(20)$$

We can observe that A is unstable. Matrix Q is selected as $Q = \begin{bmatrix} 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix}^T$ and matrix L is chosen as $L = [0]_{2\times 3}$. Then, matrix R given in (11) is computed as

In this example three cases are presented, which depend on the preassigned zero-nonzero structure of the gain matrix K: (a) a full output-feedback gain matrix; (b) a tridiagonal gain matrix; and (c) a diagonal gain matrix (totally decentralized control). In each case, the γ -value is calculated.

Case (a). In this first case, no special structure is imposed on the matrix K. According to the strategy presented in Section 4, the computed gain matrix is given by

$$K = \begin{bmatrix} -3.9461 & -0.9267 & -0.9166 \\ -2.9743 & -0.0871 & 0.7084 \\ -1.2371 & 0.3184 & -2.5569 \end{bmatrix}.$$
 (22)

In this case, we get $\gamma_a = 1.2084$.

Case (b). Suppose that we are interested in obtaining a tridiagonal gain matrix K. Then, we impose a diagonal structure on the matrix $[X_R]_{3\times 3}$ and a tridiagonal form on the matrix $[Y_R]_{3\times 3}$ in order to get the same structure in the gain matrix K. In this case, we have

$$K = \begin{bmatrix} -7.8313 & -0.5934 & 0\\ -2.5153 & -0.1913 & -0.0158\\ 0 & 0.0023 & -2.9050 \end{bmatrix}$$
 (23)

with a minimum γ -value of $\gamma_b = 1.2385$.

Case (c). To achieve a diagonal structure in the matrix K, we impose a diagonal structure on the matrices $[X_R]_{3\times 3}$ and $[Y_R]_{3\times 3}$. In this case, we obtain

$$K = \begin{bmatrix} -6.4172 & 0 & 0\\ 0 & 0.0458 & 0\\ 0 & 0 & -3.9087 \end{bmatrix}$$
 (24)

with $\gamma_c = 1.2859$.

It is worth noting that $\gamma_a < \gamma_b < \gamma_c$, since the number of variables increases when less structural conditions are imposed on the matrix variables involved in the LMI and, consequently, it has more degrees of freedom to attain a better (minimum) γ -value.

6. Conclusions

In this paper, a Linear Matrix Inequality strategy to design static output-feedback controllers has been presented. The most remarkable feature of the proposed solution is its simplicity, which makes it possible to design semi-decentralized static output-feedback controllers in a similar way to semi-decentralized static state-feedback controllers. The question of finding a proper choice of matrix L remains open, which is an interesting challenge for future research. From a practical point of view, the proposed methodology can be of great interest to a wide variety of engineering areas, where complex control problems involving several subsystems, with constrained information exchange, and a partial knowledge of the state variables, are frequently encountered.

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