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Legendre orthogonal moments have been widely used in the field of Abstract image analysis. Because their computation by a direct method is very time expensive, recent efforts have been devoted to the reduction of computational complexity. Nevertheless, the existing algorithms are mainly focused on binary images. We propose here a new fast method for computing the Legendre moments, which is not only suitable for binary images but also for grey levels. We first set up the recurrence formula of one-dimensional (1D) Legendre moments by using the recursive property of Legendre polynomials. As a result, the 1D Legendre moments of order p, L_p = $L_p(0)$, can be expressed as a linear combination of $L_{p-1}(1)$ and $L_{p-2}(0)$. Based on this relationship, the 1D Legendre moments $L_p(0)$ is thus obtained from the array of $L_1(a)$ and $L_0(a)$ where a is an integer number less than p. To further decrease the computation complexity, an algorithm, in which no multiplication is required, is used to compute these quantities. The method is then extended to the calculation of the two-dimensional Legendre moments L_{pq} . We show that the proposed method is more efficient than the direct method.

Keywords: Legendre Moments; Fast algorithm; Recurrence formula; Grey level images

1 Introduction

Since Hu introduced the moment invariants [1], moments and moment functions of image intensity values have been successfully and widely used in the field of image analysis, such as object recognition, object representation, edge detection [2]. Orthogonal moments (e.g. Legendre moment and Zernike moment) can be used to represent an image with the minimum amount of information redundancy [3]. Since the computation of orthogonal moments of a two-dimensional (2D) image by a direct method involves a significant amount of arithmetic operations, some fast algorithms have been developed to reduce the computational complexity. However, the existing methods for fast computation of Legendre moments are mainly focused on binary image [4-6]. Now the moments of a grey level image are also used in many applications, such as texture analysis [7], therefore, we propose a fast algorithm for computing the Legendre moments for grey level images. The principle is as follows. The recurrence formula of one-dimensional (1D) Legendre moments is firstly established by using the recursive property of Legendre polynomials. The 1D Legendre moments of order p, $L_p = L_p(0)$, is expressed as a linear combination of $L_{p-1}(1)$ and $L_{p-2}(0)$. Based on this relationship, the 1D Legendre moments $L_p(0)$ can thus be obtained from the array of $L_1(a)$ and $L_0(a)$ where a is an integer number less than p. An algorithm based on a systolic array in which no multiplication is required is used to compute these quantities. We propose then an extension of the method to the 2D Legendre moment L_{pq} computation.

The remainder of this paper is organized as follows. In Section 2, we first

describe a new approach for computing 1D Legendre moments for a 1D signal, and then extend the method to the 2D Legendre moment calculation. Section 3 gives the detailed analysis of the computational complexity and some experimental results. Section 4 provides some concluding remarks.

2. Fast computation of 2D Legendre moments

The (p+q)th-order Legendre moment of an image with intensity function f(x, y) is defined by

$$L_{pq} = \frac{(2p+1)(2q+1)}{4} \int_{-1}^{1} \int_{-1}^{1} P_p(x) P_q(y) f(x,y) dx dy$$
(1)

where $P_p(x)$ is *p*th order Legendre polynomial given by

$$P_{p}(x) = \frac{1}{2^{p}} \sum_{k=0}^{n/2} (-1)^{k} \frac{(2p-2k)!}{k!(p-k)!(p-2k)!} x^{p-2k}, x \in [-1,1].$$
(2)

For a digital image of size $N \times N$, Eq. (1) can be approximated by

$$L_{pq} = \frac{(2p+1)(2q+1)}{(N-1)^2} \sum_{i=1}^{N} \sum_{j=1}^{N} P_p(x_i) P_q(y_j) f(x_i, y_j)$$
(3)

with $x_i = (2i - N - 1)/(N - 1), y_j = (2j - N - 1)/(N - 1).$

The Legendre polynomial obeys the following recursive relation

$$P_{p+1}(x) = \frac{2p+1}{p+1} x P_p(x) - \frac{p}{p+1} P_{p-1}(x), p \ge 1$$
(4)

with $P_0(x) = 1$, $P_1(x) = x$.

In the following, we present an algorithm for the fast calculation of the 2D Legendre moment for grey level images. For the sake of simplicity, let us first consider the computation of the 1D Legendre moments.

For a 1D discrete signal $f(x_i)$, $1 \le i \le N$, the 1D Legendre moment is given by

$$L_{p} = \frac{2p+1}{N-1} \sum_{i=1}^{N} P_{p}(x_{i}) f(x_{i})$$
(5)

Let us now introduce the following notation

$$L_{p}(a) = \frac{2p+1}{N-1} \sum_{i=1}^{N} x_{i}^{a} P_{p}(x_{i}) f(x_{i})$$
(6)

It can be easily seen that $L_p = L_p(0)$. Thus, we turn to the fast computation of $L_p(a)$ in the following.

Substitution of Eq. (4) into Eq. (6) yields

$$L_{p}(a) = \frac{2p+1}{N-1} \sum_{i=1}^{N} x_{i}^{a} \left[\frac{2p-1}{p} x_{i} P_{p-1}(x_{i}) - \frac{p-1}{p} P_{p-2}(x_{i}) \right] f(x_{i})$$

$$= \frac{2p+1}{p} \frac{2p-1}{N-1} \sum_{i=1}^{N} x_{i}^{a+1} P_{p-1}(x_{i}) f(x_{i}) - \frac{p-1}{p} \frac{2p+1}{2p-3} \frac{2p-3}{N-1} \sum_{i=1}^{N} x_{i}^{a} P_{p-2}(x_{i}) f(x_{i})$$
(7)

therefore, we have the following recurrence relation for $p \ge 2$

$$L_{p}(a) = \frac{2p+1}{p} \left[L_{p-1}(a+1) - \frac{p-1}{2p-3} L_{p-2}(a) \right]$$
(8)

with

$$L_0(a) = \frac{1}{N-1} \sum_{i=1}^N x_i^a f(x_i) = \frac{1}{N-1} G_N(a)$$
(9)

$$L_{1}(a) = \frac{3}{N-1} \sum_{i=1}^{N} x_{i}^{a+1} f(x_{i}) = \frac{3}{N-1} G_{N}(a+1)$$
(10)

$$G_N(a) = \sum_{i=1}^{N} x_i^a f(x_i)$$
(11)

The above discussion shows that the 1D Legendre moments $L_p = L_p(0)$, for $p \ge 2$, can be deduced from the values of $L_0(a)$ and $L_1(a)$ where *a* is an integer less than *p*, $L_0(a)$ and $L_1(a)$ being obtained by $G_N(a)$. The calculation of Eq. (11) leads to distinguish two different cases: *N* odd and *N* even.

(1) N = 2L + 1

Since $x_i = (2i - N - 1)/(N - 1)$, we deduce from Eq. (11) that

$$G_{2L+1}(a) = \sum_{i=1}^{2L+1} \left(\frac{2i - 2L - 2}{2L} \right)^a f(x_i) = \frac{1}{L^a} \sum_{i=1}^{2L+1} (i - L - 1)^a f(x_i)$$

$$= \begin{cases} \frac{1}{L^a} \left[-L^a f(x_1) - (L - 1)^a f(x_2) - \dots - f(x_L) + f(x_{L+2}) + 2^a f(x_{L+3}) + \dots + L^a f(x_{2L+1}) \right] & a \text{ is odd} \\ \frac{1}{L^a} \left[L^a f(x_1) + (L - 1)^a f(x_2) + \dots + f(x_L) + f(x_{L+2}) + 2^a f(x_{L+3}) + \dots + L^a f(x_{2L+1}) \right] & a \text{ is even} \end{cases}$$
(12)

Eq. (12) can be rewritten as

$$G_{2L+1}(a) = \begin{cases} \frac{1}{L^{a}} \sum_{i=1}^{L} i^{a} g_{1}(x_{i}), & a \text{ is odd} \\ \frac{1}{L^{a}} \sum_{i=1}^{L} i^{a} g_{2}(x_{i}), & a \text{ is even} \end{cases}$$
(13)

with

$$g_1(x_i) = f(x_{L+i+1}) - f(x_{L-i+1}), \quad i = 1, 2, \dots, L$$
(14)

$$g_2(x_i) = f(x_{L+i+1}) + f(x_{L-i+1}), \quad i = 1, 2, \dots, L$$
(15)

(2) N = 2L

Eq. (11) becomes

$$G_{2L}(a) = \sum_{i=1}^{2L} \left(\frac{2i - 2L - 1}{2L - 1} \right)^{a} f(x_{i}) = \frac{1}{(2L - 1)^{a}} \sum_{i=1}^{2L} (2i - 2L - 1)^{a} f(x_{i})$$

$$= \begin{cases} \frac{1}{(2L - 1)^{a}} \left[-(2L - 1)^{a} f(x_{1}) - (2L - 3)^{a} f(x_{2}) - \dots - f(x_{L}) + f(x_{L+1}) + 3^{a} f(x_{L+2}) + \dots + (2L - 1)^{a} f(x_{2L}) \right], \quad a \text{ is odd} \\ \frac{1}{(2L - 1)^{a}} \left[(2L - 1)^{a} f(x_{1}) + (2L - 3)^{a} f(x_{2}) + \dots + f(x_{L}) + f(x_{L+1}) + 3^{a} f(x_{L+2}) + \dots + (2L - 1)^{a} f(x_{2L}) \right], \quad a \text{ is even} \end{cases}$$
(16)

or

$$G_{2L}(a) = \begin{cases} \frac{1}{(2L-1)^a} \sum_{i=1}^{L} (2i-1)^a g_3(x_i), & a \text{ is odd} \\ \frac{1}{(2L-1)^a} \sum_{i=1}^{L} (2i-1)^a g_4(x_i), & a \text{ is even} \end{cases}$$
(17)

with

$$g_3(x_i) = f(x_{L+i}) - f(x_{L-i+1}), \quad i = 1, 2, \dots, L$$
(18)

$$g_4(x_i) = f(x_{L+i}) + f(x_{L-i+1}), \quad i = 1, 2, \dots, L$$
(19)

We discuss, in the following two subsections, the way to efficiently calculate $G_N(a)$ from Eqs. (13) or (17), according to the different modalities of the 1D signal $f(x_i)$.

2.1. $f(x_i) = 1$, for i = 1, 2, ..., N.

In this case, Eqs. (13) and (17) become

$$G_{2L+1}(a) = \begin{cases} 0, & a \text{ is odd} \\ \frac{2}{L^{a}} \sum_{i=1}^{L} i^{a}, & a \text{ is even} \end{cases}$$
(20)

$$G_{2L}(a) = \begin{cases} 0, & a \text{ is odd} \\ \frac{2}{(2L-1)^a} \sum_{i=1}^{L} (2i-1)^a = \frac{2}{(2L-1)^a} \left(\sum_{i=1}^{2L} i^a - 2^a \sum_{i=1}^{L} i^a \right), & a \text{ is even} \end{cases}$$
(21)

The above equations show that to obtain the values of $G_N(a)$, we only need to calculate the following summation

$$H_M(a) = \sum_{i=1}^M i^a \tag{22}$$

For the computation of Eq. (22), which is just the 1D geometric moment of order a of a 'binary' signal, we use the formulae proposed by Spiliotis and Mertzios [8]

$$H_{M}(1) = \frac{M(M+1)}{2}, \quad H_{M}(2) = \frac{M(M+1)(2M+1)}{6}$$

$$H_{M}(3) = \frac{M^{2}(M+1)^{2}}{4}, \quad H_{M}(4) = \frac{M(M+1)(2M+1)(3M^{2}+3M+1)}{30}$$
(23)

and for $a \ge 4$, the recurrence formula

$$\binom{a+1}{1}H_M(1) + \binom{a+1}{2}H_M(2) + \dots + \binom{a+1}{a}H_M(a) = (M+1)^{a+1} - (M+1) \quad (24)$$

where $\binom{i}{j} = \frac{i!}{j!(i-j)!}$ is a combination number.

2. 2. $f(x_i) \neq f(x_j)$ for some $i \neq j$

Eq. (17) can be written as

$$G_{2L}(a) = \begin{cases} \frac{1}{(2L-1)^a} \sum_{i=1}^{2L} i^a h_1(x_i), & a \text{ is odd} \\ \frac{1}{(2L-1)^a} \sum_{i=1}^{2L} i^a h_2(x_i), & a \text{ is even} \end{cases}$$
(25)

where

$$h_1(x_i) = \begin{cases} g_3(x_{(i+1)/2}), \text{ if } i \text{ is odd} \\ 0, \text{ otherwise} \end{cases}$$
(26)

$$h_2(x_i) = \begin{cases} g_4(x_{(i+1)/2}), \text{ if } i \text{ is odd} \\ 0, \text{ otherwise} \end{cases}$$
(27)

Here $g_3(x_i)$ and $g_4(x_i)$ are given by Eqs. (18) and (19), respectively.

It can be seen from Eqs. (13) and (25) that we need to calculate the summation of the form

$$S_{M}(a) = \sum_{i=1}^{M} i^{a} g(x_{i})$$
(28)

Note that $S_M(a)$ is the 1D geometric moment of order a of an arbitrary 1D signal.

Since many algorithms are available in the literature to speed up the computation of Eq. (28), we decided to choose the method proposed by Chan et al. [9]. Their method is able to efficiently compute the grey level image moments. It makes use of a systolic array for computing the moments in which no multiplication is required. We recently applied such a method to efficiently calculating the Zernike moments [10].

Thus, the 1D Legendre moments $L_p(0)$, for $0 \le p \le M$ (*M* denoting the maximal order we want to calculate), can be efficiently obtained using the previously presented algorithm. Fig. 1 shows the computation order of $L_p(0)$ for *p* varied from 0 to 5.

Let us now describe the method for fast computation of the 2D Legendre moments L_{pq} . The double summation in Eq. (3) can be split into the following separate form

$$L_{pq} = \frac{(2p+1)(2q+1)}{(N-1)^2} \sum_{i=1}^{N} \sum_{j=1}^{N} P_p(x_i) P_q(y_j) f(x_i, y_j)$$

$$= \frac{2p+1}{N-1} \sum_{i=1}^{N} P_p(x_i) \left(\frac{2q+1}{N-1} \sum_{j=1}^{N} P_q(y_j) f(x_i, y_j) \right) = \frac{2p+1}{N-1} \sum_{i=1}^{N} P_p(x_i) Y_{iq}$$
(29)

where Y_{iq} is the *q*th-order row moment of row *i* given by

$$Y_{iq} = \frac{2q+1}{N-1} \sum_{j=1}^{N} P_p(y_j) f(x_i, y_j)$$
(30)

These equations show that the computation of 2D Legendre moments of grey level images can be decomposed into two steps. First, the 1D Legendre moments Y_{iq} , for $1 \le i \le N$ and $0 \le q \le M$, are computed by using the algorithm described in Subsections 2.1 and 2.2, according to the different image modalities of $f(x_i, y_j)$. Then, the row moments Y_{iq} are applied to compute the 2D Legendre moments L_{pq} . That is, after the first step, the 2D Legendre moments L_{pq} can be calculated as a 1D moments by setting the image intensity function $f(x_i, y_j)$ to the Y_{iq} previously computed. The algorithm for computing the 2D Legendre moments is depicted in figure 2. It should be pointed out that such a strategy can also be realized in parallel.

3. Computation complexity and experimental results

Let the image size be $N \times N$ pixels, and M the maximum order of Legendre moments to be calculated. The direct computation of Eq. (3) requires approximately $M^2N^2/2$ additions and multiplications, respectively. In the following, we give a detailed analysis of the computational complexity of our algorithm.

We first briefly describe the computational complexity of the algorithm when applied to binary images. From Ref. [8], the computation of the geometrical moments up to the order M of a binary image with $N \times N$ pixels, requires approximately 4Mpower calculations, $2M^2$ multiplications, and M^2 additions (note that these numbers are not dependent on N). The computation of the 2D Legendre moments L_{pq} , by using the recursive algorithm, needs $O(NM^3)$ additions and $O(M^3)$ multiplications. Therefore, the algorithm is very efficient in comparison with the direct method.

The computational complexity of the method for grey level images takes into account the parity of N.

(1) For odd value of N

Let us first consider the number of operations required in the computation of *i*th row moments Y_{iq} ($0 \le q \le M$). Note that the functions $g_1(x)$ and $g_2(x)$ defined by Eqs. (14) and (15) are used for odd value of *N*. To obtain the values of Y_{iq} , we must calculate $G_N(a)$ with Eq. (13) for $0 \le a \le M$. This step needs only $(M+1)^2(N/2-1)$ additions. The computation of Y_{iq} (for $0 \le q \le M$) from the pre-calculated $G_N(a)$, requires M(M-1)/2 additions and 2M(M-1) multiplications. Therefore, the computation of *N* rows Y_{iq} (for $1 \le i \le N$) needs approximately $M^2(N^2+N)/2$ additions and $2M^2N$ multiplications.

When all Y_{iq} , for $1 \le i \le N$ and $0 \le q \le M$, are obtained, the 2D Legendre moments L_{pq} , for $0 \le p+q \le M$, can be calculated in a similar way. The corresponding addition and multiplication numbers are $M^3N/12+M^2N$ and $2M^3/3+2M^2$.

Accordingly, the overall computation makes use of $M^2N^2/2+M^3N/12$ additions and $2M^2N+2M^3/3$ multiplications approximately.

(2) For even value of N

The functions $h_1(x)$ and $h_2(x)$, that are defined by Eqs. (26) and (27), will be used in the computation of $G_N(a)$. The only difference between case (2) and case (1) is that Eq. (25) is adopted instead of (13). The computation of Eq. (25) requires twice additions more than that is needed in Eq. (13). Thus, the total computational complexity is approximately $M^2N^2+M^3N/6$ additions and $2M^2N+2M^3/3$ multiplications. The computational complexities of the proposed algorithm and the direct method are summarized in Table 1. The displayed values show that the new algorithm uses a much fewer number of multiplications than the direct method, what consequently leads to a more efficient computation time.

We illustrate the algorithm efficiency with two binary and grey level images of size 256×256, respectively (first column of Table 2). The first one displays a Chinese character while the second one shows some butterflies. In both cases, the reconstruction of the image was performed using the following relation

$$\hat{f}(x_i, y_j) = \sum_{p=0}^{M} \sum_{q=0}^{p} L_{p-q,q} P_{p-q}(x_i) P_q(y_j)$$
(31)

The results are provided for different orders of the moments, and are shown in Table 2.

5. Conclusion

In this paper, a new fast algorithm for computing the 2D Legendre moments of grey level images has been presented. The proposed method has the following advantages:

- The 1D Legendre moments can be obtained by a recurrence relation. Moreover, the initial value used in the iterative method can be calculated with additions only.
- (2) The 2D moment computation can be decomposed into two 1D moment calculation.

- (3) It does not require so many multiplications that as the direct method, leading thus to a better efficiency in terms of computational time.
- (4) The algorithm can be implemented in parallel.

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Fig. 1. Computation process of $L_p(0)$ with p from 0 to 5. Grey level boxes correspond to already computed coefficients and white boxes to coefficients that will be computed from those which appear in grey level boxes.

for i = 1 to N

computing $L_0(q)$ ($0 \le q \le M$ -2) and $L_1(q)$ ($0 \le q \le M$ -1) using Eqs. (9) and (10) for q = 0 to M

computing Y_{iq} for each row *i* of the image using Eq. (8)

endfor

endfor

for p = 0 to M

computing $L_0(a)$ ($0 \le a \le M$ -p-2) and $L_1(a)$ ($0 \le a \le M$ -p-1) using Eqs. (9) and

(10) from pre-calculated Y_{iq}

for q = 0 to M - p

computing the 2D Legendre moments L_{pq} using recursive method

endfor

endfor

Fig. 2. Algorithm for computing L_{pq}

		Number of additions	Number of multiplications
N=256 M=40	direct method	$\approx M^2 N^2/2$	$\approx M^2 N^2/2$
		56 426 496	56 426 496
	our method	$\approx M^2 N^2 + M^3 N/6$	$\approx 2NM^2 + 2M^3/3$
		109 735 680	798 720
N=255	direct method	$\approx M^2 N^2/2$	$\approx M^2 N^2/2$
		55 986 525	55 986 525
M = 40		$\approx M^2 N^2 / 2 + M^3 N / 12$	$\approx 2NM^2 + 2M^3/3$
		54 010 530	795 600

Table 1 Comparison of the computational complexity for the two methods



Table 2 Results of reconstruction image for different order 24, 32, 40

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