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Lagged correlation-based deep learning for directional trend change prediction in financial time series

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Abstract

Trend change prediction in complex systems with a large number of noisy time series is a problem with many applications for real-world phenomena, with stock markets as a notoriously difficult to predict example of such systems. We approach predictions of directional trend changes via complex lagged correlations between them, excluding any information about the target series from the respective inputs to achieve predictions purely based on such correlations with other series. We propose the use of deep neural networks that employ stepwise linear regressions with exponential smoothing in the preparatory feature engineering for this task, with regression slopes as trend strength indicators for a given time interval. We apply this method to historical stock market data from 2011 to 2016 as a use case example of lagged correlations between large numbers of time series that are heavily influenced by externally arising new information as a random factor. The results demonstrate the viability of the proposed approach, with state-of-the-art accuracies and accounting for the statistical significance of the results for additional validation, as well as important implications for modern financial economics.

Keywords: Lagged correlation, Deep learning, Trend analysis, Stock markets 2010 MSC: 68T05, 62P20

1 1. Introduction

An increased interest in deep-layered machine learning approaches for time series analysis and forecasting resulted in applications in various fields, establishing this area as a challenging topic of interest (Cao and Tay, 2003; Nesreen et al., 2010). When it comes to the effective use of deep neural networks, one of the primary concerns is a sensible approach to feature engineering for useful data representations. This process often depends on domain knowledge about

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⁸ the respective area of application and is, more often than not, a time-consuming ⁹ part of research (Najafabadi et al., 2015). Some researchers equate applied ma-10 chine learning, in an attempt to emphasize the relative importance, with the 11 concept of feature engineering itself (Ng, 2012). Such representations have to 12 be informationally rich enough to incorporate the looked-for lagged correlations 13 between time series while, at the same time, being constrained to a discrete 14 number per observation and variable for input features in a feed-forward neural 15 network. Zhang and Qi (2005) find that feed-forward neural networks are not 16 able to capture the necessary information when applied to raw data from time 17 series with seasonal and trend patterns, which opens the field for approaches to 18 feature engineering that allow for an effective use of time series data for trend 19 predictions in a variety of application areas.

In this paper, we test the hypothesis that deep feed-forward neural networks combined with exponential smoothing for the training inputs are suitable for 22 learning lagged correlations between the step-wise trends of a large number of 23 time series, and that such models can be successfully applied to current research 24 on realworld forecasting problems. In order to test this approach, we apply the 25 proposed method to gradients computed for five years of historical stock price 26 data of the S&P 500 stocks in one-hour intervals for daily trends, adding the 27 complication of relatively few observations. For a more in-depth overview of soft 28 computing methods in financial market research, interested readers are referred 29 to Cavalcante et al. (2016), with Weng et al. (2018) providing an application of 30 ensemble methods to financial markets using a variety of text-based and index-31 based features.

The experiments that are conducted for this purpose demonstrate the via-³² bility of this approach by predicting price trend changes with an accuracy above ³⁴ given market baselines and within a stringent statistical validation framework. ³⁵ In order to evaluate the soundness of our conclusions, we test the results against ³⁶ the alternative possibilities of simply learning frequencies or probabilistic distri-³⁷ butions, calculate confidence intervals and *p*-values, as well as a visual analysis ³⁸ via notched box plots (McGill et al., 1978). The results of this paper deliver ³⁹ evidence for the applicability to a number of real-world problems that deal with ⁴⁰ complex relationships of large numbers of noisy time series.

⁴¹ The results for the specific tests performed for this paper are also discussed ⁴² in relation to the random walk hypothesis and the efficient-market hypothesis ⁴³ in financial economics.

⁴⁴ Our hypothesis relates to the microstructure model by Ho and Stoll (1983), ⁴⁵ which characterizes the links between quote changes in a stock and the evolution ⁴⁶ of the inventory with respect to the other stocks. The model shows that quote ⁴⁷ changes in stock *a*, which is in reaction to a transaction in stock *b*, are based ⁴⁸ on $\operatorname{cov}(Ra, Rb)/\sigma^2(Rb)$. This portfolio view of stock trading is in line with ⁴⁹ commonly deployed diversification strategies in finance and has given rise to ⁵⁰ highly popular instruments such as exchange traded funds (ETFs), which offer ⁵¹ cheap means of diversifying risk. This study has implications for perhaps the ⁵² longest running debate in the financial economics literature.

⁵³ The unpredictability of the factors influencing price discovery in stocks

makes the price discovery process noisy (Chen et al., 1986). The unpredictabil-54 ity (or randomness) of the information acquisition process in financial markets 55 is consistent with the efficient market hypothesis described by Fama (1965) and 56 Fama (1970) as well as the random walk hypothesis (Kendall and Hill, 1953; 57 Cootner, 1964; Malkiel, 1973). These theories contradict our hypothesis on the 58 existence of time-shifted correlations in stock markets. Consistent with our ex-59 pectations, our results deliver rigorously tested empirical evidence, supporting 60 the existence of time-shifted correlations in stock prices and thus contradict the 61 random walk theory. Specifically, our findings are inconsistent with Sitte and 62 Sitte (2002), who argue that the price discovery process for S&P 500 stocks is 63 a random walk due to the inability of artificial neural networks to extract any 64 information resulting in above-average predictions for those stocks. 65

Our results are, however, consistent with previous, albeit weak, evidence for 66 the absence of a random walk in financial time series via the use of artificial 67 neural networks as presented by Darrat and Zhong (2000). The consistency of 68 the efficient market hypothesis with the random walk hypothesis also implies 69 that our findings contradict much of the efficient market hypothesis, which is 70 widely supported by a large section of the finance academic literature (Fama, 71 1970; Doran et al., 2010). However, despite the seemingly established nature of 72 the random walk hypothesis, over the years, many studies, like Lo and MacKin-73 lay (1987), have questioned its validity, while others have proposed alternatives. 74 For example, one popular alternative hypothesis is that stock returns may be 75 explained by the sum of a random walk and a stationary mean-reverting com-76 ponent (Summers, 1986; Fama and French, 1988). Lo and MacKinlay (1987) 77 also advance the view that the efficient market hypothesis is an 'incomplete hy-78 pothesis'. This current paper is not an attempt to reconcile one of the longest 79 standing debates in the finance literature; rather, we propose a price predic-80 tion approach based on an amalgamation of market microstructure theory and 81 machine learning. 82

83 2. Related research

⁸⁴ 2.1. Trend prediction in time series

The feasibility of different types of artificial neural networks for trend pre-85 diction in time series was indicated early by Saad et al. (1998). Other types of 86 noise reduction, for example PCA for echo state networks, have already been 87 subjected to similar investigations, with no significant success being reported 88 (Lin et al., 2009). While research on regression gradients as input features for 89 feed-forward neural networks is sparse in the published literature, the usage of 90 directional derivatives of wavelets was recently introduced in natural language 91 processing (Gibson et al., 2013). 92

Features based on derivatives were subsequently adapted in other research areas, for example statistics and digital signal processing (Grecki and Luczak, 2013; Baggenstoss, 2015). The success of the regression derivative-based approach for trend forecasting using lagged correlations between time series presented here provides additional evidence for the viability of such methods for time series applications. Specifically, positive results show the value and applicability of deep learning methods for such scenarios.

100 2.2. Stock markets as a use case

Price changes in stock markets are, at their core, the result of human deci-101 sions which, in turn, are based on their respective beliefs about stocks' future 102 performance. Stocks are influenced not only by a company's respective perfor-103 mance, but also by newly arising information not directly linked to the latter. 104 Examples are negative effects on stock prices for airlines after the 9/11 at-105 tacks, and similar effects after news about a CEO's diminishing personal health 106 107 (Drakos, 2004; Perryman et al., 2010). Price changes are, therefore, the result of human beliefs about the future beliefs of other humans, which can be iterated 108 indefinitely and is an example of real-world time series being created by human 109 decision-making and the implementation of automated decision-making based 110 on these notions, especially in high frequency trading. 111

It can be concluded that time series of historical stock prices contain, due to 112 these factors, a large amount of noise in the form of new information influencing 113 the process, and through biases and errors in human decision-making. Markets 114 are, as a result, inherently prone to fluctuations triggered by overreactions, 115 and to dynamical reinforcement during temporary crazes (Chen et al., 1986). 116 This makes them, due to the complexity of their generation process, a suitable 117 use case to test the proposed model's ability to identify and exploit lagged 118 correlations in notoriously hard-to-predict noisy environments. 119

Relevant recent work on stock market prediction includes Zhang and Wu (2009) on changes to backpropagation, Boyacioglu and Avci (2010) on the use of fuzzy inference frameworks, Chatzis et al. (2018) on deep learning for financial crisis forecasting, Zhang et al. (2018) on unsupervised heurstic algorithms, and Malagrino et al. (2018) on Bayesian network approaches. Another area of research is concerned with text-based stock market prediction, with Nassirtoussi et al. (2014) providing a holistic overview for interested readers.

127 2.3. ANNs and stock markets

The viability of using artificial neural networks for stock market predictions 128 was first hypothesized by White (1988), with subsequent indications of success 129 by Saad et al. (1998) and Skabar and Cloete (2002). Zhang et al. (1997) re-130 port on the special suitability of artificial neural networks to such forecasting 131 problems due to their adaptability, non-linearity and arbitrary function map-132 ping. Takeuchi and Lee (2013) first made experimental results on the use of 133 deep neural network models for stock market prediction available as a working 134 paper by using the work of Hinton and Salakhutdinov (2006), and with a binary 135 prediction accuracy of 53.36%. A similar approach by Batres-Estrada (2015) 136 resulted in a comparable reported accuracy of 52.89%, also outperforming a 137 simple logistic regression. 138

¹³⁹ 3. Gradients as features

¹⁴⁰ 3.1. Approximating trend strengths

Linear regressions are a wide-spread approach to capture trends limited to a certain time frame and, as such, form the basis for these features. They take, in their general form, the following shape, with *i* indicating one of *m* observations, intercept β_0 and error term ϵ_i :

$$y_i = \beta_0 + \beta_1 x_{i,1} + \beta_2 x_{i,2} + , \dots, +\beta_p x_{i,p} + \epsilon_i$$

= $\mathbf{x}_i^T \boldsymbol{\beta} + \epsilon_i, \quad i \in \{1, \dots, m\}$ (1)

As a one-variable feature is necessary for the model's input vector, a simple linear regression is used as a least-squares estimator of equation (1). This estimator identifies one explanatory variable to minimize the squared sum of the residuals by fitting a line. The equation is presented as a minimization problem seeking β_0 and the slope β_1 for $\min_{\beta_0,\beta_1} Q(\beta_0,\beta_1)$:

$$Q(\beta_0, \beta_1) = \sum_{i=1}^{m} (y_i - \beta_0 - \beta_1 x_i)^2$$
(2)

The gradient of the resulting regression model, that is, the slope of the fitted 150 line, can then be computed by taking the first derivative. In the given task, this 151 means extracting β_1 as a feature. Information about the value of a time series 152 at a point along the timeline is lost in this process, with the resulting gradient 153 representing the strength of an upwards or downwards movement of a trend via 154 the regression model. A time interval size over which the regression is to be 155 performed has to be determined in advance. The feature matrix, which is later 156 used for the input of a feed-forward neural network, consists of the derivatives 157 w.r.t. $\beta_{1,k}$ of a simple linear regression as in equation (2) per time series $k \in$ 158 $S := \{1, \dots, s\}$, and for all separate time intervals $j \in T := \{1, \dots, t\}$, 159 meaning that $\forall j \in T, k \in S$: 160

$$\frac{\partial}{\partial \beta_{1,k}^{j}} \min_{\substack{\beta_{0,1}^{j}, \beta_{1,1}^{j} \\ \beta_{0,1}^{j}, \beta_{1,1}^{j}}} \sum_{i=1}^{m} (y_{i,k} - \beta_{0,k}^{j} - \beta_{1,k}^{j} x_{i,k}^{j})^{2} \\
\Rightarrow \begin{pmatrix} \beta_{1,1}^{1} & \beta_{1,1}^{2} \\ \beta_{1,2}^{1} & \beta_{1,2}^{2} \\ \beta_{1,2}^{1} & \beta_{1,2}^{2} \\ \vdots \\ \vdots \\ \beta_{1,s}^{1} & \beta_{1,s}^{2} \\ \beta_{1,s}^{1} \\ \beta_{1,s}^{2} \\ \beta_{1,s}^{2} \\ \vdots \\ \beta_{1,s}^{1} \\ \beta_{1,s}^{2} \\ \beta_{1,s}^{2} \\ \vdots \\ \beta_{1,s}^{1} \\ \beta_{1,s}^{2} \\ \beta_{1,s}^$$

When applied to all time intervals, this resulting feature matrix **B** of respective gradients contains directional trend strength indicators for all time series, one per row, and with one time interval per column. This representation of time interval trends is the basis for the subsequent smoothing process.

One point of concern is the reduction of the dataset due to the given time 165 interval over which a trend is approximated, which requires a sufficiently large 166 set of observations to effectively train artificial neural networks after the reduc-167 tion (Glorot and Bengio, 2010). Research on the usage of regression derivatives 168 for predictive classification tasks with time series, especially with regard to deep 169 learning approaches, remains sparse. Examples from recent years include the 170 use of such gradients for audio classification via decision trees and support vec-171 tor machines by Mierswa and Morik (2005), gradients of wavelets for tasks in 172 natural language processing by Gibson et al. (2013) and the addition of such 173 derivatives to dynamic time warping (Grecki and Łuczak, 2013). 174

175 3.2. Infinite impulse response filtering

Clarke et al. (2000) and Gehrig and Menkhoff (2006) state that technical 176 analysis, that is, the prediction of stock price changes based on historical stock 177 market data in the form of time series, is wide-spread in the current invest-178 ment industry. The exponential moving average is, in this context, one of the 179 dominant techniques used as a lagged indicator for technical analysis. In the 180 general study of time series analysis, it is better known as exponential smoothing 181 (Brown, 1956; Holt, 1957). It serves as a type of infinite impulse response fil-182 tering that can be computed recursively as follows, with α being the smoothing 183 factor used, with $\alpha \in (0, 1)$ and t as the time interval indicator: 184

$$s_0 = x_0 s_t = \alpha x_t + (1 - \alpha) s_{t-1} , \ t > 0$$
(4)

Exponential smoothing is a staple method in digital signal processing, and special consideration has to be placed on the choice of the smoothing factor α . The sensitivity of a prediction w.r.t. s_0 is inversely correlated with the size of α , with the average of at least 10 time intervals being widely recommended as the initial value for s_0 (Nahmias, 2009). The applicability of infinite impulse response filters to the smoothing of financial time series has first been emphasized by Genay et al. (2001).

¹⁹² 4. Empirical validation

¹⁹³ 4.1. Data cleansing and pre-processing

The dataset, which is provided by Thomson Reuters Tick History, features the average stock price per hourly time step from 2011-04-04 to 2016-04-01, covering about five years worth of stock market information for the current 505 S&P 500 stocks, with a combined number of 6,049,849 observations. It contains the price, date and time of an observation and the respective stock's Reuters Instrument Code (RIC).

For an effective use as feature vectors, and to avoid a contamination from a financial perspective, the price series over which the step-wise gradients are computed have to be perfectly aligned and existent for all time steps and used ²⁰³ stocks. As the dataset is imperfect, invalid time stamps and non-consistent ²⁰⁴ values for holidays are sorted out, and missing values are reconstructed via the ²⁰⁵ next preceding value of a row with the same RIC. The RICs for which a cut-off ²⁰⁶ value for a minimal number of existent observations is present are then kept. ²⁰⁷ The rest of the stocks, 56 in total, are discarded, as a further reconstruction ²⁰⁸ process would endanger the dataset of becoming corrupted through too many ²⁰⁹ reconstructed insertions.

To obtain a perfect alignment despite missing rows, we devised an algorithm optimized for speed that operates on two combined date-time vectors; one from an uninterrupted timeline and one per stock matrix, with the dataset being split into a list of matrices with one list place per RIC.

For each list place, the matrix is inflated to avoid higher computational

²¹⁵ costs via appending rows. At each discrepancy between the ideal and actual ²¹⁶ timedate vectors, the original matrix within the inflated matrix is shifted one ²¹⁷ place down, the missing row is substituted with the next adjacent values, and ²¹⁸ the missing date-time stamp is inserted. As this process operates on the fine-²¹⁹ grained level of the raw data and only replaces very few missing values, for ²²⁰ example for initial public offerings after the stock market opens and earlier ²²¹ market closings on Thanksgiving, the result on trend features over larger time ²²² intervals is negligible.

This process is repeated for all list places until all matrices feature a non-²²⁴ interrupted dataset, after which each matrix is cut at the first occurrence of the ²²⁵ last date-time stamp to deflate the matrix. The prices of the resulting list of ²²⁶ matrices are then extracted and saved as a combined matrix containing only ²²⁷ price information per column-wise time step, with one stock, as identified by ²²⁸ the respective RIC, per row of the combined matrix.

Subsequently, we compute the simple linear regression from equation (2) on ²³⁰ the values per trading day for each stock, resulting in one price trend approx-²³¹ imation per trading day. The gradients are then extracted to get the feature ²³² matrix **B** from equation (3), with 1,241 observations for 449 stocks. The expo-²³³ nential smoothing process from equation (4) with $\alpha = 0.05$ and the calculation ²³⁴ of a directional trend change indicator based on a stock price's trend change rel-²³⁵ ative to the previous step's trend, are implemented at the construction for each ²³⁶ stock's classification model to avoid storing the correct target values separately.

At the end, each matrix is cut at the first occurrence of the last data-time

stamp, and only price information per stock is retained. With this information, price trend approximations are computed, for each trading day and stock, with the simple linear regression from equation (2). This leaves us with 1,241 ob- $_{241}$ servations for 449 stocks for feature matrix **B** from equation (3), on which the $_{242}$ exponential smoothing from equation (4) is performed.

243 4.2. Setup of the use case experiments

The experimental setup shown in Figure 1 ensures that the experiments test for time-shifted correlations between time series instead of using a stock's own historical information, that is, data of the predicted stock is not part of ²⁴⁷ the model's input. This is one of the main differences to related work on time ²⁴⁸ series-based stock market prediction, for example Takeuchi and Lee (2013), ²⁴⁹ with the accuracy used as the metric by which the presence of correlations is ²⁵⁰ measured. Another difference is the use of more short-term, meaning daily ²⁵¹ instead of monthly, predictions. As we aim to find time-invariant correlations ²⁵² between stocks, five-fold cross-validation with a validation set for early stopping ²⁵³ is used to reduce the variability of results, and to use data in a frugal manner ²⁵⁴ (Seni and Elder, 2010).

INSERT FIGURE 1 HERE (COLOR IN PRINT)

Figure 1: Schematic depiction of the gradient calculation and deep classification model process. For each time series, each time interval's trend approximation is computed via a simple linear regression over a pre-determined time window, the gradient of which is then extracted to form a time interval's gradient vector $(\beta_{1,1}, \beta_{1,2}, \dots, \beta_{1,n})$ as one column of the feature matrix. The latter is then used to train a deep feed-forward neural network for the binary prediction of directional trend changes.

This way, a 60-20-20 split for training, validation and test sets is used for ²⁵⁵ each fold and stock. When performing k-fold cross-validation, a central concern ²⁵⁷ is the choice of the correct split ratios. The 60-20-20 split is a frequently used ²⁵⁸ rule of thumb in machine learning in which a validation set, in addition to the ²⁵⁹ training and test sets, are necessary. Regarding the larger size of the training ²⁶⁰ set, we want to ensure a large-enough number of data points in the training ²⁶¹ set to enable the model to learn sufficiently. Conversely, if the validation set is ²⁶² too small, the validation of the learned parameters cannot be properly assessed ²⁶³ with a representative sample, while an insufficient size of the test set leads to ²⁶⁴ the final test on unseen data being similarly non-representative. The training ²⁶⁵ examples split from the dataset are normalized element-wise using min-max ²⁶⁶ scaling. Exponential smoothing, as described before, is then applied to the ²⁶⁷ input features of all three sets.

The experiments are run for all time series as a respective target by looping 269 over an index *i* for all column-wise stock gradients and splitting the matrix into 270 the target gradients for stock *i* and the inputs for the rest of the columns. The 271 time intervals are then shifted one step by clipping the first row of the input 272 matrix and the last value of the output vector. The output vector is subsequently 273 replaced by a binary one-hot representation that indicates whether the gradients 274 for each successive time interval for stock *i* are larger or smaller than for the 275 preceding interval.

We repeat these experiments for each stock as the respective target, without 276 past information concerning the stock itself in the inputs. The output vector 277 takes the form of a one-hot representation to indicate whether gradients are 278 larger or smaller than for the preceding interval. Two output nodes are chosen 279 instead of one in accordance with the results of Takeuchi and Lee (2013) and 280 Ding et al. (2015) in favor of this setup, and to ease the structural comparability. 281 Preliminary test runs, with 20 randomly chosen stocks to avoid cherry-282 picking hyperparameters for the use case in general, showed the smallest test 283

set error for 400 nodes per hidden layer, as measured in increments of 50 nodes 285 for up to 800 nodes. The final model used for the experiments features 10 hid-286 den layers, a number that was determined by starting with one hidden layer 287 and. subsequently, adding 4 - n hidden layers for $n \in \{0, 1, 2, 3\}$, with the op-288 tion to add further single layers in case of still-increasing performance. With 289 improved performance up to the addition of nine additional hidden layers, the 290 performance plateaued at this point. Early stopping, together with ℓ_2 regu-291 larization, is used to prevent overfitting and unnecessary complexity, whereas 292 momentum is applied to prevent stochastic gradient descent from terminating 293 in small-spaced local minima. Dropout, another popular method of preventing 294 overfitting in neural network, is a popular technique in deep learning (Hinton 295 et al., 2012; Srivastava et al., 2014). Initial experiments with different levels of 296 omissions did, however, prevent the model from learning, which can be ascribed 297 to the very high levels of noise in stock market information. Epoch-based learn-298 ing rate decay is used to find a minimum along the optimizer's descent path, 299 with learning rate ν , decay coefficient δ and epoch number e:

$$\mu_e = \mu_{e-1} \cdot \qquad \frac{1}{1 + \delta \cdot e} \tag{5}$$

Hyperbolic tangent functions serve as activation functions, with sigmoid functions at the output layer. The former choice is due to the intent to combat weight saturation, while the latter function is chosen over the softmax function due to the interpretability of the results as independent probabilities, and be-304 cause these results are not needed to integrate to 1 as inputs for subsequent 305 methods.

The model's weights are initialized as scaled samples from a zero-mean Gaussian distribution to address the potential of vanishing or exploding gradients, with a variance of $\frac{2}{n_l}$ and an initial bias of 0, and with n_l denoting the number of connections in the the *n*-th layer, allowing for an easy adaptation to future ³¹⁰ experiments with rectified linear units (Glorot and Bengio, 2010; He et al., 2015).

311 4.3. Accuracy and validation measures

For each stock and fold in each model, a randomly shuffled copy of the predictions is created and tested against the correct targets in addition to the predictions, resulting in mock predictions with a distribution identical to the actual predictions. This copy can be used to test whether the model just learned the distribution of the two output classes in the training set, which would result in very similar accuracies for the actual and mock predictions when compared to the correct targets.

Another case that has to be ruled out is that of a model learning to predict the dominant class of a training set. Two targets are created for each stock and model, each containing only one of the two classes. A model that learns more actionable information from its respective inputs than the dominant class of the training set needs to perform better on the test set than both these one-class mock targets in direct comparison to the correct targets. A fourth validation ³²⁵ metric is computed by taking the maximum of all three metrics' accuracies for ³²⁶ each time step, ensuring that a baseline with at least 50% accuracy in each ³²⁷ time step is reached in case of distributions that deviate from a 50:50 distribu-³²⁸ tion. As the use of accuracy as the metric of choice can lead to questionable ³²⁹ results, we randomly sampled 50 of the dataset's stocks and evaluated them for ³³⁰ both accuracy and the area under the curve (AUC) for the receiver operating ³³¹ characteristic, with the latter being a well-established metric for skewed class ³³² distributions (Bradley, 1997). While the classes in our work are well-balanced, ³³³ this exercise provides a validation of the choice of metric, and shines a light on ³³⁴ the necessity of taking class distributions into consideration when dealing with ³³⁵ classification problems. The accuracy for this subset of stocks is 55.284%, while ³³⁶ the AUC score is 0.55278. The necessity of using an additional decimal number ³³⁷ demonstrates the similarity of both metrics for well-balanced classes such as the ³³⁸ ones used in this paper. Additionally, a linear support vector classifier (SVC) ³³⁹ is used on the same gradient-based data to enable a comparison with a simpler ³⁴⁰ approach.

The average accuracy over all stocks is given as the standard method to assess ³⁴² the predictive power of a model. These accuracies do, however, not indicate ³⁴³ whether the predictions' variations are too large to be considered successful, ³⁴⁴ that is, whether the volatility of the model grows too large. For this reason, ³⁴⁵ we also provide accuracies for the three baseline mock predictions. In addition, ³⁴⁶ the *p*-values for the predictions' accuracies via an upper-tail test are calculated ³⁴⁷ for each of the baselines and an additional baseline that contains the highest ³⁴⁸ accuracy among the three baselines for each stock, that is, for each model. ³⁴⁹ The null hypothesis H_0 in each case is that the predictions' accuracies are not ³⁵⁰ significantly larger than the respective baseline, with a very strict significance ³⁵¹ level of $\alpha = 0.001$.

Lastly, notched box plots are a commonly used visualization tool for deson scriptive statistics, using the respective data's quartiles to allow for an intuitive representation. Non-overlapping notches for two boxes indicate a statistically significant median difference at 95% confidence. Welch's *t*-test is used to achieve higher reliability for unequal variances.

In order to rule out the simpler explanation that only a few observations are ³⁵⁷ In order to rule out the simpler explanation that only a few observations are ³⁵⁸ sufficient to identify general market behavior, and to address the possibility that ³⁵⁹ using only past data to predict future trend changes yields no better accuracies ³⁶⁰ than cross-validation that also takes future observations into account, an addi-³⁶¹ tional experiment is conducted: For 20 randomly sampled non-repeating stocks, ³⁶² and with N being the size of the whole dataset, a neural network model is first ³⁶³ fully trained, as for the primary experiments, on the first observation. Then, ³⁶⁴ for l = 2 to (N-1), the model is iteratively updated by training for 3 epochs ³⁶⁵ on observations 1 to l as the training set, while being tested on observations ³⁶⁶ l + 1 to N as the test set. This procedure can be visualized as sliding a divisive ³⁶⁷ line along across the dataset, training on an ever-increasing training set while ³⁶⁸ simultaneously reducing the test set. The last point has to be kept in mind, as a ³⁶⁹ small test set does not offer a good representation of the data. For this reason, ³⁷⁰ the described procedure is stopped at the point when only 10% of observations ³⁷¹ remain in the test set to still deliver a viable estimate.

372 4.4. Results of the experiments

The use of *p*-values has to be viewed with caution, as criticism of their often ³⁷⁴ incorrect use has risen in recent years. In 2016, the American Statistical Associ-³⁷⁵ ation published an official warning regarding the wide-spread misuse of *p*-values ³⁷⁶ (Wasserstein and Lazar, 2016). Accordingly, the *p*-values are given in combi-³⁷⁷ nation with other metrics such as the lower boundary for differences in means ³⁷⁸ given a 99.9% confidence interval, notched box plots for median differences and ³⁷⁹ quartile distributions, and accuracies for models and baselines.

Figure 2 shows the accuracy of 58.10% listed in Table 1 significantly above ³⁸¹ all baselines, both for the means as measured by the *p*-values and the medians as ³⁸² indicated by the box plots, with neither the notches nor the boxes overlapping. ³⁸³ The first and third quartiles are, however, spread wider for the model when ³⁸⁴ compared to the baselines, with the exception of the SVC. In Table 1, the ³⁸⁵ accuracies for the model, the different baselines and a simple linear support ³⁸⁶ vector classifier are given, as well as the *p*-value results with regard to the

means and the minimal difference for a 99.9% confidence interval.

INSERT FIGURE 2 HERE (COLOR IN PRINT)

Figure 2: Statistical validation and accuracies. Part *a* shows a notched box plot representation of the results. Non-overlapping notches indicate a statistically significant difference in medians at 95% confidence, which is the case for all baselines. Here, *class 1* is the forecast that stock trends will change downwards, while *class 2* refers to an upward change. *predictions* denotes the performance of the model, *svc* shows the boxplot for the support vector classifier (SCV), *random* is the performance of a random forecast with the same distribution as the actual predictions, and *best-of* represents the best result among the baselines for each time step. Part *b* shows an intuitive visualization of the mean accuracies. The upper blue line represents the model's predictions, whereas predicting solely upward changes or downward changes is drawn in cyan and green, respectively. Red denotes the random vector with the same class distribution as the red line the SVC's predictions, whereas predicting solely upward changes or downward changes is drawn in light blue and green, respectively. Fulvous denotes the random vector with the same class distribution as the model's predictions, whereas predicting solely upward changes or downward changes is drawn in light blue and green, respectively. Fulvous denotes the random vector with the same class distribution as the model's predictions at the model's predictions. The averages for the model results and the randomized predictions are drawn as lines of the same color.

387

While the focus of this work is the existence and exploitation of lagged 388 correlations, one might be left to wonder what impact the omission of target 389 stock information in the inputs of each stock's run has on the results. To answer 390 this question, we repeat the experiment described above, with this information 391 included in the inputs. The reported result of 58.10% without this information 392 increases to 58.54% when information about the target stock is included. While 393 this shows that a stock's past behavior provides additional information, this 394 result demonstrates the model's ability to infer most of the relevant information 395 from lagged correlations between the target stock and other stocks. 396

As described in the discussion of accuracy and validation measures, a feed-³⁹⁸ forward neural network is trained on the first observation and then re-trained ³⁹⁹ for 3 epochs on the dataset extended by the previous time step for the remaining

accuracies of predictions					
model	rand.	class 1	class 2	best-of	SVC
0.5810	0.5002	0.4955	0.5045	0.5092	0.5474
variances of accuracies					
model	rand.	class 1	class 2	best-of	SVC
$6.12e^{-4}$	$1.43e^{-4}$	$5.93e^{-5}$	$5.93e^{-5}$	$4.50e^{-5}$	$10.87e^{-4}$
tests against baselines					
	rand.	class 1	class 2	best-of	SVC
<i>p</i> -value	$< 1e^{-3}$				

Table 1: Accuracies, variances and baseline comparison. Accuracies and variances for the model's predictions (*model*), as well as for a best-of of all baselines (*best-of*), the randomized baseline with the same class distribution (*rand.*), comparative results for a support vector classifier (*SVC*) and results for predictions for one class exclusively are provided. *class 1* denotes upwards stock trend changes and *class 2* downward stock trend changes. *p*-values and minimum differences are provided for comparison against the chosen baselines.

⁴⁰⁰ time steps' prediction. This process is repeated for 20 randomly chosen stocks, ⁴⁰¹ after which the results for the predictions are averaged. This process is imple-⁴⁰² mented until 90% of the dataset is used as the training set in order to allow for ⁴⁰³ a small number of observations to remain as a test set towards the end. Since ⁴⁰⁴ the robustness of the obtained results is an important factor to be taken into ⁴⁰⁵ account, leaving a sufficient amount of time steps as a test is crucial. If the pro-⁴⁰⁶ cess of shifting from the test to the training set would be taken to the extreme ⁴⁰⁷ by continuing until only one stock is left in the test set, the results would be ⁴⁰⁸ based on a non-representative number of time steps. From a financial markets ⁴⁰⁹ perspective on robustness, the setup of this experiment allows for the assess-⁴¹⁰ ment of the model's performance over multiple years, and thus across changing ⁴¹¹ market conditions over time. For a measurement of the model's accuracy during ⁴¹² the end of the experiments, the average of the last 100 time steps is taken and ⁴¹³ results in an average accuracy of 60.23%.

⁴¹⁴ Notably, this result outperforms the previous experiment that uses cross-⁴¹⁵ validation, which indicates an advantage of learning exclusively from data be-⁴¹⁶ fore the respective test example that is to be classified instead of using training ⁴¹⁷ examples from both before and after the test example to extract time-invariant ⁴¹⁸ market dynamics. Within the framework of the stock market, an explanation ⁴¹⁹ for this observation is that lagged trend correlations in financial markets fea-⁴²⁰ ture information that can be used for predictions about the future in which ⁴²¹ the lagged effect takes place, but to a lesser degree for predictions about past ⁴²² observations. The learned information is, in this case, local within time, render⁴²³ ing cross-validation less effective when compared to training on past data with ⁴²⁴ online updates to adapt to new information. The accuracies of this additional ⁴²⁵ experiment over the course of the training process are depicted in parts a_1 and ⁴²⁶ b_1 of Figure 3.

To determine whether the initial sharp increase in average accuracy and the 427 subsequent slower and quasi-linear increase are a result of the the market or 428 the learning, we repeat the same experiment without the first 100 time steps 429 in which the sharp increase takes place, which means starting at a later point 430 in time and excluding the model from learning about the training examples 431 before that. Part a_1 of Figure 3 shows the initial rise in accuracy for this cut-432 down dataset following a steeper path at first, but reaching the full dataset's 433 first elbow accuracy later in relation to the number of steps since starting the 434 training process. It subsequently follows a more concave curve instead of the 435 full dataset's quasi-linear increase in accuracy during that phase. Similarly, the 436 final level of the cut-down dataset is reached at about the same time as the full 437 dataset's corresponding accuracy, again in relation to the number of steps the 438 model is trained on instead of the actual point in time due to the omission of 439 the first 100 time steps and, therefore, a later point in real time. 440

The resulting average prediction accuracy is 59.50% due to the full dataset's 441 later and more pronounced accuracy peak, although both experiments feature 442 the same dip around time step 900, or time step 1000 for the full dataset. While 443 reaching the peaks in parts a_1 and b_1 of Figure 3 seems to be a result of the 444 number of time steps the models are trained on, the dips at 900 and 1000, 445 respectively, seem to be a result of the market at that time. These results 446 suggests that the primary features of the time series are due to the market, 447 whereas the profiles of the first initial accuracy increase and the subsequent 448 rise, as well as the lower maximum towards the end, can be attributed to the 449 lack of the information contained in the deleted first 100 training examples, 450 inhibiting the portion of long-term market information that would otherwise be 451 extractable from the latter. 452

INSERT FIGURE 3 HERE (COLOR IN PRINT)

Figure 3: Averaged and individual accuracies for the experiment with omitted data for the first 100 time steps. For the same 20 stocks selected via random sampling, a model is iteratively updated for 3 epochs and with the last time step's information as an extension of the training set after each new time step. Parts a_1 and a_2 show the results for averaged and individual accuracies for the case without the first 100 time steps, respectively, whereas parts b_1 and b_2 show the same visualizations for the full dataset containing the first 100 time steps.

Another result of the omission of the first 100 time steps can be seen when comparing the individual accuracies for the targeted stocks in parts b_1 and b_2 of Figure 3. While the individual stocks in both datasets' accuracies feature similar evolutions, the full dataset's accuracies show a clearer trend towards higher accuracies. This observation reflects the more linear ascend of the average accuracy and can be viewed as an indicator of market behavior information from multiple years into the past still influencing the market behavior's overall ⁴⁶⁰ predictability in the present, the implications of which are discussed later.

⁴⁶¹ Figure 4 is comprised of heatmaps for both cases in order to get a better ⁴⁶² overview of the individual 20 stocks featured in Figure 3. As can be seen, ⁴⁶³ the development of the predictive accuracy for individual stocks follows similar ⁴⁶⁴ progressions for both experiments, albeit with slightly different distributions ⁴⁶⁵ and starting points of high-accuracy periods. A more general finding in Figure ⁴⁶⁶ 4 is that some stocks are considerably easier to predict solely on other stocks' ⁴⁶⁷ prior behavior than others.

INSERT FIGURE 4 HERE (COLOR IN PRINT)

Figure 4: Heatmaps for the experiment with omitted data for the first 100 time steps. For the same 20 stocks selected via random sampling, a model is iteratively updated for 3 epochs and with the last time step's information as an extension of the training set after each new time step. Part a shows the results for averaged and individual accuracies for the case without the first 100 time steps, whereas part b show the results for the full dataset.

468 5. Discussion

469 5.1. Relevance for trend

 $^{470}_{prediction.}$ The hypothesis about general time series analysis via such network mod- $^{470}_{prediction.}$ is reinforced by the experiments: The evidence strongly suggests that deep $_{472}$ feed-forward neural networks can be used to consistently learn and, for pre-473 viously unseen data, act with an accuracy above predetermined baselines on 474 time-shifted correlations of gradients that are computed step-wise for complex 475 time series, with only the previous interval of other series instead of the tar-476 get one as input features. While adding information about the target stock 477 in the inputs is shown to provide only marginal increases in performance, a 478 simple linear SVC baseline performs significantly above naïve baselines, further 479 bolstering the relevance of the feature engineering used in this work. The ap-480 proach of this paper could be applied to other forecasting problems that involve 481 non-linear interactions between a large number of noisy time series and lagged 482 effects of their respective trend behavior, for example the metrics in areas as 483 diverse as consumer behavior and epidemic dynamics of infectious diseases. For 484 practitioners relying on expert systems to inform decisions about the future in 485 noise-laden environments, breaking through that noise is a common issue. As a 486 novel use and application of gradient-based feature engineering, in combination 487 with smoothing techniques described in Section 3.2, this paper delivers general 488 evidence for the viability as an expert system in highly noisy dynamical systems 489 subject to time series prediction problems.

⁴⁹⁰ 5.2. Comparison to related research

⁴⁹¹ Both Takeuchi and Lee (2013) and Batres-Estrada (2015) use deep learning ⁴⁹² models for the binary month-wise trend prediction of target stocks, based on ⁴⁹³ historical stock market data of the preceding 12 months, with resulting ⁴⁹⁴ accu-⁴⁹⁴ racies of 53.36% and 52.89%. We want to emphasize that these papers don't

work on the same time intervals and use additional features instead of just past 495 stock prices, which means that a comparison should be taken with a grain of 496 salt. These results are however, the closest available comparison of feed-forward 497 deep learning models for trend prediction based on historical stock market data. 498 When directly comparing the accuracies, our model outperforms both by a 499 ticeable margin, with 58.10% for cross-validation and 60.23% for training no-500 sively on past observations and re-training the model for a few iterations exclu-501 before 502 each new prediction. The same, although to a lesser degree, holds true simple linear SVC used as an additional baseline, indicating the for the 503 viability of the 504 proposed feature engineering.

505 5.3. Implications for financial economics

Firstly, the findings add to the existing evidence against the random walk 506 507 hypothesis as popularized by Malkiel (1973) and others, that is, the notion 508 that stock prices follow random walks with inherently unpredictable behavior. 509 Our findings in this respect are consistent with a growing view in the finan-510 cial economics literature. Consequently, the results also challenge the related 511 efficientmarket hypothesis developed by Fama (1965), which has since become ⁵¹² a staple in the field of financial economics. However, in order to convincingly 513 argue for an empirical rebuttal of the efficient-market hypothesis, a simulation 514 taking trading costs into account may be necessary, which could be a topic for 515 further research and would have to show consistent outperformance in the face 516 of these costs. Lastly, the higher accuracy for models trained exclusively on past 517 observations and with online updates have implications for the interpretation of 518 the underlying structures learned by the models: The latter appear to partially ⁵¹⁹ adapt to changing correlations between stocks, meaning that the learned infor-520 mation is, to a degree, temporally constrained instead of reflecting only general 521 market behavior. This shows that stock markets are, over periods of multiple 522 years, non-stationary in their correlated behavior even in the case of summary 523 findings for the S&P 500.

524 Another relevant finding is that the inclusion of information about the re-

⁵²⁵ spective target stock does provide additional information that improves pre-⁵²⁶ dictive results, but that this increase is rather small and the model is able to ⁵²⁷ infer most relevant information from lagged correlations with other stocks. This ⁵²⁸ recovery of most of the information relevant to the predictions in this paper fur-⁵²⁹ ther strengthens the arguments against both the random walk hypothesis and ⁵³⁰ the efficient-market hypothesis in most of its forms.

The efficient-market hypothesis allows for three forms of information-based ⁵³² market efficiency. Our results could be consistent for a constrained version of ⁵³³ the most basic form, the weak-form market efficiency. Specifically, this would ⁵³⁴ be for a case where the hypothesis allows for prediction methods that reliably ⁵³⁵ outperform the market and can only be implemented by a sufficiently small ⁵³⁶ number of investors so as not to result in a new aggregate equilibrium for a ⁵³⁷ typical modern economy. With a negligible amount of capital involved in the ⁵³⁸ context of the whole market, some agents, such as select quantitative hedge ⁵³⁹ funds or individuals, could consistently realize above-average returns, thus re-s40 ducing the weak form efficient-market hypothesis to a context-based version. A ⁵⁴¹ time-specific weak form efficient-market hypothesis would, in effect, acknowl-⁵⁴² edge that the hypothesis does not apply to the overall market, but does for a ⁵⁴³ majority of the trading stakeholders due to restrictions regarding the method-⁵⁴⁴ ology and the capital involved in deploying such strategies. This view bears ⁵⁴⁵ argumentative resemblance to the adaptive-market hypothesis by Lo (2004), ⁵⁴⁶ perceiving the efficient-market hypothesis as not necessarily incorrect, but in-⁵⁴⁷ complete, resulting in an attempt to merge the efficient-market hypothesis with ⁵⁴⁸ behavioral economics by applying principles of biological evolution. For ex-⁵⁴⁹ ample, Lo (2004) states that a high competition for scarce resources leads to ⁵⁵⁰ highly efficient markets, whereas a competition for abundant resources among ⁵⁵¹ few "species" in a financial market diminishes overall market efficiency.

552 5.4. Further research suggestions

⁵⁵³ High frequency trading (HFT) is the use of high-frequency stock market ⁵⁵⁴ data characterized by short holding times and high rates of cancellation for ⁵⁵⁵ equities and futures trading in a fully automated manner (Menkveld, 2013). ⁵⁵⁶ It remains a driving force in stock markets, with double-digit shares of total ⁵⁵⁷ trading volumes across different markets and competition mostly between such ⁵⁵⁸ HFT algorithms. Using our model, the interaction between those algorithms in ⁵⁵⁹ the form of lagged correlations could be further investigated to better explain ⁵⁶⁰ the behavior of this part of the stock market. Another approach is the use of ⁵⁶¹ wavelets, that is, the results of time-frequency transformation to compute a local ⁵⁶² variations representation on different scales suitable to combat noise (Nason and ⁵⁶³ von Sachs, 1999).

As described earlier, gradient-based wavelet approaches are used in the areas ⁵⁶⁵ of natural language processing and acoustic classification, and our model could ⁵⁶⁶ be used with wavelets as a more elaborate way to extract relevant information ⁵⁶⁷ from intervals in time series. The question remains whether an increased so-⁵⁶⁸ phistication equals a better model performance. While the linear SVC provides ⁵⁶⁹ a simple off-theshelf baseline, serving the same purpose as logistic regression in ⁵⁷⁰ similar papers, it still performs significantly better than naïve baselines. As a ⁵⁷¹ result, further fine tuning and modification of SVCs provide a viable approach in ⁵⁷² problems where training speed is more important than accuracy maximization.

573 6. Conclusion

⁵⁷⁴ In conclusion, we have shown in this paper that the results with regard ⁵⁷⁵ to the investigated hypothesis are positive under conscientious observance of ⁵⁷⁶ statistical validation measures. The results of the experiments deliver evidence ⁵⁷⁷ for the viability of a combination of deep feed-forward neural networks and ⁵⁷⁸ exponential smoothing applied to gradient-based features for directional trend ⁵⁷⁹ change predictions with non-linear correlations of large numbers of noisy time ⁵⁸⁰ series in the form of historical stock market data. More generally, our findings

demonstrate the value of deep learning approaches to time series analysis and show that linear regression derivatives provide useful features to extract such complex interdependencies, offering a simple indicator of trends with a high predictive value.

The findings in this paper also have implications for modern finance theory, 585 delivering strong evidence against both the random walk and efficient-market hy-586 potheses. The postulations of the efficient-market hypothesis may, however, be 587 adapted to allow for the findings as presented here. While indeed all three forms 588 of the efficient-market hypothesis are inconsistent with the evidence, tweaking 589 the weak form of the efficient-market hypothesis could lead to consistency with 590 our findings. Furthermore, while the presented findings are successfully tested 591 on stock market data and have interesting implications for hypotheses within 592 financial economics, they should also be applicable to other fields dealing with 593 trend forecasts in time series. In addition, as simple arbitrage approaches to in-594 vestment became less effective due to the growing use of such methods over the 595 last decades, it remains to be seen whether deep learning methods such as the 596 one we discuss in this paper will see a similar spread and, consequently, a failure 597 to perform due to a large enough number of market participants operating with 598 related techniques. 599

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751 Figure 1









753 Figure 3

754 Figure 4

