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Gland Segmentation in Colon Histology Images: The GlaS Challenge Contest

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Abstract

Colorectal adenocarcinoma originating in intestinal glandular structures is

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the most common form of colon cancer. In clinical practice, the morphology of intestinal glands, including architectural appearance and glandular formation, is used by pathologists to inform prognosis and plan the treatment of individual patients. However, achieving good inter-observer as well as intra-observer reproducibility of cancer grading is still a major challenge in modern pathology. An automated approach which quantifies the morphology of glands is a solution to the problem.

This paper provides an overview to the Gland Segmentation in Colon Histology Images Challenge Contest (GlaS) held at MICCAI'2015. Details of the challenge, including organization, dataset and evaluation criteria, are presented, along with the method descriptions and evaluation results from the top performing methods.

Keywords: Histology Image Analysis, Segmentation, Colon Cancer, Intestinal Gland, Digital Pathology

1 1. Introduction

Cancer grading is the process of determining the extent of malignancy and 2 is one of the primary criteria used in clinical practice to inform prognosis and 3 plan the treatment of individual patients. However, achieving good repro-4 ducibility in grading most cancers remains one of the challenges in pathology 5 practice (Cross et al., 2000; Komuta et al., 2004; Fanshawe et al., 2008). With 6 digitized images of histology slides becoming increasingly ubiquitous, digital pathology offers a viable solution to this problem (May, 2010). Analysis of 8 histology images enables extraction of quantitative morphological features, 9 which can be used for computer-assisted grading of cancer making the grad-10 ing process more objective and reproducible than it currently is (Gurcan 11 et al., 2009). This has led to the recent surge in development of algorithms 12 for histology image analysis. 13

In colorectal cancer, morphology of intestinal glands including architec-14 tural appearance and gland formation is a key criterion for cancer grading 15 (Compton, 2000; Bosman et al., 2010; Washington et al., 2009). Glands are 16 important histological structures that are present in most organ systems as 17 the main mechanism for secreting proteins and carbohydrates. An intestinal 18 gland (colonic crypt) found in the epithelial layer of the colon, is made up 19 of a single sheet of columnar epithelium, forming a finger-like tubular struc-20 ture that extends from the inner surface of the colon into the underlying 21

connective tissue (Rubin et al., 2008; Humphries and Wright, 2008). There 22 are millions of glands in the human colon. Intestinal glands are responsible 23 for absorption of water and nutrients, secretion of mucus to protect the ep-24 ithelium from a hostile chemical and mechanical environment (Gibson et al., 25 1996), as well as being a niche for epithelial cells to regenerate (Shanmu-26 gathasan and Jothy, 2000; Humphries and Wright, 2008). Due to the hostile 27 environment, the epithelial layer is continuously regenerating and is one of 28 the fastest regenerating surface in human body (Crosnier et al., 2006; Barker, 29 2014). This renewal process requires coordination between cell proliferation, 30 differentiation, and apoptosis. The loss of integrity in the epithelial cell re-31 generation, through a mechanism that is not yet clearly understood, results 32 in colorectal adenocarcinoma, the most common type of colon cancer. 33

Manual segmentation of glands is a laborious process. Automated gland 34 segmentation will allow extraction of quantitative features associated with 35 gland morphology from digitized images of CRC tissue slides. Good quality 36 gland segmentation will pave the way for computer-assisted grading of CRC 37 and increase the reproducibility of cancer grading. However, consistent good 38 quality gland segmentation for all the differentiation grades of cancer has 39 remained a challenge. This was a main reason for organizing this challenge 40 contest. 41

The Gland Segmentation in Colon Histology Images (GlaS) challenge¹ 42 brought together computer vision and medical image computing researchers 43 to solve the problem of gland segmentation in digitized images of Hema-44 toxylin and Eosin (H&E) stained tissue slides. Participants developed gland 45 segmentation algorithms, which were applied to being tissue and to colonic 46 carcinomas. A training dataset was provided, together with ground truth 47 annotations by an expert pathologist. The participants developed and op-48 timized their algorithms on this dataset. The results were judged on the 49 performance of the algorithms on test datasets. Success was measured by 50 how closely the automated segmentation matched the pathologist's. 51

⁵² 2. Related Work

Recent papers (Wu et al., 2005a,b; Gunduz-Demir et al., 2010; Fu et al.,
2014; Sirinukunwattana et al., 2015; Cohen et al., 2015) indicate the increas-

¹http://www.warwick.ac.uk/bialab/GlaScontest

ing interest in histology image analysis applied to intestinal gland segmenta tion. In this section, we review some of these methods.

Wu et al. (2005a) presented a region growing method, which first thresh-57 olds an image, in order to separate nuclei from other tissue components. 58 Large empty regions, which potentially correspond to lumen found in the 59 middle of glands, are then used to initialize the seed points for region grow-60 ing. The expanding process for each seed is terminated when a surround-61 ing chain of epithelial nuclei is reached, and subsequently false regions are 62 removed. Although this method performs well in segmenting healthy and 63 benign glands, it is less applicable to cancer cases, where the morphology of 64 glands can be substantially deformed. 65

In contrast to the above method, which mainly uses pixel-level informa-66 tion, Gunduz-Demir et al. (2010) represented each tissue component as a 67 disk. Each disk is represented by a vertex of a graph, with nearby disks 68 joined by an edge between the corresponding vertices. They proposed an al-69 gorithm, using graph connectivity to identify initial seeds for region growing. 70 To avoid an excessive expansion beyond the glandular region, caused, for ex-71 ample, by large gaps in the surrounding epithelial boundary, edges between 72 nuclear objects are used as a barrier to halt region growing. Those regions 73 that do not show glandular characteristics are eliminated at the last step. 74 The validation of this method was limited only to the dataset with healthy 75 and benign cases. 76

Fu et al. (2014) introduced a segmentation algorithm based on polar 77 coordinates. A neighborhood of each gland and a center chosen inside the 78 gland were considered. Using this center to define polar coordinates, the 79 neighborhood is displayed in (r, θ) coordinates with the r-axis horizontal 80 and the θ -axis vertical. One obtains a vertical strip, periodic with period 81 2π in the vertical direction. As a result, the closed glandular boundary 82 is transformed into an approximately vertical periodic path, allowing fast 83 inference of the boundary through a conditional random field model. Support 84 vector regression is later deployed to verify whether the estimated boundary 85 corresponds to the true boundary. The algorithm performs well in both 86 benign and malignant cases stained by Hematoxylin and DAB. However, the 87 validation on routine H&E stained images was limited only to healthy cases. 88 Sirinukunwattana et al. (2015) recently formulated a segmentation ap-80 proach based on Bayesian inference, which allows prior knowledge of the 90 spatial connectivity and the arrangement of neighboring nuclei on the ep-91 ithelial boundary to be taken into account. This approach treats each glan-92

Table 1: Details of the dataset.

Histologic Grade	Number of Images (Width x Height in Pixels)								
		Train	ing Part		Test	Part A	Test Part B		
Benign	37 <	1	(574×433)	33 🗸	1	(574×433)			
		1	(589×453)		4	(589×453)	$4 (775 \times 522)$		
		35	(775×522)		28	(775×522)			
Malignant		1	(567×430)		(1	(578×433)			
	48	3	(589×453)		2	(581×442)	$16 (775 \times 522)$		
		44	(775×522)		24	(775×522)			

dular structure as a polygon made of a random number of vertices. The 93 idea is based on the observation that a glandular boundary is formed from 94 closely arranged epithelial nuclei. Connecting edges between these epithelial 95 nuclei gives a polygon that encapsulates the glandular structure. Inference of 96 the polygon is made via Reversible-Jump Markov Chain Monte Carlo. The 97 approach shows favorable segmentation results across all histologic grades 98 (except for the undifferentiated grade) of colorectal cancers in H&E stained 99 images. This method is slow but effective. 100

Most of the works for intestinal gland segmentation have used differ-101 ent datasets and/or criteria to assess their algorithms, making it difficult to 102 objectively compare their performance. There have been many previous ini-103 tiatives that provided common datasets and evaluation measures to validate 104 algorithms on various medical imaging modalities (Murphy et al., 2011; Gur-105 can et al., 2010; Roux et al., 2013; Veta et al., 2015). This not only allows a 106 meaningful comparison of different algorithms but also allows the algorithms 107 to be implemented and configured thoroughly to obtain optimal performance 108 (Murphy et al., 2011). Following these successful initiatives, we therefore or-109 ganized the Gland Segmentation in Colon Histology Images (GlaS) challenge. 110 This challenge was a first attempt to address the issues of reproducibility and 111 comparability of the results of intestinal gland segmentation algorithms. It 112 was also aimed at speeding up even further the development of algorithms for 113 gland segmentation. Note that none of above methods for intestinal gland 114 segmentation participated in this competition. 115

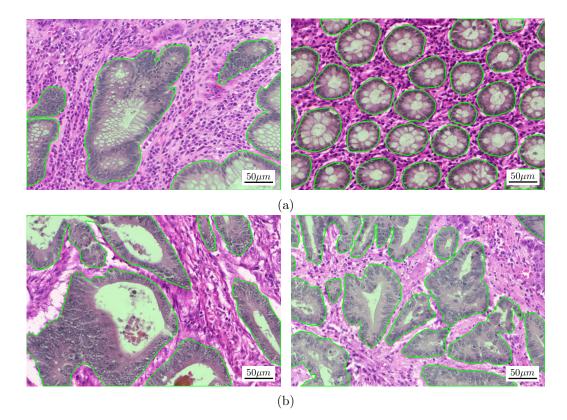


Figure 1: Example images of different histologic grades in the dataset: (a) benign and (b) malignant.

116 3. Materials

The dataset used in this challenge consists of 165 images derived from 117 16 H&E stained histological sections of stage T3 or T4² colorectal adenocar-118 cinoma. Each section belongs to a different patient, and sections were pro-119 cessed in the laboratory on different occasions. Thus, the dataset exhibits 120 high inter-subject variability in both stain distribution and tissue architec-121 ture. The digitization of these histological sections into whole-slide images 122 (WSIs) was accomplished using a Zeiss MIRAX MIDI Slide Scanner with a 123 pixel resolution of $0.465\mu m$. The WSIs were subsequently rescaled to a pixel 124 resolution of $0.620 \mu m$ (equivalent to $20 \times$ objective magnification). 125

A total of 52 visual fields from both malignant and benign areas across 126 the entire set of the WSIs were selected in order to cover as wide a vari-127 ety of tissue architectures as possible. An expert pathologist (DRJS) then 128 graded each visual field as either 'benign' or 'malignant', according to the 129 overall glandular architecture. The pathologist also delineated the boundary 130 of each individual glandular object on that visual field. We used this manual 131 annotation as ground truth for automatic segmentation. Note that different 132 glandular objects in an image may be part of the same gland. This is because 133 a gland is a 3-dimensional structure that can appear as separated objects on 134 a single tissue section. The visual fields were further separated into smaller, 135 non-overlapping images, whose histologic grades (i.e. benign or malignant) 136 were assigned the same value as the larger visual field. Representative exam-137 ple images of the two grades can be seen in Figure 1. This dataset was also 138 previously used in the gland segmentation study by Sirinukunwattana et al. 139 (2015).140

In the challenge, the dataset was separated into **Training Part**, **Test Part A**, and **Test Part B**. Note that the data were stratified according to the histologic grade and the visual field before splitting. This was done to ensure that none of the images from the same visual field appears in different parts of the dataset (i.e. Training, Test Part A, or Test Part B). However, since the data were not stratified based on patient, different visual

²The T in TNM cancer staging refers to the spread of the primary tumour. In colorectal cancer, stage T3 means the tumour has grown into the outer lining of the bowel wall, whereas stage T4 means the tumour has grown through the outer lining of the bowel wall. The cancer stage is different from the tumour histologic grade, as the latter indicates the aggressiveness of the tumour.

fields from the same slide can appear in different parts of the dataset. A 147 breakdown of the details of the dataset is shown in Table 1. The ground 148 truth as well as the histologic grade which reflects morphology of glandular 149 structures were provided for every image in the Training Part at the time of 150 release. We used Test Part A and Test Part B as off-site and on-site test 151 datasets respectively. Furthermore, to ensure blindness of evaluation, the 152 ground truth and histologic grade of each image in the test parts were not 153 released to the participants. 154

155 4. Challenge Organization

The GlaS challenge contest was officially launched by the co-organizers (KS, JPWP, DRJS, NMR) on April 21st, 2015, and was widely publicized through several channels. At the same point, a challenge website³ was set up to disseminate challenge-related information and to serve as a site for registration, submission of results, and communication between the organizers and contestants. The challenge involved 4 stages, as detailed below:

Stage 1: Registration and Release of the Training Data. The registration was open for a period of about two months (April 21st to June 30th, 2015). Interested individuals or groups of up to 3 people that were affiliated with an academic institute or an industrial organization could register and download the training data (Training Part, see Section 3 for details) to start developing their gland segmentation algorithms. From this point forward, we will refer to a separate individual or a group of registrants as a 'team'.

Stage 2: Submission of a Short Paper. In order to gain access to the first 169 part of the test data, each registered team was required to submit a 2-page 170 document containing a general description of their segmentation algorithms 171 and some preliminary results obtained from running each algorithm on the 172 training data. Each team could submit up to 3 different methods. The 173 intention of this requirement was for the organizers to identify teams who 174 were serious about participating in the challenge. The organizers based their 175 reviews on two criteria: clarity of the method description and soundness of 176 the validation strategy. Segmentation performance was not considered in this 177 review. The submission of this document was due by July 17th, 2015. 178

³http://www.warwick.ac.uk/bialab/GlaScontest

Stage 3: Release of the Test Data Part A and Submission of Segmentation 179 Results. The first part of the test data (Test Part A, see Section 3 for de-180 tails) was released on August 14th, 2015 to those teams selected from the 181 previous stage which also agreed to participate in the GlaS contest. The 182 teams were given a month to further adjust and optimize their segmentation 183 algorithms, and carry out segmentation on Part A of the test data. Each 184 team could hand-in up to 3 sets of results per method submitted in Stage 185 2. The submission of the segmentation results was due by September 14^{th} , 186 2015. Evaluation of the submitted results was not disclosed to the teams 187 until after the challenge event. 188

Stage 4: GlaS'2015 Challenge Event. The event was held in conjunction 189 with MICCAI'2015 on October 5th, 2015. All teams were asked to produce 190 segmentation results on the second part of the test data (Test Part B, see Sec-191 tion 3) within 45 minutes. The teams could either bring their own machines 192 or conduct an experiment remotely. There was no restriction on the num-193 ber of machines that the teams could use to produce results. Those teams 194 that could not be present at the event provided implementations of their 195 algorithms with which the organizers carried out the segmentation on their 196 behalf. Each team was also asked to give a short presentation, discussing 197 their work. At the end of the event, the complete evaluation of segmentation 198 results across both parts of the test data was announced, which included a 190 final ranking of the submitted methods. This information is also available 200 on the challenge website. 201

202 4.1. Challenge Statistics

By the end of Stage 1, a total of 110 teams from different academic and 203 industrial institutes had registered. A total of 21 teams submitted the 2-page 204 document for review in Stage 2, and 20 teams were invited to participate in 205 the GlaS competition event. In Stage 3, only 13 teams submitted results 206 on Part A of the test data in time. Late entries were neither evaluated nor 207 considered in the next stage of the competition. On the day of the challenge 208 event, 11 of the 13 teams that submitted the results on time in Stage 3 209 attended the on-site competition and presented their work. The organizers 210 carried out the segmentation on behalf of the other two teams that could not 211 be present. 212

²¹³ 5. Evaluation

The performance of each segmentation algorithm was evaluated based on 214 three criteria: 1) accuracy of the detection of individual glands; 2) volume-215 based accuracy of the segmentation of individual glands; and 3) boundary-216 based similarity between glands and their corresponding segmentation. It 217 may seem that volume-based segmentation accuracy would entail boundary-218 based segmentation accuracy between a gland and its segmentation. How-219 ever, in practice, this is not always the case. The volume-based metric for 220 segmentation accuracy used in this challenge, was defined and calculated us-221 ing the label that the algorithm had assigned to each pixel, but the boundary-222 based metric used the position assigned by the algorithm to the boundary 223 of each gland. Pixels labels may be fairly accurate, while the boundary 224 curves are very different. The remainder of this section describes all metrics 225 employed in the evaluation. 226

We use the concept of a pair of corresponding segmented and ground 227 truth objects as proposed in Sirinukunwattana et al. (2015). Let \mathcal{S} denote a 228 set of all segmented objects and \mathcal{G} denote a set of all ground truth objects. 229 We also include in each of these sets the empty object \emptyset . We define a function 230 $G_*: \mathcal{S} \to \mathcal{G}$, by setting, for each segmented object $S \in \mathcal{S}, G_*(S) = G \in \mathcal{G}$ 231 where G has the largest possible overlapping area with S. Although there 232 could be more than one $G \in \mathcal{G}$ that maximally overlaps S, this in practice 233 is extremely rare, and it is good enough to consider one of these G as the 234 value of $G_*(S)$. If there is no overlapping G, we set $G_*(S) = \emptyset$. (However, in 235 the context of Hausdorff distance – see Section $5.3 - G_*$ will be extended in 236 a different way.) Similarly, we define $S_*: \mathcal{G} \to \mathcal{S}$, by setting, for each $G \in \mathcal{G}$, 237 $S_*(G) = S \in \mathcal{S}$, where S has the largest possible overlapping area with G. 238 Note that G_* and S_* are, in general, neither injective, nor surjective. Nor 239 are they inverse to each other, in general. They do, however, assign to each 240 G an $S = S_*(G)$, and to each S a $G = G_*(S)$. 241

²⁴² 5.1. Detection Accuracy

The F1 score is employed to measure the detection accuracy of individual glandular objects. A segmented glandular object that intersects with at least 50% of its ground truth object is counted as true positive, otherwise it is counted as false positive. The number of false negatives is calculated as the difference between the number of ground truth objects and the number ²⁴⁸ of true positives. Given these definitions, the F1 score is defined by

$$F1score = \frac{2 \cdot Precision \cdot Recall}{Precision + Recall},$$
(1)

249 where

$$Precision = \frac{TP}{TP + FP}, \quad Recall = \frac{TP}{TP + FN}, \quad (2)$$

and TP, FP, and FN denote respectively the number of true positives, false
positives, and false negatives from all images in the dataset.

²⁵² 5.2. Volume-Based Segmentation Accuracy

²⁵³ 5.2.1. Object-Level Dice Index

The Dice index (Dice, 1945) is a measure of agreement or similarity between two sets of samples. Given G, a set of pixels belonging to a ground truth object, and S, a set of pixels belonging to a segmented object, the Dice index is defined as follows:

Dice
$$(G, S) = \frac{2|G \cap S|}{|G| + |S|},$$
 (3)

where $|\cdot|$ denotes set cardinality. The index ranges over the interval [0, 1], 258 where the higher the value, the more concordant the segmentation result 250 and the ground truth. A Dice index of 1 implies a perfect agreement. It 260 is conventional that the segmentation accuracy on an image is calculated by 261 $Dice(G_{all}, S_{all})$, where G_{all} denotes the set of pixels of all ground truth objects 262 and $S_{\rm all}$ denotes the set of pixels of all segmented objects. The calculation 263 made in this way measures the segmentation accuracy only at the pixel level, 264 not at the gland level, which was the main focus of the competition. 265

To take the notion of an individual gland into account, we employ the object-level Dice index (Sirinukunwattana et al., 2015). Let $n_{\mathcal{G}}$ be the number of non-empty ground truth glands, as annotated by the expert pathologist. Similarly let $n_{\mathcal{S}}$ be the number of glands segmented by the algorithm, that is the number of non-empty segmented objects. Let $G_i \in \mathcal{G}$ denote the i^{th} ground truth object, and let $S_j \in \mathcal{S}$ denote the j^{th} segmented object. The object-level Dice index is defined as

$$\operatorname{Dice}_{\operatorname{obj}}(\mathcal{G},\mathcal{S}) = \frac{1}{2} \left[\sum_{i=1}^{n_{\mathcal{G}}} \gamma_i \operatorname{Dice}(G_i, S_*(G_i)) + \sum_{j=1}^{n_{\mathcal{S}}} \sigma_j \operatorname{Dice}(G_*(S_j), S_j) \right], \quad (4)$$

273 where

$$\gamma_i = |G_i| / \sum_{p=1}^{n_{\mathcal{G}}} |G_p|, \quad \sigma_j = |S_j| / \sum_{q=1}^{n_{\mathcal{S}}} |S_q|$$
 (5)

On the right hand side of (4), the first summation term reflects how well each ground truth object overlaps its segmented object, and the second summation term reflects how well each segmented object overlaps its ground truth objects. Each term is weighted by the relative area of the object, giving less emphasis to small segmented and small ground truth objects.

In the competition, the object-level Dice index of the whole test dataset was calculated by including all the ground truth objects from all images in \mathcal{G} and all the segmented objects from all images in \mathcal{S} .

282 5.2.2. Adjusted Rand Index

We also included the adjusted Rand index (Hubert and Arabie, 1985) as another evaluation measure of segmentation accuracy. This index was used for additional assessment of the algorithm performance in Section 8.3.

The adjusted Rand index measures similarity between the set of all ground 286 truth objects \mathcal{G} and the set of all segmented objects \mathcal{S} , based on how pixels 287 in a pair are labeled. Two possible scenarios for the pair to be concordant 288 are that (i) they are placed in the same ground truth object in \mathcal{G} and the 289 same segmented object in \mathcal{S} , and (ii) they are placed in different ground 290 truth objects in \mathcal{G} and in different segmented objects in \mathcal{S} . Define n_{ij} as the 291 number of pixels that are common to both the i^{th} ground truth object and 292 the j^{th} segmented object, n_{i} as the total number of pixels in the i^{th} ground 293 truth object, $n_{\cdot,j}$ as the total number of pixels in the j^{th} segmented object, 294 and n as the total number of pixels. Following a simple manipulation, it can 295 be shown that the probability of agreement is equal to 296

$$P_{\text{agreement}} = \left[\binom{n}{2} + 2\sum_{i=1}^{n_{\mathcal{G}}} \sum_{j=1}^{n_{\mathcal{S}}} \binom{n_{ij}}{2} - \sum_{i=1}^{n_{\mathcal{G}}} \binom{n_{i,\cdot}}{2} - \sum_{j=1}^{n_{\mathcal{S}}} \binom{n_{\cdot,j}}{2} \right] \middle/ \binom{n}{2}.$$
(6)

Here, the numerator term corresponds to the total number of agreements, while the denominator term corresponds to the total number of all possible pairs of pixels. Under the assumption that the partition of pixels into ground truth objects in \mathcal{G} and segmented objects in \mathcal{S} follows a generalized ³⁰¹ hypergeometric distribution, the adjusted Rand index can be formulated as

$$\operatorname{ARI}(\mathcal{G}, \mathcal{S}) = \frac{\sum_{i=1}^{n_{\mathcal{G}}} \sum_{j=1}^{n_{\mathcal{S}}} {n_{i,j} \choose 2} - \sum_{i=1}^{n_{\mathcal{G}}} {n_{i} \choose 2} \sum_{j=1}^{n_{\mathcal{S}}} {n_{\cdot,j} \choose 2} / {n \choose 2}}{\frac{1}{2} \left[\sum_{i=1}^{n_{\mathcal{G}}} {n_{i,\cdot} \choose 2} + \sum_{j=1}^{n_{\mathcal{S}}} {n_{\cdot,j} \choose 2} \right] - \sum_{i=1}^{n_{\mathcal{G}}} {n_{i,\cdot} \choose 2} \sum_{j=1}^{n_{\mathcal{S}}} {n_{\cdot,j} \choose 2} / {n \choose 2}}.$$
 (7)

³⁰² The adjusted Rand index is bounded above by 1, and it can be negative.

303 5.3. Boundary-Based Segmentation Accuracy

We measure the boundary-based segmentation accuracy between the segmented objects in S and the ground truth objects in G using the object-level Hausdorff distance. The usual definition of a Hausdorff distance between ground truth object G and segmented object S is

$$H(G,S) = \max\{\sup_{x \in G} \inf_{y \in S} d(x,y), \sup_{y \in S} \inf_{x \in G} d(x,y)\}$$
(8)

where d(x, y) denotes the distance between pixels $x \in G$ and $y \in S$. In this work, we use the Euclidean distance. According to (8), Hausdorff distance is the most extreme value from all distances between the pairs of nearest pixels on the boundaries of S and G. Thus, the smaller the value of the Hausdorff distance, the higher the similarity between the boundaries of S and G, and S = G if their Hausdorff distance is zero.

To calculate the overall segmentation accuracy between a pair of corresponding segmented and ground truth objects, we now introduce object-level Hausdorff distance by imitating the definition of object-level Dice index (4). The object-level Hausdorff distance is defined as

$$H_{obj}(\mathcal{G},\mathcal{S}) = \frac{1}{2} \left[\sum_{i=1}^{n_{\mathcal{G}}} \gamma_i H(G_i, S_*(G_i)) + \sum_{j=1}^{n_{\mathcal{S}}} \sigma_j H(G_*(S_j), S_j) \right], \qquad (9)$$

where the meaning of the mathematical notation is similar to that given in Section 5.2.1. In case a ground truth object G does not have a corresponding segmented object (i.e. $S_*(G) = \emptyset$), the Hausdorff distance is calculated between G and the nearest segmented object $S \in \mathcal{S}$ to G (in the Hausdorff distance) in that image instead. The same applies for a segmented object that does not have a corresponding ground truth object.

324 6. Ranking Scheme

Each submitted entry was assigned one ranking score per evaluation met-325 ric and set of test data. Since there were 3 evaluation metrics (F1 score 326 for gland detection, object-level Dice index for volume-based segmentation 327 accuracy, and object-level Hausdorff index for boundary-based segmentation 328 accuracy) and 2 sets of test data, the total number of ranking scores was 329 6. The best performing entry was assigned ranking score 1, the second best 330 was assigned ranking score 2, and so on. In care of a tie, the standard com-331 petition ranking was applied. For instance, F1 score 0.8, 0.7, 0.7, and 0.6 332 would result in the ranking scores 1, 2, 2, and 4. The final ranking was then 333 obtained by adding all 6 ranking scores (rank sum). The entry with smallest 334 sum was placed top in the final ranking. 335

336 7. Methods

The top ranking methods are described in this section. They are selected from the total of 13 methods that participated in all stages of the challenge. The cut-off for the inclusion in this section was made where there was a substantial gap in the rank sums (see Appendix A, Figure A.5). Of the 7 selected methods, only 6 preferred to have their methods described here.

$7.1. CUMedVision^4$

A novel deep contour-aware network (Chen et al., 2016) was presented. 343 This method explored the multi-level feature representations with fully con-344 volutional networks (FCN) (Long et al., 2015). The network outputted seg-345 mentation probability maps and depicted the contours of gland objects simul-346 taneously. The network architecture consisted of two parts: a down-sampling 347 path and an up-sampling path. The down-sampling path contained convo-348 lutional and max-pooling layers while the up-sampling path contained con-349 volutional and up-sampling layers, which increased the resolutions of feature 350 maps and outputted the prediction masks. In total, there were 5 max-pooling 351 layers and 3 up-sampling layers. Each layer with learned parameters was fol-352 lowed by a non-linear mapping layer (element-wise rectified linear activation). 353

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In order to separate touching glands, the feature maps from hierarchical 354 layers were up-sampled with two different branches to output the segmented 355 object and contour masks respectively. The parameters of the down-sampling 356 path were shared and updated for these two kinds of masks. This could 357 be viewed as a multi-task learning framework with feature representations, 358 simultaneously encoding the information of segmented objects and contours. 359 To alleviate the problem of insufficient training data (Chen et al., 2015), 360 an off-the-shelf model from DeepLab (Chen et al., 2014), trained on the 361 2012 PASCAL VOC dataset⁵, was used to initialize the weights for layers in 362 the down-sampling path. The parameters of the network were obtained by 363 minimizing the loss function with standard back-propagation ⁶. 364

The team submitted two entries for evaluation. **CUMedVision1** was produced by FCN with multi-level feature representations relying only on gland object masks, while **CUMedVision2** was the results of the deep contour-aware network, which considers gland object and contour masks simultaneously.

370 7.2. CVML⁷

In the first, preprocessing, stage the images were corrected to compensate 371 for variations in the appearance due to a variability of the tissue staining pro-372 cess. This was implemented through histogram matching, where the target 373 histogram was calculated from the whole training data, and the individual 374 image histograms were used as inputs. The main processing stage was based 375 on two methods: a convolutional neural network (CNN) (Krizhevsky et al., 376 2012) for a supervised pixel classification, and a level set segmentation for 377 grouping pixels into spatially coherent structures. The employed CNN used 378 an architecture with two convolutional, pooling and fully connected layers. 379 The network was trained with three target classes. The classes were designed 380 to represent (1) the tubular interior of the glandular structure (inner class), 381 (2) epithelial cells forming boundary of the glandular structure (boundary 382 class) and (3) inter-gland tissue (outer class). The inputs to the CNN were 383 19×19 pixel patches sliding across the adjusted RGB input image. The two 384 convolutional layers used 6×6 and 4×4 kernels with 16 and 36 feature maps 385

⁵http://host.robots.ox.ac.uk:8080/pascal/VOC/voc2012/index.html

⁶More details will be available at: http://www.cse.cuhk.edu.hk/~hchen/research/ 2015miccai_gland.html

⁷School of Engineering, University of Central Lancashire, Preston, UK.

respectively. The pooling layers, implementing the mean function, used 2×2 386 receptive fields and 2×2 stride. The first and second fully connected layers 387 used the rectified linear unit and softmax functions respectively. The outputs 388 from the CNN were two probability maps representing the probability of each 389 image pixel belonging to the inner and boundary classes. These two prob-390 ability maps were normalized between -1 and 1 and used as a propagation 391 term, along with an advection term and a curvature flow term. These terms 392 were part of the hybrid level set model described in Zhang et al. (2008). In 393 the post-processing stage, a sequence of morphological operations was per-394 formed to removed small objects, fill holes and disconnect weakly connected 395 objects. Additionally, if an image boundary intersecting an object forms a 396 hole, the corresponding pixels was labeled as part of that object. The team 397 submitted a single entry for evaluation, henceforth referred to as CVML. 398

399 *7.3.* ExB⁸

This method first preprocessed the data by performing per channel zero mean and unit variance normalization, where the mean and variance were computed from the training data. The method then exploited the local invariance properties of the task by applying a set of transformations to the data. At training time, the dataset was augmented by applying affine transformations, Gaussian blur and warping. During testing, both image mirroring and rotation were applied.

The main segmentation algorithm consisted of a multi-path convolutional 407 neural network. Each path was equipped with a different set of convolutional 408 layers and configured to capture features from different views in a local-global 409 fashion. All the different paths were connected to a set of two fully connected 410 layers. A leaky rectified linear unit was used as a default activation function 411 between layers, and a softmax layer was used after the last fully connected 412 layer. Every network was trained via stochastic gradient descent with mo-413 mentum, using a step-wise learning rate schedule (Krizhevsky et al., 2012). 414 The network was randomly initialized such that unit variance was preserved 415 across layers. It was found that using more than three paths led to heavy 416 over-fitting – this was due to insufficient training data. 417

Simple-path networks were trained to detect borders of glands. The ground truth for these networks was constructed using a band of width

⁸ExB Research and Development.

 $K \in [5, 10]$ pixels along a real gland border. These values of K were found to produce optimal and equivalent quantitative results, measured by the F1 score and the object-Dice index. The output of these networks was used to better calibrate the final prediction.

In the post-processing step, a simple method was applied to clean noise and fill holes in the structures. Thresholding was applied to remove spurious structures with diameter smaller than a certain epsilon. Filling-hole criteria based on diameter size was also used.

Using the initial class discrimination (benign and malignant), a simple 428 binary classifier constructed from a convolutional neural network with 2 con-420 volutional and 1 fully connected layers was trained. This binary classifier 430 used the raw image pixels as input. The output of the classifier was used 431 together with the border networks and the post-processing method to apply 432 a different set of parameters/thresholds depending on the predicted class. 433 The hyperparameters for the entire pipeline, including post-processing and 434 border networks, were obtained through cross-validation. 435

For this method, the team submitted 3 entries. **ExB 1** was a two-path network including both the border network for detecting borders of glands and the binary classification to differentiate between the post-processing parameters. **ExB 2** was similar to ExB 1 without the use of the border network. **ExB 3** used a two-path network without any post-processing.

⁴⁴¹ 7.4. Image Analysis Lab Uni Freiburg⁹

The authors applied a u-shaped deep convolutional network "u-net"¹⁰ 442 (Ronneberger et al., 2015) for the segmentation. The input was the raw 443 RGB image and the output was a binary segmentation map (glands and 444 background). The network consisted of an analysis-path constructed from a 445 sequence of convolutional layers and max-pooling layers, followed by a synthe-446 sis path with a sequence of up-convolutional layers and convolutional layers, 447 resulting in 23 layers in total. Additional shortcut-connections propagated 448 the feature maps at all detail levels from the analysis to the synthesis path. 449 The network was trained from scratch in an end-to-end fashion with only the 450

⁹Computer Science Department and BIOSS Centre for Biological Signalling Studies, University of Freiburg, Germany.

¹⁰The implementation of the u-net is freely available at http://lmb.informatik. uni-freiburg.de/people/ronneber/u-net/.

images and ground truth segmentation maps provided by the challenge orga-451 nizers. To teach the network the desired invariances and to avoid overfitting, 452 the training data were augmented with randomly transformed images and 453 the correspondingly transformed segmentation maps. The applied transfor-454 mations were random elastic deformations, rotations, shifts, flips, and blurs. 455 The color transformations were random multiplications applied in the HSV 456 color space. To avoid accidentally joining touching objects, a high pixel-wise 457 loss weight was introduced for pixels in thin gaps between objects in the 458 training dataset (see Ronneberger et al. (2015)). The exact same u-net lay-450 out with the same hyperparameters as in Ronneberger et al. (2015) was used 460 for the challenge. The only difference were more training iterations and a 461 slower decay of the learning rate. 462

The team submitted two entries. The first entry **Freiburg1** was a connected component labelling applied to the raw network output. The second entry **Freiburg2** post-processed the segmentation maps with morphological hole-filling and deletion of segments smaller than 1000 pixels.

467 7.5. LIB¹¹

Intestinal glands were divided according to their appearance into three categories: hollow, bounded, and crowded. A hollow gland was composed of lumen and goblet cells and it could be a hole in the tissue surface. A bounded gland had the same composition, but in addition, it was surrounded by a thick epithelial layer. A crowded gland was composed of bunches of epithelial cells clustered together and it might have shown necrotic debris.

The tissue was first classified into one of the above classes before beginning 474 the segmentation. The classification relied on the characterization of the 475 spatial distribution of cells and the topology of the tissue. Therefore, a 476 closing map was generated with a cumulative sum of morphological closing 477 by a disk of increasing radius (1 to 40 pixels) on the binary image of nuclear 478 objects, which were segmented by the k-means algorithm in the RGB colour 479 space. The topological features were calculated from a normalized closing 480 map in MSER fashion (Maximally Stable Extremal Region, Matas et al. 481 (2004)) as the number of regions below three different thresholds (25%, 50%)482 and 62.5%) and above one threshold (90%), their sizes and the mean of 483

¹¹Sorbonne Universités, UPMC Univ Paris 06, CNRS, INSERM, Biomedical Imaging Laboratory (LIB), Paris, France.

their corresponding values in the closing map. The first three thresholds
characterized the holes and the fourth one characterized the thickness of
nuclear objects. After classifying the tissue with a Naive Bayes classifier
trained on these features, a specific segmentation algorithm was applied.

Three segmentation algorithms were presented, one for each category. 488 Hollow glands were delineated by morphological dilation on regions below 489 50%. Bounded gland candidates were first detected as hollow glands, then 490 the thickness of nuclear objects surrounding the region was evaluated by gen-491 erating a girth map and a solidity map (Ben Cheikh et al., 2016), then after 492 classifying nuclear objects, the epithelial layer was added or the candidate 493 was removed. Crowded glands were identified as populous regions (regions 494 above 90%), and then morphological filtering was applied for refinement. The 495 team submitted a single entry labeled as **LIB** for evaluation. 496

497 7.6. $vision_4 Gla S^{12}$

Given an H&E-stained RGB histopathological section, the gland segmen-498 tation method was based on a pixel-wise classification and an active contour 490 model, and it proceeded in three steps (Kainz et al., 2015). In a first prepro-500 cessing step the image was rescaled to half the spatial resolution, and color 501 deconvolution separated the stained tissue components. The red channel of 502 the deconvolved RGB image represented the tissue structure best and was 503 therefore considered for further processing. Next, two convolutional neu-504 ral networks (CNNs) (LeCun et al., 2010) of seven layers each were trained 505 for pixel-wise classification on a set of image patches. Each network was 506 trained with ReLU nonlinearities, and stochastic gradient descent with mo-507 mentum, weight decay, and dropout regularization to minimize a negative 508 log-likelihood loss function. The first CNN, called Object-Net, was trained 509 to distinguish four classes: (i) benign background, (ii) benign gland, (iii) 510 malignant background, and (iv) malignant gland. For each image patch the 511 probability distribution over the class labels was predicted, using a softmax 512 function. The Object-Net consisted of three convolutional layers followed 513 by max-pooling, a final convolutional layer and three fully connected layers. 514

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The second – architecturally similar – CNN called Separator-Net, learned to 515 predict pixels of gland-separating structures in a binary classification task. 516 Ground truth was generated by manually labeling image locations, close 517 to two or more gland borders, as gland-separating structures. In the final 518 step the segmentation result was obtained by combining the outputs of the 519 two CNNs. Predictions for benign and malignant glands were merged, and 520 predictions of gland-separating structures were subtracted to emphasize the 521 foreground probabilities. Background classes were handled similarly. Using 522 these refined foreground and background maps, a figure-ground segmentation 523 based on weighted total variation was employed to find a globally optimal 524 solution. This approach optimized a geodesic active contour energy, which 525 minimized contour length while adhering to the refined CNN predictions 526 (Bresson et al., 2007). The team submitted a single entry, referred to as 527 vision4GlaS. 528

529 8. Results and Discussion

530 8.1. Summary of the Methods

The methods described above take one of the following two approaches 531 to segmentation: (a) they start by identifying pixels corresponding to glands 532 which are then grouped together to form separated, spatially coherent ob-533 jects; (b) they begin with candidate objects that are then classified as glands 534 or non-glands. All methods that are based on CNNs (CUMedVision, CVML, 535 ExB, Freiburg, and vision4GlaS) follow the former approach. CVML, ExB, 536 and vision4GlaS built CNN classifiers that assign a gland-related or non-537 gland-related label to every pixel in an image, by taking patch(es) centered 538 at the pixel as input. ExB, in particular, use multi-path networks into which 539 patches at different sizes are fed, in order to capture contextual informa-540 tion at multiple scales. CUMedVision and Freiburg, on the other hand, base 541 their pixel classifier on a fully convolutional network architecture (Long et al., 542 2015), allowing simultaneous pixel-wise label assignment at multiple pixel lo-543 cations. To separate gland-related pixels into individual objects, CVML and 544 vision4GlaS deploy contour based approaches. ExB trains additional net-545 works for glandular boundary, while CUMedVision and Freiburg explicitly 546 include terms for boundary in the training loss function of their networks. 547 The only method that follows the latter approach for object segmentation 548 is LIB. In this method, candidate objects forming part of a gland (i.e., lu-549

men, epithelial boundary) are first identified, and then classified into different
 types, followed by the final step of segmentation.

A variety of data transformation and augmentation were employed to deal 552 with variation within the data. In order to counter the effect of stain vari-553 ation, CVML and ExB performed transformations of the RGB color chan-554 nels, vision4GlaS used a stain deconvolution technique to obtain only the 555 basophilic channel in their preprocessing step. By contrast, Freiburg tackled 556 the issue of stain variability through data augmentation, which implicitly 557 forces the networks to be robust to stain variation to some extent. As is 558 common among methods using CNNs, spatial transformations, such as affine 550 transformations (e.g. translation, rotation, flip), elastic deformations (e.g. 560 pincushion and barrel distortions), and blurring, were also used in the data 561 augmentation to teach the network to learn features that are spatially invari-562 ant. The other benefit of data augmentation is it provides, to some extent, 563 avoidance of over-fitting. 564

ExB, LIB, and vision4GlaS incorporated histologic grades of glands in their segmentation approach. In ExB, procedures and/or parameter values used in boundary detection and post-precessing steps were different, subject to the predicted histologic grade of an image. vision4GlaS classified pixels based on histological information. Although not explicit, LIB categorized candidate objects forming glands according to their appearance, related to histologic grades, before treating them in different ways.

As a post-processing step, many segmentation algorithms employed simple criteria and/or a sequence of morphological operations to improve their segmentation results. A common treatment was to eliminate small spurious segmented objects. Imperfections in pixel labelling can result in the appearance of one or more holes in the middle of an object. Filling such holes is often necessary. In addition to these operations, CVML performed morphological operations to separate accidentally joined objects.

579 8.2. Evaluation Results

Table 2 summarizes the overall evaluation scores and ranks achieved by each entry from each test part. We list the entries according to the order of their rank sum, which indicates the overall performance across evaluation measures and tasks of the entries. The lower the rank sum, the more favorable the performance. The top three entries according to the overall rank sum in descending order are CUMedVision2, ExB1, and ExB3. However,

Table 2: Summary results. The evaluation is carried out according to the challenge criteria described in Section 6. A ranking score is assigned to each algorithm according to its performance in each evaluation measure, obtained from each test part. The entries are listed in a descending order based on their rank sum

F1score				Dice _{obj}				H _{obj}					
Method Part A		Part B		Part A		Part B		Part A		Part B		Rank Sum	
	Score	Rank	Score	Rank	Score	Rank	Score	Rank	Score	Rank	Score	Rank	
CUMedVision2	0.912	1	0.716	3	0.897	1	0.781	5	45.418	1	160.347	6	17
ExB1	0.891	4	0.703	4	0.882	4	0.786	2	57.413	6	145.575	1	21
ExB3	0.896	2	0.719	2	0.886	2	0.765	6	57.350	5	159.873	5	22
Freiburg2	0.870	5	0.695	5	0.876	5	0.786	3	57.093	3	148.463	3	24
CUMedVision1	0.868	6	0.769	1	0.867	7	0.800	1	74.596	7	153.646	4	26
ExB2	0.892	3	0.686	6	0.884	3	0.754	7	54.785	2	187.442	8	29
Freiburg1	0.834	7	0.605	7	0.875	6	0.783	4	57.194	4	146.607	2	30
CVML	0.652	9	0.541	8	0.644	10	0.654	8	155.433	10	176.244	7	52
LIB	0.777	8	0.306	10	0.781	8	0.617	9	112.706	9	190.447	9	53
vision4GlaS	0.635	10	0.527	9	0.737	9	0.610	10	107.491	8	210.105	10	56

⁵⁸⁶ if rank sum is considered with respect to the test part, the three best en-⁵⁸⁷ tries are CUMedVision2, ExB2, and ExB3 for part A; whereas in part B, ⁵⁸⁸ CUMedVision1, ExB1, and Freiburg2 come at the top. A summary of the ⁵⁸⁹ ranking results from the competition can be found in Appendix A. Some seg-⁵⁹⁰ mentation results and their corresponding evaluation scores are illustrated in ⁵⁹¹ Figure 2 to give a better idea of how the evaluation scores correlate with the ⁵⁹² quality of the segmentation.

593 8.3. Additional Experiments

In the challenge, the split of the test data into two parts – Part A (60 594 images) for off-site test and Part B (20 images) for on-site test – to some 595 extent introduces bias into the performance evaluation of the segmentation 596 algorithms due to equal weight given to performance on the two test parts. 597 The algorithms that perform particularly well on Test Part B would therefore 598 get a better evaluation score even though they may not have performed as 599 well on Test Part A, where the majority of the test dataset is to be found. 600 In addition, the imbalance between the benign and malignant classes in Test 601 Part B, only 4 benign (20%) and 16 malignant (80%) images, would also favor 602 algorithms that perform well on the malignant class. In order to alleviate 603 these issues, we merged the two test parts and re-evaluated the performance 604 of all the entries. In addition, as suggested by one of the participating teams, 605

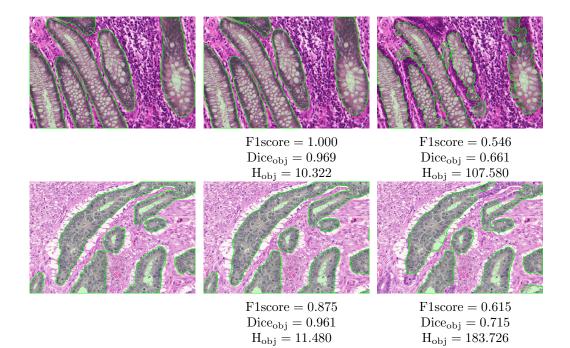


Figure 2: Example images showing segmentation results from some submitted entries. In each row, (left) ground truth, (middle) the best segmentation result, and (right) the worst segmentation result. For each image, the corresponding set of evaluation scores for the segmentation result is reported underneath the image.

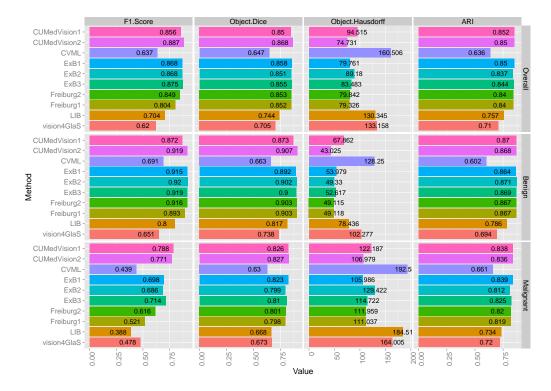


Figure 3: Performance scores achieved by different entries on the combined test data. Evaluation is conducted on three subsets of the data: (1st row) the whole test data, (2nd row) benign, and (3rd row) malignant.

Table 3: Ranking results of the entries when the two parts of test data are combined. Two set of ranking scheme are considered: a) $F1score + Dice_{obj} + H_{obj}$ and b) $F1score + ARI + H_{obj}$. In addition to the evaluation on the whole test data (overall), the entries are evaluated on a subset of the data according to the histologic labels, i.e. benign and malignant.

	Final Ranking								
Entry	F1sco	re + Dico	e _{obj} +H _{obj}	$\rm F1 score + ARI + H_{obj}$					
	Overall	Benign	Malignant	Overall	Benign	Malignant			
CUMedVision1	7	7	3	4	6	3			
CUMedVision2	1	1	1	1	2	2			
CVML	10	10	10	10	10	10			
ExB1	2	6	2	2	7	1			
ExB2	6	3	7	7	1	7			
ExB3	3	5	4	3	3	4			
Freiburg1	4	4	6	6	5	6			
Freiburg2	5	2	5	5	4	5			
LIB	8	8	9	8	8	9			
vision4GlaS	9	9	8	9	9	8			

the adjusted Rand index is included as another performance measurement for segmentation.

The evaluation scores calculated from the combined two test parts are 608 presented as bar chart in Figure 3. The final rankings based on the rank 609 sums of evaluation scores calculated from the combined two test parts are 610 reported in Table 3. Here, two set of rank sums are considered: one calculated 611 according to the criteria of the competition (i.e., $F1score+Dice_{obj}+H_{obj}$), and 612 the other where the adjusted Rand index is used instead of the object-level 613 Dice index to evaluate segmentation accuracy (i.e., $F1score + ARI + H_{obi}$). 614 For both sets of rank sums, the new ranking orders are largely similar to 615 those reported in Section 8.2, with a few swaps in the order, while the top 616 three entries remaining the same, namely CUMedVision2, ExB1, ExB3. 617

The main factors that negatively affect the performance of the methods are a number of challenges presented by the dataset. Firstly, large white empty areas corresponding to the lumen of the gastrointestinal tract which are not in the interior of intestinal glands can easily confuse the segmentation algorithms (Figure 4a). Secondly, characteristics of non-glandular tissue can

sometimes resemble that of the glandular tissue. For instance, connective tis-623 sue in muscularis mucosa or sub-mucosa layers of the colon is stained white 624 and pinkish and has less dense nuclei, thus resembling the inner part of glands 625 (Figure 4b). In the case where there is less stain contrast between nuclei and 626 cytoplasm due to elevated levels of Hematoxylin stain, non-glandular tissue 627 with dense nuclei can look similar to malignant epithelial tissue (Figure 4c). 628 Thirdly, small glandular objects are blended into the surrounding tissue and 629 can be easily mis-detected (Figure 4d). A careful inspection of the segmenta-630 tion results generated by each entry showed that methods by CUMedVision, 631 ExB, and Freiburg better avoid over-segmentation or under-segmentation 632 when facing the above-mentioned pitfalls. 633

The performance of each entry with respect to the histologic grade of 634 cancer was also examined. Their evaluation scores based on benign and 635 malignant samples are reported in the second and the third rows of Figure 636 3 respectively, and the ranking orders derived from the rank sums of the 637 scores are shown in Table 3. Based on these results, one can get a better 638 contrast between the performance of the entries that enforce border separa-639 tion and those that do not. By applying a predicted border mask to separate 640 clumped segmented objects, CUMedVision2 performs better than CUMedVi-641 sion1, which tends to produce segmentation results that merge neighboring 642 glands together, in both benign and malignant cases. Similarly, ExB1 is 643 able to segment malignant glands better than ExB2 and ExB3 that do not 644 utilize border separation. However, this can have an adverse effect if the al-645 gorithm already yields segmentation results that separate individual objects 646 well, such as in the case of ExB1 which under-segments benign glandular 647 objects as compared to its counterparts ExB2 and ExB3. 648

649 8.4. General Discussion

The objectives of this challenge were to raise the research community's 650 awareness of the existence of the intestinal gland segmentation problem in 651 routine stained histology images, and at the same time to provide a plat-652 form for a standardized comparison of the performance of automatic and 653 semi-automatic algorithms. The challenge attracted a lot of attention from 654 researchers, as can be seen from the number of registered teams/individuals 655 and the number of submissions at each stage of the competition. Interest-656 ingly, some of the teams had no experience in working with histology images 657 before. We would like to emphasize that finding the best performing ap-658 proach is not the main objective of the competition, but rather pushing the 659

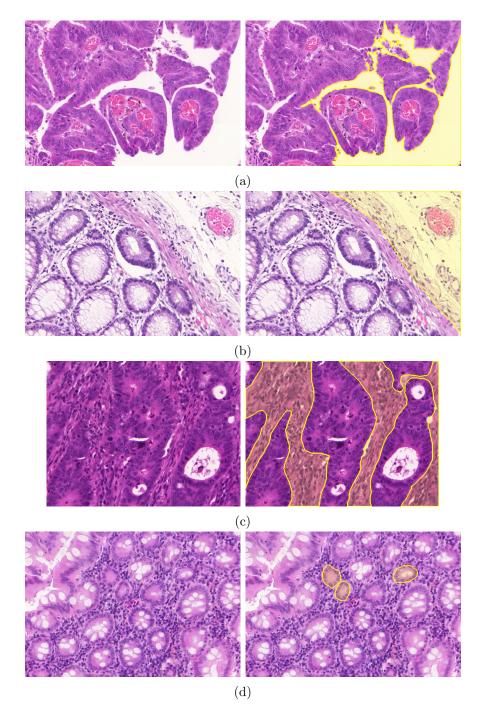


Figure 4: Example images showing some challenging features in the dataset: (a) lumen of the gastrointestinal tract, (b) sub-mucosa layer, (c) area with dense nuclei in mucosa layer, and (d) small glands. Each example is shown with (left) the original image and (right) the overlaid image highlighting the area with challenging characteristic.

boundaries of the-state-of-the-art approaches. Already, we have seen quite interesting developments from many participating teams and the leading algorithms have produced excellent results, both qualitatively and quantitatively.

As noted in the Introduction, morphometric analysis of the appearance 664 of cells and tissues, especially those forming glands from which tumors origi-665 nate, is one of the key components towards precision medicine, and segmen-666 tation is the first step to attain morphological information. Some may have 667 argued that there is no need to perform segmentation, but instead, to fol-668 low conventional pattern recognition approaches by extracting mathematical 669 features which normally capture local and/or global tissue architecture and 670 then identifying features that are most suited to the objective of the study. 671 It is true that there are a number of successful works that follow such an 672 approach (Jafari-Khouzani and Soltanian-Zadeh, 2003; Tabesh et al., 2007; 673 Altunbay et al., 2010; Basavanhally et al., 2010; Ozdemir and Gunduz-Demir, 674 2013; Gultekin et al., 2015). However, because these extracted features are 675 often physically less interpretable in the eyes of practitioners, it is difficult to 676 adopt such an approach in clinical settings. On the other hand, the appear-677 ance of glands such as size and shape obtained through segmentation is easy 678 to interpret. Segmentation also helps to localize other type of information 679 (e.g., texture, spatial arrangement of cells) that is specific to the glandular 680 areas. 681

Even though the dataset used in the challenge included images of different 682 histologic grades taken from several patients, it lacked other aspects. First of 683 all, inter-observer variability was not taken into account as the ground truth 684 was generated by a single expert. This is because the intricate and arduous 685 nature of the problem makes it difficult to find several volunteer experts to 686 perform manual segmentation. Considerable experience is required in order 687 to delineate boundaries of malignant glands, which are not so well-defined 688 as those of the benign ones. Moreover, a single image can contain a large 689 number of glands to be segmented, making the task very laborious. Sec-690 ondly, digitization variability was also not considered in this dataset. It is, in 691 fact, very important to evaluate the robustness of algorithms when the data 692 are scanned by different instruments. As whole-slide scanners are becoming 693 increasingly available, this type of real-world problem should be expected. 694

The choice of evaluation measures would also affect the comparative results. In this challenge, we emphasized object segmentation and accordingly defined the object-level Dice index and the object-level Hausdorff distance to

measure segmentation accuracy at the object level rather than at the pixel 698 level. Nonetheless, it has been suggested that these measures are too strict, 699 as they put a severe penalty on mismatch of the objects. One could replace 700 these measures by less conservative ones, for example, adjusted Rand in-701 dex (Hubert and Arabie, 1985) or a topology preserving warping error (Jain 702 et al., 2010) for a volume-based metric and elastic distance (Younes, 1998; 703 Joshi et al., 2007) for a boundary-based metric. For this reason, we included 704 adjusted rand index as an alternative to object-level Dice index in Section 705 8.3. As we have already pointed out, this results in only a minor change in the 706 ranking order of the entries. Another aspect that was not explicitly included 707 in the evaluation was execution times. Nevertheless, all the algorithms were 708 capable of completing the segmentation task on the on-site test data (Part 709 B) in the given amount of time with or without limitation of resources. Time 710 efficiency is required to process large scale data, such as whole-slide images, 711 whose volume is growing by the day as slides are routinely scanned. Still, in 712 medical practice, accuracy is far more important than speed. 713

It is worth noting that the used evaluation metrics used here are clini-714 cally relevant. As mentioned in the Introduction, morphology of intestinal 715 glands is the key criterion for colorectal cancer grading. This includes shape, 716 size, and formation of the glands. Thus, in terms of clinical relevance, the 717 object-Hausdorff distance is used in accessing the shape similarity between 718 the segmentation results and the ground truth. The object-Dice index is used 719 in assessing the closeness between the volume of the segmentation results and 720 that of the ground truth, which is important in estimating the size of individ-721 ual glands. Although not directly clinically relevant, F1 score is important 722 in assessing the accuracy of the identified glands. Since the morphological 723 assessment is done on the basis of tissue slide including several thousands of 724 glands, an algorithm with high value of F1 score is more preferable as it can 725 detect a larger number of glands. 726

Gland segmentation algorithms presented here are not ready for deployment into clinic in their present form. Although some of the top algorithms produce good segmentation results for the contest dataset and will probably fare well in the real world, there needs to be a large-scale validation involving data from multiple centers annotated by multiple pathologists before any of these algorithms can be deployed in a diagnostic application.

The challenge is now completed, but the dataset will remain available for research purposes so as to continually attract newcomers to the problem and to encourage development of state-of-the-art methods. Extension of the

dataset to address inter-observer and inter-scanner variability seems to be the 736 most achievable aim in the near future. Beyond the scope of segmentation, 737 there lie various extremely interesting future research directions. Previous 738 studies have shown the strong association between the survival of colorectal 739 cancer patients and tumor-related characteristics, including lymphocytic in-740 filtration (Galon et al., 2006; Fridman et al., 2012), desmoplasia (Tommelein 741 et al., 2015), tumor budding (Mitrovic et al., 2012), and necrosis (Richards 742 et al., 2012). A systematic analysis of these characteristics with the help 743 of gland segmentation as part of automatic image analysis framework could 744 lead to a better understanding of the relevant cancer biology as well as bring 745 precision and accuracy into assessment and prediction of the outcome of the 746 cancer. 747

748 9. Conclusions

This paper presented a summary of the Gland Segmentation in Colon 749 Histology Images (GlaS) Challenge Contest which was held in conjunction 750 with the 18th International Conference on Medical Image Computing and 751 Computer Assisted Interventions (MICCAI'2015). The goal of the challenge 752 was to bring together researchers interested in the gland segmentation prob-753 lem, to validate the performance of their existing or newly invented algo-754 rithms on the same standard dataset. In the final round, the total num-755 ber of submitted entries for evaluation was 19, and we presented here in 756 this paper 10 of the leading entries. The dataset used in the challenge has 757 been made publicly available and can be accessed at the challenge website 758 (http://www.warwick.ac.uk/bialab/GlasContest/). Those who are in-759 terested in developing or improving their own approaches are encouraged to 760 use this dataset for quantitative evaluation. 761

762 10. Acknowledgements

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777 Appendix A. The Complete Contest Results

A summary of the ranking results from the contest is given in Figure A.5.

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	Rank								
Method	F1 \$	Score	Objec	t Dice	Object H	Sum			
	Part A	Part B	Part A	Part B	Part A	Part B			
CUMedVision 2	1	3	1	5	1	6	17		
ExB 1	4	4	4	2	6	1	21		
ExB 3	2	2	2	6	5	5	22		
Freiburg 2 ^a	5	5	5	3	3	3	24		
CUMedVision 1	6	1	8	1	8	4	28		
ExB 2	3	6	3	7	2	8	29		
Freiburg 1 ^a	8	8	6	4	4	2	32		
CVIP Dundee ^b	7	7	7	8	7	10	46		
CVML	10	9	11	9	11	7	57		
LIB	9	17	9	12	9	9	65		
vision4GlaS	11	10	10	14	10	11	66		
LIST	13	11	14	11	14	14	77		
Ching-Wei Wang 1°	12	12	15	13	16	16	84		
Bioimage Informatics	16	15	17	10	18	12	88		
Ching-Wei Wang 2°	14	13	16	15	17	17	92		
SUTECH	15	18	13	18	13	15	92		
ISI Kolkatta	18	16	18	19	12	13	96		
FIMM	19	19	12	17	15	19	101		
Ching-Wei Wang 3c	17	14	19	16	19	18	103		

a Image Analysis Lab Uni Freiburg: Freiburg 2 = post-processing, Freiburg 1 = raw

^bCVIP Dundee: feature level fusion

Ching-Wei Wang: Ching-Wei Wang 1 = no preprocess fill hole, Ching-Wei Wang 2 = no preprocess hole, Ching-Wei Wang 3 = preprocess fill hole

Figure A.5: The ranking results from the GlaS Challenge Contest.

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