

# A Hybrid Evolutionary Algorithm for Heterogeneous Fleet Vehicle Routing Problems with Time Windows

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## Abstract

This paper presents a hybrid evolutionary algorithm (HEA) to solve heterogeneous fleet vehicle routing problems with time windows. There are two main types of such problems, namely the Fleet Size and Mix Vehicle Routing Problem with Time Windows (F) and the Heterogeneous Fixed Fleet Vehicle Routing Problem with Time Windows (H), where the latter, in contrast to the former, assumes a limited availability of vehicles. The main objective is to minimize the fixed vehicle cost and the distribution cost, where the latter can be defined with respect to en-route time (T) or distance (D). The proposed unified algorithm is able to solve the four variants of heterogeneous fleet routing problem, called FT, FD, HT and HD, where the last variant is new. The HEA successfully combines several metaheuristics and offers a number of new advanced efficient procedures tailored to handle the heterogeneous fleet dimension. Extensive computational experiments on benchmark instances have shown that the HEA is highly effective on FT, FD and HT. In particular, out of the 360 instances we obtained 75 new best solutions and matched 102 within reasonable computational times. New benchmark results on HD are also presented.

*Keywords:* vehicle routing, time windows, heterogeneous fleet, genetic algorithm, neighborhood search

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## 1. Introduction

In heterogeneous fleet vehicle routing problems with time windows, one considers a fleet of vehicles with various capacities and vehicle-related costs, as well as a set of customers with known demands and time windows. These problems consist of determining a set of vehicle routes such that each customer is visited exactly once by a vehicle within a prespecified time window, all vehicles start and end their routes at a depot, and the load of each vehicle does not exceed its capacity. As is normally the case in vehicle routing problem with time windows (VRPTW), customer service must start within the time window, but the vehicle may wait at a customer location if it arrives before the beginning of the time window. There are two main categories of such problems, namely the Fleet Size and Mix Vehicle Routing Problem with Time Windows (F) and the Heterogeneous Fixed Fleet Vehicle Routing Problem with Time Windows (H). In category F, there is no limit in the number of available vehicles of each type, whereas such a limit exists in category H. Note that it is easy to find feasible solutions to the instances of category F since there always exists a feasible assignment of vehicles to routes. However, this is not always the case for the instances of category H.

Two measures are used to compute the total cost to be minimized. The first is the sum of the fixed vehicle cost and of the *en-route time* (T), which includes traveling time and possible waiting time at the customer locations before the opening of their time windows (we assume that travel time and cost are equivalent). In this case, service times are only used to check feasibility and for performing adjustments to the departure time from the depot in order to minimize pre-service waiting times. The second cost measure is based on *distance* (D) and consists of the fixed vehicle cost and the distance traveled by the vehicle, as is the case in the standard VRPTW (Solomon, 1987).

We differentiate between four variants defined with respect to the problem category and to the way in which the objective function is defined, namely FT, FD, HT and HD. The first variant is FT, described by Liu and Shen (1999b) and the second is FD, introduced by Bräysy et al. (2008). The third variant HT was defined and solved by Paraskevopoulos et al. (2008). Finally, HD is a new variant which we introduce in this paper. HD differs from HT

29 by considering the objective function  $D$  instead of  $T$ . This variant has never been studied  
30 before.

31 Hoff et al. (2010) and Belfiore and Yoshizaki (2009) describe several industrial aspects and  
32 practical applications of heterogeneous vehicle routing problems. The most studied versions  
33 are the fleet size and mix vehicle routing problem, described by Golden et al. (1984), which  
34 considers an unlimited heterogeneous fleet, and the heterogeneous fixed fleet vehicle routing  
35 problem, proposed by Taillard (1999). For further details, the reader is referred to the  
36 surveys of Baldacci et al. (2008) and of Baldacci and Mingozzi (2009).

37 The FT variant has several extensions, e.g., multiple depots (Dondo et al., 2007; Bet-  
38 tinelli et al., 2011), overloads (Kritikos and Ioannou, 2013), and split deliveries (Belfiore  
39 and Yoshizaki, 2009, 2013). There exist several exact algorithms for the capacitated vehicle  
40 routing problem (VRP) (Toth and Vigo, 2002; Baldacci et al., 2010), and for the hetero-  
41 geneous VRP (Baldacci and Mingozzi, 2009). However, to the best of our knowledge, no  
42 exact algorithm has been proposed for the heterogeneous VRP with time windows, i.e., FT,  
43 FD and HT. The existing heuristic algorithms for these three variants are briefly described  
44 below.

45 Liu and Shen (1999b) proposed a heuristic for FT which starts by determining an initial  
46 solution through an adaptation of the Clarke and Wright (1964) savings algorithm, previ-  
47 ously presented by Golden et al. (1984). The second stage improves the initial solution by  
48 moving customers by means of parallel insertions. The algorithm was tested on a set of 168  
49 benchmark instances derived from the set of Solomon (1987) for the VRPTW. Dullaert et  
50 al. (2002) described a sequential construction algorithm for FT, which is an extension of the  
51 insertion heuristic of Golden et al. (1984). Dell'Amico et al. (2007) described a multi-start  
52 parallel regret construction heuristic for FT, which is embedded into a ruin and recreate  
53 metaheuristic. Bräysy et al. (2008) presented a deterministic annealing metaheuristic for  
54 FT and FD. In a later study, Bräysy et al. (2009) described a hybrid metaheuristic al-  
55 gorithm for large scale FD instances. Their algorithm combines the well-known threshold  
56 acceptance heuristic with a guided local search metaheuristic having several search limitation  
57 strategies. An adaptive memory programming algorithm was proposed by Repoussis and

58 Tarantilis (2010) for FT, which combines a probabilistic semi-parallel construction heuristic,  
59 a reconstruction mechanism and a tabu search algorithm. Computational results indicate  
60 that their method is highly successful and improves many best known solutions. In a re-  
61 cent study, Vidal et al. (2014) introduced a genetic algorithm based on a unified solution  
62 framework for different variants of the VRPs, including FT and FD. To our knowledge,  
63 Paraskevopoulos et al. (2008) are the only authors who have studied HT. Their two-phase  
64 solution methodology is based on a hybridized tabu search algorithm capable of solving both  
65 FT and HT.

66 This brief review shows that the two problem categories F and H have already been  
67 solved independently through different methodologies. We believe there exists merit for the  
68 development of a unified algorithm capable of efficiently solving the two problem categories.  
69 This is the main motivation behind this paper.

70 This paper makes three main scientific contributions. First, we develop a unified hybrid  
71 evolutionary algorithm (HEA) capable of handling the four variants of the problem. The  
72 HEA combines two state-of-the-art metaheuristic concepts which have proved highly suc-  
73 cessful on a variety of VRPs: Adaptive Large Neighborhood Search (ALNS) (see Ropke and  
74 Pisinger, 2006a; Pisinger and Ropke, 2007; Demir et al., 2012) and population based search  
75 (see Prins, 2004; Vidal et al., 2014). The second contribution is the introduction of sev-  
76 eral algorithmic improvements to the procedures developed by Prins (2009) and Vidal et al.  
77 (2012). We use a ALNS equipped with a range of operators as the main EDUCATION proce-  
78 dure within the search. We also propose an advanced version of the SPLIT algorithm of Prins  
79 (2009) capable of handling infeasibilities. Finally, we introduce an innovative aggressive IN-  
80 TENSIFICATION procedure on elite solutions, as well as a new diversification scheme through  
81 the REGENERATION and the MUTATION procedures of solutions. The third contribution is  
82 to introduce HD as a new problem variant.

83 The remainder of this paper is structured as follows. Section 2 presents a detailed descrip-  
84 tion of the HEA. Computational experiments are presented in Section 3, and conclusions  
85 are provided in Section 4.

## 2. Description of the Hybrid Evolutionary Algorithm

We start by introducing the notation related to FT, FD, HT and HD. All problems are defined on a complete graph  $G = (N, A)$ , where  $N = \{0, \dots, n\}$  is the set of nodes, and node 0 corresponds to the depot. Let  $A = \{(i, j) : 0 \leq i, j \leq n, i \neq j\}$  denote the set of arcs. The distance from  $i$  to  $j$  is denoted by  $d_{ij}$ . The customer set is  $N_c$  in which each customer  $i$  has a demand  $q_i$  and a service time  $s_i$ , which must start within time window  $[a_i, b_i]$ . If a vehicle arrives at customer  $i$  before  $a_i$ , it then waits until  $a_i$ . Let  $K = \{1, \dots, k\}$  be the set of available vehicle types. Let  $e_k$  and  $Q_k$  denote the fixed vehicle cost and the capacity of vehicle type  $k$ , respectively. The travel time from  $i$  to  $j$  is denoted by  $t_{ij}$  and is independent of the vehicle type. The distribution cost from  $i$  to  $j$  associated with a vehicle of type  $k$  is  $c_{ij}^k$  for all problem types. In HT and HD, the available number of vehicles of type  $k \in K$  is  $n_k$ , whereas the constant can be set to an arbitrary large value for problems FT and FD. The objectives are as discussed in the Introduction.

The remainder of this section introduces the main components of the HEA. A general overview of the HEA is given in Section 2.1. More specifically, Section 2.2 presents the offspring EDUCATION procedure. Section 2.3 presents the initialization of the population. The selection of parent solutions, the ordered crossover operator and the advanced algorithm SPLIT are described in Sections 2.4, 2.5 and 2.6, respectively. Section 2.7 presents the INTENSIFICATION procedure. The survivor selection mechanism is detailed in Section 2.8. Finally, the diversification stage, including the REGENERATION and MUTATION procedures, is described in Section 2.9.

### 2.1. Overview of the Hybrid Evolutionary Algorithm

The general structure of the HEA is presented in Algorithm 1. The modified version of the classical Clarke and Wright savings algorithm and the ALNS operators are combined to generate the initial population (Line 1). Two parents are selected (Line 3) through a binary tournament, following which the crossover operation (Line 4) generates a new offspring  $C$ . The advanced SPLIT algorithm is applied to the offspring  $C$  (Line 5), which optimally segments the giant tour by choosing the vehicle type for each route. The EDUCATION

114 procedure (Line 6) uses the ALNS operators to educate offspring  $C$  and inserts it back into  
 115 the population. If  $C$  is infeasible, the EDUCATION procedure is iteratively applied until a  
 116 modified version of  $C$  is feasible, which is then inserted into the population.

117 The probabilities associated with the operators used in the EDUCATION procedure and  
 118 the penalty parameters are updated by means of an adaptive weight adjustment procedure  
 119 (AWAP) (Line 7). Elite solutions are put through an aggressive INTENSIFICATION proce-  
 120 dure, based on the ALNS algorithm (Line 8) in order to improve their quality. If, at any  
 121 iteration, the population size  $n_a$  reaches  $n_p + n_o$ , then a survivor selection mechanism is  
 122 applied (Line 9). The population size, shown by  $n_a$ , changes during the algorithm as new  
 123 offsprings are added, but is limited by  $n_p + n_o$ , where  $n_p$  is a constant denoting the size of  
 124 the population initialized at the beginning of the algorithm and  $n_o$  is a constant showing the  
 125 maximum allowable number of offsprings that can be inserted into the population. At each  
 126 iteration of the algorithm, MUTATION is applied to a randomly selected individual from the  
 127 population with probability  $p_m$ . If there are no improvements in the best known solution for  
 128 a number of consecutive iterations  $it_r$ , the entire population undergoes a REGENERATION  
 129 (Line 10). The HEA terminates when the number of iterations without improvement  $it_t$  is  
 130 reached (Line 11).

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**Algorithm 1** The general framework of the HEA

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- 1: *Initialization*: initialize a population with size  $n_p$
  - 2: **while** number of iterations without improvement  $< it_t$  **do**
  - 3:     *Parent selection*: select parent solutions  $P_1$  and  $P_2$
  - 4:     *Crossover*: generate offspring  $C$  from  $P_1$  and  $P_2$
  - 5:     SPLIT: partition  $C$  into routes
  - 6:     EDUCATION: educate  $C$  with ALNS and insert into population
  - 7:     AWAP: update probabilities of the ALNS operators
  - 8:     INTENSIFICATION: intensify elite solution with ALNS
  - 9:     *Survivor selection*: if the population size  $n_a$  reaches  $n_p + n_o$ , then select survivors
  - 10:    *Diversification*: diversify the population with MUTATION or REGENERATION proce-  
       dures
  - 11: **end while**
  - 12: Return best feasible solution
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131 2.2. EDUCATION

132 The EDUCATION procedure is systematically applied to each offspring in order to improve  
 133 its quality. The ALNS algorithm is used as a way of educating the solutions in the HEA. This  
 134 is achieved by applying both the destroy and repair operators, and a number of removable  
 135 nodes are modified in each iteration. An example of the removal and insertion phases is  
 136 illustrated in Figure 1. The operators used within the HEA are either adapted or inspired  
 137 from those employed by various authors (Ropke and Pisinger, 2006a,b; Pisinger and Ropke,  
 138 2007; Demir et al., 2012; Paraskevopoulos et al., 2008).

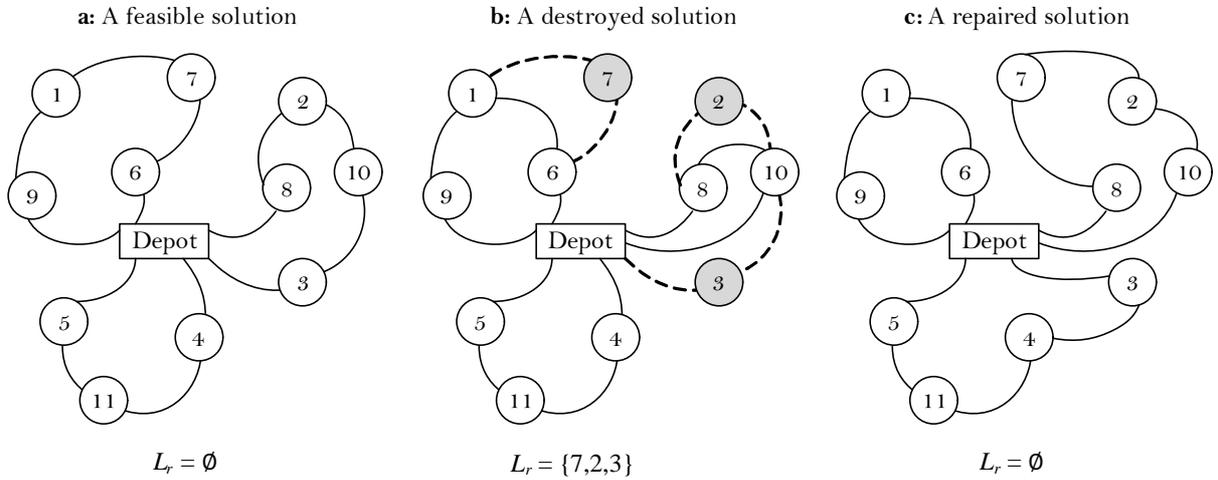


Figure 1: Illustration of the EDUCATION procedure

139 The EDUCATION procedure is detailed in Algorithm 2. All operators are repeated  $O(n)$   
 140 times and the complexity given are the overall repeats. The removal procedure (line 4 of  
 141 Algorithm 2) runs for  $n'$  iterations, removes  $n'$  customers from the solution and add to the  
 142 removal list  $L_r$ , where  $n'$  is in the interval of removable nodes  $[b_l^e, b_u^e]$ . An insertion operator  
 143 is then selected to iteratively insert the nodes, starting from the first customer of  $L_r$ , into  
 144 the partially destroyed solution until  $L_r$  is empty (line 5). The feasibility conditions in terms  
 145 of capacity and time windows for FT, FD, HT and HD, and in terms of fleet size for HT  
 146 and HD, are always respected during the insertion process. We do not allow overcapacity  
 147 of the vehicle and service start outside the time windows for all problem types, and we also  
 148 do not allow the use of additional vehicles beyond the fixed fleet size for HT and HD. The

149 removal and insertion operators are randomly selected according to their past performance  
150 and a certain probability as explained further in Section 2.2.3. The cost of an individual  $C$   
151 before the removal is denoted by  $\omega(C)$ , and its cost after the insertion is denoted by  $\omega(C^*)$ .

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**Algorithm 2** EDUCATION

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1:  $\omega(C^*) = 0$ , iteration = 0
2: while there is no improvement and  $C$  is feasible do
3:    $L_r = \emptyset$  and select a removal operator
4:   Apply a removal operator to the individual  $C$  to remove a set of nodes and add them
   to  $L_r$ 
5:   Select an insertion operator and apply it to the partially destroyed individual  $C$  to
   insert the nodes of  $L_r$ 
6:   Let  $C^*$  be the new solution obtained by applying insertion operator
7:   if  $\omega(C^*) < \omega(C)$  and  $C^*$  is feasible then
8:      $\omega(C) \leftarrow \omega(C^*)$ 
9:   iteration  $\leftarrow$  iteration + 1
10: end while
11: Return educated feasible solution

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152 The heterogeneous fleet version of the ALNS that we use here was recently introduced  
153 by Koç et al. (2014). It educates solutions by considering the heterogeneous fleet aspect.  
154 The ALNS integrates fleet sizing within the destroy and repair operators. In particular, if  
155 a node is removed, we check whether the resulting route can be served by a smaller vehicle.  
156 We then update the solution accordingly. If inserting a node requires additional vehicle  
157 capacity we then consider the option of using larger vehicles. For each node  $i \in N_c \setminus L_r$ , let  
158  $f^h(i)$  be the current vehicle fixed cost associated with the vehicle serving  $i$ . Let  $\Delta(i)$  be the  
159 saving obtained as a result of using a removal operator on node  $i$  without considering the  
160 vehicle fixed cost. Let  $f_1^{h*}(i)$  be the vehicle fixed cost after removal of node  $i$ . Consequently,  
161  $f_1^{h*}(i) < f^h(i)$  only if the route containing node  $i$  can be served by a smaller vehicle when  
162 removing node  $i$ . The savings in vehicle fixed cost can be expressed as  $f^h(i) - f_1^{h*}(i)$ ,  
163 respectively. Thus, for each removal operator, the total savings of removing node  $i \in N_c \setminus L_r$ ,  
164 denoted  $RC(i)$ , is calculated as follows:

$$RC(i) = \Delta(i) + (f^h(i) - f_1^{h*}(i)). \quad (1)$$

165 In a destroyed solution, the insertion cost of node  $j \in L_r$  after node  $i$  is defined as  $\Omega(i, j)$   
166 for a given node  $i \in N_c \setminus L_r$ . Let  $f_2^{h*}(i)$  be the vehicle fixed cost after the insertion of node  
167  $i$ , i.e.,  $f_a^{h*} > f^h$  only if the route containing node  $i$  necessitates the use of a larger capacity  
168 vehicle after inserting node  $i$ . The cost differences in vehicle fixed cost can be expressed as  
169  $f_2^{h*}(i) - f^h(i)$ . Thus, the total insertion cost of node  $i \in N_c \setminus L_r$ , for each insertion operator  
170 is

$$IC(i) = \Omega(i, j) + (f_2^{h*}(i) - f^h(i)). \quad (2)$$

### 171 2.2.1. Removal Operators

172 Nine removal operators are used in the destroy phase of the EDUCATION procedure and  
173 are described in detail below.

174 1. *Random removal* (RR): The RR operator randomly selects a node  $j \in N \setminus \{0\} \setminus L_r$ ,  
175 removes it from the solution. The worst-case time complexity of the RR operator is  $O(n)$ .

176 2. *Worst distance removal* (WDR): The purpose of the WDR operator is to choose a  
177 number of expensive nodes according to their distance based cost. The cost of a node  $j \in$   
178  $N \setminus \{0\} \setminus L_r$  is the distance from its predecessor  $i$  and its distance to its successor  $k$ . The WDR  
179 operator iteratively removes nodes  $j^*$  from the solution where  $j^* = \arg \max_{j \in N \setminus \{0\} \setminus L_r} \{d_{ij} +$   
180  $d_{jk} + f^h(i) - f_1^{h*}(i)\}$ . The time complexity of this operator is  $O(n^2)$ .

181 3. *Worst time removal* (WTR): The WTR operator is a variant of the WDR operator.  
182 For each node  $j \in N \setminus \{0\} \setminus L_r$  costs are calculated, depending on the deviation between the  
183 arrival time  $z_j$  and the beginning of the time window  $a_j$ . The WTR operator iteratively  
184 removes customers from the solution, where  $j^* = \arg \max_{j \in N \setminus \{0\} \setminus L_r} \{|z_j - a_j| + f^h(i) - f_1^{h*}(i)\}$ .  
185 The ALNS iteratively applies this process to the solution after each removal. The WTR  
186 operator can be implemented in  $O(n^2)$  time.

187 4. *Neighborhood removal* (NR): In a given solution with a set  $\mathfrak{R}$  of routes, the NR operator  
188 calculates an average distance  $\bar{d}(R) = \sum_{(i,j) \in R} d_{ij} / |R|$  for each route  $R \in \mathfrak{R}$ , and selects a  
189 node  $j^* = \arg \max_{(R \in \mathfrak{R}; j \in R)} \{\bar{d}(R) - d_{R \setminus \{j\}} + f^h(i) - f_1^{h*}(i)\}$ , where  $d_{R \setminus \{j\}}$  denotes the average  
190 distance of route  $R$  excluding node  $j$ . The time complexity of this operator is  $O(n^2)$ .

191 5. *Shaw removal* (SR): The general idea behind the SR operator, which was introduced

192 by Shaw (1998), is to remove a set of customers that are related in a predefined way and  
 193 are therefore easy to change. The SR operator removes a set of  $n'$  similar customers. The  
 194 similarity between two customers  $i$  and  $j$  is defined by the relatedness measure  $\delta(i, j)$ . This  
 195 includes four terms: a distance term  $d_{ij}$ , a time term  $|a_i - a_j|$ , a relation term  $l_{ij}$ , which is  
 196 equal to  $-1$  if  $i$  and  $j$  are in the same route, and  $1$  otherwise, and a demand term  $|q_i - q_j|$ .  
 197 The relatedness measure is given by

$$\delta(i, j) = \varphi_1 d_{ij} + \varphi_2 |a_i - a_j| + \varphi_3 l_{ij} + \varphi_4 |q_i - q_j|, \quad (3)$$

198 where  $\varphi_1$  to  $\varphi_4$  are weights that are normalized to find the best candidate solution. The  
 199 operator starts by randomly selecting a node  $i \in N \setminus \{0\} \setminus L_r$ , and selects the node  $j^*$  to  
 200 remove where  $j^* = \arg \min_{j \in N \setminus \{0\} \setminus L_r} \{\delta(i, j) + f^h(i) - f_1^{h^*}(i)\}$ . The operator is iteratively  
 201 applied to select a node which is most similar to the one last added to  $L_r$ . The time  
 202 complexity of this operator is  $O(n^2)$ .

203 6. *Proximity-based removal* (PBR): This operator is a second variant of the classical  
 204 Shaw removal operator. The selection criterion of a set of routes is solely based on the  
 205 distance. Therefore, the weights are  $\varphi_1 = 1$  and  $\varphi_2 = \varphi_3 = \varphi_4 = 0$ . The PBR operator can  
 206 be implemented in  $O(n^2)$  time.

207 7. *Time-based removal* (TBR): The TBR operator removes a set of nodes that are  
 208 related in terms of time. It is a special case of the Shaw removal operator where  $\varphi_2 = 1$  and  
 209  $\varphi_1 = \varphi_3 = \varphi_4 = 0$ . Its time complexity is  $O(n^2)$ .

210 8. *Demand-based removal* (DBR): The DBR operator is yet another variant of the Shaw  
 211 removal operator with  $\varphi_4 = 1$  and  $\varphi_1 = \varphi_2 = \varphi_3 = 0$ . It can be implemented in  $O(n^2)$  time.

212 9. *Average cost per unit removal* (ACUTR): The average cost per unit (ACUT) is  
 213 described by Paraskevopoulos et al. (2008) to measure the utilization efficiency of a vehicle  
 214  $\Pi(R)$  on a given route  $R$ .  $\Pi(R)$  is expressed as the ratio of the total travel cost and fixed  
 215 vehicle cost over the total demand carried by a vehicle  $k$  traversing route  $R$ :

$$\Pi(R) = \frac{\sum_{(i,j) \in A} c_{ij} x_{ij}^k + e^k}{\sum_{i \in N \setminus \{0\}} q_i x_{ij}^k}. \quad (4)$$

216 The aim of the ACUTR operator is to calculate the cost of each route and remove the one  
 217 with the least  $\Pi(R)$  value from the solution. The ACUTR operator can be implemented in  
 218  $O(n^2)$  time.

### 219 2.2.2. Insertion Operators

220 Three insertion operators are used in the repair phase of the EDUCATION procedure.

221 1. *Greedy insertion* (GI): The aim of this operator is to find the best possible insertion  
 222 position for all nodes in  $L_r$ . For node  $i \in N \setminus L_r$  succeeded in the destroyed solution by  
 223  $k \in N \setminus \{0\} \setminus L_r$ , and node  $j \in L_r$  we define  $\gamma(i, j) = d_{ij} + d_{jk} - d_{ik}$ . We find the least-cost  
 224 insertion position for  $j \in L_r$  by  $i^* = \arg \min_{i \in N \setminus L_r} \{\gamma(i, j) + f_2^{h^*}(i) - f^h(i)\}$ . This process  
 225 is iteratively applied to all nodes in  $L_r$ . The time complexity of this operator is  $O(n^2)$ .

226 2. *Greedy insertion with noise function* (GINF): The GINF operator is based on the GI  
 227 operator but extends it by allowing a degree of freedom in selecting the best place for a  
 228 node. This is done by calculating the noise cost  $v(i, j) = \gamma(i, j) + f_2^{h^*}(i) - f^h(i) + d_{max}p_n\epsilon$   
 229 where  $d_{max}$  is the maximum distance between all nodes,  $p_n$  is a noise parameter used for  
 230 diversification and is set equal to 0.1, and  $\epsilon$  is a random number in  $[-1, 1]$ . The time  
 231 complexity of this operator is  $O(n^2)$ .

232 3. *Greedy insertion with en-route time* (GIET): This operator calculates the *en-route*  
 233 time difference  $\eta(i, j)$  between before and after inserting the customer  $j \in L_r$ . For node  
 234  $i \in N \setminus L_r$  succeeded in the destroyed solution by  $k \in N \setminus \{0\} \setminus L_r$ , and node  $j \in L_r$ , we define  
 235  $\eta(i, j) = \tau_{ij} + \tau_{jk} - \tau_{ik}$  where  $\tau_{ij}$  is the *en-route* time from node  $i$  to node  $j$ . We find the  
 236 least-cost insertion position for  $j \in L_r$  by  $i^* = \arg \min_{i \in N \setminus L_r} \{\eta(i, j) + f_2^{h^*}(i) - f^h(i)\}$ . The  
 237 GIET operator can be implemented in  $O(n^2)$  time.

### 238 2.2.3. Adaptive Weight Adjustment Procedure

239 Each removal and insertion operator has a certain probability of being chosen in every  
 240 iteration. The selection criterion is based on the historical performance of every operator and  
 241 is calibrated by a roulette-wheel mechanism (Ropke and Pisinger, 2006a; Demir et al., 2012).  
 242 After  $it_w$  iterations of the roulette wheel segmentation, the probability of each operator is  
 243 recalculated according to its total score. Initially, the probabilities of each removal and

244 insertion operator are equal. Let  $p_i^t$  be the probability of operator  $i$  in the last  $it_w$  iterations,  
 245  $p_i^{t+1} = p_i^t(1 - r_p) + r_p\pi_i/\tau_i$ , where  $r_p$  is the roulette wheel probability, for operator  $i$ ;  $\pi_i$  is its  
 246 score and  $\tau_i$  is the number times it was used during the last segment. At the start of each  
 247 segment, the scores of all operators are set to zero. The scores are changed by  $\sigma_1$  if a new  
 248 best solution is found, by  $\sigma_2$  if the new solution is better than the current solution and by  
 249  $\sigma_3$  if the new solution is worse than the current solution.

### 250 2.3. Initialization

251 The procedure used to generate the initial population is based on a modified version  
 252 of the Clarke and Wright and ALNS algorithms. An initial individual solution is obtained  
 253 by applying Clarke and Wright algorithm and by selecting the largest vehicle type for each  
 254 route. Then, until the initial population size reaches  $n_p$ , new individuals are created by  
 255 applying to the initial solution operators based on random removals and greedy insertions  
 256 with a noise function (see Section 2.2). We have selected these two operators in order to  
 257 diversify the initial population. The number of nodes removed is randomly chosen from the  
 258 initialization interval  $[b_l^i, b_u^i]$ , which is defined by a lower and an upper bound calculated as  
 259 a percentage of the total number of nodes in an instance.

### 260 2.4. Parent Selection

261 In evolutionary algorithms, the evaluation function of individuals is often based on the  
 262 solution cost. However, this kind of evaluation, does not take into account other important  
 263 factors such as the diversity of the population which plays a critical role. Vidal et al. (2012)  
 264 proposed a new method, named *biased fitness*  $bf(C)$ , to tackle this issue. This method  
 265 considers the cost of an individual  $C$ , as well as its *diversity contribution*  $dc(C)$  to the  
 266 population. This function is continuously updated and is used to measure the quality of  
 267 individuals during selection phases. The  $dc(C)$  is defined as

$$dc(C) = \frac{1}{n_c} \sum_{C' \in N_c} \beta(C, C'), \quad (5)$$

268 where  $N_c$  is the set of the  $n_c$  closest neighbours of  $C$  in the population. Thus,  $dc(C)$  calculates  
 269 the average distance between  $C$  and its neighbours in  $N_c$ . The distance between two parents  
 270  $\beta(C, C')$  is the number of pairs of adjacent requests in  $C$  which are no longer adjacent,  
 271 (called broken), in  $C'$ . For example, let  $C = \{4, 5, 6, 7, 8, 9, 10\}$  and  $C' = \{10, 7, 8, 9, 5, 6, 4\}$ ,  
 272 in  $C'$  the pairs  $\{4, 5\}$ ,  $\{6, 7\}$  and  $\{9, 10\}$  are broken and  $\beta(C, C') = 3$ . The algorithm selects  
 273 the broken pairs distance (see Prins, 2009) to compute the distance  $\beta$ . The main idea behind  
 274  $dc(C)$  is to assess the differences between individuals.

275 The evaluation function of an individual  $C$  in a population is

$$bf(C) = r_c(C) + (1 - \frac{n_e}{n_a})r_{dc}(C), \quad (6)$$

276 which is based on the rank  $r_c(C)$  of solution cost, and on the rank  $r_{dc}(C)$  of the *diversity*  
 277 *contribution*. The rank  $r_{dc}(C)$  is based on the diversity contribution calculated in equation  
 278 (5), according to which the solutions are ranked in decreasing order of their  $dc(C)$  value. In  
 279 (6),  $n_e$  is the number of elite individuals and  $n_a$  is the current number of individuals.

280 The HEA selects two parents through a binary tournament to yield an offspring. The  
 281 selection process randomly chooses two individuals from the population and keeps the one  
 282 having the best biased fitness.

## 283 2.5. Crossover

284 Following the parent selection phase, two parents undergo the classical ORDERED CROSSOVER  
 285 or OX without trip delimiters. The OX operator is well suited for cyclic permutations, and  
 286 the giant tour encoding allows recycling crossovers designed for the traveling salesman prob-  
 287 lem (TSP) (see Prins, 2004, 2009). Initially, two positions  $i$  and  $j$  are randomly selected in  
 288 the first parent  $P_1$ . Subsequently, the substring  $(i, \dots, j)$  is copied into the first offspring  $O_1$ ,  
 289 at the same positions. The second parent  $P_2$  is then swept cyclically from position  $j + 1$   
 290 onwards to fill the empty positions in  $O_1$ . The second offspring  $O_2$  is generated likewise by  
 291 exchanging the roles of  $P_1$  and  $P_2$ . In the original version of OX, two offsprings are obtained.  
 292 However in the HEA, we only randomly select one offspring.

293 *2.6. SPLIT Algorithm*

294 This algorithm is a tour splitting procedure which optimally partitions a solution into  
 295 feasible routes. Each solution is a permutation of customers without trip delimiters and  
 296 can therefore be viewed as a giant TSP tour for a vehicle with a large enough capacity.  
 297 This algorithm was successfully applied in evolutionary based algorithms for several routing  
 298 problems (Prins, 2004, 2009; Vidal et al., 2012, 2013).

299 We propose an advanced tour splitting procedure, denoted by SPLIT, which is embedded  
 300 in the HEA to segment a giant tour and to determine the fleet mix composition. This is  
 301 achieved through a controlled exploration of infeasible solutions (see Cordeau et al., 2001  
 302 and Nagata et al., 2010), by relaxing the limits on time windows and vehicle capacities. Vi-  
 303 olations of these limits are penalized through an objective function containing extra terms  
 304 to account for infeasibilities. This is in contrast to Prins (2009) who does not allow in-  
 305 feasibilities, and in turn solves a resource-constrained shortest path problem using dynamic  
 306 programming to determine the best fleet mix on a given solution. Our implementation also  
 307 differs from those of Vidal et al. (2013) since it allows for infeasibilities that are not just  
 308 related to time windows or load, but also to the fleet size in the case of HT and HD.

309 We now describe the SPLIT algorithm. Let  $\mathfrak{R}$  be the set of all routes in individual  $C$ ,  
 310 and let  $R$  be a route. While formally  $R$  is a vector, for convenience we denote the number  
 311 of its components by  $|R|$ . Therefore,  $R = (i_0 = 0, i_1, i_2, \dots, i_{|R|-1}, i_{|R|} = 0)$ , we also write  
 312  $i \in R$  if  $i$  is a component of  $R$ , and  $(i, j) \in R$  if  $i$  and  $j$  appear in succession in  $R$ . Let  $z_t$   
 313 be the arrival time at the  $t^{\text{th}}$  customer in  $R$ , thus the time window violation of route  $R$  is  
 314  $\sum_{t=1}^{|R|-1} \max\{z_t - b_{i_t}, 0\}$ . The total load for route  $R$  is  $\sum_{t=1}^{|R|-1} q_{i_t}$ , and we consider solutions  
 315 with a total load not exceeding twice the capacity of the largest vehicle given by  $Q_{max}$  (Vidal  
 316 et al., 2013). Furthermore, for route  $R$  and for each vehicle type  $k$  we compute  $y(k)$ , which  
 317 is the number of vehicles of type  $k$  used in the solution.

318 Let  $\lambda_t$ ,  $\lambda_l$  and  $\lambda_f$  represent the penalty values for any violations of the time windows, the  
 319 vehicle capacity and the fleet size, respectively. The variable  $x_{ij}^k$  is equal to 1 if customer  $i$   
 320 immediately precedes customer  $j$  visited by vehicle  $k$ . The fixed cost associated with using  
 321 a vehicle of type  $k \in K$  is denoted by  $e_k$ . For each route  $R \in \mathfrak{R}$  traversed by vehicle  $k \in K$ ,

322 the cost including penalties is

$$\nu(R, k) = \sum_{(i,j) \in R} c_{ij}^k x_{ij}^k + e_k + \lambda_t \sum_{t=1}^{|R|-1} \max\{z_t - b_{i_t}, 0\} + \lambda_l \max\left\{\sum_{t=1}^{|R|-1} q_{i_t} - Q_{max}, 0\right\}, \quad (7)$$

323 which brings various objectives together to be able to guide to the search towards infeasible  
 324 solutions. Thus, the total cost of individual  $C$  is

$$\Delta(C) = \sum_{R \in \mathfrak{R}} \sum_{k \in K} \nu(R, k) + \lambda_f \sum_{k \in K} \max\{0, y(k) - n_k\}, \quad (8)$$

325 where  $n_k$  is set equal to a sufficiently large number (e.g.,  $n$ ) for FT and FD, in order for the  
 326 last term in Equation (8) to be zero.

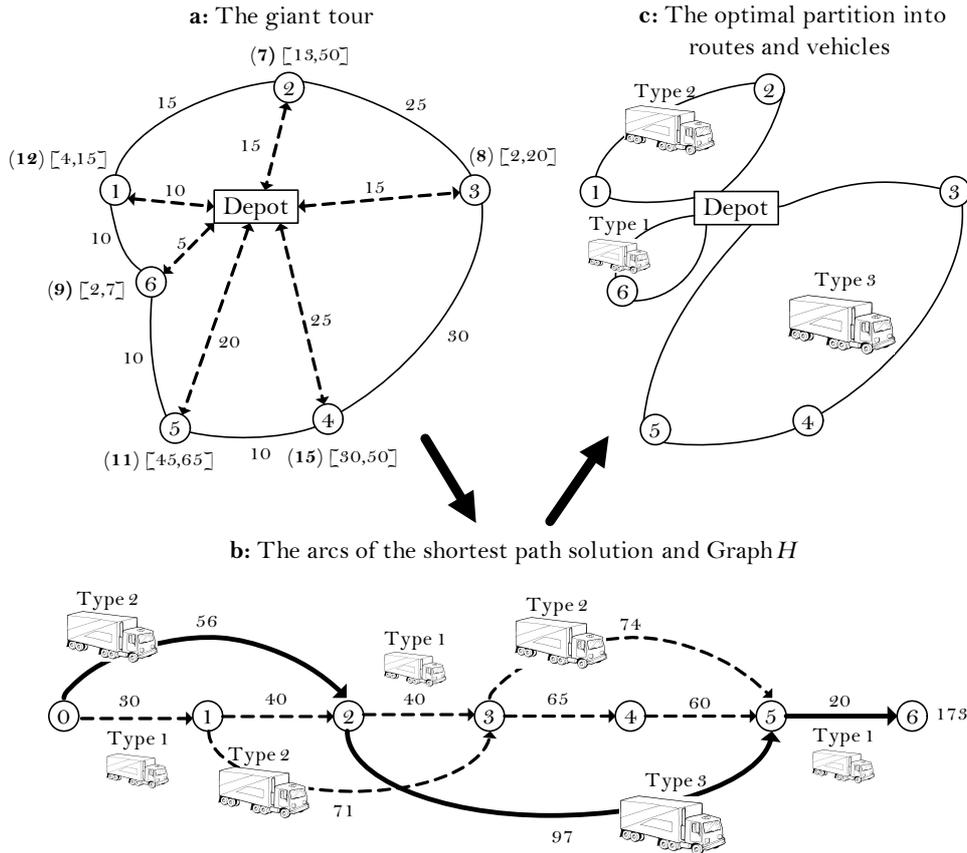


Figure 2: Illustration of procedure SPLIT

327 Figure 2 shows the steps of this advanced procedure using on an FD instance. The arc

328 costs, demands and time windows are given in Figure 2.a. In particular, the number in  
 329 bold within the parentheses associated with each node is the demand for that customer; the  
 330 two numbers within brackets define the time window. Service times are identical and equal  
 331 to 4 for each customer, and three different types of vehicles are available. The capacity  $q_k$   
 332 and fixed cost  $e_k$  of vehicles of type  $\{1,2,3\}$  are  $q_1 = 10$ ,  $q_2 = 20$ ,  $q_3 = 30$  and  $e_1 = 6$ ,  
 333  $e_2 = 8$ ,  $e_3 = 10$ , respectively. The algorithm starts with a giant TSP tour which includes  
 334 six customers and uses one vehicle with unlimited capacity. The SPLIT algorithm computes  
 335 an optimal compound segmentation in three routes corresponding to three sequences of  
 336 customers  $\{1,2\}$ ,  $\{3,4,5\}$  and  $\{6\}$  with three vehicle choices, Type 2, Type 3 and Type 1,  
 337 respectively, as shown in Figure 2.b. The resulting solution is shown in Figure 2.c. An  
 338 optimal partitioning of the giant tour into routes for offspring  $C$  corresponds to a minimum-  
 339 cost path.

340 The penalty parameters of the SPLIT algorithm are initially set to an initial value and  
 341 are dynamically adjusted during the algorithm. If an individual is still infeasible after the  
 342 first EDUCATION procedure, then the penalty parameters are multiplied by  $\lambda_m$  and the  
 343 EDUCATION procedure restarts. When this solution becomes feasible, the parameters are  
 344 reset to their initial values. These values are  $\lambda_t = \lambda_l = \lambda_f = 3$ ,  $\lambda_m = 10$ .

## 345 2.7. INTENSIFICATION

346 We introduce a two-phase aggressive INTENSIFICATION procedure to improve the quality  
 347 of elite individuals. This procedure intensifies the search within promising regions of the  
 348 solution space. The detailed pseudo-code of this method is shown in Algorithm 3. The  
 349 algorithm starts with an elite list of solutions  $L_e$ , which takes the best  $n_e$  individuals from  
 350 the main population as measured by equation (2). Step 1 is similar to the main EDUCATION  
 351 procedure (Section 2.2). Step 2 attempts to explore different regions of the search space  
 352 with the RR operator, intensifies this area by applying the GI operator for FD and HD, and  
 353 GIET for FT and HT, to a partially the destroyed solution. Steps 1 and 2 terminate when  
 354 there is no improvement to the solution and the main loop terminates when  $n_e$  successive  
 355 iterations have been performed.

356 Due to the difficulty of the problems considered in this paper, we have developed a  
357 two-phase aggressive INTENSIFICATION procedure after having tried several variants such as  
358 one-phase with only Step 1 or Step 2, three-phase with Step 1, Step 2 and Step 1 and various  
359 other combinations. We have also considered other operators. Our analysis has shown that  
360 this two-phase structure yields better solutions than all other considered variants.

---

**Algorithm 3** INTENSIFICATION

---

```

1: Initialize  $L_e = \{\chi_1, \dots, \chi_n\}$ ,  $i \leftarrow 1$ 
2: while all elite solutions are intensified do
3:    $\chi \leftarrow \chi_i$ 
4:   Step 1
5:   while there is improvement and elite solution  $\chi$  is feasible do
6:      $L_r = \emptyset$  and select a removal operator
7:     Apply to the elite solution  $\chi$  to remove nodes and add them to  $L_r$ 
8:     Select an insertion operator and apply it to the destroyed elite solution  $\chi$  by
        inserting the node of  $L_r$ 
9:     Let  $\chi^*$  be the new solution obtained by applying insertion operator
10:    if  $\omega(\chi^*) < \omega(\chi)$  then
11:       $\omega(\chi) \leftarrow \omega(\chi^*)$ 
12:    end while
13:    Step 2
14:    while there is improvement and  $\chi^*$  is feasible do
15:       $L_r = \emptyset$  and apply RR operator to the elite solution  $\chi$  to remove nodes and add
        them to  $L_r$ 
16:      Apply GI or GIET operator to the partially destroyed elite solution  $\chi$  by inserting
        the node of  $L_r$ 
17:      Let  $\chi^*$  be the new elite solution obtained by applying insertion operator
18:      if  $\omega(\chi^*) < \omega(\chi)$  then
19:         $\omega(\chi) \leftarrow \omega(\chi^*)$ 
20:      end while
21:     $i \leftarrow i + 1$ 
22:  end while
23: Return elite solutions

```

---

361 *2.8. Survivor Selection*

362 In population-based metaheuristics, avoiding premature convergence is a key challenge.  
363 Ensuring the diversity of the population, in other words to search a different location in the  
364 solution space during the algorithm, in the hope of being closer to the best known or optimal

365 solutions constitutes a major trade-off between solutions in a population. The method of  
 366 Vidal et al. (2012), aims to ensure the diversity of the population and preserve the elite  
 367 solutions. The second part of this method is the survivor selection process (the first part  
 368 was discussed in Section 2.3). In this way, elite individuals are protected.

### 369 2.9. Diversification

370 The efficient management of feasible solutions plays a significant role in population di-  
 371 versity. The performance of the HEA is improved by applying a MUTATION after the ED-  
 372 UCATION procedure. Over the iterations, individuals tend to become more similar, making  
 373 it difficult to avoid premature convergence. To overcome this difficulty, we introduce a new  
 374 scheme in order to increase the population diversity. The diversification stage includes two  
 375 procedures, namely REGENERATION and MUTATION, representations of which are shown in  
 376 Figure 3.

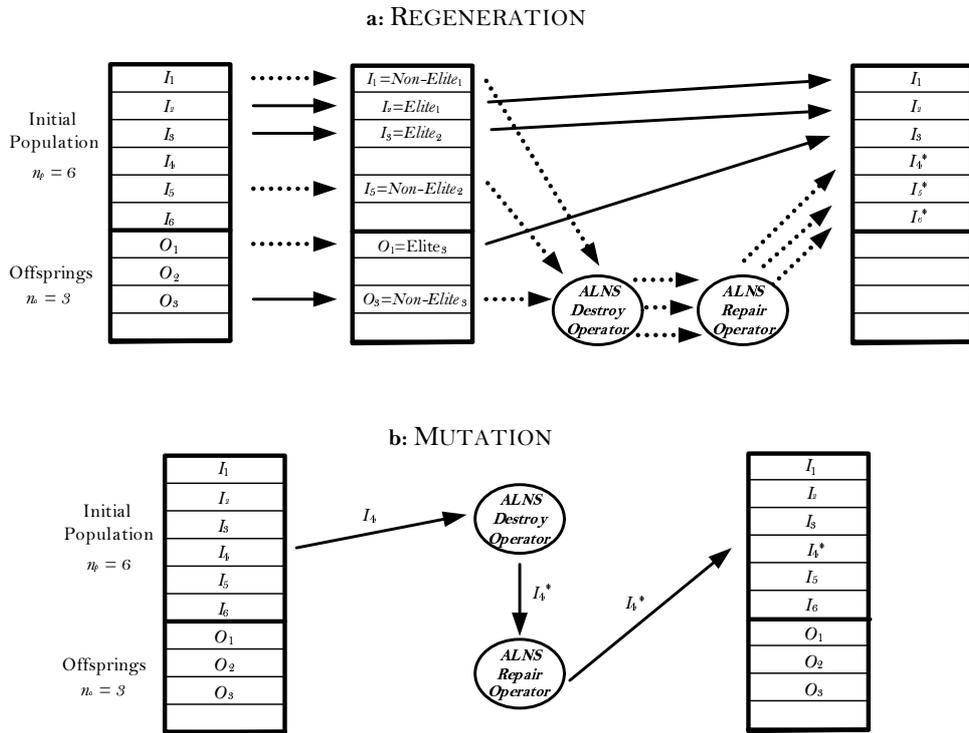


Figure 3: Illustration of the diversification stage

377 A REGENERATION procedure (Figure 3.a) takes place when the maximum allowable

378 iterations for REGENERATION  $it_r$  is reached without an improvement in the best solution  
379 value. In this procedure, the  $n_e$  elite individuals are preserved and are transferred to the  
380 next generation. The remaining  $n_p - n_e$  individuals, which are ranked according to their  
381 biased fitness, are subjected to the RR and GINF operators, to create new individuals. At  
382 the end of this procedure, only  $n_p$  new individuals are kept in the population.

383 The MUTATION procedure is applied with probability  $p_m$ . Figure 3.b illustrates the  
384 MUTATION procedure. In this procedure, an individual  $C$  different from the best solution  
385 is randomly selected. Two randomized structure based ALNS operators, the RR and the  
386 GINF, are then used to change the positions of a specific number of nodes, which are chosen  
387 from the interval  $[b_l^m, b_u^m]$  of removable nodes in the MUTATION procedure.

### 388 **3. Computational Experiments**

389 This section presents the results of computational experiments performed in order to  
390 assess the performance of the HEA. The HEA was implemented in C++ and run on a  
391 computer with one gigabyte RAM and Intel Xeon 2.6 GHz processor. We first describe the  
392 benchmark instances and the parameters used within the algorithm. This is followed by a  
393 presentation of the results.

#### 394 *3.1. Data Sets and Experimental Settings*

395 The benchmark data sets of Liu and Shen (1999b), derived from the classical Solomon  
396 (1987) VRPTW instances with 100 nodes, are used as the test-bed. These sets include 56  
397 instances, split into a random data set R, a clustered data set C and a semi-clustered data  
398 set RC. Sets shown by R1, C1 and RC1 have a short scheduling horizon and small vehicle  
399 capacities, in contrast to sets denoted R2, C2 and RC2 with a long scheduling horizon and  
400 large vehicle capacities. Liu and Shen (1999b) introduced three types of cost structures,  
401 namely large, medium and small, and have denoted them by A, B and C, respectively. The  
402 authors also introduced several vehicle types with different capacities and fixed vehicle costs  
403 for each of the 56 instances. This results in a total of 168 benchmark instances for FT or  
404 FD.

405 The benchmark set used by Paraskevopoulos et al. (2008) for HT is a subset of the FT  
406 instances, in which the fleet size is set equal to that found in the best known solutions of Liu  
407 and Shen (1999a). In total, there are 24 benchmark instances derived from Liu and Shen  
408 (1999a) for HT. We use the same set for HD, with the new objective.

409 Evolutionary algorithms use a set of correlated parameters and configuration decisions.  
410 In our implementation, we initially used the parameters suggested by Vidal et al. (2012,  
411 2013) for the genetic algorithm, but we have conducted several experiments to further fine-  
412 tune these parameters on instances C101A, C203A, R101A, R211A, RC105A and RC207A.  
413 Following these tests, the following parameter values were used in our experiments:  $it_t =$   
414  $5000, it_r = 2000, it_w = 500, n_p = 25, n_o = 25, n_e = 10, n_c = 3, p_m \in [0.4, 0.6], [b_l^i, b_u^i] =$   
415  $[0.3, 0.8], [b_l^e, b_u^e] = [0.1, 0.16], [b_l^m, b_u^m] = [0.1, 0.16], \sigma_1 = 3, \sigma_2 = 1, \sigma_3 = 0$ . For the Adaptive  
416 Large Neighborhood Search (ALNS), we have used the same parameter values as in Demir  
417 et al. (2012), namely  $r_p = 0.1, \varphi_1 = 0.5, \varphi_2 = 0.25, \varphi_3 = 0.15, \varphi_4 = 0.25$ . All of these settings  
418 are identical for all four considered problems.

419 Table 1 presents the results of a fine-tuning experiment on parameters  $n_p$  and  $n_o$ , and to  
420 test the effect of these parameters on the solution quality.

Table 1: Average percentage deviations of the solution values found by the HEA from best-known solution values with varying  $n_p$  and  $n_o$

$n_p$	$n_o$				
	10	25	50	75	100
10	0.42	0.26	0.38	0.56	0.69
25	0.19	<b>0.11</b>	0.26	0.37	0.49
50	0.39	0.29	0.30	0.45	0.57
75	0.56	0.42	0.51	0.61	0.68
100	0.67	0.53	0.61	0.72	0.78

421 The table shows the percent gap between the solution value obtained by the HEA and  
422 the best-known solution (BKS) value, averaged over the six chosen instances. The maximum  
423 population size is dependent on  $n_p$  and  $n_o$ , both of which have a significant impact on the  
424 solution quality, where the best setting is obtained with  $n_p = n_o = 25$ .

425 *3.2. Comparative Analysis*

426 We now present a comparative analysis of the results of the HEA with those reported in  
427 the literature. In particular, we compare ourselves against LSa (Liu and Shen, 1999a), LSb  
428 (Liu and Shen, 1999b), T-RR-TW (Dell’Amico et al., 2007), ReVNTS (Paraskevopoulos et  
429 al., 2008), MDA (Bräysy et al., 2008), BPDRT (Bräysy et al., 2009), AMP (Repoussis and  
430 Tarantilis, 2010) and UHGS (Vidal et al., 2014). The comparisons are presented in tables,  
431 where the columns show the total cost (TC), and percent deviations (Dev) of the values  
432 of solutions found by each method with respect to the HEA. The first column displays the  
433 instance sets and the number of instances in each set in parentheses. The rows named Avg  
434 (%), Min (%) and Max (%) show the average, minimum and maximum deviations across all  
435 benchmark instances, respectively. A negative deviation shows that the solution found by  
436 the HEA is of better quality. In the column labeled BKS, “=” shows the total number of  
437 matches and “<” shows the number of new BKS found for each instance set.

438 Ten separate runs are performed for each instance, the best one of which is reported.  
439 For each instance, a boldface refers to match with current BKS, where as a boldface with a  
440 “\*” indicates new BKS. For detailed results, the reader is referred to Appendix A. Tables  
441 A.1-A.6 present the fixed vehicle cost (VC), the distribution cost (transportation cost) (DC),  
442 the computational time in minutes (Time) and the actual number of vehicles used (Mix),  
443 where the letters A–E correspond to the vehicle types and the upper numbers denote the  
444 number of each type of vehicle used. For example, ( $A^2B^1$ ) indicates that two vehicles of  
445 type A and one vehicle of type B are used in the solution.

446 Tables 2 and 3 summarize the average comparison results of the current state-of-the-art  
447 solution methods for FT and FD, compared with the HEA. According to Tables 2 and 3,  
448 the HEA is highly competitive, with average deviations ranging from  $-6.78\%$  to  $0.03\%$  and  
449 a worst-case performance of  $0.66\%$  for FT. The average performance of our HEA is better  
450 than that of all the competitors for FT, except for the algorithm of Vidal et al. (2014) which  
451 is slightly better on average. However, the HEA found 17 new best solution and outperforms  
452 this algorithm on to the second type of FT instances, which are less tight in terms of vehicle  
453 capacity. As for FD, average cost reductions range from  $-0.90\%$  to  $-0.02\%$  and the worst-

454 case performance is 0.94%. The HEA outperforms all other algorithms in the literature for  
 455 FD, including the UHGS of Vidal et al. (2014).

Table 2: Average results for FT

Instance set	T-RR-TW		ReVNTS		MDA		AMP		UHGS		HEA	BKS	
	TC	Dev	TC	Dev	TC	Dev	TC	Dev	TC	Dev	TC	=	<
R1A (12)	4180.83	-1.51	4128.48	-0.24	4131.31	-0.31	4113.89	0.12	<b>4103.16</b>	0.38	4118.70	0	0
R1B (12)	1927.57	-1.65	1902.19	-0.31	1898.88	-0.13	1896.83	-0.03	<b>1891.63</b>	0.25	1896.35	0	<b>1*</b>
R1C (12)	1615.44	-2.56	1582.18	-0.45	1579.17	-0.26	1578.12	-0.19	<b>1574.32</b>	0.05	1575.09	1	0
C1A (9)	7229.02	-1.20	7143.35	0.00	7141.15	0.03	7139.96	0.05	<b>7138.93</b>	0.06	7143.35	2	0
C1B (9)	2384.77	-0.99	2361.78	-0.02	2365.49	-0.18	2359.82	0.06	<b>2359.63</b>	0.07	2361.29	2	<b>1*</b>
C1C (9)	1629.70	-0.62	1621.09	-0.09	1621.83	-0.14	<b>1618.91</b>	0.04	1619.18	0.00	1619.18	6	0
RC1A (8)	5117.96	-3.49	4961.69	-0.33	4948.53	-0.07	4948.02	-0.06	<b>4915.10</b>	0.61	4945.14	0	0
RC1B (8)	2163.51	-1.35	2142.65	-0.37	2129.60	0.24	2136.73	-0.09	<b>2129.04</b>	0.27	2134.74	0	<b>2*</b>
RC1C (8)	1784.51	-1.36	1769.93	-0.53	1758.29	0.13	1762.34	-0.10	<b>1752.19</b>	0.48	1760.59	0	0
R2A (11)	3568.97	-9.06	3304.57	-0.98	3310.70	-1.17	3287.80	-0.47	<b>3267.31</b>	0.16	3272.48	2	<b>1*</b>
R2B (11)	1727.04	-17.40	1498.97	-1.88	1495.37	-1.64	1487.09	-1.08	1480.30	-0.61	<b>1471.27*</b>	1	<b>7*</b>
R2C (11)	1436.22	-15.30	1281.31	-2.84	1257.65	-0.94	1260.97	-1.20	<b>1237.79</b>	0.66	1245.97	0	0
C2A (8)	6267.75	-9.07	5759.02	-0.22	5797.38	-0.89	5749.98	-0.06	5760.29	-0.24	<b>5746.44*</b>	4	0
C2B (8)	1897.62	-8.53	1754.07	-0.32	1756.08	-0.43	1748.99	-0.03	1750.37	-0.11	<b>1748.52*</b>	2	<b>1*</b>
C2C (8)	1276.29	-4.78	1232.98	-1.22	1223.86	-0.47	1224.08	-0.49	1221.17	-0.25	<b>1218.12*</b>	4	<b>2*</b>
RC2A (8)	4752.95	-8.24	4406.28	-0.34	4399.12	-0.18	4388.88	0.05	<b>4381.73</b>	0.21	4391.16	0	0
RC2B (8)	2156.11	-15.40	1888.83	-1.13	1899.20	-1.68	1874.86	-0.38	1877.84	-0.54	<b>1867.80*</b>	0	<b>2*</b>
RC2C (8)	1828.95	-19.50	1567.22	-2.43	1562.19	-2.10	1541.13	-0.72	1545.29	-0.99	<b>1530.08*</b>	0	0
Min (%)		-19.50		-2.84		-2.10		-1.20		-0.99			
Avg (%)		-6.78		-0.76		-0.57		-0.25		0.03			
Max (%)		-0.62		0.00		0.24		0.12		0.66			
All												24	17*
Runs	1		1		3		1		10		10		
Processor	P 600M		PIV 1.5GHz		Ath 2.6GHz		PIV 3.4GHz		Opt 2.2GHz		Xe 2.6GHz		
Avg Time	14.15		20.00		10.97		16.67		5.08		4.83		

456 Table 4 presents the comparison results for each HT instance against LSa and ReVNTS.  
 457 We note that LSa only solved FT and not HT, which was the basis for setting the number  
 458 of available vehicles in ReVNTS. The results show that the HEA outperforms both methods  
 459 and yields higher quality solutions within short computation times. On average, the total  
 460 cost reductions obtained were -12.68% and -0.34% compared to LSa and ReVNTS, with  
 461 minimum deviations of -29.47% and -2.01% and maximum deviations of -1.26% and  
 462 0.35%, respectively. Finally, Table 5 shows the results obtained on the newly introduced  
 463 HD.

464 Looking at the results obtained on the HT instances, on average the HEA yields 1.23%  
 465 and 0.13% lower vehicle fixed costs than the LSa and ReVNTS, respectively. The HEA  
 466 decreases the distribution cost (en-route time based cost) by 42.19% and 1.03%, compared  
 467 with LSa and ReVNTS, respectively. These results indicate that the HEA is able find better

Table 3: Average results for FD

Instance set	MDA		BPDRT		UHGS		HEA	BKS	
	TC	Dev	TC	Dev	TC	Dev	TC	=	<
R1A (12)	4068.59	-0.67	4060.96	-0.48	<b>4031.28</b>	0.25	4041.46	0	0
R1B (12)	1854.60	-0.82	-	-	1841.43	-0.11	<b>1839.39*</b>	0	<b>4*</b>
R1C (12)	1539.48	-0.91	1539.90	-0.93	1530.25	-0.30	<b>1525.56*</b>	0	<b>8*</b>
C1A (9)	7085.56	-0.03	7085.91	-0.04	<b>7082.98</b>	0.00	<b>7082.98</b>	9	0
C1B (9)	2335.11	-0.09	-	-	<b>2332.89</b>	0.00	2332.90	9	0
C1C (9)	1615.75	-0.02	1615.40	-0.01	1615.49	-0.01	<b>1615.38*</b>	9	0
RC1A (8)	4944.48	-0.57	4935.52	-0.38	<b>4891.25</b>	0.51	4916.41	0	0
RC1B (8)	2121.62	-0.87	-	-	2107.08	-0.18	<b>2103.21*</b>	0	<b>7*</b>
RC1C (8)	1741.78	-0.94	1749.66	-1.40	1734.36	-0.51	<b>1725.44*</b>	2	<b>6*</b>
R2A (11)	3193.41	-1.36	3180.59	-0.96	3151.96	-0.05	<b>3150.29*</b>	7	<b>4*</b>
R2B(11)	1392.92	-3.06	-	-	1351.905	-0.02	<b>1351.52*</b>	4	<b>2*</b>
R2C (11)	1149.65	-2.06	1149.11	-2.01	1128.708	-0.20	<b>1126.42*</b>	5	<b>4*</b>
C2A (8)	5690.87	-0.07	5689.40	-0.04	<b>5686.75</b>	0.00	<b>5686.75</b>	8	0
C2B (8)	1698.51	-0.69	-	-	<b>1686.75</b>	0.00	<b>1686.75</b>	8	0
C2C (8)	1186.03	-0.07	1185.70	-0.04	<b>1185.19</b>	0.00	<b>1185.19</b>	8	0
RC2A (8)	4241.33	-0.73	4231.25	-0.49	<b>4210.10</b>	0.00	<b>4210.10</b>	5	<b>1*</b>
RC2B (8)	1704.13	-1.04	-	-	1686.63	-0.01	<b>1686.47*</b>	0	<b>5*</b>
RC2C (8)	1374.55	-1.11	1385.32	-1.91	1358.24	0.08	1359.33	1	<b>3*</b>
Min (%)		-4.30		-7.74		-1.49			
Avg (%)		-0.90		-0.74		-0.02			
Max (%)		0.07		0.10		0.94			
All								<b>75</b>	<b>44*</b>
Runs	3		1		10		10		
Processor	Ath 2.6G		Duo 2.4G		Opt 2.2G		Xe 2.6G		
Avg Time	3.56		-		4.72		4.56		

468 fleet mix composition and lower distribution costs than the other methods.

469 In summary, the HEA was able to find 41 BKS for 168 FT instances, where 17 are strictly  
470 better than those obtained by competing heuristics. As for FD, the algorithm has identified  
471 119 BKS out of the 168 instances, 44 of which are strictly better than those obtained by  
472 previous heuristics. The results are even more striking for HT, with 17 BKS on the 24  
473 instances, 14 of which are strictly better than those reported earlier. Overall, the HEA  
474 improves 75 BKS and matches 102 BKS out of 360 benchmark instances.

#### 475 4. Conclusions

476 We have proposed a unified heuristic for four types of heterogeneous fleet vehicle routing  
477 problems with time windows. The first two are the Fleet Size and Mix Vehicle Routing Prob-  
478 lem with Time Windows (F) and the Heterogeneous Fixed Fleet Vehicle Routing Problem  
479 with Time Windows (H). Each of these two problems was solved under a time and a dis-  
480 tance objective, yielding the four variants FT, FD, HT and HD. We have developed a unified  
481 hybrid evolutionary algorithm (HEA) capable of solving all variants without any modifica-

Table 4: Results for HT

Instance set	LSa			ReVNTS			HEA					BKS	
	Mix	TC	Dev	Mix	TC	Dev	DC	VC	Mix	TC	Time	=	<
R101A	$A^1B^{11}C^{11}D^1$	5061	-10.29	$B^{10}C^{11}D^1$	<b>4583.99</b>	0.10	1998.76	2590	$B^{10}C^{11}D^1$	4588.76	5.49	0	0
R102A	$A^1B^4C^{14}D^2$	5013	-13.25	$B^3C^{14}D^2$	4420.68	0.13	1736.54	2640	$A^1B^4C^{13}D^2$	<b>4376.54*</b>	6.78	0	1*
R103A	$B^7C^{15}$	4772	-13.57	$B^6C^{15}$	<b>4195.05</b>	0.16	1621.71	2580	$B^6C^{15}$	4201.71	7.45	0	0
R104A	$B^9C^{14}$	4455	-10.61	$B^8C^{14}$	4065.52	-0.94	1487.69	2540	$B^9C^{13}$	<b>4027.69*</b>	6.14	0	1*
C101A	$A^1B^{10}$	9272	-5.02	$B^{10}$	<b>8828.93</b>	0.00	828.93	8000	$B^{10}$	<b>8828.93</b>	3.67	1	0
C102A	$A^{19}$	8433	-17.89	$A^{19}$	<b>7137.79</b>	0.21	1453.13	5700	$A^{19}$	7153.13	4.12	0	0
C103A	$A^{19}$	8033	-12.78	$A^{19}$	7143.88	-0.30	1422.57	5700	$A^{19}$	<b>7122.57*</b>	3.45	0	1*
C104A	$A^{19}$	7384	-4.25	$A^{19}$	7104.96	-0.30	1383.74	5700	$A^{19}$	<b>7083.74*</b>	3.13	0	1*
RC101A	$A^7B^7C^7$	5687	-7.99	$A^4B^7C^7$	5279.92	-0.26	1876.36	3390	$A^4B^7C^7$	<b>5266.36*</b>	5.73	0	1*
RC102A	$A^5B^6C^8$	5649	-10.77	$A^4B^5C^8$	5149.95	-0.99	1709.55	3390	$A^4B^5C^8$	<b>5099.55*</b>	5.14	0	1*
RC103A	$A^{11}B^2C^8$	5419	-8.58	$A^{10}B^2C^8$	5002.41	-0.22	1691.29	3300	$A^{10}B^2C^8$	<b>4991.29*</b>	4.90	0	1*
RC104A	$A^2B^{13}C^3D^1$	5189	-3.43	$A^2B^{13}C^3D^1$	5024.25	-0.15	1596.97	3420	$A^2B^{13}C^3D^1$	<b>5016.97*</b>	5.21	0	1*
R201A	$A^5$	4593	-21.43	$A^5$	<b>3779.12</b>	0.09	1532.49	2250	$A^5$	3782.49	7.45	0	0
R202A	$A^5$	4331	-20.85	$A^5$	<b>3578.91</b>	0.14	1333.92	2250	$A^5$	3583.92	8.45	0	0
R203A	$A^4B^1$	4220	-18.74	$A^4B^1$	3582.54	-0.81	1053.92	2500	$A^4B^1$	<b>3553.92*</b>	7.12	0	1*
R204A	$A^5$	3849	-24.89	$A^5$	3143.68	-2.01	831.80	2250	$A^5$	<b>3081.80*</b>	6.99	0	1*
C201A	$A^4B^1$	6711	-9.29	$A^4B^1$	<b>6140.64</b>	0.00	740.64	5400	$A^4B^1$	<b>6140.64</b>	4.89	1	0
C202A	$A^1C^3$	7720	-1.26	$A^1C^3$	7752.88	-1.69	623.96	7000	$A^1C^3$	<b>7623.96*</b>	4.26	0	1*
C203A	$C^2D^1$	7466	-2.23	$C^2D^1$	<b>7303.37</b>	0.00	603.37	6700	$C^2D^1$	<b>7303.37</b>	4.37	1	0
C204A	$A^5$	6744	-18.72	$A^5$	5721.09	-0.72	680.46	5000	$A^5$	<b>5680.46*</b>	5.29	0	1*
RC201A	$C^1E^3$	5871	-6.08	$C^1E^3$	<b>5523.15</b>	0.21	1684.59	3850	$C^1E^3$	5534.59	6.47	0	0
RC202A	$A^1C^1D^1E^2$	5945	-15.43	$A^1C^1D^1E^2$	<b>5132.08</b>	0.35	1450.23	3700	$A^1C^1D^1E^2$	5150.23	6.35	0	0
RC203A	$A^1B^1C^5$	5790	-29.47	$A^1B^1C^5$	4508.27	-0.81	1221.92	3250	$A^1B^1C^5$	<b>4471.92*</b>	6.01	0	1*
RC204A	$A^{14}B^2$	4983	-17.47	$A^{14}B^2$	4252.87	-0.26	1441.83	2800	$A^{14}B^2$	<b>4241.83*</b>	5.87	0	1*
Min (%)			-29.47			-2.01							
Avg (%)			-12.68			-0.34							
Max (%)			-1.26			0.35							
Total												<b>3</b>	<b>14*</b>
Runs	3			1			10						
Processor	P 233M			PIV 1.5GHz			Xe 2.6GHz						
Avg Time	-			20.00			5.61						

Table 5: Results for HD

Instance set	HEA				
	DC	VC	Mix	TC	Time
R101A	1765.41	2590	$B^{10}C^{11}D^1$	4355.41	5.19
R102A	1716.44	2640	$B^4C^{13}D^2$	4356.44	6.24
R103A	1500.16	2580	$B^6C^{15}$	4080.16	6.57
R104A	1434.72	2520	$B^7C^{14}$	3954.72	5.89
C101A	828.94	8000	$B^{10}$	8828.94	4.25
C102A	1380.17	5700	$A^{19}$	7080.17	3.97
C103A	1379.21	5700	$A^{19}$	7079.21	3.99
C104A	1375.06	5700	$A^{19}$	7075.06	2.98
RC101A	1772.28	3390	$A^4B^7C^7$	5162.28	6.41
RC102A	1598.05	3420	$A^2B^6C^8$	5018.05	5.24
RC103A	1626.55	3300	$A^{10}B^2C^8$	4926.55	4.39
RC104A	1575.91	3420	$A^2B^{13}C^3D^1$	4995.91	4.88
R201A	1198.76	2250	$A^5$	3448.76	6.74
R202A	1058.16	2250	$A^5$	3308.16	8.13
R203A	882.39	2500	$A^4B^1$	3382.39	7.49
R204A	768.14	2250	$A^5$	3018.14	5.47
C201A	682.38	5400	$A^4B^1$	6082.38	4.21
C202A	618.62	7000	$A^1C^3$	7618.62	3.69
C203A	603.37	6700	$C^2D^1$	7303.37	3.67
C204A	677.66	5000	$A^5$	5677.66	5.11
RC201A	1494.47	3850	$C^1E^3$	5344.47	6.72
RC202A	1156.02	3700	$A^1C^1D^1E^2$	4856.02	6.48
RC203A	996.25	3250	$A^1B^1C^5$	4246.25	6.93
RC204A	1395.32	2800	$A^{14}B^2$	4195.32	6.17
Average				5224.77	5.45
Runs	10				
Processor	Xe 2.6GHz				
Avg Time	5.45				

482 tion. This heuristic combines state-of-the-art metaheuristic principles such as heterogeneous  
483 adaptive large scale neighborhood search and population search. We have integrated within  
484 our HEA an innovative INTENSIFICATION strategy on elite solutions and we have developed  
485 a new diversification scheme based on the REGENERATION and the MUTATION of solutions.  
486 We have also developed an advanced version of the SPLIT algorithm of Prins (2009) to de-  
487 termine the best fleet mix for a set of routes. Finally, we have introduced the new variant  
488 HD. Extensive computational experiments were carried out on benchmark instances. In the  
489 case of FT, our HEA clearly outperforms all previous algorithms except that of Vidal et al.  
490 (2014). It performs slightly worse on average, but is superior on instances which are less  
491 tight in terms of vehicle capacity. On the FD instances, our HEA outperforms the three  
492 existing algorithms. Overall, the HEA has identified 160 new best solutions out of 336 on  
493 the F instances, 61 of which are strictly better than previously known solutions. On the  
494 HT instances, our HEA outperforms the two existing algorithms and has identified 17 best  
495 known solutions out of 24, 14 of which are strictly better than previously found solutions.  
496 The HD instances are solved here for the first time. Overall, we have improved 75 solutions  
497 out of 360 instances, and we have matched 102 others. All instances were solved within a  
498 modest computational effort. Our algorithm is not only highly competitive, but it is also  
499 flexible in that it can solve four problem classes with the same parameter settings.

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## 505 **Appendix**

506 Table A.1 to A.6 present the detailed results on all benchmark instances for FT and FD.

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Table A.1: Results for FT for cost structure A

Instance set	ReVNTS		MDA		AMP		UHGS		HEA				
	TC	Dev	TC	Dev	TC	Dev	TC	Dev	DC	VC	Mix	TC	Time
R101A	4539.99	0.04	4631.31	-1.97	<b>4536.4</b>	0.12	4608.62	-1.50	1951.70	2590	$A^1B^2C^{17}$	4541.70	5.26
R102A	4375.70	-0.47	4401.31	-1.06	<b>4348.92</b>	0.14	4369.74	-0.30	1775.10	2580	$B^6C^{15}$	4355.10	5.87
R103A	4120.63	0.26	4182.16	-1.23	<b>4119.04</b>	0.30	4145.68	-0.30	1551.23	2580	$B^6C^{15}$	4131.23	4.19
R104A	3992.65	-0.01	3981.28	0.27	<b>3986.35</b>	0.14	3961.39	0.77	1302.10	2690	$B^5C^{11}D^3$	3992.10	5.02
R105A	4229.69	0.07	4236.84	-0.10	4229.67	0.07	<b>4209.84</b>	0.54	1672.54	2560	$B^4C^{16}$	4232.54	4.73
R106A	4137.96	0.01	4118.48	0.48	4130.82	0.18	<b>4109.08</b>	0.71	1538.30	2600	$B^4C^{18}$	4138.30	5.13
R107A	4061.10	-0.66	4035.96	-0.04	4031.16	0.08	<b>4007.87</b>	0.66	1474.32	2560	$B^4C^{16}$	4034.32	5.4
R108A	3986.07	-0.50	3970.26	-0.10	3962.2	0.10	<b>3934.48</b>	0.80	1406.10	2560	$B^4C^{16}$	3966.10	4.78
R109A	4086.72	-0.68	4060.17	-0.03	4052.21	0.17	<b>4020.75</b>	0.94	1429.02	2630	$C^{17}D^1$	4059.02	4.6
R110A	4030.85	-0.86	3995.18	0.03	3999.09	-0.07	<b>3965.88</b>	0.76	1436.31	2560	$B^4C^{16}$	3996.31	4.17
R111A	4018.80	0.03	4017.81	0.06	4016.19	0.10	<b>3985.68</b>	0.86	1460.10	2560	$B^4C^{13}D^2$	4020.10	4.98
R112A	3961.63	-0.10	3947.30	0.26	3954.65	0.07	<b>3918.88</b>	0.98	1397.60	2560	$B^4C^{16}$	3957.60	5.78
C101A	<b>7226.51</b>	0.00	<b>7226.51</b>	0.00	<b>7226.51</b>	0.00	<b>7226.51</b>	0.00	1526.51	5700	$A^{19}$	<b>7226.51</b>	2.97
C102A	7137.79	0.11	<b>7119.35</b>	0.37	7137.79	0.11	<b>7119.35</b>	0.37	1445.65	5700	$A^{19}$	7145.65	3.10
C103A	7143.88	0.00	7107.01	0.52	7141.03	0.04	<b>7102.86</b>	0.57	1443.88	5700	$A^{19}$	7143.88	2.70
C104A	7104.96	-0.31	<b>7081.50</b>	0.02	7086.70	-0.05	7081.51	0.02	1382.92	5700	$A^{19}$	7082.92	2.01
C105A	7171.48	0.05	7199.36	-0.34	<b>7169.08</b>	0.08	7196.06	-0.3	1475.00	5700	$A^{19}$	7175.00	2.45
C106A	<b>7157.13</b>	0.09	7180.03	-0.23	<b>7157.13</b>	0.09	7176.68	-0.20	1463.32	5700	$A^{19}$	7163.32	3.01
C107A	7135.43	0.07	7149.17	-0.13	<b>7135.38</b>	0.07	7144.49	-0.10	1440.20	5700	$A^{19}$	7140.20	2.78
C108A	7115.71	0.07	7115.81	0.07	7113.57	0.10	<b>7111.23</b>	0.14	1420.98	5700	$A^{19}$	7120.98	2.45
C109A	7095.55	-0.05	7094.65	-0.04	7092.49	-0.01	<b>7091.66</b>	0.00	1391.66	5700	$A^{19}$	<b>7091.66</b>	2.37
RC101A	5253.86	-0.35	5253.97	-0.35	5237.19	-0.03	<b>5217.90</b>	0.33	1815.42	3420	$A^2B^8C^7$	5235.42	4.97
RC102A	5053.48	-0.47	5059.58	-0.59	5053.62	-0.48	<b>5018.47</b>	0.22	1639.69	3390	$A^4B^3C^9$	5029.69	5.64
RC103A	4892.80	-0.47	4868.94	0.02	4885.58	-0.32	<b>4822.21</b>	0.98	1480.00	3390	$A^4B^3C^9$	4870.00	5.14
RC104A	4783.31	-0.29	4762.85	0.14	4761.28	0.17	<b>4737.00</b>	0.68	1289.30	3480	$A^3B^1C^9D^1$	4769.30	4.97
RC105A	5112.91	0.10	5119.80	-0.03	5110.86	0.14	<b>5097.35</b>	0.41	1788.10	3330	$A^3B^{11}C^5$	5118.10	5.32
RC106A	4997.98	-0.79	4960.78	-0.04	4966.27	-0.15	<b>4935.91</b>	0.46	1568.62	3390	$A^4B^9C^6$	4958.62	6.01
RC107A	4862.67	-0.78	4828.17	-0.06	4819.91	0.11	<b>4783.08</b>	0.87	1405.21	3420	$A^4B^7C^7$	4825.21	5.37
RC108A	4736.50	0.38	4734.15	0.43	4749.44	0.11	<b>4708.85</b>	0.97	1244.77	3510	$A^1B^2C^9D^1$	4754.77	4.71
R201A	3779.12	-0.50	3922.00	-4.3	<b>3753.42</b>	0.19	3782.88	-0.6	1510.43	2250	$A^5$	3760.43	8.97
R202A	3578.91	-0.70	3610.38	-1.58	3551.12	0.09	<b>3540.03</b>	0.40	1304.20	2250	$A^5$	3554.20	9.98
R203A	3334.08	-0.56	3350.18	-1.05	3336.60	-0.64	<b>3311.35</b>	0.13	1065.50	2250	$A^5$	3315.50	8.76
R204A	3143.68	-2.20	3390.14	-10.20	3103.84	-0.91	<b>3075.95</b>	0.00	825.95	2250	$A^5$	<b>3075.95</b>	7.98
R205A	3371.47	-1.12	3465.81	-3.95	3367.90	-1.01	<b>3334.27</b>	0.00	1084.27	2250	$A^5$	<b>3334.27</b>	8.45
R206A	3272.79	-0.29	3268.36	-0.15	3264.70	-0.04	<b>3242.40</b>	0.64	1013.40	2250	$A^5$	3263.40	8.17
R207A	3213.60	-1.94	3231.26	-2.51	3158.69	-0.20	<b>3145.08</b>	0.23	902.29	2250	$A^5$	3152.29	9.29
R208A	3064.76	-1.58	3063.10	-1.52	3056.45	-1.30	3017.52	-0.01	767.12	2250	$A^5$	<b>3017.12*</b>	8.51
R209A	3191.63	0.08	3192.95	0.04	3194.74	-0.01	<b>3183.36</b>	0.34	944.28	2250	$A^5$	3194.28	9.37
R210A	3338.75	-0.89	3375.38	-2.00	3325.28	-0.48	<b>3287.66</b>	0.65	1059.26	2250	$A^5$	3309.26	8.79
R211A	3061.47	-1.35	3042.48	-0.73	3053.08	-1.08	<b>3019.93</b>	0.02	770.56	2250	$A^5$	3020.56	7.99
C201A	<b>5820.78</b>	0.16	5891.45	-1.05	<b>5820.78</b>	0.16	5878.54	-0.80	830.20	5000	$A^5$	5830.20	5.00
C202A	5779.59	-0.05	5850.26	-1.27	5783.76	-0.12	<b>5776.88</b>	0.00	776.88	5000	$A^5$	<b>5776.88</b>	5.17
C203A	5750.58	-0.15	5741.90	-0.00	5736.94	0.09	<b>5741.12</b>	0.00	741.89	5000	$A^5$	<b>5741.12</b>	4.76
C204A	5721.09	-0.72	5691.51	-0.19	5718.49	-0.67	<b>5680.46</b>	0.00	680.46	5000	$A^5$	<b>5680.46</b>	4.21
C205A	5750.53	0.02	5786.71	-0.61	<b>5747.67</b>	0.06	5781.15	-0.50	751.40	5000	$A^5$	5751.40	6.79
C206A	5757.93	-0.29	5795.15	-0.94	<b>5738.09</b>	0.06	5767.70	-0.50	741.30	5000	$A^5$	5741.30	4.3
C207A	5723.91	0.02	5743.52	-0.32	<b>5721.16</b>	0.07	5731.44	-0.10	725.10	5000	$A^5$	5725.10	4.17
C208A	5767.78	-0.75	5884.20	-2.78	5732.95	-0.14	<b>5725.03</b>	0.00	725.03	5000	$A^5$	<b>5725.03</b>	5.21
RC201A	4726.22	-0.39	4740.21	-0.69	<b>4701.88</b>	0.13	4737.59	-0.60	2007.80	2700	$A^{18}$	4707.80	4.50
RC202A	4518.49	0.02	4522.36	-0.07	4509.11	0.23	<b>4487.48</b>	0.71	1619.40	2900	$A^{10}B^4$	4519.40	4.67
RC203A	4327.57	-0.20	4312.52	0.15	4313.42	0.13	<b>4305.49</b>	0.32	1469.10	2850	$A^{12}B^3$	4319.10	5.27
RC204A	4166.73	-0.26	4141.04	0.35	4157.32	-0.04	<b>4137.93</b>	0.43	1005.77	3150	$A^2B^5C^2$	4155.77	5.19
RC205A	4645.41	-1.08	4652.57	-1.24	4585.20	0.23	<b>4615.04</b>	-0.40	1795.67	2800	$A^{14}B^2$	4595.67	6.89
RC206A	4416.41	0.40	4431.64	0.06	4427.73	0.15	<b>4405.16</b>	0.66	1584.30	2850	$A^9B^3C^1$	4434.30	5.03
RC207A	4338.94	-0.53	4310.11	0.13	4313.07	0.07	<b>4290.14</b>	0.60	1215.90	3100	$A^4B^7$	4315.90	6.27
RC208A	4109.90	-0.70	4091.92	-0.26	4103.31	-0.54	<b>4075.04</b>	0.16	1031.37	3050	$A^5B^5C^1$	4081.37	5.17

Table A.2: Results for FT for cost structure  $B$ 

Instance set	ReVNTS		MDA		AMP		UHGS		HEA				
	TC	Dev	TC	Dev	TC	Dev	TC	Dev	DC	VC	Mix	TC	Time
R101B	<b>2421.19</b>	0.16	2486.76	-2.54	<b>2421.19</b>	0.16	<b>2421.19</b>	0.16	1849.10	576	$A^1B^4C^9D^5$	2425.10	3.78
R102B	2219.03	-0.30	2227.48	-0.68	<b>2209.50</b>	0.13	<b>2209.50</b>	0.13	1608.37	604	$A^2B^1C^6D^8$	2212.37	3.97
R103B	1955.57	-0.18	<b>1938.93</b>	0.67	1953.50	-0.08	<b>1938.93</b>	0.67	1313.99	638	$A^1B^1C^4D^6E^2$	1951.99	4.28
R104B	1732.26	-1.01	1714.73	0.01	<b>1713.36</b>	0.09	<b>1713.36</b>	0.09	1026.86	688	$A^1C^1D^5E^4$	1714.86	4.01
R105B	2030.83	-0.29	2027.98	-0.15	2030.83	-0.29	2027.98	-0.15	1436.91	588	$B^3C^5D^8$	<b>2024.91*</b>	3.68
R106B	1924.03	-0.1	1919.03	0.16	<b>1919.02</b>	0.16	<b>1919.02</b>	0.16	1338.10	584	$B^1C^6D^8$	1922.10	4.19
R107B	1781.01	0.12	1789.58	-0.36	<b>1780.52</b>	0.15	<b>1780.52</b>	0.15	1127.20	656	$C^2D^8E^2$	1783.20	5.30
R108B	1667.51	-0.36	1649.24	0.74	1665.78	-0.25	<b>1649.24</b>	0.74	983.58	678	$C^1D^5E^4$	1661.58	4.78
R109B	1844.99	-0.87	<b>1828.63</b>	0.03	1840.54	-0.63	<b>1828.63</b>	0.03	1185.10	644	$B^1C^1D^{10}E^1$	1829.10	4.91
R110B	1792.75	-0.78	<b>1774.46</b>	0.24	1788.18	-0.53	<b>1774.46</b>	0.24	1178.80	600	$B^1C^3D^{10}$	1778.80	5.21
R111B	1780.03	-0.27	<b>1769.71</b>	0.31	1772.51	0.15	<b>1769.71</b>	0.31	1141.24	634	$C^3D^7E^2$	1775.24	4.78
R112B	1677.13	-0.01	<b>1669.78</b>	0.43	1667.00	0.60	1667.00	0.60	1071.00	606	$C^2D^{11}$	1677.00	6.21
C101B	<b>2417.52</b>	0.00	<b>2417.52</b>	0.00	<b>2417.52</b>	0.00	<b>2417.52</b>	0.00	977.52	1440	$A^8B^6$	<b>2417.52</b>	1.99
C102B	<b>2350.54</b>	0.00	<b>2350.54</b>	0.00	<b>2350.54</b>	0.00	<b>2350.54</b>	0.00	930.54	1420	$A^5B^7$	<b>2350.54</b>	2.45
C103B	2349.42	-0.18	2353.64	-0.36	2347.99	-0.11	2347.99	-0.11	925.31	1420	$A^5B^7$	<b>2345.31*</b>	3.47
C104B	2332.94	-0.10	2328.62	0.08	<b>2325.78</b>	0.21	<b>2325.78</b>	0.21	950.59	1380	$A^7B^6$	2330.59	3.09
C105B	2374.01	0.10	<b>2373.53</b>	0.12	2375.04	0.06	<b>2373.53</b>	0.12	956.45	1420	$A^5B^7$	2376.45	3.06
C106B	2381.14	0.22	2404.56	-0.76	<b>2381.14</b>	0.22	<b>2381.14</b>	0.22	966.43	1420	$A^5B^7$	2386.43	2.95
C107B	2357.52	0.06	2370	-0.47	2357.67	0.06	<b>2357.52</b>	0.06	939.00	1420	$A^5B^7$	2359.00	2.45
C108B	<b>2346.38</b>	0.08	<b>2346.38</b>	0.08	<b>2346.38</b>	0.08	<b>2346.38</b>	0.08	968.15	1380	$A^7B^6$	2348.15	2.79
C109B	2346.58	-0.38	2339.89	-0.10	<b>2336.29</b>	0.06	<b>2336.29</b>	0.06	957.6	1380	$A^7B^6$	2337.60	2.56
RC101B	2469.50	-0.22	<b>2462.60</b>	0.06	2464.66	-0.02	<b>2462.60</b>	0.06	1732.19	732	$A^1B^4C^{10}$	2464.19	4.47
RC102B	2277.79	-0.32	<b>2263.45</b>	0.31	2272.68	-0.10	<b>2263.45</b>	0.31	1538.43	732	$A^1B^3C^9D^1$	2270.43	4.12
RC103B	2057.55	-0.80	<b>2035.62</b>	0.27	2041.24	-0.00	<b>2035.62</b>	0.27	1291.20	750	$B^1C^9D^2$	2041.20	3.98
RC104B	1914.93	0.38	<b>1905.06</b>	0.90	1916.85	0.28	<b>1905.06</b>	0.90	1172.27	750	$B^1C^6D^4$	1922.27	4.21
RC105B	2337.93	-0.44	<b>2308.59</b>	0.82	2325.99	0.07	<b>2308.59</b>	0.82	1625.70	702	$A^1B^7C^8$	2327.70	4.56
RC106B	2168.44	-0.99	<b>2149.56</b>	-0.11	2160.45	-0.62	2149.56	-0.11	1415.14	732	$A^1B^2C^8D^2$	<b>2147.14*</b>	4.21
RC107B	2008.39	-0.62	<b>2000.77</b>	-0.23	2003.26	-0.36	2000.77	-0.23	1264.09	732	$A^1B^2C^5D^4$	<b>1996.09*</b>	4.19
RC108B	1906.69	0.12	1910.83	-0.10	1908.72	0.01	<b>1906.69</b>	0.12	1176.89	732	$A^1B^1C^7D^3$	1908.89	3.11
R201B	1965.10	-0.45	2002.53	-2.37	<b>1953.42</b>	0.14	<b>1953.42</b>	0.14	1456.21	500	$A^4B^1$	1956.21	6.21
R202B	1765.09	-0.72	1790.38	-2.17	<b>1751.12</b>	0.07	<b>1751.12</b>	0.07	1302.4	450	$A^5$	1752.40	8.00
R203B	1535.08	-1.31	1541.19	-1.72	1536.60	-1.41	1535.08	-1.31	1065.17	450	$A^5$	<b>1515.17*</b>	5.78
R204B	1306.72	-2.12	1284.33	-0.37	1303.84	-1.90	1284.33	-0.37	829.57	450	$A^5$	<b>1279.57*</b>	6.89
R205B	1575.75	-1.70	1563.62	-0.92	1560.07	-0.69	1560.07	-0.69	1099.39	450	$A^5$	<b>1549.39*</b>	6.49
R206B	1477.34	-1.86	1464.53	-0.98	1464.70	-0.99	1464.53	-0.98	1000.37	450	$A^5$	<b>1450.37*</b>	5.21
R207B	1386.84	-2.04	1380.41	-1.56	<b>1358.69</b>	0.04	<b>1358.69</b>	0.04	909.18	450	$A^5$	1359.18	6.31
R208B	1261.09	-3.34	1244.74	-2.00	1256.45	-2.96	1244.74	-2.00	770.36	450	$A^5$	<b>1220.36*</b>	5.47
R209B	1418.51	-2.37	1431.37	-3.30	1394.74	-0.66	1394.74	-0.66	935.65	450	$A^5$	<b>1385.65*</b>	7.14
R210B	1529.04	-2.23	1516.66	-1.40	1525.28	-1.97	1516.66	-1.40	1045.75	450	$A^5$	<b>1495.75*</b>	6.93
R211B	1268.14	-3.95	1255.06	-2.88	1253.08	-2.72	<b>1219.93</b>	0.00	770.56	450	$A^5$	<b>1219.93</b>	7.45
C201B	<b>1816.14</b>	0.25	1820.64	0.00	<b>1816.14</b>	0.25	1820.64	0.00	740.64	1080	$A^4B^1$	1820.64	3.11
C202B	<b>1768.51</b>	0.09	1795.40	-1.43	<b>1768.51</b>	0.09	<b>1768.51</b>	0.09	690.10	1080	$A^2B^1C^1$	1770.10	4.58
C203B	1744.28	-0.61	1733.63	0.00	1734.82	-0.07	<b>1733.63</b>	0.00	653.63	1080	$A^2B^1C^1$	<b>1733.63</b>	3.19
C204B	1736.09	-3.31	1708.69	-1.68	1716.18	-2.13	<b>1680.46</b>	0.00	680.46	1000	$A^5$	<b>1680.46</b>	3.17
C205B	1747.68	0.50	1782.74	-1.49	<b>1747.68</b>	0.50	1778.30	-1.24	716.54	1040	$A^1B^3$	1756.54	5.21
C206B	1756.93	0.92	1772.87	0.02	<b>1756.01</b>	0.97	1767.70	0.31	733.17	1040	$A^1B^3$	1773.17	3.46
C207B	1732.20	-0.16	1729.49	-0.01	1729.39	-0.00	1729.49	-0.01	689.39	1040	$A^1B^3$	<b>1729.39*</b>	2.97
C208B	1730.72	-0.38	1724.2	0.00	<b>1723.2</b>	0.06	1724.20	0.00	684.20	1040	$A^1B^3$	1724.20	3.13
RC201B	2231.69	0.19	2343.79	-4.83	2230.54	0.24	<b>2329.59</b>	-4.19	1615.90	620	$A^4B^4C^2$	2235.90	4.17
RC202B	2002.62	0.96	2091.53	-3.44	2022.54	-0.03	2057.66	-1.76	1392.00	630	$A^3B^3C^3$	<b>2022.00*</b>	5.47
RC203B	1843.72	-0.18	1852.74	-0.67	1841.26	-0.05	<b>1824.54</b>	0.86	1190.40	650	$B^3C^4$	1840.40	5.12
RC204B	1611.28	-3.57	1565.31	-0.62	1575.18	-1.25	1555.75	-0.01	885.74	670	$B^1C^4D^1$	<b>1555.74*</b>	4.98
RC205B	2195.62	-1.23	2195.75	-1.23	<b>2166.62</b>	0.11	2174.74	-0.26	1529.00	640	$A^2B^2C^4$	2169.00	6.47
RC206B	1887.23	0.60	1923.56	-1.31	1893.13	0.29	<b>1883.08</b>	0.82	1218.70	680	$B^5C^1D^1$	1898.70	4.14
RC207B	1780.72	-2.93	1745.85	-0.92	1743.23	-0.76	<b>1714.14</b>	0.92	1080.00	650	$B^3C^4$	1730.00	5.14
RC208B	1557.74	-4.50	1488.19	0.16	1526.78	-2.42	<b>1483.20</b>	0.50	830.64	660	$C^6$	1490.64	4.43

Table A.3: Results for FT for cost structure  $C$ 

Instance set	ReVNTS		MDA		AMP		UHGS		HEA				
	TC	Dev	TC	Dev	TC	Dev	TC	Dev	DC	VC	Mix	TC	Time
R101C	<b>2134.90</b>	0.11	2199.78	-2.93	<b>2134.90</b>	0.11	2199.79	-2.93	1840.20	297	$A^1B^2C^9D^6$	2137.20	3.14
R102C	<b>1913.37</b>	0.08	1925.55	-0.56	<b>1913.37</b>	0.08	1925.56	-0.56	1599.87	315	$A^2B^3C^4D^7E^1$	1914.87	6.21
R103C	1633.62	-0.77	<b>1609.94</b>	0.69	1631.47	-0.63	1615.38	0.36	1310.20	311	$A^1C^4D^8E^1$	1621.20	3.24
R104C	1382.82	-0.52	1370.84	0.35	1377.81	-0.16	<b>1363.26</b>	0.90	1025.60	350	$D^8E^3$	1375.60	4.47
R105C	1729.57	-0.44	<b>1722.05</b>	0.00	1729.57	-0.44	<b>1722.05</b>	0.00	1403.05	319	$B^2C^2D^{11}$	<b>1722.05</b>	3.17
R106C	1607.96	0.15	1602.87	0.47	1607.96	0.15	<b>1599.04</b>	0.71	1285.40	325	$A^1C^5D^6E^2$	1610.40	4.08
R107C	1455.09	-0.05	1456.02	-0.12	1452.52	0.12	<b>1442.97</b>	0.78	1126.30	328	$C^2D^8E^2$	1454.30	3.51
R108C	1331.54	-0.12	1336.28	-0.48	1330.28	-0.03	<b>1321.68</b>	0.62	979.92	350	$D^6E^4$	1329.92	5.33
R109C	1525.65	-1.23	1507.77	-0.04	1519.37	-0.81	<b>1505.59</b>	0.10	1185.10	322	$B^1C^1D^{10}E^1$	1507.10	4.73
R110C	1463.91	-0.89	1446.41	0.32	1457.43	-0.44	<b>1443.92</b>	0.49	1109.06	342	$C^3D^4E^4$	1451.06	5.46
R111C	1451.92	-1.09	1447.88	-0.80	1443.34	-0.49	<b>1423.47</b>	0.89	1098.32	338	$B^1D^9E^2$	1436.32	6.14
R112C	1355.78	-1.09	1335.41	0.42	1339.44	0.12	<b>1329.07</b>	0.90	988.10	353	$C^2D^5E^4$	1341.10	4.17
C101C	1628.94	0.00	<b>1628.31</b>	0.04	1628.94	0.00	1628.94	0.00	828.94	800	$B^{10}$	1628.94	1.97
C102C	<b>1610.96</b>	0.00	<b>1610.96</b>	0.00	<b>1610.96</b>	0.00	<b>1610.96</b>	0.00	860.96	750	$A^1B^9$	<b>1610.96</b>	2.53
C103C	1611.14	-0.25	1619.68	-0.78	<b>1607.14</b>	0.00	<b>1607.14</b>	0.00	857.14	750	$A^1B^9$	<b>1607.14</b>	3.79
C104C	1610.07	-0.68	1613.96	-0.92	<b>1598.50</b>	0.04	1599.90	-0.04	869.21	730	$A^3B^8$	1599.21	2.89
C105C	1628.94	0.00	<b>1628.38</b>	0.03	1628.94	0.00	1628.94	0.00	828.94	800	$B^{10}$	1628.94	1.97
C106C	<b>1628.94</b>	0.00	<b>1628.94</b>	0.00	<b>1628.94</b>	0.00	<b>1628.94</b>	0.00	828.94	800	$B^{10}$	<b>1628.94</b>	2.01
C107C	1628.94	0.00	<b>1628.38</b>	0.03	1628.94	0.00	1628.94	0.00	828.94	800	$B^{10}$	1628.94	1.99
C108C	<b>1622.89</b>	0.13	<b>1622.89</b>	0.13	<b>1622.89</b>	0.13	<b>1622.89</b>	0.13	825	800	$B^{10}$	1625.00	2.45
C109C	1619.02	-0.03	<b>1614.99</b>	0.22	<b>1614.99</b>	0.22	1615.93	0.17	888.61	730	$A^3B^8$	1618.61	3.54
RC101C	2089.37	0.13	2084.48	0.36	2089.37	0.13	<b>2082.95</b>	0.44	1702.10	390	$B^7C^5D^3$	2092.10	4.54
RC102C	1918.96	-0.90	1895.92	0.31	1906.68	-0.25	<b>1895.05</b>	0.36	1529.89	372	$A^2B^2C^8D^2$	1901.89	4.19
RC103C	1674.50	-0.83	1660.62	0.00	1666.24	-0.33	<b>1650.30</b>	0.63	1300.7	360	$C^{12}$	1660.70	3.56
RC104C	1543.55	-0.19	1537.09	0.23	1540.13	0.03	<b>1526.04</b>	0.95	1159.60	381	$A^1C^5D^5$	1540.60	3.47
RC105C	1972.57	-0.84	1957.52	-0.07	<b>1953.99</b>	0.11	1957.14	-0.05	1584.09	372	$A^2B^2C^8D^2$	1956.09	4.16
RC106C	1793.12	-0.71	1776.08	0.25	1787.69	-0.41	<b>1774.94</b>	0.31	1393.45	387	$A^2B^1C^6D^4$	1780.45	3.49
RC107C	1635.65	-0.95	1614.04	0.39	1622.90	-0.16	<b>1607.11</b>	0.81	1245.30	375	$B^3C^5D^4$	1620.30	3.07
RC108C	1531.69	0.06	1535.14	-0.17	1531.69	0.06	<b>1523.96</b>	0.56	1157.60	375	$B^2C^6D^4$	1532.60	3.56
R201C	1745.39	-0.82	1729.92	0.07	1728.42	0.16	<b>1716.02</b>	0.88	1461.20	270	$A^6$	1731.20	6.78
R202C	1537.33	-0.50	1537.35	-0.50	1527.92	0.12	<b>1515.96</b>	0.90	1304.70	225	$A^5$	1529.70	8.14
R203C	1338.42	-3.22	1308.70	-0.92	1311.60	-1.15	<b>1286.35</b>	0.80	1071.72	225	$A^5$	1296.72	6.50
R204C	1080.66	-2.64	1062.46	-0.91	1085.71	-3.12	<b>1050.95</b>	0.19	802.90	250	$A^5$	1052.90	7.89
R205C	1350.12	-2.66	1311.84	0.26	1335.07	-1.51	<b>1309.27</b>	0.45	1090.20	225	$A^5$	1315.20	6.71
R206C	1254.67	-2.26	1251.51	-2.00	1239.70	-1.04	<b>1216.35</b>	0.86	1001.93	225	$A^5$	1226.93	6.59
R207C	1186.05	-5.38	1149.23	-2.11	1139.61	-1.25	<b>1120.08</b>	0.48	900.50	225	$A^5$	1125.50	6.98
R208C	1022.31	-2.44	1009.26	-1.13	1022.11	-2.42	<b>992.12</b>	0.59	772.97	225	$A^5$	997.97	5.87
R209C	1233.07	-5.91	1178.45	-1.21	1171.41	-0.61	<b>1155.79</b>	0.73	939.31	225	$A^4B^1$	1164.31	7.14
R210C	1284.72	-1.18	1289.35	-1.55	1281.08	-0.90	<b>1257.89</b>	0.93	1019.70	250	$A^4B^1$	1269.70	6.14
R211C	1061.70	-6.64	1013.84	-1.83	1028.08	-3.26	<b>994.93</b>	0.07	770.58	225	$A^5$	995.58	6.17
C201C	1269.41	-1.47	1269.41	-1.47	1269.41	-1.47	1269.41	-1.47	650.97	600	$A^2C^2$	<b>1250.97*</b>	2.97
C202C	1252.24	-0.92	1242.66	-0.15	1244.54	-0.30	<b>1239.54</b>	0.11	700.86	540	$A^2B^1C^1$	1240.86	3.54
C203C	1228.13	-2.89	<b>1193.63</b>	0.00	1203.42	-0.82	<b>1193.63</b>	0.00	653.63	540	$A^2B^1C^1$	<b>1193.63</b>	3.14
C204C	1207.03	-2.59	<b>1176.52</b>	0.00	1188.18	-0.99	<b>1176.52</b>	0.00	636.52	540	$A^2B^1C^1$	<b>1176.52</b>	3.67
C205C	1245.51	-0.44	1245.62	-0.45	1239.60	0.04	<b>1238.30</b>	0.15	640.1	600	$A^2B^2$	1240.10	4.29
C206C	1229.63	-0.03	1245.05	-1.29	<b>1229.23</b>	0.00	1238.30	-0.74	629.23	600	$A^2C^2$	<b>1229.23</b>	4.38
C207C	1221.16	-0.97	1215.42	-0.49	1213.07	-0.30	1209.49	-0.01	689.48	520	$A^2B^1C^1$	<b>1209.48*</b>	3.56
C208C	1210.72	-0.54	<b>1204.20</b>	0.00	1205.18	-0.08	<b>1204.20</b>	0.00	684.2	520	$A^1B^3$	<b>1204.20</b>	3.01
RC201C	1957.60	-2.07	2004.53	-4.52	<b>1915.42</b>	0.13	1996.79	-4.11	1577.90	340	$A^3B^3C^2D^1$	1917.90	4.65
RC202C	1699.48	-1.16	1766.52	-5.15	<b>1677.62</b>	0.14	1732.66	-3.13	1355.00	325	$A^1B^5C^1D^1$	1680.00	6.10
RC203C	1510.13	-0.66	1517.98	-1.19	1504.35	-0.28	<b>1496.11</b>	0.27	1160.20	340	$A^2B^1C^3E^1$	1500.20	6.27
RC204C	1256.91	-2.84	1238.66	-1.35	1241.45	-1.58	<b>1220.75</b>	0.12	887.16	335	$B^1C^4E^1$	1222.16	5.47
RC205C	1901.71	-4.32	1854.22	-1.71	<b>1822.07</b>	0.05	1844.74	-1.19	1453	370	$B^2C^4D^1$	1823.00	5.29
RC206C	1598.84	-2.21	1590.22	-1.66	1586.61	-1.43	<b>1553.65</b>	0.68	1224.3	340	$B^5C^1E^1$	1564.30	4.70
RC207C	1431.65	-3.61	1396.16	-1.05	1406.26	-1.78	<b>1377.52</b>	0.30	1026.71	355	$C^3D^1E^1$	1381.71	5.67
RC208C	1181.47	-2.61	1145.84	0.48	1175.23	-2.07	<b>1140.10</b>	0.98	821.40	330	$C^6$	1151.40	5.17

Table A.4: Results for FD for cost structure A

Instance set	MDA		BPDRT		UHGS		HEA				
	TC	Dev	TC	Dev	TC	Dev	DC	VC	Mix	TC	Time
R101A	4349.80	-0.75	4342.72	-0.58	<b>4314.36</b>	0.07	1787.52	2530	$A^1B^{10}C^{12}$	4317.52	4.14
R102A	4196.46	-0.54	4189.21	-0.37	<b>4166.28</b>	0.18	1623.84	2550	$A^1B^5C^{15}$	4173.84	5.98
R103A	4052.85	-0.53	4051.62	-0.50	<b>4027.36</b>	0.10	1401.40	2630	$B^1C^{18}$	4031.40	5.21
R104A	3978.48	-0.81	3972.65	-0.66	<b>3936.40</b>	0.25	1276.44	2670	$B^3C^{15}D^1$	3946.44	4.12
R105A	4161.72	-0.67	4152.50	-0.45	<b>4122.50</b>	0.28	1574.06	2560	$A^1B^5C^{15}$	4134.06	6.01
R106A	4095.20	-0.87	4085.30	-0.62	<b>4048.59</b>	0.28	1500.05	2560	$B^4C^{16}$	4060.05	5.12
R107A	4006.61	-0.54	3996.74	-0.29	<b>3970.51</b>	0.37	1395.12	2590	$B^3C^{15}D^1$	3985.12	4.78
R108A	3961.38	-0.73	3949.50	-0.43	<b>3928.12</b>	0.11	1342.60	2590	$B^3C^{15}D^1$	3932.60	6.54
R109A	4048.29	-0.58	4035.89	-0.27	<b>4015.71</b>	0.23	1464.83	2560	$B^4C^{16}$	4024.83	6.12
R110A	3997.88	-0.61	3991.63	-0.46	<b>3961.68</b>	0.30	1373.51	2600	$B^1C^{18}$	3973.51	5.21
R111A	4011.63	-0.59	4009.61	-0.54	<b>3964.99</b>	0.58	1368.00	2620	$B^3C^{15}D^1$	3988.00	5.12
R112A	3962.73	-0.83	3954.19	-0.61	<b>3918.88</b>	0.29	1300.19	2630	$C^{17}D^1$	3930.19	4.71
C101A	7098.04	-0.06	7097.93	-0.06	<b>7093.45</b>	0.00	1393.45	5700	$A^{19}$	<b>7093.45</b>	2.47
C102A	7086.11	-0.08	7085.47	-0.07	<b>7080.17</b>	0.00	1380.17	5700	$A^{19}$	<b>7080.17</b>	2.65
C103A	7080.35	-0.02	7080.41	-0.02	<b>7079.21</b>	0.00	1379.21	5700	$A^{19}$	<b>7079.21</b>	2.01
C104A	7076.90	-0.03	<b>7075.06</b>	0.00	<b>7075.06</b>	0.00	1375.06	5700	$A^{19}$	<b>7075.06</b>	1.97
C105A	7096.19	-0.04	7096.22	-0.04	<b>7093.45</b>	0.00	1393.45	5700	$A^{19}$	<b>7093.45</b>	2.65
C106A	7086.91	-0.04	7088.35	-0.06	<b>7083.87</b>	0.00	1383.87	5700	$A^{19}$	<b>7083.87</b>	2.17
C107A	7084.92	-0.00	7090.91	-0.09	<b>7084.61</b>	0.00	1384.61	5700	$A^{19}$	<b>7084.61</b>	2.39
C108A	7082.49	-0.04	7081.18	-0.02	<b>7079.66</b>	0.00	1379.66	5700	$A^{19}$	<b>7079.66</b>	1.97
C109A	7078.13	-0.01	7077.68	-0.01	<b>7077.30</b>	0.00	1377.30	5700	$A^{19}$	<b>7077.30</b>	2.19
RC101A	5180.74	-0.14	5168.23	0.10	<b>5150.86</b>	0.44	1843.47	3330	$A^3B^{13}C^4$	5173.47	5.14
RC102A	5029.59	-0.21	5025.22	-0.13	<b>4987.24</b>	0.63	1658.83	3360	$A^6B^6C^7$	5018.83	4.26
RC103A	4895.57	-0.94	4888.53	-0.79	<b>4804.61</b>	0.94	1430.20	3420	$A^2B^6C^8$	4850.20	6.47
RC104A	4760.56	-0.74	4747.38	-0.47	<b>4717.63</b>	0.16	1395.40	3330	$A^3B^2C^8D^1$	4725.40	5.29
RC105A	5060.37	-0.23	5068.54	-0.39	<b>5035.35</b>	0.27	1748.86	3300	$A^5B^8C^6$	5048.86	4.78
RC106A	4997.86	-0.68	4972.11	-0.16	<b>4936.74</b>	0.55	1514.13	3450	$B^7C^8$	4964.13	5.29
RC107A	4865.76	-0.83	4861.04	-0.73	<b>4788.69</b>	0.76	1435.60	3390	$A^4B^5C^8$	4825.60	4.17
RC108A	4765.37	-0.86	4753.12	-0.60	<b>4708.85</b>	0.34	1334.79	3390	$A^4B^2C^8D^1$	4724.79	4.63
R201A	3484.95	-1.11	3530.24	-2.42	<b>3446.78</b>	0.00	1196.78	2250	$A^5$	<b>3446.78</b>	6.13
R202A	3335.95	-1.17	3335.61	-1.16	3308.16	-0.33	1047.42	2250	$A^5$	<b>3297.42*</b>	7.46
R203A	3173.95	-1.05	3164.03	-0.73	<b>3141.09</b>	0.00	891.09	2250	$A^5$	<b>3141.09</b>	6.14
R204A	3065.15	-1.56	3029.83	-0.39	<b>3018.14</b>	0.00	768.14	2250	$A^5$	<b>3018.14</b>	6.28
R205A	3277.69	-1.82	3261.19	-1.31	<b>3218.97</b>	0.00	968.97	2250	$A^5$	<b>3218.97</b>	6.38
R206A	3173.30	-0.86	3165.85	-0.62	<b>3146.34</b>	0.00	896.34	2250	$A^5$	<b>3146.34</b>	8.14
R207A	3136.47	-1.92	3102.79	-0.83	3077.58	-0.01	827.36	2250	$A^5$	<b>3077.36*</b>	6.47
R208A	3050.00	-1.76	3009.13	-0.40	<b>2997.24</b>	0.00	747.25	2250	$A^5$	<b>2997.25</b>	6.34
R209A	3155.73	-1.16	3155.60	-1.16	3122.42	-0.09	869.56	2250	$A^5$	<b>3119.56*</b>	4.99
R210A	3219.23	-1.54	3206.23	-1.13	3174.85	-0.14	920.41	2250	$A^5$	<b>3170.41*</b>	5.47
R211A	3055.04	-1.16	3026.02	-0.20	<b>3019.93</b>	0.00	769.93	2250	$A^5$	<b>3019.93</b>	7.93
C201A	5701.45	-0.11	5700.87	-0.10	<b>5695.02</b>	0.00	695.02	5000	$A^5$	<b>5695.02</b>	3.46
C202A	5689.70	-0.08	5689.70	-0.08	<b>5685.24</b>	0.00	685.24	5000	$A^5$	<b>5685.24</b>	3.17
C203A	5685.82	-0.08	<b>5681.55</b>	0.00	<b>5681.55</b>	0.00	681.55	5000	$A^5$	<b>5681.55</b>	4.29
C204A	5690.30	-0.22	<b>5677.69</b>	0.00	<b>5677.66</b>	0.00	677.67	5000	$A^5$	<b>5677.66</b>	3.97
C205A	5691.70	-0.01	5691.70	-0.01	<b>5691.36</b>	0.00	691.36	5000	$A^5$	<b>5691.36</b>	3.46
C206A	5691.70	-0.04	5691.70	-0.04	<b>5689.32</b>	0.00	689.32	5000	$A^5$	<b>5689.32</b>	2.97
C207A	5689.82	-0.04	5692.36	-0.09	<b>5687.35</b>	0.00	687.35	5000	$A^5$	<b>5687.35</b>	4.10
C208A	<b>5686.50</b>	0.00	5689.59	-0.05	<b>5686.50</b>	0.00	686.50	5000	$A^5$	<b>5686.50</b>	3.56
RC201A	4407.68	-0.71	4404.07	-0.62	4374.09	0.06	1476.82	2900	$A^{10}B^4$	4376.82	5.14
RC202A	4277.67	-0.78	4266.96	-0.53	<b>4244.63</b>	0.00	1294.63	2950	$A^8B^5$	<b>4244.63</b>	4.26
RC203A	4204.85	-0.83	4189.94	-0.47	<b>4170.17</b>	0.00	1120.17	3050	$A^6B^3C^2$	<b>4170.17</b>	6.14
RC204A	4109.86	-0.56	4098.34	-0.27	<b>4087.11</b>	0.00	937.112	3150	$A^5B^2C^3$	<b>4087.11</b>	5.47
RC205A	4329.96	-0.84	4304.52	-0.25	<b>4291.93</b>	0.04	1343.73	2950	$A^8B^5$	4293.73	4.19
RC206A	4272.08	-0.48	4272.82	-0.49	<b>4251.88</b>	0.00	1251.88	3000	$A^6B^6$	<b>4251.88</b>	4.27
RC207A	4232.81	-1.20	4219.52	-0.89	4185.98	-0.08	1182.44	3000	$A^6B^6$	<b>4182.44*</b>	5.64
RC208A	4095.71	-0.51	4093.83	-0.46	<b>4075.04</b>	0.00	975.04	3100	$A^4B^4C^2$	<b>4075.04</b>	5.31

Table A.5: Results for FD for cost structure  $B$ 

Instance set	MDA		BPDRT		UHGS		HEA				
	TC	Dev	TC	Dev	TC	Dev	DC	VC	Mix	TC	Time
R101B	2226.94	-0.20	-	-	2228.67	-0.27	1664.56	558	$B^3C^{13}D^2$	<b>2222.56*</b>	4.27
R102B	2071.90	-1.16	-	-	2073.63	-1.25	1476.12	572	$A^1B^2C^{10}D^5$	<b>2048.12*</b>	3.28
R103B	1857.22	-0.08	-	-	<b>1853.66</b>	0.11	1249.74	606	$A^1C^7D^6E^1$	1855.74	5.27
R104B	1707.31	-1.24	-	-	<b>1683.33</b>	0.18	1026.42	660	$A^1C^1D^{10}E^1$	1686.42	5.09
R105B	1995.07	-0.71	-	-	1988.86	-0.40	1390.96	590	$C^{10}D^6$	<b>1980.96*</b>	3.37
R106B	1903.95	-0.72	-	-	<b>1888.31</b>	0.10	1290.28	600	$C^9D^5E^1$	1890.28	4.19
R107B	1766.18	-0.81	-	-	1753.35	-0.08	1140.02	612	$C^4D^8E^1$	<b>1752.02*</b>	5.26
R108B	1666.89	-1.06	-	-	<b>1647.88</b>	0.09	983.37	666	$B^1C^1D^8E^1$	1649.37	3.97
R109B	1833.54	-0.79	-	-	<b>1818.15</b>	0.05	1209.10	610	$B^1C^4D^8E^1$	1819.10	3.99
R110B	1781.74	-1.12	-	-	<b>1758.64</b>	0.19	1161.96	600	$C^2D^{11}$	1761.96	5.47
R111B	1768.74	-1.47	-	-	<b>1740.86</b>	0.13	1121.16	622	$C^4D^8E^1$	1743.16	5.69
R112B	1675.76	-0.76	-	-	<b>1661.85</b>	0.07	1029.09	634	$C^1D^{10}E^1$	1663.09	5.01
C101B	2340.98	-0.04	-	-	<b>2340.15</b>	0.00	960.15	1380	$A^7B^6$	<b>2340.15</b>	2.98
C102B	2326.53	-0.04	-	-	<b>2325.70</b>	0.00	945.70	1380	$A^7B^6$	<b>2325.70</b>	2.73
C103B	2325.61	-0.04	-	-	<b>2324.60</b>	0.00	944.60	1380	$A^7B^6$	<b>2324.60</b>	3.64
C104B	<b>2318.04</b>	0.00	-	-	<b>2318.04</b>	0.00	938.04	1380	$A^7B^6$	<b>2318.04</b>	2.98
C105B	2344.64	-0.19	-	-	<b>2340.15</b>	0.00	960.15	1380	$A^7B^6$	<b>2340.15</b>	2.71
C106B	2345.85	-0.24	-	-	<b>2340.15</b>	0.00	960.15	1380	$A^7B^6$	<b>2340.15</b>	3.19
C107B	2345.60	-0.23	-	-	<b>2340.15</b>	0.00	960.15	1380	$A^7B^6$	<b>2340.15</b>	2.94
C108B	2340.17	-0.07	-	-	<b>2338.58</b>	0.00	958.58	1380	$A^7B^6$	<b>2338.58</b>	3.88
C109B	<b>2328.55</b>	0.00	-	-	<b>2328.55</b>	0.00	948.55	1380	$A^7B^6$	<b>2328.55</b>	3.12
RC101B	2417.16	-0.40	-	-	2412.71	-0.22	1693.43	714	$A^2B^7C^8$	<b>2407.43*</b>	3.46
RC102B	2234.47	-0.69	-	-	<b>2213.92</b>	0.24	1487.23	732	$A^2B^7C^5D^2$	2219.23	5.14
RC103B	2025.74	-0.51	-	-	2016.28	-0.04	1295.55	720	$B^1C^{10}D^1$	<b>2015.55*</b>	3.69
RC104B	1912.65	-0.86	-	-	1897.04	-0.03	1146.40	750	$B^1C^6D^4$	<b>1896.40*</b>	4.57
RC105B	2296.16	-0.96	-	-	2287.51	-0.58	1530.28	744	$A^1B^6C^6D^2$	<b>2274.28*</b>	5.69
RC106B	2157.84	-1.21	-	-	2140.86	-0.41	1400.13	732	$A^1B^2C^8D^2$	<b>2132.13*</b>	3.12
RC107B	2008.02	-1.18	-	-	1989.34	-0.24	1252.67	732	$A^1B^2C^5D^1$	<b>1984.67*</b>	2.45
RC108B	1920.91	-1.32	-	-	1898.96	-0.16	1133.97	762	$B^1C^6D^4$	<b>1895.97*</b>	2.67
R201B	1687.44	-2.47	-	-	<b>1646.78</b>	0.00	1196.78	450	$A^5$	<b>1646.78*</b>	6.79
R202B	1527.74	-1.73	-	-	1508.16	-0.42	1051.81	450	$A^5$	<b>1501.81*</b>	7.23
R203B	1379.15	-2.84	-	-	<b>1341.09</b>	0.00	891.092	450	$A^5$	<b>1341.09</b>	4.56
R204B	1243.56	-2.09	-	-	<b>1218.14</b>	0.00	768.14	450	$A^5$	<b>1218.14</b>	4.11
R205B	1471.97	-3.60	-	-	<b>1418.97</b>	0.13	970.81	450	$A^5$	1420.81	6.47
R206B	1400.84	-3.97	-	-	<b>1346.34</b>	0.08	897.41	450	$A^5$	1347.41	6.99
R207B	1333.53	-4.30	-	-	<b>1277.58</b>	0.08	828.57	450	$A^5$	1278.57	6.78
R208B	1225.37	-2.23	-	-	<b>1197.24</b>	0.12	748.6	450	$A^5$	1198.70	5.47
R209B	1370.30	-3.62	-	-	<b>1322.42</b>	0.00	872.42	450	$A^5$	<b>1322.42</b>	5.47
R210B	1418.54	-3.51	-	-	1374.31	-0.28	920.41	450	$A^5$	<b>1370.41*</b>	5.93
R211B	1263.72	-3.54	-	-	<b>1219.93</b>	0.05	770.57	450	$A^5$	1220.57	7.81
C201B	1700.87	-0.35	-	-	<b>1695.02</b>	0.00	695.02	1000	$A^5$	<b>1695.02</b>	2.11
C202B	1687.84	-0.15	-	-	<b>1685.24</b>	0.00	685.24	1000	$A^5$	<b>1685.24</b>	2.33
C203B	1696.25	-0.87	-	-	<b>1681.55</b>	0.00	681.55	1000	$A^5$	<b>1681.55</b>	2.57
C204B	1705.94	-1.69	-	-	<b>1677.66</b>	0.00	677.66	1000	$A^5$	<b>1677.66</b>	3.69
C205B	1711.00	-1.16	-	-	<b>1691.36</b>	0.00	691.36	1000	$A^5$	<b>1691.36</b>	3.07
C206B	1691.70	-0.14	-	-	<b>1689.32</b>	0.00	689.32	1000	$A^5$	<b>1689.32</b>	3.19
C207B	1704.88	-1.04	-	-	<b>1687.35</b>	0.00	687.35	1000	$A^5$	<b>1687.35</b>	3.76
C208B	1689.59	-0.18	-	-	<b>1686.50</b>	0.00	686.50	1000	$A^5$	<b>1686.50</b>	2.41
RC201B	1965.31	-1.24	-	-	<b>1938.36</b>	0.14	1321.16	620	$A^4B^1C^4$	1941.16	6.98
RC202B	1771.87	-0.22	-	-	1772.81	-0.27	1128.04	640	$A^1B^1C^5$	<b>1768.04*</b>	6.47
RC203B	1619.55	-1.00	-	-	1604.04	-0.03	943.548	660	$A^1B^1C^5$	<b>1603.55*</b>	6.15
RC204B	1501.10	-0.79	-	-	1490.25	-0.07	829.27	660	$C^6$	<b>1489.27*</b>	3.47
RC205B	1853.58	-1.10	-	-	<b>1832.53</b>	0.04	1193.34	640	$A^1B^7C^1$	1833.34	3.98
RC206B	1761.49	-2.15	-	-	1725.44	-0.06	1074.41	650	$A^3B^1C^3D^1$	<b>1724.41*</b>	4.54
RC207B	1666.03	-0.96	-	-	<b>1646.37</b>	0.23	1000.23	650	$B^3C^4$	1650.23	5.01
RC208B	1494.11	-0.83	-	-	1483.20	-0.1	821.743	660	$C^6$	<b>1481.74*</b>	4.08

Table A.6: Results for FD for cost structure  $C$ 

Instance set	MDA		BPDRT		UHGS		HEA				
	TC	Dev	TC	Dev	TC	Dev	DC	VC	Mix	TC	Time
R101C	1951.20	-0.71	1951.89	-0.75	1951.20	-0.71	1629.38	308	$A^1B^8C^5D^6$	<b>1937.38*</b>	4.17
R102C	1770.40	-0.46	1778.29	-0.91	1785.35	-1.31	1465.22	297	$A^2C^{11}D^5$	<b>1762.22*</b>	3.23
R103C	1558.17	-0.72	1555.26	-0.54	1552.34	-0.35	1224.98	322	$A^1C^6D^7E^1$	<b>1546.98*</b>	3.69
R104C	1367.82	-1.14	1372.08	-1.46	1355.15	-0.21	1013.37	339	$A^1C^1D^5E^4$	<b>1352.37*</b>	5.17
R105C	1696.67	-0.91	1698.26	-1.00	1694.56	-0.78	1381.44	300	$B^3C^4D^9$	<b>1681.44*</b>	4.13
R106C	1589.25	-0.23	1590.11	-0.28	<b>1583.17</b>	0.16	1274.65	311	$B^2C^5D^7E^1$	1585.65	3.67
R107C	1435.21	-0.76	1439.81	-1.08	1428.08	-0.26	1080.37	344	$A^1C^1D^7E^3$	<b>1424.37*</b>	5.98
R108C	1334.75	-1.24	1334.68	-1.23	<b>1314.88</b>	0.27	968.444	350	$A^1C^1D^5E^4$	1318.44	4.78
R109C	1515.22	-0.54	1514.13	-0.47	<b>1506.59</b>	0.03	1185.1	322	$B^1C^1D^{10}E^1$	1507.10	4.11
R110C	1457.42	-0.97	1461.85	-1.28	1443.92	-0.04	1101.37	342	$B^1C^1D^{10}E^1$	<b>1443.37*</b>	4.78
R111C	1439.43	-1.41	1439.14	-1.39	1420.15	-0.05	1089.43	330	$A^1B^1D^7E^3$	<b>1419.43*</b>	5.14
R112C	1358.17	-2.27	1343.26	-1.15	<b>1327.58</b>	0.03	989.01	339	$C^1D^7E^3$	1328.01	4.67
C101C	<b>1628.94</b>	0.00	<b>1628.94</b>	0.00	<b>1628.94</b>	0.00	828.94	800	$B^{10}$	<b>1628.94</b>	1.99
C102C	<b>1597.66</b>	0.00	<b>1597.66</b>	0.00	<b>1597.66</b>	0.00	847.66	750	$A^1B^9$	<b>1597.66</b>	2.14
C103C	<b>1596.56</b>	0.00	<b>1596.56</b>	0.00	<b>1596.56</b>	0.00	846.56	750	$A^1B^9$	<b>1596.56</b>	2.65
C104C	1594.06	-0.21	1590.86	-0.01	<b>1590.76</b>	0.00	840.76	750	$A^1B^9$	<b>1590.76</b>	2.11
C105C	<b>1628.94</b>	0.00	<b>1628.94</b>	0.00	<b>1628.94</b>	0.00	828.94	800	$B^{10}$	<b>1628.94</b>	2.41
C106C	<b>1628.94</b>	0.00	<b>1628.94</b>	0.00	<b>1628.94</b>	0.00	828.94	800	$B^{10}$	<b>1628.94</b>	1.74
C107C	<b>1628.94</b>	0.00	<b>1628.94</b>	0.00	<b>1628.94</b>	0.00	828.94	800	$B^{10}$	<b>1628.94</b>	2.03
C108C	<b>1622.75</b>	0.00	<b>1622.75</b>	0.00	<b>1622.75</b>	0.00	892.75	730	$A^3B^8$	<b>1622.75</b>	2.56
C109C	<b>1614.99</b>	0.00	<b>1614.99</b>	0.00	1615.93	0.06	864.99	750	$A^1B^9$	<b>1614.99</b>	2.97
RC101C	2048.44	-0.72	2053.55	-0.97	2043.48	-0.47	1637.89	396	$A^1B^6C^8D^1$	<b>2033.89*</b>	4.16
RC102C	1860.48	-0.68	1872.49	-1.33	<b>1847.92</b>	0.00	1481.92	366	$A^1B^5C^5D^3$	<b>1847.92</b>	4.03
RC103C	1660.81	-0.88	1663.08	-1.02	<b>1646.35</b>	0.00	1271.35	375	$C^8D^3$	<b>1646.35</b>	4.17
RC104C	1536.24	-1.14	1540.61	-1.43	1522.04	-0.20	1143.96	375	$C^4D^6$	<b>1518.96*</b>	5.14
RC105C	1913.09	-1.49	1929.89	-2.39	1913.06	-1.49	1497.92	387	$A^2B^3C^8D^2$	<b>1884.92*</b>	4.57
RC106C	1772.05	-1.03	1776.52	-1.28	1770.95	-0.97	1372.99	381	$A^1B^2C^8D^2$	<b>1753.99*</b>	3.44
RC107C	1615.74	-0.91	1633.29	-2.01	1607.11	-0.37	1211.12	390	$B^1C^6D^4$	<b>1601.12*</b>	3.47
RC108C	1527.35	-0.72	1527.87	-0.76	1523.96	-0.50	1126.36	390	$A^1C^4D^6$	<b>1516.36*</b>	3.64
R201C	1441.46	-0.84	1466.13	-2.56	1443.41	-0.97	1204.50	225	$A^5$	<b>1429.50*</b>	4.54
R202C	1298.10	-1.96	1296.78	-1.86	1283.16	-0.79	1048.11	225	$A^5$	<b>1273.11*</b>	7.12
R203C	1145.38	-2.62	1127.28	-1.00	<b>1116.09</b>	0.00	891.09	225	$A^5$	<b>1116.09</b>	4.58
R204C	1019.77	-2.68	1000.89	-0.78	<b>993.14</b>	0.00	768.14	225	$A^5$	<b>993.14</b>	6.81
R205C	1222.03	-2.19	1240.74	-3.76	<b>1193.97</b>	0.15	970.81	225	$A^5$	1195.81	6.21
R206C	1138.26	-1.51	1141.13	-1.76	<b>1121.34</b>	0.00	896.34	225	$A^5$	<b>1121.34</b>	5.14
R207C	1086.42	-3.21	1067.97	-1.46	<b>1052.58</b>	0.00	827.58	225	$A^5$	<b>1052.58</b>	5.23
R208C	976.11	-0.25	979.50	-0.60	<b>969.90</b>	0.39	748.70	225	$A^5$	973.70	5.47
R209C	1140.96	-4.20	1140.96	-4.20	1097.42	-0.22	869.97	225	$A^5$	<b>1094.97*</b>	5.64
R210C	1161.87	-1.43	1170.29	-2.17	1149.85	-0.38	920.48	225	$A^5$	<b>1145.48*</b>	6.17
R211C	1015.84	-2.10	1008.54	-1.37	<b>994.93</b>	0.00	769.93	225	$A^5$	<b>994.93</b>	6.17
C201C	<b>1194.33</b>	0.00	<b>1194.33</b>	0.00	<b>1194.33</b>	0.00	694.33	500	$A^5$	<b>1194.33</b>	4.50
C202C	1189.35	-0.35	<b>1185.24</b>	0.00	<b>1185.24</b>	0.00	685.24	500	$A^5$	<b>1185.24</b>	2.36
C203C	<b>1176.25</b>	0.00	<b>1176.25</b>	0.00	<b>1176.25</b>	0.00	656.25	520	$A^1B^3$	<b>1176.25</b>	3.07
C204C	1176.55	-0.10	1176.55	-0.10	<b>1175.37</b>	0.00	675.37	500	$A^5$	<b>1175.37</b>	3.09
C205C	<b>1190.36</b>	0.00	<b>1190.36</b>	0.00	<b>1190.36</b>	0.00	690.36	500	$A^5$	<b>1190.36</b>	4.50
C206C	<b>1188.62</b>	0.00	<b>1188.62</b>	0.00	<b>1188.62</b>	0.00	668.62	520	$A^1B^3$	<b>1188.62</b>	3.99
C207C	<b>1184.88</b>	0.00	<b>1187.71</b>	-0.24	<b>1184.88</b>	0.00	684.88	500	$A^5$	<b>1184.88</b>	3.17
C208C	1187.86	-0.11	1186.50	0.00	1186.50	0.00	686.50	500	$A^5$	<b>1186.50</b>	2.87
RC201C	1632.41	-0.41	1630.53	-0.30	<b>1623.36</b>	0.14	1285.71	340	$A^1B^7C^1$	1625.71	6.01
RC202C	1459.84	-1.02	1461.44	-1.13	1447.27	-0.15	1095.12	350	$A^1B^3C^4$	<b>1445.12*</b>	4.12
RC203C	1295.07	-1.69	1292.92	-1.52	1274.04	-0.04	943.55	330	$B^3C^4$	<b>1273.55*</b>	3.67
RC204C	1171.26	-1.15	1162.91	-0.43	1159.00	-0.09	807.94	350	$C^2D^3$	<b>1157.94*</b>	5.14
RC205C	1525.28	-0.66	1632.67	-7.74	<b>1512.53</b>	0.19	1180.34	335	$A^1B^4C^3$	1515.34	5.01
RC206C	1425.15	-1.84	1420.89	-1.53	<b>1395.18</b>	0.30	1074.41	325	$A^1B^1C^5$	1399.41	3.27
RC207C	1332.40	-1.13	1328.29	-0.82	<b>1314.44</b>	0.23	987.50	330	$C^6$	1317.50	5.47
RC208C	1155.02	-1.31	1152.92	-1.12	<b>1140.10</b>	0.00	790.09	350	$C^2D^3$	<b>1140.10</b>	5.99