

1 **Reliability of the Kinematic Theory parameters during handwriting tasks on a**  
2 **vertical setup**

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33

34 **Abbreviations**

35 CI: Confidence Interval

36 CV: Coefficient of Variation

37 ICC: Intraclass Correlation Coefficient

38 MDC: Minimal Detectable Change

39 SEM: Standard Error of Measurement

40 SNR: Signal-to-Noise Ratio

41

42 **Figures and Tables:**

43 Figure 1: single-column fitting image

44 Figure 2: two-column fitting image

45 Tables 1, 2 and 3: two-column fitting tables

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## Highlights

- ✓ Kinematic Theory has reliable test-retest parameters in all types of strokes
- ✓ The Sigma-Lognormal model reconstructs data similarly from day to day
- ✓ The Kinematic Theory offers clinical insights in the detection of fatigue
- ✓ Kinematic Theory and the Sigma-Lognormal model can be used to study shoulder fatigue
- ✓ The *mode*, *median* and *time delay* are effective parameters for fatigue detection

47 **Abstract**

48 *Background:* The Kinematic Theory and its Sigma-Lognormal model have been used extensively  
49 in motor control analyses. It has recently shown promise in its ability to detect neuromuscular  
50 fatigue in the shoulder. The use of an ergonomic setup composed of a vertically oriented tablet  
51 offers a good demonstration for use in future clinical applications. However, parameters'  
52 reliability of this theory needs to be evaluated. The aim of this study is to assess the test-retest  
53 reliability of these parameters in the specific case of fatigue detection.

54 *Method:* Forty participants performed two sessions of fast strokes handwriting (simple strokes,  
55 triangles, horizontal and vertical oscillations) on a tablet placed at shoulder's height. Reliability  
56 was assessed using the intraclass correlation coefficient (ICC), their relative standard error of  
57 measurement (SEM) and coefficient of variation. The minimal detectable change was also  
58 reported.

59 *Findings:* In general, a moderate to excellent reliability was denoted in the main parameters of  
60 each test (ICC: 0.54-0.91). The parameters related to shoulder fatigue detection had good to  
61 excellent reliability (ICC: 0.77-0.90) with low SEM (SEM: 4.75-6.99%).

62 *Conclusion:* Most of the parameters have good test-retest reliability, and the setup seems  
63 adequate for shoulder fatigue detection.

64

65 **Keywords:** Sigma-Lognormal model; Kinematic Theory; Reliability; Shoulder; Muscle fatigue;  
66 Fatigue detection.

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## 70 **1. Introduction**

71 Muscle fatigue corresponds to a decline in strength production during a task [1], and results in  
72 atypical stresses, which can possibly lead to musculoskeletal injuries over time [2]. Those  
73 injuries are omnipresent in the population, especially in the shoulder [3]. Overuse injuries affect  
74 quality of life and are expensive to treat, requiring physiotherapy treatments over a period of  
75 years [4]. It is then essential to detect shoulder muscle fatigue before the onset of an injury. In the  
76 long pathway of assessing a test as clinically usable, an important step is to evaluate its  
77 diagnostic accuracy [5]. To that extent, screening tests have to be reliable with sensitive and  
78 specific data, but must also be affordable and easy to implement [6]. According to Weir [7], the  
79 Intraclass Correlation Coefficient (ICC) and the Standard Error of Measurement are powerful  
80 metrics in the quantification of data reliability.

81 Current methods can detect shoulder fatigue, but unfortunately have limitations that prohibits  
82 their use in a clinical environment [8]. A common method includes questionnaires such as the  
83 Borg's Rating of Perceived Exertion Scale, which represents a participant's subjective level of  
84 exertion during exercise [9]. However, studies correlating this rating with physiological variables  
85 of exertion are not always consistent [10, 11], as the rating depends on motivation and is  
86 subjective. Objective measures can be used, such as biomarkers, but their assessment is often  
87 invasive [12]. Less invasive biomarkers such as those obtained from surface electromyography  
88 may be used, where the analysis of the signal amplitude and power spectrum density can be used  
89 to detect fatigue [13-15]. This is a reliable measure for fatigue detection [8, 16], as the median  
90 and mean power frequencies tend to be greatly reliable (Intraclass Correlation Coefficient > 0.80)  
91 [17]. However, a good electrode placement is essential to avoid cross-talk and maintain a good  
92 reliability [18, 19]. The post-collection data processing is also time-consuming, which is a  
93 disadvantage for clinical evaluation. Other methods, such as mecanomyography, sonomyography  
94 or near-infrared spectroscopy can also be used to detect fatigue. However, they are combined  
95 most of the time with electromyography, which is difficult to implement in clinics [8].

96 Recently, a new method for shoulder fatigue detection has been settled using the Kinematic  
97 Theory of Rapid Human Movements [20, 21]. More broadly, the Kinematic Theory has been  
98 utilized to assess patients with Parkinson's disease [22], concussion [23], attention deficit  
99 hyperactivity disorder [24], as well as aging phenomena [25], and stroke risk factors [26]. This

100 theory assesses behavior through their end-effector kinematics [27, 28] (see section 2.3). The  
101 movement velocity is described as the synergy of impulse responses from neuromuscular systems  
102 generating the movement. Each response is modeled through a lognormal equation whose  
103 parameters describe the participant's motor control conditions [29]. The ideal movement is  
104 known and a change in the parameters baseline highlights neuromuscular problems, such as  
105 shoulder neuromuscular fatigue [20, 21]. Theoretically, identified parameters may be related to  
106 the central or the peripheral nervous systems (as well as to the agonistic or antagonistic systems)  
107 and to the motor program execution, as described in Appendix A. The specificity of the  
108 Kinematic Theory has therefore a prescreening potential that could be used by medical  
109 professional in their diagnoses. To characterize the cranio-caudal sequence of turning while  
110 walking [30], we know that the reliability in the kinematic parameters is moderate to good  
111 (Intraclass Correlation Coefficient = 0.64-0.81). However, to the best of our knowledge, the  
112 reliability of handwriting tasks for clinical applications has never been assessed. In the specific  
113 example of shoulder fatigue, handwriting data were recorded on a vertical setup [20], an  
114 ergonomic and easy to use tablet, and has shown potential for clinical applications [5]. After the  
115 onset of fatigue, the parameters related to motor program execution increased significantly, but  
116 their reliability was not assessed in this study.

117 The objective of this study is then to assess the test-retest reliability of the parameters extracted  
118 through Kinematic Theory from handwriting movements recorded with a vertically oriented  
119 digitizing tablet. A characterization of the reliability of these parameters will allow a better  
120 comprehension of the parameters' reproducibility and of their measurement errors for motor  
121 control studies.

122

123 **2. Materials and methods**

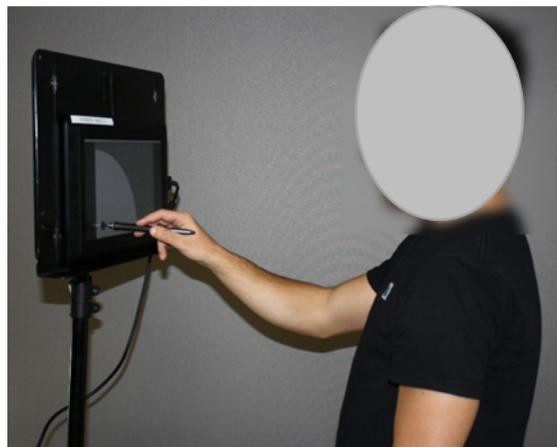
124 *2.1. Participants*

125 Forty healthy active adults participated in the study (18 males and 22 females, age:  $24.8 \pm 4.3$   
126 years, height:  $173.3 \pm 9.8$  cm, mass:  $69.6 \pm 12.6$  kg, dominant hand 6 left-handed and 34 right-  
127 handed). Participants were excluded if: (i) they had upper-limb musculoskeletal disorders; (ii)  
128 neurological problems or (iii) history of shoulder surgery in the past years. The study was  
129 approved by Polytechnique Montréal research ethics committee (CER-1819-23 v.3).

130 *2.2. Protocol*

131 Fast stroke kinematics were recorded on a Wacom Cintiq 13HD tablet (sampling frequency:  
132 200 Hz) during two test sessions. The tablet was positioned at the participant's shoulder height,  
133 as measured while standing (Figure 1). The tablet was positioned so that the participant's  
134 fingertip was touching the bottom of the tablet with a shoulder flexion of  $90^\circ$ . The same tablet  
135 height was used for all tests for each individual. They were also asked to stand at a comfortable  
136 distance from the tablet. Four series of fast strokes were drawn on the tablet with the participant's  
137 dominant hand in a random sequence: 30 simple strokes, 30 triangles, 10-second horizontal  
138 oscillations and 10-second vertical oscillations at their maximal speed. A training period of five  
139 to seven fast strokes was given before simple strokes and triangles. The current test is part of a  
140 larger study, which fully describes the procedure of collecting data [20]. Test and retest were  
141 recorded by a single tester with a minimum of one-day interval (up to two months).

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143

144 **Figure 1:** Position of the participant while drawing strokes. The tablet was positioned at the  
145 shoulder's height.

### 146 2.3. *Extraction of kinematic parameters, the Sigma-Lognormal model*

147 Numerous models have been used over the last few decades to study human motor control:  
148 models relying on neural networks, on equilibrium points, behavioral models, coupled oscillator  
149 models, kinematic models, motor synergetic models, non-Euclidean and Riemann models as well  
150 as models exploiting minimization principles (minimization of: acceleration, energy, time, jerk,  
151 snap, torque changes, and sensory-motor noise), sensory-motor optimal control models (see  
152 Plamondon [31] for an exhaustive list of references). Many of these models exploit the properties  
153 of various mathematical functions to represent human movements: exponentials, second order  
154 systems, Gaussians, beta functions, splines, and trigonometric functions. Among these,  
155 Kinematic Theory [27, 28, 32, 33] and its sigma-lognormal model [34, 35] is one of the most  
156 efficient methodologies for reproducing human-like movements. It has been tested time and again  
157 over the last few decades by numerous researchers, using various input devices under various  
158 experimental (1D, 2D and 3D) conditions [36]. It has even been mathematically demonstrated  
159 that it is the ultimate minimization theory, and that the process of trajectory selection could be  
160 described as the process of recruiting a sufficient number of neuromuscular subsystems to  
161 approximate the lognormal profile [37]. For all of these reasons, we have chosen to use  
162 Kinematic Theory in the present study.

163 Empirical data of each stroke were modeled thanks to the Sigma-Lognormal model of the  
164 Kinematic Theory. To do so, the in-house program named Script Studio was used [34].

165 The key concept behind the Kinematic Theory is twofold. First, it postulates that the invariant  
166 properties of simple pointing movements can be considered as specific movement primitives [38]  
167 that reflect the asymptotic behavior of complex systems, made up of a large number of coupled  
168 neuromuscular networks, whose impulse response can be modelled using lognormal functions.

169 From a mathematical point of view, when a command  $D_i$  is input to a lognormal neuromuscular  
170 system at a given time  $t_{0i}$  a velocity profile is produced at the output of such a system:

$$\left| \dot{v}_i^r(t; t_{0i}, \mu_i, \sigma_i^2) \right| = D_i \Lambda_i(t; t_{0i}, \mu_i, \sigma_i^2) \quad (1)$$

$$\Lambda_i(t; t_{0i}, \mu_i, \sigma_i^2) = \frac{1}{\sigma_i \sqrt{2\pi} (t - t_{0i})} \exp \left\{ \frac{-[\ln(t - t_{0i}) - \mu_i]^2}{2\sigma_i^2} \right\} \quad (2)$$

171

172 and where the set of parameters describing a lognormal pulse  $\Lambda_i$  refers to

173  $D_i$  : the input command, which is the intended distance to be covered with the pulse;

174  $t_{0i}$  : the time occurrence of that command, as instantiated in the central nervous system (CNS);

175  $\mu_i$  : the log time delay (i.e., the time delay on a logarithmic time scale);

176  $\sigma_i$  : the log response time (i.e., the response time on a logarithmic time scale).

177

178 Accordingly, the sequence of lognormal velocity patterns observed in any movements are the

179 results of an asymptotic convergence that can be interpreted as reflecting the behavior of subjects

180 who are in perfect control of their movements. In other words, the production of complex

181 movements is reached through the exploitation of the Lognormality Principle, by time

182 superimposing and summing up lognormal vectors, with the goal of minimizing their number in a

183 given task, to produce efficient, fluent gestures, optimizing the energy required to generate these.

184 This summation process is referred to as the Sigma-Lognormal model:

185

$$\vec{v}(t) = \sum_{i=1}^N \vec{v}_i(t; t_{0i}, \mu_i, \sigma_i^2) = \sum_{i=1}^N \begin{bmatrix} \cos(\theta_i(t)) \\ \sin(\theta_i(t)) \end{bmatrix} v_i(t); N \geq 2 \quad (3)$$

$$v_i(t) = D_i \Lambda_i(t; t_{0i}, \mu_i, \sigma_i^2) = \frac{D_i}{\sigma_i (t - t_{0i}) \sqrt{2\pi}} \exp \left( \frac{[\ln(t - t_{0i}) - \mu_i]^2}{-2\sigma_i^2} \right) \quad (4)$$

where

$$\theta_i(t) = \theta_{si} + \frac{(\theta_{ei} - \theta_{si})}{D_i} \int_0^t v_i(\tau) d\tau \quad (5)$$

186 and where  $\theta_{si}$  and  $\theta_{ei}$  stand respectively for the starting and ending angular direction of each

187 discontinuous primitive or stroke.

188 From a practical point of view, what is interesting is that Kinematic Theory can be reverse

189 engineered to decompose any movements into its lognormal constituents using specific software

190 [34, 36, 39-41] that provide a set of central and peripheral parameters describing the

191 neuromuscular state of the subject who has produced a given movement. Each lognormal

192 function describes the impulse response of a neuromuscular component involved in the

193 movement execution (Figure 2A). All lognormals are scaled in time ( $t_{0i}$ ) and space ( $D_i$ ) (2).  
194 Under a physiological point of view,  $t_{0i}$  (s) represents the time at which the brain send the  
195 command to execute the movement of the  $i$ -th lognormal; and  $D_i$  (mm) is the amplitude of a  
196 lognormal. In case of an oscillatory movement, it is possible to calculate the time difference  
197 between two consecutive  $t_0$  ( $\Delta(t_0)$ , s) to get the rhythmicity of a command sent during the test. All  
198 lognormals also have their own distribution, defined by the mean ( $\mu_i$ ) and the standard deviation  
199 ( $\sigma_i$ ) of the normal distribution associated. These two parameters are related to the timing  
200 properties of the neuromuscular system:  $\mu$  also called the log-time delay (s) and  $\sigma$  the  
201 log-response time (s). Nevertheless, as the reconstruction is performed for a complex movement  
202 with a change in direction (e.g. when drawing a triangle), the notion of trajectory is important.  
203 Each lognormal describes a trajectory part of the action plan. When all of the lognormals are  
204 combined, they form the complete action plan and thus the overall trajectory of the movement. In  
205 consequence, each lognormal has a starting ( $\theta_s$ ) and ending angle ( $\theta_e$ ) to define its own trajectory.  
206 The number of lognormal functions ( $NbLog$ ) depends on the movement and its fluidity. The  
207 optimization of the reconstruction relies on the Signal-to-Noise Ratio ( $SNR$ ), which is considered  
208 to be excellent if higher than 25 dB. For more details regarding the Theory and the extraction of  
209 parameters, can be found in [27], Plamondon, Feng and Woch [32], [34].

210 Aside from the eight main parameters (i.e.  $t_0$ ,  $D$ ,  $\theta_s$ ,  $\theta_e$ ,  $\mu$ ,  $\sigma$ ,  $NbLog$ ,  $SNR$ ), six derived parameters  
211 were calculated as follows [32, 42]: (i) the *mode* (s) which corresponds to the time when the  
212 maximum velocity of the lognormal is reached; (ii) the *median* (s) that is the time when half the  
213 value of the lognormal integral is attained; (iii) the *time delay* (s) which corresponds to the  
214 response command rapidity of a given system; (iv) the *response time* (s) which evaluates the  
215 impulse response spread; (v) the *asymmetry* (no units) which describes the general shape of the  
216 lognormal; and (vi) the  $SNR/NbLog$  that depicts the motor control quality. The *reaction time*  
217 ( $RT$ ), a classical parameter that is not otherwise part of the Theory, was also extracted in order to  
218 calculate the *conduction time* (s), which represents the duration of the command propagation  
219 [43]. The supplementary material (APPENDIX A) of the present study provides a more detailed  
220 explanation of these parameters and their physiological meaning.

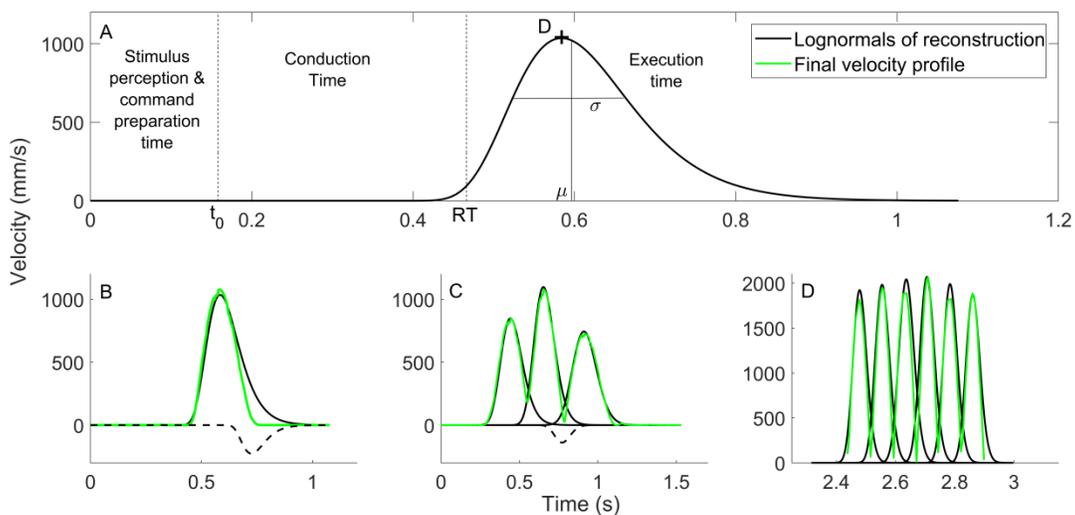
221

222 2.4. Data processing

223 Simple strokes were divided into their largest *agonist* and *antagonist* components (Figures 2B).  
224 When only one lognormal described the stroke, it was automatically labeled as *agonist*.  
225 Lognormals with parameters outside of the  $\text{mean} \pm 3\text{SD}$  were rejected. For the *NbLog*, the *SNR*,  
226 the *SNR/NbLog*, the *reaction time* and the *conduction time*, no distinctions between  
227 *agonist/antagonist* components were made, as they refer to global stroke properties. The mean  
228 value of each parameter was calculated.

229 Triangles were split into the *agonist* components explaining the three main strokes (Figures 2C).  
230 Outliers were manually removed when the action plan of the reconstruction was found to be  
231 incorrect. Finally, lognormals with parameters outside of the  $\text{mean} \pm 3\text{SD}$  were rejected. The mean  
232 value of each parameter was calculated, except for  $t_0$  as only the first one was considered.

233 For the horizontal and vertical oscillations (50-160 mm long), only lognormals extracted from a  
234 stable phase were analyzed (*i.e.* from 2 to 10-s oscillations). Each stroke of the oscillatory  
235 movement was considered as *agonist* (Figure 2D). Lognormals with an amplitude below 50 mm  
236 and with parameters outside of the  $\text{mean} \pm 3\text{SD}$  were considered as artefacts, therefore rejected.  
237 The mean value of each parameter was calculated, except for the *reaction time*, the *conduction*  
238 *time*, the *SNR* and the *SNR/NbLog*, since only a single value per test and participant can be  
239 recorded.



240

241 **Figure 2:** Reconstruction of the different types of strokes. (Green) is the final velocity profile and  
242 (black) are the lognormals used for reconstruction referred as *agonists* (solid lines) or *antagonists*  
243 (dashed lines). (A) is a visualization of the parameters on a lognormal. (B) is the reconstruction  
244 of a simple stroke. (C) is the reconstruction of a triangle. (D) is an example of a signal portion  
245 reconstruction for the oscillations.

## 246 2.5. Statistical analysis

247 An analysis of variance (ANOVA) based on intraclass correlation coefficients (ICC) was  
248 performed (Matlab, the Mathworks Intraclass Correlation Coefficient (ICC) version 1.3.1.0 of  
249 Arash Salarian) to get the test-retest reliability. ICC were calculated by parameters at 95%  
250 confidence intervals using a two-way mixed effects model based on absolute agreement [44]. An  
251 average measurements model was used for mean values whereas a single measure model was  
252 used for single values (*i.e. reaction time, conduction time, SNR and SNR/NbLog* in the  
253 oscillations). The scores were interpreted in line with the scale used in Koo and Li [44]: poor  
254 (<0.50), moderate (0.50-0.75), good (0.75-0.90) and excellent (>0.90) reliability. As explained in  
255 Bartko [45], a value of zero was set in case of negative ICC. The absolute and relative standard  
256 error of measurement (SEM), the coefficient of variation (CV) and the minimal detectable change  
257 (MDC) were also reported to estimate the measurement errors. These measurements are the gold  
258 standards in reliability analyses of movement science [46, 47]. Bland-Altman plots were also  
259 drawn (see APPENDIX B) to display the degree of agreement of the intra-participant  
260 measurements for *SNR, asymmetry,  $\sigma$  and conduction time*.

261 **3. Results**

262 Data are expressed as mean±SD. In the simple strokes (Table 3.1), the time  $t_0$  had good  
263 reliability, both for the *agonist* (ICC=0.80) and *antagonist* components (ICC=0.89). The  
264 coefficient of variation was higher in the *agonist* than in the *antagonist* components (respectively  
265 36.81% and 25.51%). Regarding  $\sigma$ , the ICC was moderate with a value of 0.62 for the *agonist*  
266 components and 0.69 for the *antagonist*. Their CVs were 18.12% and 23.27% respectively. The  
267 *mode*, *median*, *time delay* and *response time* had good to excellent reliability, ranging from 0.85  
268 to 0.90 in both components, with a low SEM (5.44 - 14.11%) and a minimal detectable change  
269 (MDC) of 0.10 s. Parameters describing the global state of the neuromotor system (*NbLog*, *SNR*  
270 and *SNR/NbLog*) had a moderate ICC ranging from 0.56 to 0.73 with low SEM values (from  
271 2.35% to 5.41%). The *conduction time* had a moderate ICC (0.67) with a high CV (38.78%).

272

273 **Table 1:** Test-retest reliability of kinematic parameters extracted from simple strokes with the  
 274 Sigma-Lognormal model. Red, orange, green and blue respectively represents poor, moderate,  
 275 good and excellent reliability.

Parameter	Test	Retest	ICC (95% CI)	SEM	SEM (%)	CV (%)	MDC
<b>Agonist component</b>							
$t_0$	0.24 ± 0.11	0.26 ± 0.09	0.80 (0.63-0.90)	0.04	16.29	36.81	0.11
$D$	206.40 ± 20.75	208.40 ± 23.31	0.86 (0.74-0.93)	7.74	3.73	9.96	21.46
$\mu$	-1.34 ± 0.26	-1.40 ± 0.19	0.76 (0.54-0.87)	0.10	7.44	15.05	0.28
$\sigma$	0.27 ± 0.07	0.27 ± 0.05	0.62 (0.28-0.80)	0.03	11.19	18.12	0.08
$ \cos(\vartheta_s) $	0.79 ± 0.09	0.78 ± 0.09	0.91 (0.82-0.95)	0.03	3.17	10.32	0.07
$ \cos(\vartheta_e) $	0.94 ± 0.04	0.95 ± 0.03	0.83 (0.66-0.91)	0.01	1.47	3.53	0.04
Mode	0.51 ± 0.09	0.51 ± 0.10	0.85 (0.71-0.92)	0.04	6.99	17.83	0.10
Median	0.53 ± 0.10	0.52 ± 0.10	0.86 (0.73-0.93)	0.04	6.72	17.89	0.10
Time Delay	0.54 ± 0.10	0.53 ± 0.11	0.87 (0.75-0.93)	0.04	6.60	17.99	0.10
Response Time	0.07 ± 0.02	0.07 ± 0.02	0.84 (0.67-0.92)	0.01	10.10	25.02	0.02
Asymmetry	0.10 ± 0.05	0.09 ± 0.04	0.51 (0.09-0.74)	0.03	29.24	41.81	0.07
<b>Antagonist component</b>							
$t_0$	0.46 ± 0.12	0.45 ± 0.13	0.89 (0.79-0.94)	0.04	8.59	25.51	0.11
$D$	30.11 ± 6.00	29.69 ± 7.42	0.70 (0.44-0.84)	3.22	10.76	19.80	8.92
$\mu$	-1.80 ± 0.18	-1.84 ± 0.24	0.19 (0.00-0.57)	0.14	7.86	8.71	0.40
$\sigma$	0.37 ± 0.10	0.36 ± 0.10	0.69 (0.41-0.84)	0.05	12.98	23.27	0.13
$ \cos(\vartheta_s) $	0.94 ± 0.05	0.96 ± 0.05	0.00 (0.00-0.46)	0.03	3.41	3.39	0.09
$ \cos(\vartheta_e) $	0.89 ± 0.10	0.91 ± 0.07	0.86 (0.74-0.93)	0.03	3.17	8.55	0.08
Mode	0.64 ± 0.11	0.63 ± 0.11	0.88 (0.77-0.94)	0.04	5.64	16.14	0.10
Median	0.66 ± 0.11	0.65 ± 0.12	0.89 (0.79-0.94)	0.04	5.49	16.59	0.10
Time Delay	0.67 ± 0.12	0.66 ± 0.12	0.90 (0.81-0.95)	0.04	5.44	16.97	0.10
Response Time	0.06 ± 0.02	0.06 ± 0.02	0.81 (0.64-0.90)	0.01	14.11	32.13	0.02
Asymmetry	0.21 ± 0.11	0.20 ± 0.11	0.66 (0.37-0.82)	0.05	26.49	45.75	0.15
<b>Whole signal</b>							
NbLog	2.28±0.27	2.19±0.25	0.73 (0.49-0.86)	0.12	5.41	10.50	0.34
SNR	30.05±1.34	30.06±1.21	0.56 (0.15-0.77)	0.71	2.35	3.53	1.96
SNR/NbLog	13.89±1.68	14.41±1.75	0.67 (0.37-0.82)	0.86	6.11	10.57	2.40
RT	0.41±0.08	0.41±0.10	0.82 (0.65-0.90)	0.04	8.55	19.90	0.10
$ t_0-RT $	0.17±0.09	0.15±0.05	0.67 (0.39-0.83)	0.04	22.18	38.78	0.10

276 ICC: Intraclass Correlation Coefficient, CI: Confidence Interval, SEM: Standard Error of Measurement, CV: Coefficient of Variation, MDC:  
 277 Minimal Detectable Change

278  
 279 For the triangles (Table 3.2),  $t_0$  presented a good reliability (ICC=0.81), with a SEM of 10.41%.  
 280 Parameters related to the peripheral system,  $\mu$  and  $\sigma$ , had respectively moderate (0.68) and good  
 281 (0.78) reliability, with a low value of SEM (11.69% and 8.76%). The derived parameters (the  
 282 *mode, median, time delay, response time* and *asymmetry*) had good reliability, ranging from 0.77

283 to 0.79 with a low CV (10.4% - 15.8%) except for the *asymmetry* (42.2%). Their MDC was  
 284 0.11 s. The *SNR* had poor reliability (0.13) with a low SEM (1.10%) whereas the *SNR/NbLog* had  
 285 moderate reliability. The *conduction time* had good reliability (0.77, 95%CI: 0.57-0.88), with a  
 286 CV of 39.46%.

287 **Table 2:** Test-retest reliability of kinematic parameters extracted from triangles with the  
 288 Sigma-Lognormal model. Red, orange and green respectively represents poor, moderate and  
 289 good reliability. No parameters had an excellent reliability.

Parameter	Test	Retest	ICC (95% CI)	SEM	SEM (%)	CV (%)	MDC
$t_0$	0.25 ± 0.06	0.25 ± 0.07	0.81 (0.64-0.90)	0.03	10.41	23.67	0.07
<i>D</i>	151.87 ± 8.36	154.15 ± 9.05	0.54 (0.14-0.75)	4.92	3.21	4.72	13.63
$\mu$	-0.75 ± 0.17	-0.77 ± 0.19	0.68 (0.40-0.83)	0.09	11.69	20.67	0.25
$\sigma$	0.20 ± 0.04	0.19 ± 0.04	0.78 (0.58-0.88)	0.02	8.76	18.51	0.05
<i>Mode</i>	0.79 ± 0.08	0.77 ± 0.10	0.77 (0.57-0.88)	0.04	5.08	10.61	0.11
<i>Median</i>	0.82 ± 0.09	0.79 ± 0.10	0.77 (0.57-0.88)	0.04	5.02	10.47	0.11
<i>Time Delay</i>	0.82 ± 0.09	0.80 ± 0.10	0.77 (0.57-0.88)	0.04	5.00	10.42	0.11
<i>Response time</i>	0.08 ± 0.02	0.08 ± 0.01	0.79 (0.43-0.91)	0.01	7.28	15.84	0.02
<i>Asymmetry</i>	0.06 ± 0.03	0.05 ± 0.02	0.78 (0.58-0.88)	0.01	19.99	42.19	0.03
<i>NbLog</i>	5.43 ± 0.65	5.09 ± 0.50	0.78 (0.25-0.91)	0.25	4.82	10.27	0.70
<i>SNR</i>	26.78 ± 0.41	26.97 ± 0.45	0.13 (0.00-0.52)	0.30	1.10	1.18	0.82
<i>SNR/NbLog</i>	5.12 ± 0.63	5.47 ± 0.51	0.74 (0.19-0.90)	0.27	5.03	9.95	0.74
<i>RT</i>	0.42 ± 0.07	0.43 ± 0.09	0.85 (0.71-0.92)	0.03	7.01	17.84	0.08
$ t_0-RT $	0.17 ± 0.07	0.19 ± 0.08	0.77 (0.57-0.88)	0.03	18.82	39.46	0.09

290 ICC: Intraclass Correlation Coefficient, CI: Confidence Interval, SEM: Standard Error of Measurement, CV: Coefficient of Variation, MDC:  
 291 Minimal Detectable Change

292  
 293 Parameters were categorized similarly for the horizontal and vertical oscillations (Table 3.3),  
 294 except for the *reaction time* and the *conduction time*.  $\Delta t_0$  had good reliability (ICC=0.79 and 0.80)  
 295 and a low SEM (horizontal oscillations: 5.07%; vertical oscillations: 6.92%). Poor reliability was  
 296 observed for  $\sigma$ , *asymmetry* and *SNR*. The *SNR/NbLog* had moderate reliability, ranging from 0.64  
 297 to 0.70 (95% CI: 0.29-0.82). The *mode*, *median*, *time delay* and *response time* had an ICC  
 298 considered as good (horizontal oscillations: 0.83; vertical oscillations: 0.79-0.80). The *conduction*  
 299 *time* had poor reliability in the horizontal oscillations and moderate in the vertical oscillations,  
 300 with a low SEM (horizontal oscillations: 17.60%; vertical oscillations: 19.49%). The *NbLog* was  
 301 exactly the same for every participant for both the horizontal or vertical oscillations.

302 **Table 3:** Test-retest reliability of kinematic parameters extracted from horizontal and vertical  
 303 oscillations with the Sigma-Lognormal model. Red, orange and green respectively represents  
 304 poor, moderate and good reliability. No parameters had an excellent reliability.

Parameter	Test	Retest	ICC (95% CI)	SEM	SEM (%)	CV (%)	MDC
<b>Horizontal oscillations</b>							
$\Delta(t_0)$	0.09 ± 0.01	0.09 ± 0.01	0.79 (0.52-0.90)	0.00	5.07	11.04	0.01
<i>D</i>	119.74 ± 22.42	116.30 ± 20.94	0.86 (0.73-0.92)	7.72	6.54	17.25	21.39
$\mu$	-0.75 ± 0.13	-0.79 ± 0.10	0.83 (0.62-0.92)	0.05	5.91	14.39	0.13
$\sigma$	(0.06 ± 0.83)E-03	(0.06 ± 1.33)E-03	0.07 (0.00-0.50)	3.51E-04	0.61	0.63	9.73E-04
<i>Mode</i>	0.57 ± 0.08	0.54 ± 0.06	0.83 (0.59-0.92)	0.03	4.75	11.38	0.07
<i>Median</i>	0.57 ± 0.08	0.55 ± 0.06	0.83 (0.59-0.92)	0.03	4.75	11.38	0.07
<i>Time Delay</i>	0.57 ± 0.08	0.55 ± 0.06	0.83 (0.59-0.92)	0.03	4.75	11.38	0.07
<i>Response Time</i>	(30.0 ± 3.67)E-03	(30.0 ± 2.71)E-03	0.83 (0.63-0.92)	1.22E-03	4.54	11.16	3.39E-03
<i>Asymmetry</i>	(3.36 ± 0.25)E-03	(3.43 ± 0.72)E-03	0.03 (0.00-0.48)	4.19E-05	1.27	1.29	1.16E-04
<i>RT</i>	0.48 ± 0.11	0.45 ± 0.10	0.36 (0.00-0.66)	0.07	14.43	18.06	0.18
<i> \Delta(t_0)-RT </i>	-0.38 ± 0.10	-0.36 ± 0.10	0.33 (0.00-0.64)	0.07	17.60	21.51	0.18
<i>SNR</i>	28.21 ± 1.20	28.62 ± 0.97	0.00 (0.00-0.26)	0.77	2.71	2.64	2.13
<i>SNR(dB)/NbLog</i>	0.23 ± 0.04	0.22 ± 0.03	0.70 (0.44-0.84)	0.02	7.04	12.83	0.04
<b>Vertical oscillations</b>							
$\Delta(t_0)$	0.10 ± 0.02	0.09 ± 0.01	0.80 (0.49-0.91)	0.01	6.92	15.38	0.02
<i>D</i>	116.04 ± 21.12	114.44 ± 22.21	0.84 (0.69-0.91)	8.12	7.05	17.41	22.52
$\mu$	-0.68 ± 0.17	-0.75 ± 0.14	0.81 (0.49-0.91)	0.06	8.86	20.11	0.18
$\sigma$	(0.06 ± 4.74)E-04	(0.06 ± 2.82)E-03	0.25 (0.00-0.60)	0.0013	2.30	2.66	3.60E-03
<i>Mode</i>	0.61 ± 0.11	0.57 ± 0.08	0.79 (0.47-0.90)	0.04	6.80	14.87	0.11
<i>Median</i>	0.61 ± 0.11	0.57 ± 0.08	0.79 (0.47-0.90)	0.04	6.80	14.87	0.11
<i>Time Delay</i>	0.61 ± 0.11	0.57 ± 0.08	0.79 (0.47-0.90)	0.04	6.80	14.87	0.11
<i>Response Time</i>	0.03 ± 0.01	0.03 ± 0.004	0.80 (0.50-0.91)	0.00	6.57	14.84	0.01
<i>Asymmetry</i>	(3.30 ± 0.06)E-03	(3.55 ± 1.56)E-03	0.06 (0.00-0.50)	0.00	22.40	23.14	2.13E-03
<i>RT</i>	0.46 ± 0.15	0.43 ± 0.10	0.55 (0.16-0.76)	0.07	15.61	23.25	0.19
<i> \Delta(t_0)-RT </i>	-0.37 ± 0.14	-0.34 ± 0.10	0.53 (0.12-0.75)	0.07	19.49	28.56	0.19
<i>SNR</i>	28.00 ± 1.43	28.07 ± 1.30	0.45 (0.15-0.67)	0.86	3.07	4.14	2.39
<i>SNR(dB)/NbLog</i>	0.25 ± 0.05	0.23 ± 0.04	0.64 (0.29-0.82)	0.02	10.26	17.10	0.07

305 ICC: Intraclass Correlation Coefficient, CI: Confidence Interval, SEM: Standard Error of Measurement, CV: Coefficient of Variation, MDC:  
 306 Minimal Detectable Change

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## 309 4. Discussion

310 The aim of this study was to assess the test-retest reliability of fast strokes' kinematic parameters  
311 drawn on a tablet using a vertical setup. They were extracted according to the Sigma-Lognormal  
312 model with the aim of using the setup for clinical applications in fatigue detection. Overall, most  
313 of the parameters from the four tests seem to present sufficient reliability for clinical applications.

### 314 4.1. Reliability of the four tests

315 In general, the four series of tests seem to present an adequate level of reliability. The movement  
316 execution with the dominant hand enables one to attain superior levels of motor control quality,  
317 and have less variability in the gesture [48]. As found by Smits, Tolonen, Cluitmans, van Gils,  
318 Zietsma, Tijssen and Maurits [49], a zigzag graphical task (*i.e.* a combination of simple strokes)  
319 had already been assessed as good, with an ICC of 0.89 for its movement time and of 0.82 for its  
320 mean error. Other handwriting tasks were considered to have excellent reliability (ICC=0.927) in  
321 their average absolute velocity [50], meaning that the overall kinematics of handwriting seems to  
322 be reliable from day to day for an individual. This result is reflected in the kinematic parameters  
323 for each test. When analyzing simple strokes through the theory, the parameters describing the  
324 action plan ( $t_0$ ,  $D$ ,  $\theta_s$  and  $\theta_e$ ) of the *agonist* system seem to be more reliable than for the  
325 *antagonist* (*e.g.*  $D$  *agonist* ICC=0.86,  $D$  *antagonist* ICC=0.70;  $|\cos(\theta_s)|$  *agonist* ICC=0.91,  
326  $|\cos(\theta_s)|$  *antagonist* ICC=0.00). The parameters of the *agonist* system are reliable as the strokes  
327 are equally oriented each time thanks to the guiding sheet. However, as determined by  
328 Plamondon and Djiova [35], glitches at the end of the movement, can change the velocity profile  
329 of the stroke. Those glitches do not occur in the main orientation of the movement, *i.e.* the  
330 *agonist* system, and can therefore enlarge the variability of the *antagonist* system. Even if  
331 glitches were partly rejected during the data processing, they could have still influenced the  
332 reliability of the *antagonist* parameters and also explain the poor ICC value of  $\mu$  *antagonist*. A  
333 detailed comparison with a Delta-Lognormal extraction (*i.e.* simple strokes defined only by two  
334 Lognormals) could help to determine the most appropriate and accurate extraction method for  
335 simple strokes [51]. When analyzing more complex movements, such as the triangles or the  
336 oscillations, a good reliability is also denoted in general. Except for the logresponse time  $\sigma$  in the  
337 oscillations, the intrinsic parameters of a lognormal ( $t_0$  or  $\Delta(t_0)$ ,  $D$ ,  $\mu$ ,  $\sigma$ ) are reliable from day to  
338 day. In fact their ICC values may be lowered by the very low inter-participant variability, as

339 explained in Weir [7]. This explanation could also be relevant for the *SNR*, which has a poor ICC  
340 for every test. As a stopping criterion for the reconstruction program Script Studio is for the *SNR*  
341 to attain 25dB, the *SNR/NbLog* should be analyzed instead when evaluating the motor control  
342 quality [25, 52]. The triangles, which are more complex tests than simple strokes and oscillations,  
343 may be more reliable for the assessment of fine motor control quality because the inter-session  
344 learning effect is smaller, as mentioned in Smits, Tolonen, Cluitmans, van Gils, Zietsma, Tijssen  
345 and Maurits [49]. The Sigma-Lognormal model seems to reconstruct the data similarly each time  
346 it is deployed, whether for a simple stroke or a complex movement, leading to parameters with  
347 sufficient reliability.

#### 348 4.2. *The setup as a new clinical tool for the detection of shoulder fatigue*

349 The vertical setup was specific to shoulder neuromuscular fatigue detection [20, 21] and its  
350 clinical relevance still needs to be assessed. As explained in Van den Bruel, Cleemput,  
351 Aertgeerts, Ramaekers and Buntinx [5], any tool being used to assess neuromuscular fatigue  
352 clinically needs to be easily implementable with quickly accessible data. The tablet linked to the  
353 computer offers numerous advantages as the whole process is integrated [53]. However, triangles  
354 had to be manually verified, because some reconstructions presented inaccuracies in their  
355 trajectory. As Script Studio optimizes the reconstruction on the velocity profile, a trajectory offset  
356 can be observed [34, 54]. The use of “iDeLog”, a new algorithm that optimizes parameters based  
357 on both speed and trajectory may avoid outliers and speed up the data formatting process [40].  
358 This will be the subject of a follow-up study. Nevertheless, the simplicity of the use of the tablet  
359 and the possibility of improvements in algorithm optimization leads us to believe that the setup  
360 will soon be capable of meeting the requirements for clinical implementation.

361 In addition to this, clinical guidelines require data to be reliable with high sensitivity and  
362 specificity [6]. As shown in Laurent, Plamondon and Begon [20], the *mode*, *median* and *time*  
363 *delay* present the most significant differences pre and post shoulder fatigue in internal and  
364 external rotation. Their reliability on all tests was good to excellent, ranging from 0.77 to 0.90. In  
365 comparison, goniometers and inclinometers, have a reliability ranging from moderate to excellent  
366 in external and internal rotation (goniometer: ICC from 0.64 to 0.91, inclinometer: ICC from 0.63  
367 to 0.97) [55, 56]. The latter are tools that are currently used in clinics for the evaluation of the  
368 articular amplitude, which may be used as to assess shoulder neuromuscular disorders [57].

369 These disorders can also be assessed with a muscular force evaluation. To that extent, stationary  
370 dynamometers have high reliability with ICC ranging from 0.87 to 0.94 [58]. However the  
371 minimal detectable changes (MDC) were not reported [58, 59], or had high values (21 to 43%  
372 MDC) [60] limiting their assessment of sensitivity to changes. In our study, the MDC were  
373 higher than the mean difference pre and post fatigue [20]. However, the effect sizes of the pre and  
374 post fatigue differences always ranged from moderate to good, indicating that the observed  
375 phenomenon of variation was high and that a clinically relevant change has still occurred. The  
376 MDC might be too severe in the assessment of the sensitivity to changes in our study. Further  
377 studies need to be undertaken to specify the sensitivity and specificity after internal and external  
378 rotation fatigue using Kinematic Theory. For clinical requirements, these values tend to have to  
379 be excellent, as in medical imaging (sensitivity and specificity > 0.85) [61, 62]. Otherwise, a  
380 combination of several tests with different values of sensitivity and specificity is also possible, as  
381 is done with physical tests [63, 64]. Tests with a high sensitivity will correctly identify persons  
382 who have a pathology, while tests with a high specificity will correctly reject those without the  
383 pathology [65]. The theory is reliable from day to day and its use in shoulder fatigue detection  
384 could be clinically relevant, when sensitivity and specificity are assessed.

#### 385 *4.3. Further clinical applications*

386 Kinematic Theory has been used in many applications for motor control evaluation. A tablet is an  
387 ergonomic and standardized method [53], which has already shown many interesting results in  
388 studies such as Parkinson's disease [22], concussion [23], attention deficit hyperactivity disorder  
389 [24], aging phenomena [25], stroke risk factors [26]. Contrary to the present study, these data  
390 were recorded on a setup horizontally oriented, with sitting participants. Another study from  
391 Fischer, Plamondon, O'Reilly and Savaria [66] reconstructed handwriting from a whiteboard, in a  
392 vertical orientation. Portnoy, Rosenberg, Alazraki, Elyakim and Friedman [67] postulated that  
393 whether on a vertical or horizontal surface, the graphic product performance level during  
394 handwriting will not be affected. However, without efficient support from the table as in a  
395 horizontal set-up, upper-limb muscles have higher amplitude activation [68, 69]. Moreover, the  
396 handwriting kinematics on horizontal surfaces seems more fluid than on vertical surfaces [70]. A  
397 better reliability may thus be expected on horizontal surfaces with sitting participants than on  
398 vertical surfaces with standing participants. As simple strokes and more complex tasks (*i.e.*

399 triangles and oscillations) were reliable after the Sigma-Lognormal model analysis, it can be  
400 expected that the parameters extracted from any kind of well-specified movement are reliable  
401 from one day to another.

#### 402 4.4. Limitations

403 A first limitation to our study is that participants were not constrained when executing their  
404 strokes. The distance between the participant and the tablet in-between days was not controlled in  
405 this study. Although differences in posture might affect the kinematics, forcing a given posture  
406 might have created biases in the results of some participants who might have been obligated to  
407 use strategies that were not optimal for them. We thus chose to prioritize a comfortable, self-  
408 selected posture, which is important during a clinical test involving maximal speed. As a result,  
409 different strategies were used by the individual participants, especially for the vertical  
410 oscillations. However, postural difference between test days for the participants could have  
411 affected the kinematics [71] and could therefore lead to decreased reliability in some tests,  
412 especially the vertical oscillations. A standardization of the distance between the participant and  
413 the tablet, and the standing posture could be means by which to increase the intra-participant  
414 reliability, but would add complexity to the setup for clinical testing. Further studies evaluating  
415 the parameters' reliability with comparison of self-selected *versus* controlled posture could help  
416 improve the reliability of handwriting tasks for clinical application. In addition, tiredness and  
417 boredom could be observed in such studies. As the model describes the neuromotor condition of  
418 the participant [33, 72], it could be of interest to add a fatigue scale or a subjective scale to know  
419 if the participants were tired [73]. Performing the study at the same moment of the day (whether  
420 always the morning or afternoon) could also heighten the reliability as handwriting speed could  
421 be affected by circadian variations [74]. The use of neurostimulants should also be documented,  
422 as they have an effect on fatigue [75]. Furthermore, a learning process can be observed between  
423 two sessions as the velocity in handwriting can be affected by familiarity and practice of the test  
424 [76]. Despite the training period at the beginning of each session, kinematic profiles appeared  
425 faster on the second day in our study, as in Smits, Tolonen, Cluitmans, van Gils, Zietsma, Tijssen  
426 and Maurits [49], and parameters for the second day showed more variability. To diminish the  
427 inter-session variability, additional training sessions could be assigned at least one day before the  
428 recording session. For clinical reasons, the same study should be performed on fatigued

429 participants. Despite the need for some improvements, the method in the present study seems  
430 appropriate for fatigue detection and with these improvements should be feasible for clinical use.

431 **5. Conclusion (89)**

432 Most of the parameters have good test-retest reliability in the four series of tests presented. Both  
433 agonist lognormals and more complex movements were modelled by parameters that presented  
434 high reliability. The *mode*, *median* and *time delay* had good to excellent reliability supporting  
435 their use in shoulder fatigue detection. However, the minimal detectable change may need to be  
436 refined. Nevertheless, the theory has many other applications and its use on a horizontal surface  
437 (*e.g.* in a sitting position) leads us to believe that the reliability of the data could be even better  
438 for other applications.

439

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445

446 **Competing interests**

447 The authors declare that the research was conducted in the absence of any commercial or  
448 financial relationships that could be construed as a potential competing interest. Any research  
449 group interested to extend this study by performing model comparison with their own software  
450 should contact the authors for planning a non-commercial collaboration.

451 **Author contribution**

452 **Anaïs Laurent:** Conceptualization, Methodology, Validation, Formal analysis, Investigation,  
453 Writing – Original Draft. **Réjean Plamondon and Mickaël Begon:** Conceptualization,  
454 Methodology, Supervision, Writing – Review & Editing.

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655

## Supplementary Material, Appendix A

**Equations 1 to 3:** Mathematical model of movement reconstruction according to Kinematic Theory.

$$\vec{v}(t) = \sum_{i=1}^N \vec{v}_i(t; t_{0i}, \mu_i, \sigma_i^2) = \sum_{i=1}^N \begin{bmatrix} \cos(\theta_i(t)) \\ \sin(\theta_i(t)) \end{bmatrix} v_i(t) \quad (1)$$

$$v_i(t) = D_i \Lambda_i(t; t_{0i}, \mu_i, \sigma_i^2) \quad (2)$$

$$= \frac{D_i}{\sigma_i(t - t_{0i})\sqrt{2\pi}} \exp\left(\frac{[\ln(t - t_{0i}) - \mu_i]^2}{-2\sigma_i^2}\right)$$

where

$$\theta_i(t) = \theta_{si} + \frac{(\theta_{ei} - \theta_{si})}{D_i} \int_0^t v_i(\tau) d\tau \quad (3)$$

**Table A.1:** Resume of the **main parameters** extracted and their meaning

$t_0$	The time that it takes the brain to perceive the stimulus and emit the command to the musculoskeletal system. It refers to the moment when a population of neurons sends a motor command, and it occurs after the audible stimulus is perceived and the motor command prepared. From this parameter, we can calculate $\Delta(t_0)$ , which is the elapsed time between two successive $t_0$ . It reflects the rhythmicity of an input command, and is used in oscillation tasks only.
<b>D</b>	The distance covered by the resulting lognormal.
$\theta_s$	The starting angle of the lognormal.
$\theta_e$	The ending (terminal) angle of the lognormal.
$\mu$	Also known as the logtime delay, it represents the time taken to reach half of the distance movement on a logarithmic scale. It corresponds to the rapidity of the reaction to a command by a system.
$\sigma$	Also known as the logresponse time, it represents the time taken from the neuromuscular system to respond to a command on a logarithmic scale. It is also linked to the movement duration and is a measure of the asymmetry of the lognormal.
<b>Nblog</b>	The number of lognormals required to reconstruct the velocity profile of the movement.
<b>SNR</b>	A measure of the quality of the movement reconstruction.

**Table A.2:** Resume of the **derived parameters** extracted and their meaning

<b>Mode</b>	The time at which the maximum value of the lognormal impulse response is reached. $M = t_0 + e^{\mu - \sigma^2}$
<b>Median</b>	The time at which the half value of the integral under the lognormal curve (50% of the covered distance) is reached. $m = t_0 + e^{\mu}$
<b>Time delay</b>	The rapidity of the neuromuscular system in response to a command. $\bar{t} = t_0 + e^{\mu + 0.5\sigma^2}$
<b>Response time</b>	A measure of the spread of the impulse response. $s = (\bar{t} - t_0) \sqrt{(e^{\sigma^2} - 1)}$
<b>Asymmetry</b>	Characterizes the shape of the lognormal. $A_c = 1 - e^{-\sigma^2}$
<b>SNR/NbLog</b>	A performance criterion that represents the motor control fluency of a gesture. The lognormality principle predicts that the ideal movement converges toward a lognormal profile. When the <i>SNR/NbLog</i> is higher, the movement is more similar to the ideal one, as postulated by the lognormal behavior.
<b>Command propagation</b>	The duration of the command propagation. It represents the elapsed time between the emission of the command from the brain ( $t_0$ ) to the execution of the command, the reaction time ( <i>RT</i> ). In the present study, the reaction time was computed as the time required to reach 10% of the maximal velocity during the test. $CP = RT - t_0$

Note:  $\Delta(t_0)$  is used instead of  $t_0$  for the calculus in the oscillations

## Supplementary Material, Appendix B

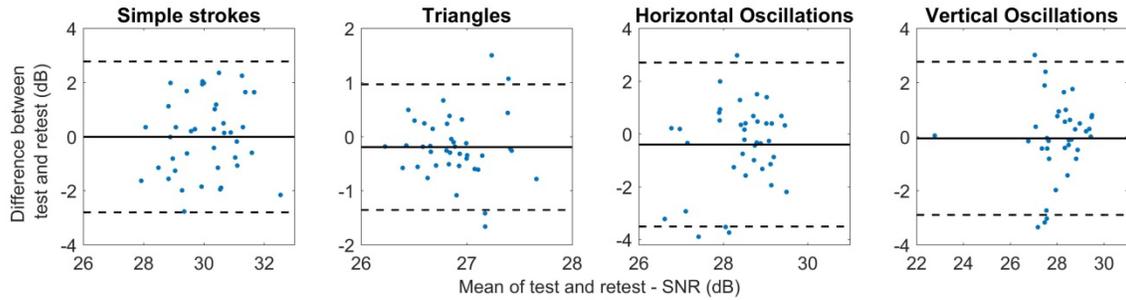


Figure B.1: Bland Altman plots of the SNR for simple strokes, triangles, horizontal and vertical oscillations with the mean difference (solid lines) and the limits of agreement (dotted lines).

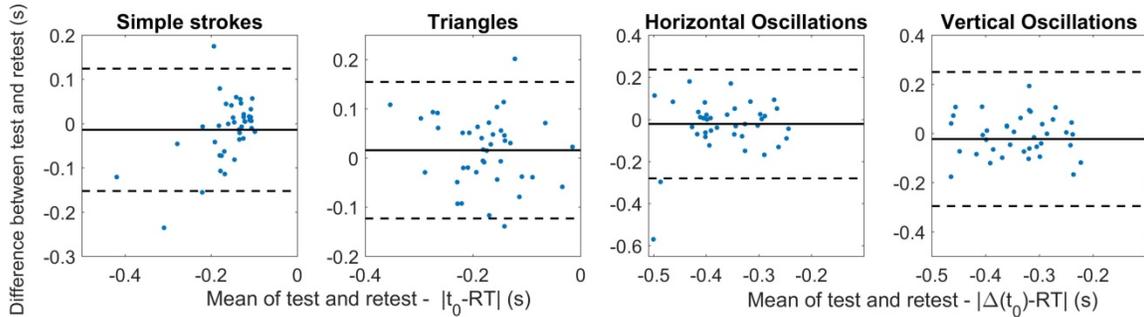


Figure B.1: Bland Altman plots of  $|t_0 - RT|$  for the simple strokes and triangles; and for  $|\Delta(t_0) - RT|$  for horizontal and vertical oscillations with the mean difference (solid lines) and the limits of agreement (dotted lines).

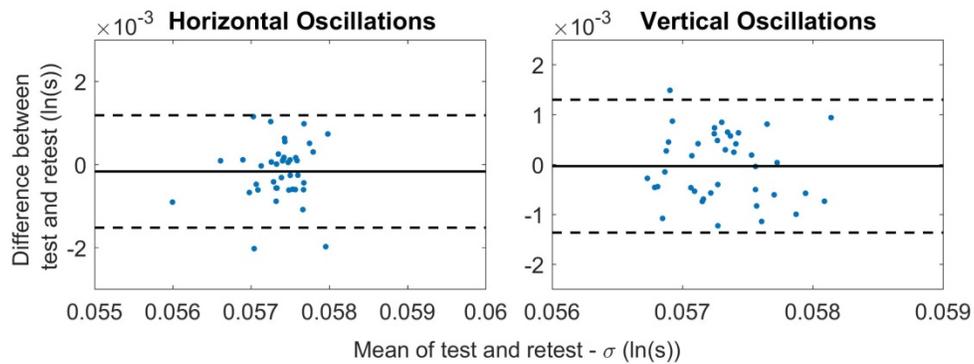


Figure B.2: Bland Altman plots of  $\sigma$  for the horizontal and vertical oscillations with the mean difference (solid lines) and the limits of agreement (dotted lines).

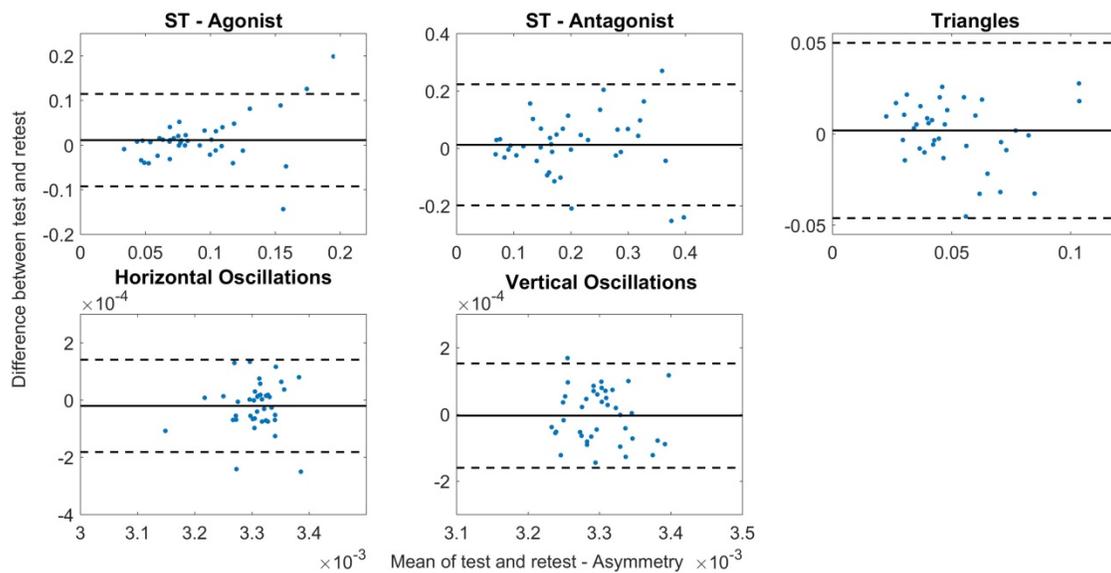


Figure B.3: Bland Altman plots of the asymmetry for the agonist and antagonist components of simple strokes (ST), triangles, horizontal and vertical oscillations with the mean difference (solid lines) and the limits of agreement (dotted lines).