

D-Log: A WiFi Log-based differential scheme for enhanced indoor localization with single RSSI source and infrequent sampling rate

Ren, Yongli; Salim, Flora; Tomko, Martin; Bai, Yuntian Brian; Chan, Jeffrey; Qin, Kai; Sanderson, Mark https://researchrepository.rmit.edu.au/esploro/outputs/journalArticle/D-Log-A-WiFi-Log-based-differential-scheme/9921860126101341/filesAndLinks? index=0

Ren, Y., Salim, F., Tomko, M., Bai, Y. B., Chan, J., Qin, K., & Sanderson, M. (2017). D-Log: A WiFi Log-based differential scheme for enhanced indoor localization with single RSSI source and infrequent sampling rate. Pervasive and Mobile Computing, 37, 94–114. https://doi.org/10.1016/j.pmcj.2016.09.018 Document Version: Submitted Version

Published Version: https://doi.org/10.1016/j.pmcj.2016.09.018

Repository homepage: https://researchrepository.rmit.edu.au © 2016 Elsevier B.V. All rights reserved. Downloaded On 2024/04/28 04:03:08 +1000

Please do not remove this page



Thank you for downloading this document from the RMIT Research Repository.

The RMIT Research Repository is an open access database showcasing the research outputs of RMIT University researchers.

RMIT Research Repository: http://researchbank.rmit.edu.au/

Citation:

Ren, Y, Salim, F, Tomko, M, Bai, Y, Chan, J, Qin, K and Sanderson, M 2017, 'D-Log: A WiFi log-based differential scheme for enhanced indoor localization with single RSSI source and infrequent sampling rate', Pervasive and Mobile Computing, vol. 37, pp. 94-114.

See this record in the RMIT Research Repository at: https://researchbank.rmit.edu.au/view/rmit:39132

Version: Submitted Version

Copyright Statement:

© 2016 ACM.

Link to Published Version: http://dx.doi.org/10.1145/3015022.3015031

PLEASE DO NOT REMOVE THIS PAGE

D-Log: A WiFi Log-based Differential Scheme for Enhanced Indoor Localization with Single RSSI Source and Infrequent Sampling Rate

Yongli Ren^a, Flora Dilys Salim^a, Martin Tomko^b, Yuntian Brian Bai^c, Jeffrey Chan^a, Kyle Kai Qin^a, Mark Sanderson^a

^aSchool of Science, Computer Science and Information Technology, RMIT University, Victoria 3000, Australia ^bDepartment of Infrastructure Engineering, The University of Melbourne, Victoria 3010, Australia ^cSchool of Math and Geospatial Science, RMIT University, Victoria 3000, Australia

Abstract

Currently, large amounts of Wi-Fi access logs are collected in diverse indoor environments, but cannot be widely used for fine-grained spatio-temporal analysis due to coarse positioning. We present a Log-based Differential (D-Log) scheme for post-hoc localization based on differentiated location estimates obtained from large-scale Access Point (AP) logs of WiFi connectivity traces, which can be used for data analysis and knowledge discovery of visitor behaviours. Specifically, the location estimates are calculated by utilizing a combination of Received Signal Strength Indicator (RSSI) records from two neighbouring APs. D-Log exploits real-world industry WiFi logs where RSSI data sampled at low rates from single AP sources are recorded in each connectivity trace. The approach is independent of device and network infrastructure type. D-Log is evaluated using WiFi logs collected from controlled environment as well as real-world uncontrolled public indoor spaces, which includes discrete single-AP RSSI traces of around 100,000 mobile devices over a one-year period. The experiment results indicate that, despite of the challenges with the infrequent sampling rate and the limitations of the data that only records RSSI from single AP sources in each instance, D-Log performs comparatively well to the state-of-the-art RSSI-based localization methods and presents a viable alternative for many application areas where high-accuracy positioning infrastructure may not be cost effective or where positioning applications are considered on legacy information infrastructure.

Keywords: RSSI, WiFi log, localization

1 1. Introduction

The use of a RSSI from multiple WiFi APs to estimate the position of mobile devices in a wireless net-2 worked environment is a well established procedure. Three main approaches are commonly used when RSSI 3 traces are available: trilateration, scene analysis (WiFi fingerprinting), and proximity-based localization. 4 Most of these methods aim to generate an accurate estimate of a mobile device's position in the networked environment. Furthermore, these approaches often demand either that the WiFi networks are configured for 6 high sampling rates and continuous monitoring from multiple access points, or require users to install an app 7 on their device for data collection. This leads to implementation barriers such as high setup, engineering, 8 and calibration cost and the requirements for user participation. Hence, there is a need for approaches 9 applicable to low sampling rates and single access point monitoring. Another source of data that has thus 10 far been barely examined for enhancing localization: large volumes of WiFi AP logs of non-continuous WiFi 11 connectivity traces that are normally stored in an external system, representing timestamped connections 12 between a device and a single Access Point, along with the associated RSSI. With such data, a research 13

Email addresses: yongli.ren@rmit.edu.au (Yongli Ren), flora.salim@rmit.edu.au (Flora Dilys Salim), tomkom@unimelb.edu.au (Martin Tomko), yuntianbrian.bai@rmit.edu.au (Yuntian Brian Bai), jeffrey.chan@rmit.edu.au (Jeffrey Chan), kyleqin2008@gmail.com (Kyle Kai Qin), mark.sanderson@rmit.edu.au (Mark Sanderson)



Figure 1: (a) Coverage areas of two adjacent APs and the cell boundary overlap. The overlapping area is 10 - 20% of a cell's area. (b) An experimental illustration of the dependence of the accuracy of the method on the number of available RSSI observations during handover.

14 question emerges:

15

How to perform accurate indoor localization using large-scale logs of discrete single-AP RSSI traces with low sampling rate?

18

¹⁹ This problem opens a new direction for localization research. Specifically, we describe a robust WiFi log-²⁰ based localization scheme which is:

- non-intrusive: it expects nothing from the client mobile device, e.g. there is no need to install an app, turning-on of sensors other than WiFi;
- 23 2. generic: it is simple to deploy and applicable in any WiFi installation, which has an overlap between the
 24 coverage areas of adjacent APs and is capable of recording RSSI values when handovers occur between
 25 them. Additionally, the knowledge of the relative transmitter output power of the APs should be
 26 known by the operator;
- light-weight: it uses algorithms that are simple to implement and maintain and do not overload existing
 computational infrastructures;
- 4. effective: as long as a mobile device connects to the WiFi network, the localization technique can be applied; and
- 5. accurate: the scheme delivers accuracy that is comparable to scene analysis, and exceeds the classical path loss model [1, 2], as demonstrated in the evaluation.
- The D-Log positioning method is an enhancement over existing methods that roughly localize a device anywhere in the service area of an AP, by providing an estimate of the distance between the mobile device and the connected AP. This allows to further restrict the space in which the device is found. D-Log focuses on static localization, not the continuous tracking of people's movement.
- D-Log works by improving distance estimations from discrete single-AP RSSI traces of a mobile device. Specifically, D-Log applies the WiFi path loss model in combination with knowledge of the distance of neighbouring APs in a WiFi network and the probability distribution of each logged RSSI record to better estimate this distance. The key point is to utilize a combination of RSSI records from two neighbouring APs where handovers occur: a location that is known with some certainty [3, 4]. This information can be used to reduce errors introduced from the path loss model.

D-Log computes an enhanced distance estimate of a mobile device within the region served by a given AP for each individual logged RSSI record. D-Log treats these estimates as independent instances drawn from the same distribution. Applying probability theory, the average of these measurements allows estimation, with greater accuracy, of the distance between the AP and the mobile device. The theoretical analysis is provided to show D-Log's performance in terms of localization accuracy (Section 3.5).

Consider two neighbouring APs a_x and a_y and the mobile device at the distance d_t , served by AP a_x , 48 as shown in Fig. 1a. D-Log calculates one estimate of d_t by using each logged RSSI value when a handover 49 occurred. As there are a large number of WiFi log records for numerous devices, D-Log obtains a large 50 number of estimates of d_t at handover, and uses them to determine the average estimate as the distance to 51 the handover location d_t . This allows us to establish the empirical signal strength decay progression around 52 an AP, along which any non-handover locations can be interpolated for any observation of RSSI. Thus, 53 we use the knowledge of the handover to calibrate the signal strength decay function based on a path loss 54 model for each AP. Fig. 1b illustrates the dependence of the accuracy of the D-Log method on the number 55 of RSSI observations during handover, based on the experiments discussed later. As the number of logged RSSI records increases, the average error of the position estimate decreases (Fig. 1b), converging towards a 57 limit value little above 3.0m, achieved at around 300 observations. 58

Once a sufficient amount of WiFi AP logs has been recorded, they can be used to train the D-Log 59 algorithm. D-Log can then be used in (near) real-time, similar to other existing RSSI-based localization 60 methods. The D-Log scheme is, however, primarily meant to be deployed to improve the location estimate 61 in mobile device access records collected in a WiFi system in a post-processing step. Note that such logs are 62 collected at infrequent sampling rates from a single RSSI source to which the device is connected to. Most 63 existing RSSI-based methods are infeasible in such scenarios. Such enhancement of location estimation is 64 important for the improvement of indoor context estimation supporting a range of applications exploiting 65 indoor behaviour information mining and recommender systems [5, 6], in environments with free and publicly 66 available WiFi networks. Potential application areas include retail and advertising (e.g. shopping malls, 67 airports), leisure and tourism (e.g. attractions, entertainment areas), rich media consumption (e.g. smart 68 displays), teaching and learning support (e.g. in universities), and operational logistics (e.g. in airports, 69 transport hubs). Once accurate post-hoc localization of users within indoor spaces is possible, large-scale 70 Web activity and connectivity logs from the WiFi systems will enable extensive indoor information behaviour 71 mining and long-term prediction of user behaviours [7, 8]. 72

The remainder of the paper is organized as follows. Section 2 presents the related work. The D-Log scheme is detailed in Section 3, where a theoretical analysis is provided to show the performance benefit of D-Log. Section 4 presents the data that we experiment with. Section 5 includes the evaluation of the proposed method, and Section 6 concludes the paper and discusses possible future research.

77 2. Related Work

78 2.1. Indoor localization techniques

Existing research on indoor localization can be categorized into device-based [9, 10, 11, 12, 13], device-free
(passive) localization [14, 15], and infrastructure-based localization[16, 17, 18].

Device-based localization has gained popularity in recent years. This is due to the ability to integrate data 81 from multiple smartphone sensors (e.g. [19]) and thus allow for the combination of dead reckoning [12, 20, 21] 82 and particle filter estimation methods [22]. Although such a rich combination of signals improves indoor 83 localization, this is outside the scope of this paper, which is focused on post-hoc localisation based on 84 (sparse) WiFi AP logs of all the registered WiFi users. For device-based localization, it requires on-device 85 processing, typically via a mobile app, as well as continuous sampling of data. Given the requirement of 86 user participation and uptake with a mobile app, it limits the coverage of indoor monitoring. Full coverage 87 is often considered as a major requirement for indoor monitoring by facility owners and operators. 88

The most recent, albeit less common technique is device-free (passive) localization [14, 15]. Mobile device-free localization does not require a device attached or carried by indoor visitors. But such methods require high and continuous sampling rates and substantial post-processing efforts. They operate well only in controlled environments, and multi-user tracking capability is often limited to small numbers of simultaneously tracked objects. The most recent device-free (passive) localization method is capable of tracking three users simultaneously [23]. Given the challenges with multi-user tracking and the need for highly densed monitoring points and RSSI sampling, this is not applicable for tracking users in large-scale public indoor spaces.

Many infrastructure based techniques utilise trilateration, which requires RSSI from multiple nearby APs. However, these techniques are expensive to implement, since the WiFi networks have to be deployed with a data logging configuration allowing multiple access points to be monitored across each device connection for passive localization. This is typically not the case with most indoor environments currently operating WiFi networks. As such, the logs acquired cannot be mined for accurate indoor spatial behaviour estimation.

Some research employs fusion of techniques. In [21], in-device recorded RSSI from a single access point is used, however, the technique relies on dead reckoning to provide a perceived triangulation on the device. Khan et. al. improved the coverage of localization through active participation of users [24]. Other localization techniques employ the use of ZigBee networks (e.g. [25, 26]), RFID tags [27], or propagation model and autonomous crowdsourcing [28].

107 2.2. RSSI use in indoor localization

With regard to the use of RSSI from WiFi access points in localizing devices of a WiFi network, traditionally, there are three main methods that are widely employed: trilateration, scene analysis, and proximity analysis [29, 30].

First is trilateration, which estimates the position of a device by calculating its distance from multiple 111 reference points [30]. When RSSI traces from multiple access points are available, the use of this path 112 loss based method is a more accurate approach to localize a device, rather than using Time-of-Arrival 113 or Time-Difference-of-Arrival calculation [30] to approximate a device location, as the latter two methods 114 require a clear Line-Of-Sight (LOS) between the transmitter and the receiver [30]. An example of the use 115 of trilateration is in [17], where WiFi RSSI traces from multiple reference (access) points were recorded in 116 order to monitor around 18,000 devices in a hospital. They used WiFi signals measured on mobile devices to 117 first localize users in the building, extracted the spatial and temporal features from the traces, analyzed the 118 flow of people from entrance to exit, and classified their behaviours based on the user roles [17]. However, 119 in our study, RSSI from multiple reference points are not available, hence, trilateration is not applicable. 120

The second established RSSI-based localization approach is Radio Frequency (RF) based scene analysis, 121 a method to use prior-collected features, or fingerprints, of a scene to determine the location [29]. The 122 most widely used scene analysis method is RSSI-based fingerprinting [30]. Swangmuang and Krishnamurthy 123 presented an analytical model to predict the performance of fingerprinting-based indoor localization systems 124 by applying proximity graphs [31]. A WiFi RSSI fingerprint for each location is used to match the monitored 125 (indoor) environment for accurate localization of the device [32]. In some cases, fingerprinting at the actual 126 site is not feasible, e.g., in a very large shopping mall or airport. Since fingerprinting requires a large amount 127 of time and resources and costly system calibration in the beginning [32], the real-world use of this approach 128 was difficult. For example, in a highly dynamic environment, where layouts and objects often change, 129 RF fingerprints could easily change due to alterations of the indoor environment, hence requires frequent 130 fingerprinting [12]. [33] used knowledge about the geometry of the environment and made assumptions 131 about continuous indoor movement tracking to address this problem, while [34] collected user feedback to 132 improve the fingerprinting process. Want et. al. proposed a combination of subarea fingerprinting and 133 gradient descent search to improve localization by probabilistic fitting [35], but this fingerprinting approach 134 requires high frequency sampling. 135

The third approach is proximity-based localization, which uses RSSI captured on users' devices to compute approximate sets of devices that are located in proximity to each other to localize the position of a device relative to another device [29]. This method does not apply in our study since we do not use apps or device-based approach to localize a user.

In this paper, we propose the D-Log scheme as a new reference scheme for post-hoc localization, which aims to be easy to implement and maintain, is independent of devices and network infrastructure, and is effective and reasonably accurate. In Table 1, we compare D-Log with existing schemes, including trilateration,

Schemes Cost Client AP **RSSI** Source Sampling Rate Signal Comments Place-(No. Sensors of /App ments APs) Trilateration RSSI Med No Normal At least 3 Low (continuous) Infrastructure-based Scene analysis RSSI& High Yes Normal Multiple High (continuous) Device-based Sensors Proximity analysis RSSI High Yes Dense Multiple High (continuous) Device-based Device free RSSI High Yes Dense Multiple High (continuous) Device-free/passive RSSI Low (discrete) D-Log No Normal Single Log-based Low

Table 1: Comparison of indoor localization schemes.

scene analysis, proximity analysis and device free approaches in terms of their deployment characteristics.
 The D-Log scheme is low cost, because it only requires infrequent RSSI sampling from single RSSI source,

rather than continuous RSSI sampling from multiple RSSI sources like others (e.g. scene analysis).

¹⁴⁶ 3. Log-Based Differential Scheme

¹⁴⁷ In this section, we formulate the targeted research question and present two D-Log algorithms to estimate ¹⁴⁸ the distance of the mobile device to the AP. Furthermore, the complexities of the D-Log algorithms are ¹⁴⁹ analysed, and a theoretical analysis is provided to show the performance benefit of the entire proposed ¹⁵⁰ D-Log scheme.

¹⁵¹ 3.1. Problem Formulation

In this paper, the research question is the estimation of a mobile device location within the coverage 152 area of several WiFi APs based on logs of discrete RSSI traces from single APs. We assume that the WiFi 153 log includes discrete RSSI measurements relating to a single AP connection at any one time, in contrast 154 to the trilateration and scene analysis methods requiring multiple parallel RSSI observations. Single RSSI 155 records are recorded in most real-world Wi-Fi system data logs, where non-serving APs and their RSSI are 156 not recorded. Although these single-AP RSSI traces are normally discrete and sampled at low frequency, 157 the quantity of records obtained from different devices for each WiFi AP is large. For example, the real-158 world WiFi log we examined (as detailed in Section 4), was collected with a 5min sampling rate for each 159 registered mobile device; logging only the RSSI values for currently connected APs. This resulted in 480,924 160 connections distributed amongst 35 APs, with in average around 13,000 records per AP. This large volume 161 of available records for each AP creates an opportunity to accurately estimate the distance of a mobile device 162 from an AP given its RSSI value. 163

There are several techniques to calculate d_t given an RSSI value r_t for a mobile device when associating with an AP. The path loss model [1, 2] enables to determine the device distance based on the full set of inputs:

$$\hat{d}_t = 10^{\left(\frac{TX_{pwr} - r_t - L_{tx} - L_{rx} + G_{rx} + G_{rx} - PL - s}{10e}\right)} \tag{1}$$

where d_t denotes the estimated distance between the transmitter and the receiver (the client mobile device) 167 in meters; TX_{pwr} is the transmitter output power in dB; r_t is the detected RSSI in dB; L_{tx} is the sum of 168 all transmitter-side cable and connector losses in dB; L_{rx} is the sum of all receiver-side cable and connector 169 losses in dB; G_{tx} is the transmitter-side antenna gain in dBi; G_{rx} is the receiver-side antenna gain in dBi; 170 PL is the reference path loss in dB for the desired frequency when the receiver-to-transmitter distance is one 171 meter; s is the standard deviation associated with the degree of shadow fading present in the environment; 172 e denotes the path loss exponent for the environment. Note, although Eq. 1 takes a range of factors into 173 consideration, the estimation of d_t is not accurate, as the RSSI values r_t at location p_x vary and can be 174 affected by a large number of external factors, e.g. the people movement through the space, the layout of 175 the walls and the materials used in the environment. 176



(a) Theoretically circular shaped coverage (b) Practically irregular-shaped coverage

Figure 2: Illustration of d_m , h and d_{ofst} in D-Log algorithm with both theoretically circular shaped and practically irregular shaped coverage of several Wi-Fi APs. Here, the irregular shaped Wi-Fi AP coverage is obtained by following the study of wireless performance and coverage from Cisco Meraki [36].

Let us consider a general case: given two sets of sample RSSI values \mathcal{R}_x and \mathcal{R}_y , collected when the 177 handover between two adjacent access points a_x and a_y happens, we denote $r_x^i \in \mathcal{R}_x$ a sample RSSI 178 value observed when a mobile device is disassociating with a_x and then immediately associating with a_x 's 179 topological adjacent AP a_y ; similarly, each $r_y^i \in \mathcal{R}_y$ denotes a sample RSSI value observed when a device is 180 disassociating with a_y and then immediately associating with a_x . As there is only one observed RSSI value 181 to the connected AP for the mobile device at any time, then other methods that rely on concurrent RSSI 182 measurements from multiple APs are not applicable (e.g. trilateration and scene analysis). To address this 183 problem, we propose the D-Log scheme to estimate d_t from the RSSI records $r_x^i \in \mathcal{R}_x$, not from r_t directly. 184 Specifically, D-Log computes three other distances to interpolate d_t : 1) the distance d_m of mid-point of the 185 overlapping coverage areas between a_x and a_y ; 2) the size, h of the handover area between a_x and a_y ; 3) the 186 offset d_{ofst} between the mobile device and the handover boundary of a_x . As the two RSSI observations at 187 handover have a number of inputs identical (assuming the transmitting power of the APs is either known 188 or their proportions are known), this differential scheme allows to reduce the number of degrees of freedom 189 influencing the distance determination. This indirect estimation enables D-Log to obtain a large number of 190 distinct estimates for d_m , h and d_{ofst} , respectively, because there are a large number of $r_x^i \in \mathcal{R}_x$ in the log. 191 As $r_x^i \in \mathcal{R}_x$ was collected independently in the log, the estimates from them are thus independent to each 192 other. Then, from the aspect of probability theory, these observations can be used to estimate d_m , h and 193 d_{ofst} , respectively. Take d_m as an example, 194

$$\hat{\mu}(d_m) = E(d_m | r_x) = E(\hat{d}_m^i) = \frac{1}{n} \sum_{i=1}^n d_m^i,$$
(2)

where d_m^i is the estimated distance of d_m based on a logged RSSI value r_x^i , and n is the number of log records. Moreover, this estimator has large practical application, as large datasets of RSSI logs are common and useful for a number of applications. Thus, the final interpolated d_t is accurate, and this will be detailed in the following sections.

199 3.2. D-Log Algorithm

Here, we propose the basic D-Log algorithm to estimate the location of a mobile device within the coverage area of an AP. The D-Log algorithm performs the localization using the following four steps:

• Step 1: Estimation of the distance d_m for the mid-point p_m of the overlapping coverage areas of two adjacent APs, a_x and a_y . Given a set of the RSSI values $r_x^i \in \mathcal{R}_x$ and $r_y^i \in \mathcal{R}_y$, obtained when the

handover happens between a_x and a_y , we define that 204

$$\hat{d}_m = E(\hat{d}_m^i) = \frac{1}{n} \sum_{i=1}^n \hat{d}_m^i = \frac{1}{n} \sum_{i=1}^n \frac{\hat{d}_x^i - \hat{d}_y^i + D}{2},$$
(3)

where n denotes the number of sample RSSI values in \mathcal{R}_x and \mathcal{R}_y , D is the known distance between 205 a_x and a_y , and \hat{d}_x^i and \hat{d}_y^i are the estimate distance from r_x^i and r_y^i by using Eq. 1, representing the 206 distance from where the handover occurs to a_x and a_y , respectively. 207

• Step 2: Estimation of the size of the handover area of two adjacent APs: 208

$$\hat{h} = E(\hat{h}^i) = \frac{1}{n} \sum_{i=1}^n \hat{h}^i = \frac{1}{n} \sum_{i=1}^n (\hat{d}^i_x + \hat{d}^i_y - D).$$
(4)

• Step 3: Estimation of the offset between the mobile device at p_t and the handover boundary of the 209 access point a_x . 210

$$\hat{d}_{ofst} = E(\hat{d}^{i}_{ofst}) = \frac{1}{n} \sum_{i=1}^{n} \hat{d}^{i}_{ofst} = \frac{1}{n} \sum_{i=1}^{n} (\hat{d}^{i}_{x} - \dot{\hat{d}}_{t}),$$
(5)

- where \dot{d}_t denotes the estimate distance from p_t to AP a_x by Eq. 1. 211
- Step 4: Calculation of the distance of the mobile device at p_t within the signal coverage area of a_x . 212

$$\hat{d}_t = \hat{d}_m + \frac{\hat{h}}{2} - \hat{d}_{ofst}.$$
 (6)

Note, Eq. 6 differentiates the estimate of \hat{d}_t from each r_x^i and r_y^i via Eq. 3, 4, and 5 from Step 1, 2 and 213 3. Thus, the D-Log algorithm can provide accurate localization of a mobile device within the coverage area 214 of a_x . Once the distance to the mid point and the interpolation of RSSI values of a_x are determined, they 215 can be applied to locate the mobile device at any distance from the serving AP as long as they are within 216 the range. In addition, Fig. 2 shows an illustration of d_m , h and d_{ofst} in D-Log algorithm. Specifically, 217 Fig. 2a shows these parameters when the Wi-Fi AP coverage shape is considered as circles theoretically, 218 while Fig. 2b shows them when the coverage shape is irregular in practice. 219

3.3. Weighted D-Log Algorithm 220

The WiFi logs can be used to determine the distribution of the RSSI values when the handover happen 221 between two adjacent APs a_x and a_y . Fig. 3 shows the distribution of these RSSI values collected in a real-222 world WiFi infrastructure in a large shopping mall in Australia (detailed in Section 4), and it is observed 223 that they do not follow a uniform distribution. Highly frequent observations of the RSSI (here, around 2000 224 RSSI observations with r = -70 dB) bear higher impact on the final D-Log estimate than the less frequent 225 ones (e.g. the 400 observations with r = -90 dB). Commercial WiFi networks optimized for coverage often 226 set -70dB as a threshold value for received signal strength [37]. Following this, we propose a weighted 227 D-Log algorithm by taking the RSSI sample frequency into consideration. Thus, we define the weighted 228 version of the simple expectation location estimator (in Eq. 2) as: 229

$$\hat{\mu}(d_m) = E(d_m | r_x) = E(\hat{d}_m^i) = \frac{1}{\sum_i^u c_x^i} \sum_{i=1}^u c_x^i d_m^i, \tag{7}$$

where c_x^i is the frequency of r_x^i , u denotes the number of unique r_x^i , and $\sum_i^u c_x^i = n$.



Figure 3: Distribution of RSSI values when handover happen between two adjacent APs in a real-world WiFi log, discussed in Section 4

Therefore, the corresponding weighted versions of \hat{d}_m , \hat{h} , \hat{d}_{ofst} and \hat{d}_t are defined as:

$$\hat{d}'_m = E(\hat{d}^i_m) = \sum_{i=1}^u \frac{w^i_x (\hat{d}^i_x - \hat{d}^i_y + D)}{2},$$
(8)

$$\hat{h}' = E(\hat{h}^i) = \sum_{i=1}^u w_x^i (\hat{d}_x^i + \hat{d}_y^i - D),$$
(9)

$$\hat{d}'_{ofst} = E(\hat{d}^i_{ofst}) = \sum_{i=1}^u w^i_x (\hat{d}^i_x - \dot{\hat{d}}_t),$$
(10)

$$\hat{d}'_t = \hat{d}'_m + \frac{\hat{h}'}{2} - \hat{d}'_{ofst}, \qquad (11)$$

where $w_x^i = \frac{c_x^i}{\sum c_x^i}$, and c_x^i denotes the frequency of sample r_x^i .

233 3.4. Complexity Analysis

One advantage of the proposed D-Log scheme is its low computational complexity. The complexity of 234 the D-Log algorithm is O(n), where n denotes the average number of log records per AP; the complexity 235 of the weighted D-Log algorithm is O(u), where u denotes the number of unique RSSI values per AP. This 236 indicates that D-Log scheme is efficient and only depends on the local log records for neighbouring APs, 237 which enables the processing of large volume of records in parallel. In contrast, the complexity of the other 238 RSSI based localization methods are often much larger than D-Log. For example, the complexity of machine 239 learning based scene analysis (fingerprinting) models, is the same as that of the deployed machine learning 240 methods, e.g. the complexity of SVM-based localization method is $O(\max(na, a) \cdot \min(na, a)^2)$ [38], where 241 n is the number of training records, and a is the number of APs. 242

243 3.5. Performance Analysis

In this section, we provide a theoretical analysis of the performance of the unweighted D-Log algorithm. The distance from where each r_x^i is observed to a_x can be estimated with Eq. 1, although there is an error ε caused by systematic and stochastic factors. For access point a_x , we define the estimation from r_x^i as

$$\hat{d}_x^i = d_x^i + \varepsilon_x^i,\tag{12}$$



Figure 4: The distribution and (ECDF) CDF of ε and the reference Gaussian distribution

where \hat{d}_x^i is the distance estimation from r_x^i with Eq. 1, d_x^i is the real distance, and ε_x^i is the error for this estimation. Then, for access point a_y , we obtain

$$\hat{d}_y^i = d_y^i + \varepsilon_y^i. \tag{13}$$

We further assume that the estimation error ε from each sample RSSI value is independent and identically 250 distributed (i.i.d), and we adopt the Gaussian distribution for theoretical analysis. This is motivated from 251 the experimental results. Specifically, Fig. 4a shows the distribution of ε in our controlled experiment, 252 which is detailed in Section 4. The dashed blue line depicts the observation empirical distribution of ε in the 253 experiment, and the solid black line depicts the reference Gaussian distribution with the mean and standard 254 deviation of ε . Fig. 4b shows the Empirical distribution function (ECDF) of ε (the dashed blue line) and 255 the Cumulative Distribution Function(CDF) of the reference Gaussian distribution. It is observed that the 256 reference Gaussian distribution fits the observation distribution of ε (with D = 0.0558, p-value = 0.5609 in 257 Kolmogorov-Smirnov test), and it is thus a suitable model for the following theoretical analysis. 258

²⁵⁹ Consequently, the Probability Density Function (PDF) of ε is:

$$p(\varepsilon) \sim N(\mu_{\varepsilon}, \sigma_{\varepsilon}^2).$$
 (14)

As stated in Eq. 2, we measure \hat{d} by applying the sample mean as the location estimator, and the distance on each observed RSSI can be considered as an observation. In the first step of D-Log algorithm, for the calculation of \hat{d}_m , according to Eq. 3 and Eq. 14, we obtain

$$\hat{d}_m = E(d_m^i) = \frac{1}{n} \sum_{i=1}^n \frac{\hat{d}_x^i - \hat{d}_y^i + D}{2} = \frac{1}{2}(d_x - d_y + D) + \frac{1}{2n} \sum_{i=1}^n (\varepsilon_x^i - \varepsilon_y^i),$$
(15)

where d_x and d_y are the real distances of the handover boundary for a_x and a_y , respectively. Similarly,

$$\hat{h} = E(\hat{h}^{i}) = (d_{x} + d_{y} - D) + \frac{1}{n} \sum_{i=1}^{n} (\varepsilon_{x}^{i} + \varepsilon_{y}^{i}).$$
(16)

For the estimation of the offset between the mobile device at p_t and the handover boundary of the access point a_x , according to Eq. 5 and Eq. 14, we obtain

$$\hat{d}_{ofst} = E(\hat{d}_{ofst}^{i}) = \frac{1}{n} \sum_{i=1}^{n} (\hat{d}_{x}^{i} - \dot{\hat{d}}_{t}) = (d_{x} - d_{t}) + \frac{1}{n} \sum_{i=1}^{n} (\varepsilon_{x}^{i} - \varepsilon_{t}),$$
(17)



(a) The distribution of $\varepsilon_{\hat{d}_t}$ with various n (b) the trend of the standard error $\sigma_{\hat{d}_t}$ with various n

Figure 5: The impact of n on $\varepsilon_{\hat{d}_t}$ and $\sigma_{\hat{d}_t}$

where d_t is the real distance between the test point p_t to a_x , and ε_t is the error when calculating \hat{d}_t .

²⁶⁷ Consequently, in the last step of D-Log, according to Eq. 6, Eq. 15, Eq. 16, Eq. 17 and Eq. 14, we obtain:

$$\hat{d}_{t} = \hat{d}_{m} + \frac{\hat{h}}{2} - \hat{d}_{ofst} = d_{t} + \frac{1}{2n} \sum_{i=1}^{n} (\varepsilon_{x}^{i} - \varepsilon_{y}^{i}) + \frac{1}{n} \sum_{i=1}^{n} (\varepsilon_{x}^{i} + \varepsilon_{y}^{i}) - \frac{1}{n} \sum_{i=1}^{n} (\varepsilon_{x}^{i} - \varepsilon_{t}).$$
(18)

Thus, according to Eq. 18 and Eq. 14, we obtain the $100(1 - \alpha)\%$ confidence interval $CI(\hat{d}_t)$ for the estimation of \hat{d}_t , which has been widely used to indicate the reliability of an estimation [39],

$$CI(\hat{d}_t) = d_t \pm z_{\frac{\alpha}{2}} \sqrt{\frac{5\sigma_{\varepsilon}^2}{n}},\tag{19}$$

where $z_{\frac{\alpha}{2}}$ is a standard normal variate which exceeded with a probability of $\frac{\alpha}{2}$. Therefore, the standard error of \hat{d}_t is:

$$\sigma_{\hat{d}_t} = \sqrt{\frac{5\sigma_{\varepsilon}^2}{n}},\tag{20}$$

where n denotes the sample size.

Theorem 1. The standard error $\sigma_{\hat{d}_t}$ of D-Log scheme is bounded to be no more than $\sqrt{5\sigma_{\varepsilon}^2}$, with equality if and only if n = 1.

PROOF 1. As the sample size $n \ge 1$, based on Eq. 20, we obtain:

$$\sigma_{\hat{d}_t} \le \sqrt{5\sigma_{\varepsilon}^2},\tag{21}$$

where the equality is satisfied when n = 1.

Fig. 5 shows the distribution of D-Log's localization error, $\varepsilon_{\hat{d}_t}$, and the trend of $\sigma_{\hat{d}_t}$, with various *n* values

in our real-world indoor experiment environment, which is detailed in Section 4. Specifically, where n = 1,

- $\sigma_{\hat{d}_t}$ meets the worst case with the value of 11.9, as there is only 1 row of RSSI logs available. However, when more logs are available as shown in Fig. 5b, $\sigma_{\hat{d}_t}$ starts to decrease as *n* increases. It indicates that 1) as *n*
- increases, $\sigma_{\hat{d}_t}$ decreases; 2) D-Log has a floor level, which is influenced by the localization environment.

Table 2: Aggregate statistics of the WiFi log collected in a real-world large indoor retail environment

Number of user devices:	94,396
Number of AP association:	480,924
Number of Visits:	183,745
Number of WiFi APs:	35
Average of AP association per AP :	13,741

282 4. Data

In this section, we present the data used for the evaluation of the performance of the proposed D-Log scheme. We evaluate the performance of the D-Log scheme in two environments: a controlled environment and a real-world large indoor environment. The complexity of the two environments is different, and so is the evaluation setup. While in the simulated environment, the mobile devices used in the training and testing set of the controlled environment are identical and therefore the variability of the used WiFi is controlled, this is not the case in the real-world large indoor environment.

289 4.1. Experiment Data

Here, we describe the experiment data from the two experimental environments: the controlled environment and the real-world large indoor environment.

For the controlled environment, we set up an experimental WLAN with 4 access points in a university 292 meeting room (dimension: 7m by 5m). We have partitioned the room into $35 (1m \times 1m)$ square grids, and 203 used 16 of them as the test locations. These test locations were located along walls and in locations not 294 occupied by furniture. Then, we recorded the RSSI values during handover of the carried mobile device 295 (a smartphone) from one test AP to another. These recordings supply the training RSSI logs for D-Log 296 scheme. For testing purposes, we collected around 6000 sample RSSI records (about 360 per location) 297 from all detected APs, which will be used to evaluate the performance of D-Log scheme and the compared 298 state-of-the-art localization methods. 299

Additionally, we have conducted real-world experiments in a large inner-city shopping mall in Sydney, 300 Australia, covered by 67 WiFi APs across 90,000 square meters. We used three levels of the mall to conduct 301 our experiments, in an area of around 35,000 square meters covered by 35 WiFi APs. The WiFi log were 302 collected from September 2012 to October 2013, and were stored in an external system. It contains around 303 half a million AP access records from around 100,000 mobile devices. Specifically, the log includes the 304 WiFi access point associated with the user's mobile device sampled at every 5 minutes, and the respective 305 RSSI value for each association. These data are used as training data for the D-Log scheme with some 306 preprocessing that is detailed in Section 4.2. Table 2 shows the statistics of the log. Note, all user identifiable 307 information (registration details and WiFi MAC addresses) were replaced by a hash key in a non-reversible 308 way. To examine the localization performance in this real industry environment, we selected 43 test locations 309 across the three floors of the mall, and collected around 4000 sample RSSI records (around 100 per location) 310 from all detected APs. Fig. 6 shows the floor maps and the test locations. Specifically, we collected 10 test 311 locations on the 1^{st} floor, 15 on the 2^{nd} floor, and 18 on the 3^{rd} floor. Moreover, note this real-world RSSI 312 log contains much complexities, which may influence all RSSI based localization methods, e.g. the variance 313 mobile devices/antenna/Wi-Fi chipsets. There are 694 different mobile models from 53 manufacturers in 314 our collected WiFi logs, and Table 3 and 4 show the most common manufacturers and models of the used 315 devices in the log, respectively. 316

317 4.2. Pre-processing the WiFi AP Log

The real-world industry WiFi log we used was sampled at 5 minutes frequency for each user visit, and for each device, only the RSSI values for current connected AP were logged. Table 5 shows a sample of the log for a specific user.

Table 3:	Most	common	manufacturers	of u	ised	mobile	devices

Manufacturer	#	Manufacturer	#	Manufacturer	#
Apple	66921	Unidentified	187	Xiaomi	22
Samsung	10587	Huawei	114	Toshiba	16
Generic (Android)	9018	Amazon	106	ZTE	13
HTC	1861	Sony	90	Fujitsu	12
RIM	1284	Microsoft	82	Opera	11
SonyEricsson	697	Asus	53	KDDI	11
Nokia	585	Pantech	41	NEC	9
Google	401	Sharp	35	Alcatel	8
LG	347	DoCoMo	32	HP	7
Motorola	240	Acer	26	Lenovo	7

Table 4: Most common models of used mobile devices

Model	#	Model	#	Model	#
iPhone $(Apple)$	54873	Galaxy Nexus (Samsung)	420	BlackBerry 9780 (RIM)	177
iPad (Apple)	7523	GT-I9305 (Samsung)	414	Desire HD (HTC)	173
iPod Touch (Apple)	4525	GT-I9000 (Samsung)	407	Desire (HTC)	159
Android 4.1 (Generic)	4173	GT-N7000 (Samsung)	358	PJ83100 (HTC)	145
GT-I9300 (Samsung)	2791	Fennec (Generic)	291	LT26i (SonyEricsson)	142
GT-I9100 (Samsung)	2602	BlackBerry Bold Touch 9900 (<i>RIM</i>)	261	BlackBerry 9800 (<i>RIM</i>)	139
Android (Generic)	1989	Nexus 4 (Google)	231	Nexus S $(Google)$	130
Android 4.0 (Generic)	1801	GT-S5830 (Samsung)	220	BlackBerry 9700 (<i>RIM</i>)	127
GT-N7100 (Samsung)	849	GT-I9305T (Samsung)	214	A510 (<i>HTC</i>)	126
Android 2.3 (Generic)	452	Unidentified (Generic)	199	S710E (HTC)	124

This infrequent sampling rate from single RSSI source makes it infeasible to apply existing localization 321 methods, including trilateration, scene analysis, proximity analysis and device free method. This is because 322 all of these existing methods require RSSI traces from multiple sources with frequent continuous sampling. 323 So, doing localization based on this sort of data is not trivial. We conducted some data pre-precessing as 324 follows: 1) We carry two mobile devices (one IOS iPhone 4 and one Android Sumsung S4) to the mall to 325 record the RSSI values when a handover happens between neighbouring APs, and treat these RSSI values 326 as the handover boundaries of corresponding APs; then 2) for each AP, we extract all the RSSI values 327 that are less than those identified handover boundaries from the real-world WiFi log, so as to estimate the 328 distribution of the RSSI values when handovers happen. Finally, these extracted subset of RSSI values are 329 used as training samples for the D-Log scheme. 330

Table 5: Examples of the WiFi log for user E154GCHIJDESPLMX5KFJC

Hashed MAC address	WiFi AP	RSSI	association time	disassociation time	Duration (sec)
E154GCHIJDESPLMX5KFJC	AP 1	-76	2013-02-04 14:16:24	2013-02-04 14:21:24	300
E154GCHIJDESPLMX5KFJC	AP 3	-72	2013-02-04 14:21:24	2013-02-04 14:26:24	300
E154GCHIJDESPLMX5KFJC	AP 7	-75	2013-02-04 14:26:24	2013-02-04 14:31:24	300
		•••			



Figure 6: The floor maps in the mall where the experiments are conducted. The red dots represent the Wi-Fi APs, and the blue stars denote the test locations where ground-truth RSSI information were collected.

331 5. Experiment Results

In this section, we present the experimental configuration and the performance of the proposed D-Log scheme in terms of localisation accuracy achieved by D-Log. Note, this localization relates to the determination of the distance of the mobile device from the AP and therefore the reported error indicate the width of the band in which the mobile device is located.

336 5.1. Experiment Baselines

To examine the performance of D-Log scheme thoroughly, we compare the proposed D-Log scheme with 337 two state-of-the-art RSSI-based localization methods: scene analysis methods, and Path Loss model [1, 2]. 338 There are two reasons we choose these two baselines: 1) By comparing with scene analysis, we demonstrate 339 how closely the D-Log scheme performs comparing to the state-of-the-art, because scene analysis is one of 340 the most accurate and most popular RSSI-based localization methods; 2) the path loss model is selected 341 to perform a fair comparison because it also makes an estimate of the radius of the receiver like the D-342 Log scheme. For the scene analysis methods, we choose two algorithms: SVM-based method [40] and the 343 Bayesian Network-based method [30], given that these two are among the state-of-the-art learning techniques 344 applied for fingerprint-based indoor localization. 345

346 5.2. Experimental Configuration

347 5.2.1. Evaluation Metrics

The experiments were conducted on a PC running the Windows 7 Operating System with 8 GB RAM and Intel Core i7 CPU, and we conducted a 10-fold cross validation and report the results. Note that We deployed the well-known LibSVM¹ package to perform the SVM-based method, and Weka (Data mining Software in Java²) to perform the Bayesian Network-based method; For the proposed D-Log scheme and the state-of-the-art Path Loss model, we implemented them in Java.

¹https://www.csie.ntu.edu.tw/~cjlin/libsvm

²http://www.cs.waikato.ac.nz/ml/weka/

Following literature [31], we apply the mean precision $P(\mathcal{T})$ and the mean absolute error (ε , localization accuracy) as the measurement metric:

$$P(\mathcal{T}) = \frac{|\mathcal{T}_c|}{|\mathcal{T}|},\tag{22}$$

$$\varepsilon = \frac{\sum |d_t - \hat{d}_t|}{|\mathcal{T}|},\tag{23}$$

where \mathcal{T} is the test set, $|\mathcal{T}_c|$ denotes the number of test locations that are correctly assigned to its true 355 location, $|\mathcal{T}|$ denotes the size of \mathcal{T} , including both correctly assigned and incorrectly assigned test locations, 356 d_t is the true distance, and the \hat{d}_t is the estimated distance. For D-Log and Path Loss model, while 357 calculating $|\mathcal{T}_c|$, if $d_t - \sigma_{\varepsilon} < \hat{d}_t < d_t + \sigma_{\varepsilon}$, \hat{d}_t is considered as the true location, otherwise false location. For 358 SVM-based method [40] and the Bayesian Network-based method [30], they output the labels of each test 359 location. While calculating ε , if the output label is the real label of the test location, ε for this test location 360 is 0, otherwise the difference between the true distance d_t and the distance from the AP to the output label 361 location, which is d_t . 362

363 5.2.2. Parameter Estimation

Like other localization methods, there are parameters in the proposed D-Log scheme, which are the 364 parameters in the path loss model as shown in Eq. 1. Some of these parameters are known (e.g. the 365 transmitter output power), or can be measured by site surveying process (e.g. path loss exponent e), 366 but some others are hard to measure or measure accurately in practice. For example, in the investigated 367 mall, a large variety of different brands and models of receivers (mobile phones) are involved, which makes it 368 infeasible to measure the receiver-side related parameters; the presence of obstructions and people movement 369 is changing frequently, which makes it hard to accurately measure other parameters, e.g. the path loss 370 exponent e and the standard deviation of shadow fading s [2]. 371

Thus, similar to other localization methods again, some data mining techniques can be applied to estimate these parameters. For example, Durgin et. al. applied linear regression to estimate the path loss exponent e and the reference path loss PL at 1m transmitter-receiver separation by using pairwise RSSI measurements and log distances [1]. Recently, cross validation has been widely used to estimate parameters of indoor localization models, e.g. kernel-based indoor localization algorithms [41], machine learning based algorithms [42], and powerline positioning algorithms [43]. Following this, we deploy cross validation to estimate the parameters of D-Log scheme by using pairwise RSSI measurements and log distances.

Specifically, because we used the collected experimental data to both estimate the parameters of the 379 models and evaluate them, we deployed a nested cross validation to ensure the final model evaluation is 380 unbiased [44]. Note that, there are two disjoint datasets in D-Log scheme, the RSSI logs, and the pairwise 381 RSSI records and distances collected at test locations. We call the RSSI logs the *training* set, and divide 382 the pairwise RSSI records and distances collected at test locations into another two disjoint subsets: the 383 validation set and the test set. Therefore, the training set, the validation set and the test set are independent 384 to each other. Consequently, the learnt parameters will not overfit the data, and the final localization results 385 are unbiased [44, 45]. 386

Although theoretically the nested cross validation strategy can search and estimate the parameters in 387 anyway, it is practically helpful to obtain the ranges of these parameters as accurate as possible. To estimate 388 the ranges of these parameters accurately and to not disturb the investigated mall's daily business (running 389 7 days), we set up a shopping mall like simulation environment in the RMIT Indoor Positioning Lab. 390 Specifically, we set up a Wi-Fi network in the simulation environment with the same configurations of that 391 in the investigation mall, e.g. the wireless networking standard 802.11n(2.4GHz) and the model of access 392 points; and we used three different phones (one IOS iPhone 4, one Android Sumsung S4 and one HTC ONE) 393 with a Java program installed to measure the receiver-side related parameters. Then, an expert, one author 394 of this paper, measured the ranges of all parameters, which are used to determine the possible candidate 395 values for each parameter. The detailed procedure of the deployed nested cross validation strategy is shown 396

Table 6: Comparison of localization precision in controlled environment. Note, weighted D-Log, D-Log and path loss model used logs of single-AP traces; SVM-based method and Bayesian Network-Based Method used the RSSI records from multiple APs.

	Weighted D-Log	D-Log	SVM-Based	Bayesian Network-Based	Path Loss
$P(\mathcal{T})$	61.3%	60.1%	69.1%	66.9%	32.9%
ε (m)	0.93	1.01	0.91	1.03	1.82

³⁹⁷ in Algorithm 1.

1 randomly divide the pairwise RSSI records and distances collected at test locations into k equal sized subsets;

- 2 for each subset do // outer loop
- **3** use this subset as *test* set, and the rest k 1 subsets as *validation* set;
- 4 for each candidate value of the parameters in the measured ranges do // inner loop
 - use this candidate parameter to build D-Log model on the *training* RSSI Logs;
 - validate the model on the *validation* set and calculate localization error for each pair of RSSI records and distances;
- 7 average the localization error of all pairs to get $\varepsilon_{validation}$ on the validation set;

8 end

- **9** select parameters that minimize $\varepsilon_{validation}$;
- build model with the learnt parameters, and calculate $P(\mathcal{T})$ and ε on the *test* set;

11 end

5

6

398

12 average $P(\mathcal{T})$ and ε on all *test* set as the final result;

Algorithm 1: Nested cross validation

Note that, the *training* set, the validation set and the test are disjoint to each other. The deployed nested 399 cross validation includes two loops: *inner* loop and *outer* loop. The inner loop is designed to estimate the 400 parameters, which is a loop of a variant leave-one-out cross validation in D-Log scheme due to the following 401 two factors: 1) the training set is always the same and is always disjoint with the validation set and the 402 test set; 2) $\varepsilon_{validation}$ is obtained by repeating and averaging the calculation of localization error on each 403 pair of RSSI records and distances in the *validation* set with current parameters. The outer loop is used to 404 evaluate the performance of the model, which is a standard k-fold cross validation, and we set k = 10 in 405 this study. 406

407 5.3. Controlled Environment

Here, we present the experiment results in the controlled environment, including the localization accuracy
 and the impact of sample size.

410 5.3.1. Localization Accuracy

Table 6 shows the results of localization precision $P(\mathcal{T})$ and ε in the controlled environment. It is 411 obtained that, for $P(\mathcal{T})$, the *chi*-squared test shows that there is no statistical significant difference (with 412 chi-squared = 0.6735, p-value = 0.7141) between D-Log, SVM-based method, and Bayesian Network-based 413 method. This indicates that the D-Log scheme performs well in comparison to the high-cost high-complexity 414 scene analysis methods, SVM-based method and Bayesian Network-based method. Furthermore, the D-Log 415 scheme performs significantly better than the path loss model. More importantly, D-Log scheme achieves 416 similar performance to SVM-based method, Bayesian Network-based method in terms of ε . The weighted 417 D-Log algorithm achieves a localization error of 0.93 meters, which is only slightly higher than that of 418 the SVM-based method (0.91 meters); at the same time, it outperforms both Bayesian Network-based 419 method (1.03 meters) and the Path Loss model (1.82 meters). Overall, D-Log scheme achieves comparable 420 localization accuracy to the high-cost high-complexity localization methods. 421



Figure 7: The impact of sample size in the controlled environment

Table 7: Single-floor localization performance in the real-world mall environment. Note, weighted D-Log, D-Log and path loss model used logs of single-AP traces; SVM-based method and Bayesian Network-Based Method used the RSSI records from multiple APs.

Floor	Metric	Weighted D-Log	D-Log	SVM-Based	Bayesian Network-based	Path Loss
1^{st}	$P(\mathcal{T})$	92.3%	92.3%	96.1%	91.0%	10.3%
	ε (m)	1.53	1.53	0.44	1.46	7.74
2^{nd}	$P(\mathcal{T})$	81.6%	81.6%	89.5%	81.6%	21.1%
	ε (m)	2.93	2.93	1.54	4.09	8.98
3^{rd}	$P(\mathcal{T})$	74.3%	74.3%	84.4%	77.9%	44.9%
	ε (m)	4.07	4.07	3.38	6.24	8.14

422 5.3.2. Impact of Sample Size

D-Log scheme uses the RSSI values measured during handover between two neighbouring APs, so it is 423 important to examine the impact of the size of these sample RSSI values. Fig. 7 shows the performance of 424 the D-Log scheme over the number of RSSI values per AP in terms of both localization precision $P(\mathcal{T})$ and 425 error ε . It is observed that, as the size of training RSSI values increases, $P(\mathcal{T})$ consistently increases and ε 426 consistently decreases. This is as what we have analysed in Eq. 20 in Section 3.5, because the confidence 427 interval of D-Log's estimation is proportional to the size of the sample observations. When only several 428 sample observations are available, the performance is inferior, but improves and stabilizes when the sample 429 size is greater than 10 observations in the controlled environment. 430

431 5.4. Large Real-World Environment

Here, we evaluate the proposed D-Log scheme in a real-world large indoor retail environment, an innercity shopping mall in Sydney, Australia, by using the anonymized real-world WiFi log of an opt-in free WiFi network operated by the mall owner. Note that this real-world mall environment is different from the environment of the department meeting room in the controlled environment, especially in terms of environment complexity, which may affect the values of RSSI readings, including brands/models of mobile devices, antenna models, Wi-Fi chipsets [46], and people movement [47] etc.

438 5.4.1. Localization Accuracy

Table 7 shows the localization accuracy in both $P(\mathcal{T})$ and ε within specific single floor. Here, all compared algorithms assume the training set is restricted to the data collected on the same floor as the test location,

Table 8: Multi-floor localization performance in the real-world mall environment. Note, weighted D-Log, D-Log and path loss model used logs of single-AP traces; SVM-based method and Bayesian Network-based method used the RSSI records from multiple APs.

	Weighted D-Log	D-Log	SVM-Based	Bayesian Network-Based	Path Loss
$P(\mathcal{T})$	81.1%	81.1%	84.3%	82.3%	28.4%
ε (m)	3.07	3.07	2.89	4.3	8.34



Figure 8: The impact of sampling rate in the real-world mall environment

an approaches replicated from a similar experimental environment [48]. For $P(\mathcal{T})$, it is observed that D-441 log scheme performs comparatively to SVM-based method and Bayesian Network-based method across all 442 three tested floors, and the *chi*-squared test results confirm that there is no significant difference in their 443 performance: the 1st floor (*chi*-squared = 0.1508, *p*-value = 0.9274), the 2nd floor (*chi*-squared = 0.4939, 444 *p*-value = 0.7812), the 3^{rd} floor (*chi*-squared = 0.6645, *p*-value = 0.7173). For ε , when the complexity of the 445 test location increases from the 1^{st} floor to the 3^{rd} floor, D-Log scheme starts outperforming the Bayesian 446 Network-based method. This indicates that in the complex environment, some scene analysis methods 447 will be limited to the capability of the deployed data mining method. In contrast, D-Log exhibits strong 448 robustness in these complex environments. 440

Table 8 shows the results of $P(\mathcal{T})$ and ε across multiple floors. To illustrate the performance of algorithms in this scenario, following [48], we remove the floor information by projecting the training points collected on different floors to a single plane, and execute all the compared algorithms. Again, the D-Log scheme significantly outperforms the Path Loss model and Bayesian network-based method, and performs comparably well to the SVM-based method.

Overall, the D-Log scheme performs comparatively to the state-of-the-art localization algorithms while utilizing less resources and being computationally less complex. In addition, we observe that in both single-floor and multiple-floor environments, weighted D-Log algorithm performs equivalently to the D-Log algorithm. This is due to the large size of the WiFi log, enabling the two methods to converge in performance.

459 5.4.2. Impact of Sampling Rate

As analysed in Section 3.5, D-Log scheme can provide accurate localization accuracy by utilizing large RSSI logs, and it is independent of the sampling rate when logging the WiFi RSSI traces. Fig. 8 shows the sample size and the $P(\mathcal{T})$ and ε performance of D-Log algorithm when the sampling rate of our real-world WiFi logs varies from 5 minutes to 3 hours. The sample size is presented as the fraction of the sampling



Figure 9: The impact of sample size in the real-world environment

Table 9: Comparison of possible handover RSSI values

	Pre-processing	Average	Fixed $-70dB$ [37]	30% of least RSSIs	Path Loss
$P(\mathcal{T})$	81.1%	61.9%	59.5%	63.1%	28.4%
ε (m)	3.07	4.21	4.41	4.23	8.34

rate at the default 5 minutes. While the sampling rate drops from 5 minutes to 3 hours, $P(\mathcal{T})$ drops from 81.1% to 75.0%, and ε increases from 3.07 meters to 3.78 meters. In other words, while the sampling rate drops 18 times, there is no corresponding reduction in $P(\mathcal{T})$ and ε . This indicates that the sampling rate of the WiFi logs has little impact on the performance of D-Log scheme.

The small decrease of localization accuracy when sampling rate drops is caused by the drop of corresponding sample sizes. Specifically, when sampling rate varies from 5 minutes to 3 hours, the size of the corresponding RSSI samples drops by 75.4%. A detailed discussion of the impact of sample size in this real-world environment is discussed in the following section.

472 5.4.3. Impact of Sample Size in Real-World Environment

In the real-world environment, the collected Wi-Fi logs capture heterogeneous mobile devices, thus 473 impacting on localization. We therefore examine the impact of this noisy training sample on the performance 474 of the D-Log scheme. Fig. 9 shows the $P(\mathcal{T})$ and ε performance of D-Log in function of the training sample 475 proportion used in the D-Log scheme, where each result in the figure is executed 10 times and then averaged. 476 We observe that $P(\mathcal{T})$ increases proportionally with number of training samples, while ε decreases, which 477 is consistent with the findings from the controlled environment in Section 5.3. Specifically, the first several 478 samples can largely boost the performance of the D-Log algorithm, and makes it outperform the classic 479 path loss model; the elbow-point is achieved at around 2% of training samples, which is around 250 training 480 samples. This indicates that in large complex environments, D-Log scheme is also robust to the noises of 481 the training data, and can achieve accuracy comparable with competing methods with a limited number of 482 training samples. Recall that the accuracy of the positioning relates to the determination of the distance of 483 the mobile device from the AP, not to an exact point in 2D space. 484

485 5.4.4. Impact of Handover RSSI

To accurately estimate the distance between a mobile device and the servicing AP, D-Log scheme requires the RSSI values when handover happens between adjacent APs in the WiFi network. However, in some



Figure 10: The impact of possible handover RSSI values

existing logs the RSSI values may be collected at very coarse frequency, e.g. the 5 minutes sampling interval in the WiFi log we experimented with. To test the applicability of such a coarsely sampled log, we have collected the accurate RSSI values at exact handover moments as a baseline (see Sec 4.2), and compared it to the subset of records estimated to have happened at, or close to, the handover. Here, we discuss the impact of the uncertainty of the handover identification on the calibration of the D-Log scheme. The baseline D-Log accuracy achieved based on the pre-processed input is compared to the following three methods:

- Average: uses the average of RSSI values of each AP in the log as the handover threshold;
- Fixed -70dB: applies a fixed value of -70dB as the handover threshold. This RSSI value is commonly suggested by commercial WiFi network installation manuals, e.g. Cisco [37];
- Least RSSI: for this method, it is assumed that the potential handovers happened when the disassociation time of a_x is the same as the association time of a_y , which is a_x 's adjacent AP in the WiFi network (recall, that our logs have a sampling frequency of 5mins). Then, a limited fraction of the least of these RSSI values is used to select records assumed to relate to handover RSSIs. Fig. 10 shows the performance of this method as a function of the fraction of least RSSI values. Initially, when only a small proportion (no more than 30%) of the least RSSI values are selected, the performance increases steeply; beyond 30%, the performance deteriorates.

Table 9 shows the performance of these methods in terms of $P(\mathcal{T})$ and ε . We observe that: 1) the D-Log scheme with the proposed pre-processing steps in Sec 4.2 achieves the best performance; 2) D-Log scheme with possible handover RSSIs, including Average, Fixed -70dB [37] and 30% of least RSSI, outperforms significantly the path loss model. This indicates that even when accurate handover RSSIs are not available, D-Log scheme still outperforms the state-of-the-art path loss model. Furthermore, with minimal environment fingerprinting that is substantially simpler than fingerprinting required by other methods, D-Log is able to achieve very good performance.

511 5.5. Discussion

⁵¹² The proposed D-Log scheme fulfils the five requirements introduced in the introduction of the paper:

non-intrusive: D-Log scheme works on the logs of discrete single-AP RSSI traces collected on the AP side, and does not need any information related with the client mobile devices, e.g. no need to install apps, or turning-on of phone sensors;

- generic: as long as there is an overlap between the signal coverage areas of two adjacent APs, a valid localization can be performed. Note this is generally a priority in WiFi network design. Similarly, the transmitting power of all APs is typically standard and identical for large-scale deployments and can be found in manufacturer's manuals [37];
- light-weight: the proposed D-Log scheme is composed of simple computational components with only
 basic computational requirements;

4. effective: as long as a mobile device connects to the WiFi network, its RSSI value can be identified. Thus, D-Log can make a valid estimate of the radius to the connected AP;

524 5. accurate: the accuracy of the D-Log scheme is comparable to other state-of-the-art RSSI-based local-525 ization methods as shown by our analysis in Section 3.5, with values sufficient for applications requiring 526 an estimate of the immediate spatial context of the user.

⁵²⁷ One limitation of the D-Log scheme is that it builds on the Path Loss model which requires certain ⁵²⁸ parameters of the WiFi network to be known, as shown in Eq. 1. These parameters are known or can be ⁵²⁹ measured by site surveying process, or can be learnt by using cross validation as shown in Section 5.2.2.

Due to the above discussed characteristics, D-Log can be applied in a range of applications, e.g. fine-530 grained spatio-temporal analysis, spatial data management and indoor behaviour analysis [8]. For example, 531 Fig. 11 shows how D-Log scheme can help when only discrete single AP-traces are available. Specifically, 532 the figure on the left shows the D-Log's positioning of two particular mobile devices (the two purple stars). 533 Namely, for each mobile device, the red line denotes the mean of the distribution of the estimated distance 534 between the mobile device and its serving AP, and the pink region corresponds to the standard deviation 535 around the estimated distance. Note that theoretically both the red line and the corresponding pink region 536 are circular rings, but in practice this region's geometry may not resemble a circle due to some reasons, 537 e.g. the varying signal strength distribution. The path loss model can also position the device in a similar 538 way, but with much worse accuracy than that of D-Log, which is theoretically analysed in Section 3.5. The 539 application of D-Log is highlighted in inset (right), showing localization improvement (the dark cyan line 540 and the corresponding light cyan region) over simple service area positioning approximated by a Voronoi 541 polygon [49] (thick blue line) and adjusted Voronoi regions (orange line), each centered on a single AP, that 542 encompass all the points that are closest to that AP and accessible to the visitors based on the floorplan 543 layout data [50]. Specifically, take the test mobile device near the bottom as an example. The corresponding 544 adjusted Voronoi region covers around 319 m^2 , and D-Log positions it in a circular region of approximately 545 57 m^2 . By overlapping the D-Log positioning results with the adjusted Voronoi region, the localization 546 of the device is improved to a more accurate region of approximately 33 m^2 as shown in Fig. 11 (right). 547 The computational cost of determining this enhanced region is only linearly proportional to the number of 548 locations considered. 549

Finally, like other RSSI based localization methods, the layouts of the environment or the configurations
 of APs affect the proposed D-Log scheme. If they change, new AP logs need to be collected before positioning.
 However, the layout does not change frequently, hence data collection and model re-training will occur only
 as required.

554 6. Conclusions

In this paper, we investigated the following problem: How to perform accurate indoor localization using 555 large-scale logs of discrete single-AP RSSI traces with low sampling rate? We have provided a novel means 556 of post-hoc localization scheme, which is based on WiFi logs only, named the *D-Log* scheme, and proposed 557 two algorithms: the D-Log algorithm and the weighted D-Log algorithm, with D-Log focusing on accuracy 558 and weighted D-Log focusing on efficiency. While D-Log does not allow for the exact computation of 559 the coordinates of the user's position, our contribution is to enhance the position estimation of post-hoc 560 561 localization based on logs of single-AP traces with infrequent sampling rates. D-Log emerges as a novel means of localization enhancement which is simple and allows for improved estimation of the spatial context of the 562 device in an indoor environment. In addition, high absolute accuracy is not always necessary. Approaches 563 enabling contextual reasoning based on topological relationships of objects with approximate boundaries, 564



Figure 11: Illustration of the aim of D-Log (left), and how D-Log can help in reasoning about the tracked device location in spatial data management (right). The band around the ring indicates the accuracy of the D-Log positioning.

such as the egg-yolk model [51, 52] can be used to improve the estimate of the spatial context in which a user 565 is active. We suggest that, by analysing spatial relations of vague regions [53], we can improve our estimates 566 of spatial indoor behaviour of users and thus improve our estimates and predictions of indoor information 567 needs [54, 5]. Coupled with detailed knowledge of the environmental layout, D-Log enables a substantially 568 improved estimation of the likely space in which a user may be located. Together with other signal about 569 the users behaviour (movement history, web browsing logs), D-Log enables sophisticated reasoning about 570 the users' location. Accurate estimates of the indoor context (e.g., proximity to a specific shopping mall) 571 are critical for the improvement of indoor services and have great economical potential in the near future. 572 In the future, we plan to combine D-Log scheme with trilateration to get better localization performance. 573

Acknowledgement 574

This research is supported by a Linkage Project grant of the Australian Research Council (LP120200413). 575

References 576

- [1] G. Durgin, T. S. Rappaport, H. Xu, Measurements and models for radio path loss and penetration loss in and around 577 homes and trees at 5.85 GHz, IEEE Transactions on Communications 46 (11) (1998) 1484-1496. doi:10.1109/26.729393. 578
- [2]Cisco Systems Inc., Location Tracking Approaches, in: Wi-Fi Location-Based Services 4.1 Design Guide, 2008, Ch. 2. 579
- URL http://www.cisco.com/c/en/us/td/docs/solutions/Enterprise/Mobility/WiFiLBS-DG.pdf 580 [3] J. A. Santana, E. Macías, Á. Suárez, D. Marrero, V. Mena, Adaptive Estimation of WiFi RSSI and Its Impact Over 581
- Advanced Wireless Services, Mobile Networks and Applications (2016) 1–13.doi:10.1007/s11036-016-0729-1. 582 A. Suárez, J. A. Santana, E. M. Macias-Lopez, V. E. Mena, J. M. Canino, D. 583 Marrero.
- RSSI Prediction in WiFi Considering Realistic Heterogeneous Restrictions, Network Protocols and Algorithms 6 (4) 584 (2014) 19. doi:10.5296/npa.v6i4.6066. 585 586
 - URL http://www.macrothink.org/journal/index.php/npa/article/view/6066
- Y. Ren, M. Tomko, K. Ong, B. Yuntian, M. Sanderson, The influence of indoor spatial context on user information [5] 587 588 behaviours, in: M.-D. Albakour, C. Macdonald, I. Ounis, C. L. A. Clarke, V. Bicer (Eds.), Workshop on Information Access in Smart Cities, held in conjunction with the 36th European Conference on Information Retrieval ECIR 2014, 589 ACM. 2014. 590

- [6] A. Misra, R. K. Balan, LiveLabs: Initial reflections on building a large-scale mobile behavioral experimentation testbed, 591 SIGMOBILE Mob. Comput. Commun. Rev. 17 (4) (2013) 47-59. doi:10.1145/2557968.2557975. URL http://doi.acm.org/10.1145/2557968.2557975 593
 - S. Scellato, M. Musolesi, C. Mascolo, V. Latora, A. T. Campbell, Nextplace: A spatio-temporal prediction framework for pervasive systems, in: Proceedings of the 9th International Conference on Pervasive Computing, Pervasive'11, Springer-Verlag, Berlin, Heidelberg, 2011, pp. 152–169.
 - Y. Ren, M. Tomko, F. Salim, K. Ong, M. Sanderson, Analyzing Web Behavior in Indoor Retail Spaces, Journal of the Association for Information Science and Technology.
 - [9] C. Luo, H. Hong, M. C. Chan, PiLoc: A self-calibrating participatory indoor localization system, in: IPSN-14 Proceedings of the 13th International Symposium on Information Processing in Sensor Networks, 2014, pp. 143–153. doi:10.1109/IPSN.2014.6846748.
- K. P. Subbu, B. Gozick, R. Dantu, LocateMe: Magnetic-fields-based indoor localization using smartphones, ACM Trans. 602 [10]Intell. Syst. Technol. 4 (4) (2013) 73:1-73:27. doi:10.1145/2508037.2508054. 603 URL http://doi.acm.org/10.1145/2508037.2508054 604
- [11] A. Rai, K. K. Chintalapudi, V. N. Padmanabhan, R. Sen, Zee: Zero-effort crowdsourcing for indoor localization, in: Proceedings of the 18th Annual International Conference on Mobile Computing and Networking, Mobicom '12, ACM, New York, NY, USA, 2012, pp. 293-304. doi:10.1145/2348543.2348580. 607
 - URL http://doi.acm.org/10.1145/2348543.2348580

592

594 595

596

597

598

599

600

601

605

606

608

628

- [12] H. Wang, S. Sen, A. Elgohary, M. Farid, M. Youssef, R. R. Choudhury, No need to war-drive: Unsupervised indoor 609 610 localization, in: Proceedings of the 10th International Conference on Mobile Systems, Applications, and Services, MobiSys '12, ACM, New York, NY, USA, 2012, pp. 197–210. 611
- [13] J. T. Biehl, M. Cooper, G. Filby, S. Kratz, LoCo: A ready-to-deploy framework for efficient room localization using wi-fi, 612 in: Proceedings of the 2014 ACM International Joint Conference on Pervasive and Ubiquitous Computing, UbiComp '14, 613 ACM, New York, NY, USA, 2014, pp. 183-187. doi:10.1145/2632048.2636083. 614 URL http://doi.acm.org/10.1145/2632048.2636083 615
- [14] M. Youssef, M. Mah, A. Agrawala, Challenges: Device-free passive localization for wireless environments, in: Proceedings 616 of the 13th Annual ACM International Conference on Mobile Computing and Networking, MobiCom '07, ACM, New 617 York, NY, USA, 2007, pp. 222-229. doi:10.1145/1287853.1287880. 618 ${\rm URL}\; {\tt http://doi.acm.org/10.1145/1287853.1287880}$ 619
- Paul, E. A. Wan, F. Adenwala, E. Schafermeyer, N. Preiser, J. Kaye, P. G. Jacobs, [15]A. S. 620 MobileRF: A robust device-free tracking system based on a hybrid neural network HMM classifier, in: Proceedings 621 of the 2014 ACM International Joint Conference on Pervasive and Ubiquitous Computing, UbiComp '14, ACM, New 622 York, NY, USA, 2014, pp. 159-170. doi:10.1145/2632048.2632097. 623 624
- URL http://doi.acm.org/10.1145/2632048.2632097 [16] P. Castro, P. Chiu, T. Kremenek, R. R. Muntz, A probabilistic room location service for wireless networked environments, 625 in: Proceedings of the 3rd International Conference on Ubiquitous Computing, UbiComp '01, Springer-Verlag, London, 626 627 UK, UK, 2001, pp. 18-34.
 - URL http://dl.acm.org/citation.cfm?id=647987.741335
- [17]A. Ruiz-Ruiz, H. Blunck, T. Prentow, A. Stisen, M. Kjaergaard, Analysis methods for extracting knowledge from large-scale 629 WiFi monitoring to inform building facility planning, in: 2014 IEEE International Conference on Pervasive Computing 630 and Communications (PerCom), 2014, pp. 130-138. doi:10.1109/PerCom.2014.6813953. 631
- [18]S. Bell, W. R. Jung, V. Krishnakumar, Wifi-based enhanced positioning systems: Accuracy through mapping, calibration, 632 and classification, in: Proceedings of the 2Nd ACM SIGSPATIAL International Workshop on Indoor Spatial Awareness, 633 ISA'10, ACM, New York, NY, USA, 2010, pp. 3-9. 634
- M. Azizyan, I. Constandache, R. Roy Choudhury, SurroundSense: Mobile phone localization via ambience fingerprinting, 635 [19] in: Proceedings of the 15th Annual International Conference on Mobile Computing and Networking, MobiCom '09, ACM, 636 New York, NY, USA, 2009, pp. 261-272. doi:10.1145/1614320.1614350. 637
- URL http://doi.acm.org/10.1145/1614320.1614350 638
- [20]H. Bao, W.-C. Wong, A novel map-based dead-reckoning algorithm for indoor localization, Journal of Sensor and Actua-639 tor Networks 3 (1) (2014) 44-63. doi:10.3390/jsan3010044. 640 URL http://www.mdpi.com/2224-2708/3/1/44 641
- [21] A. T. Mariakakis, S. Sen, J. Lee, K.-H. Kim, Sail: Single access point-based indoor localization, in: Proceedings of the 642 12th Annual International Conference on Mobile Systems, Applications, and Services, MobiSys '14, ACM, New York, NY, 643 USA, 2014, pp. 315-328. doi:10.1145/2594368.2594393. 644
- URL http://doi.acm.org/10.1145/2594368.2594393 645
- J. Hightower, G. Borriello, Particle filters for location estimation in ubiquitous computing: A case study, in: In Proceedings 646 [22] of International Conference on Ubiquitous Computing (UbiComp, 2004, pp. 88-106. 647
- I. Sabek, M. Youssef, A. Vasilakos, ACE: An Accurate and Efficient Multi-Entity Device-Free WLAN Localization System, [23]648 IEEE Transactions on Mobile Computing 14 (2) (2015) 261-273. doi:10.1109/TMC.2014.2320265. 649
- A. Khan, S. K. A. Imon, S. K. Das, A novel localization and coverage framework for real-time participatory urban 650 24 monitoring, Pervasive and Mobile Computing 23 (2015) 122-138. doi:10.1016/j.pmcj.2015.07.001. 651
- [25]F. Salim, M. Williams, N. Sony, M. Dela Pena, Y. Petrov, A. A. Saad, B. Wu, Visualization of wireless sensor networks 652 using ZigBee's received signal strength indicator (RSSI) for indoor localization and tracking, in: 2014 IEEE Interna-653 654 tional Conference on Pervasive Computing and Communications Workshops (PERCOM Workshops), 2014, pp. 575-580. doi:10.1109/PerComW.2014.6815270. 655

- [26] A. Savioli, E. Goldoni, P. Savazzi, P. Gamba, Low complexity indoor localization in wireless sensor networks by UWB 656 and inertial data fusion, arXiv e-print 1305.1657 (may 2013) 657
- [27] D. Hahnel, W. Burgard, D. Fox, K. Fishkin, M. Philipose, Mapping and localization with rfid technology, in: ICRA'04. 658 2004 IEEE International Conference on Robotics and Automation, Vol. 1, IEEE, 2004, pp. 1015–1020. 659
- 660 [28] Y. Zhuang, Z. Syed, J. Georgy, N. El-Sheimy, Autonomous smartphone-based wifi positioning system by using access points localization and crowdsourcing, Pervasive and Mobile Computing 18 (2015) 118-136. doi:10.1016/j.pmcj.2015.02.001. 661
- [29]J. H, Hightower, G. Borriello, Location systems for ubiquitous computing, Computer 34 (8) (2001) 57–66. 662
- H. Liu, H. Darabi, P. Banerjee, J. Liu, Survey of wireless indoor positioning techniques and systems, IEEE [30]663 Transactions on Systems, Man, and Cybernetics, Part C: Applications and Reviews 37 (6) (2007) 1067-1080. 664 doi:10.1109/TSMCC.2007.905750. 665
- [31]N. Swangmuang, P. Krishnamurthy, An effective location fingerprint model for wireless indoor localization, Pervasive and 666 Mobile Computing 4 (6) (2008) 836-850. doi:10.1016/j.pmcj.2008.04.005. 667
- E. Mok, G. Retscher, Location determination using WiFi fingerprinting versus WiFi trilateration, Journal of Location 668 [32] Based Services 1 (2) (2007) 145-159. doi:10.1080/17489720701781905. 669
 - URL http://dx.doi.org/10.1080/17489720701781905

670

695

- [33] M. Werner, L. Schauer, A. Scharf, Reliable trajectory classification using wi-fi signal strength in indoor sce-671 narios, in: Position, Location and Navigation Symposium - PLANS 2014, 2014 IEEE/ION, 2014, pp. 663-670. 672 673 doi:10.1109/PLANS.2014.6851429.
- [34] A. K. M. Mahtab Hossain, H. Nguyen Van, W.-S. Soh, Utilization of user feedback in indoor positioning system, Pervasive 674 675 and Mobile Computing 6 (4) (2010) 467-481. doi:10.1016/j.pmcj.2010.04.003. 676
 - URL http://www.sciencedirect.com/science/article/pii/S1574119210000416
- [35] B. Wang, S. Zhou, L. T. Yang, Y. Mo, Indoor positioning via subarea fingerprinting and surface fitting with received 677 signal strength, Pervasive and Mobile Computing 23 (2015) 43-58. doi:10.1016/j.pmcj.2015.06.011. 678
- [36] Cisco Meraki, Understanding Wireless Performance and Coverage. URL https://documentation.meraki.com/MR/WiFi 679 _Basics_and_Best_Practices/Understanding_Wireless_Performance_and_Coverage, Tech. rep. 680
- [37]Cisco Systems Inc., Voice over Wireless LAN 4.1 Design Guide, Tech. Rep. Cisco Validated Design I (2010). 681
- O. Chapelle, Training a support vector machine in the primal., Neural computation 19 (5) (2007) 1155-1178. [38]682 683 doi:10.1162/neco.2007.19.5.1155.
- G. K. B. Richard A. Johnsom, Statistics: Principles and Methods, 6th Edition, John Wiley and Sons, 2009. 684 [39]
- [40] C. L. Wu, L. C. Fu, F. L. Lian, WLAN location determination in e-home via support vector classification, 685 IEEE International Conference on Networking, Sensing and Control, 2004, Vol. 2, 2004, pp. 1026-1031. 686 in: doi:10.1109/ICNSC.2004.1297088. 687
- [41] P. Agrawal, N. Patwari, Kernel Methods For RSS-Based Indoor Localization, in: S. A. R. Zekavat, R. M. Buehrer (Eds.), 688 Handbook of Position Location: Theory, Practice, and Advances, first edit Edition, John Wiley & Sons, Inc., 2012, Ch. 14, 689 pp. 457-486. 690
- H. Zou, X. Lu, H. Jiang, L. Xie, A Fast and Precise Indoor Localization Algorithm Based on an Online Sequential Extreme [42]691 692 Learning Machine, Sensors 15 (1) (2015) 1804-1824. doi:10.3390/s150101804
- [43] S. N. Patel, K. N. Truong, G. D. Abowd, PowerLine Positioning : A Practical Sub-Room-Level, in: UbiComp'06 Proceed-693 ings of the 8th international conference on Ubiquitous Computing, 2006, pp. 441-458. 694
 - B. D. Ripley, Pattern Recognition and Neural Networks, 1st Edition, Cambridge University Press, 1996. [44]
- S. Arlot, A. Celisse, A survey of cross-validation procedures for model selection, Statistics Surveys 4 (2010) 40–79. [45]696 arXiv:0907.4728, doi:10.1214/09-SS054. 697 698
 - URL http://eprints.pascal-network.org/archive/00006812/
- G. Lui, T. Gallagher, B. Li, A. G. Dempster, C. Rizos, Differences in RSSI readings made by different Wi-Fi chipsets: A 699 46 limitation of WLAN localization, in: 2011 International Conference on Localization and GNSS, ICL-GNSS 2011, 2011, 700 pp. 53-57. doi:10.1109/ICL-GNSS.2011.5955283. 701
- J. S. C. Turner, M. F. Ramli, L. M. Kamarudin, A. Zakaria, a. Y. M. Shakaff, D. L. Ndzi, C. M. Nor, N. Hassan, S. M. [47]702 Mamduh, The study of human movement effect on Signal Strength for indoor WSN deployment, in: IEEE Conference on 703 Wireless Sensor (ICWISE), 2013, pp. 30-35. doi:10.1109/ICWISE.2013.6728775. 704
- V. Otsason, A. Varshavsky, A. Lamarca, E. D. Lara, Accurate GSM Indoor Localization, in: Proceeding UbiComp'05 705 [48]Proceedings of the 7th international conference on Ubiquitous Computing, 2005, pp. 141–158. doi:10.1007/11551201_9. 706 A. Okabe, B. Boots, K. Sugihara, S. N. Chiu, Spatial Tesselations: Concepts and Applications of Voronoi Diagrams, 2nd 707 [49]
- Edition, Wiley Series in Probability and Statistics, John Wiley and Sons, Ltd., Chichester, UK, 1999. 708 [50] Y. B. Bai, S. Wu, Y. Ren, K. Ong, G. Retscher, A. Kealy, M. Tomko, M. Sanderson, H. Wu, K. Zhang, A new approach
- 709 for indoor customer tracking based on a single wi-fi connection, in: Fifth International Conference on Indoor Positioning 710 and Indoor Navigation IPIN2014, IEEE, 2014. 711
- A. G. Cohn, N. M. Gotts, The egg-yolk representation of regions with indeterminate boundaries, Geographic objects with [51]712 713 indeterminate boundaries 2 (1996) 171–187.
- T. Beaubouef, F. Petry, Vagueness in spatial data: Rough set and egg-yolk approaches, in: L. Monostori, J. Vancza, M. Ali 714 (Eds.), Engineering of Intelligent Systems, Vol. 2070 of Lecture Notes in Computer Science, Springer, Berlin, Heidelberg, 715 2001, pp. 367-373. doi:10.1007/3-540-45517-5_41. 716
- [53]A. J. Roy, J. G. Stell, Spatial relations between indeterminate regions, International Journal of Approximate Reasoning 717 718 27(3)(2001)205-234.
- 719 [54]Y. Ren, K. Ong, M. Tomko, M. Sanderson, How people use the web in large indoor spaces, in: 2014 ACM International Conference on Information and Knowledge Management CIKM 2014, ACM, 2014, pp. 1879–1882. 720