## 5. Appendices

## Appendix A. Delay Mechanism Pseudo-code

Table A1.: Pseudo-code for assigning delay propagation mechanism 2 - arrival backward propagation

```
Data: Darwin HSP
Result: Assign delay type 2 mechanism minutes
for All Data do
    if Deviation from departure of primary train from station A =0 then
        Next iteration
    end
    Filter secondary train journeys on the same day
    Filter secondary train journeys that are arriving at station A
    Filter secondary train journeys that are scheduled to arrive at station A after primary train is
        scheduled to depart from station A
    Filter secondary train journeys that actually have scheduled arrival time at station A before
        primary train departs from station A
    for Filtered journeys do
        | Assign delay type 2 mechanism minutes
    end
end
```

Table A2.: Pseudo-code for assigning delay propagation mechanism 3-arrival forward propagation

```
Data: Darwin HSP
Result: Assign delay type 3 mechanism minutes
for All Data do
    if Deviation from arrival of primary train at station B =0 then
        Next iteration
    end
    Filter secondary train journeys on the same day
    Filter secondary train journeys that are arriving at station B
    Filter secondary train journeys that are scheduled to arrive at station B after primary train is
        scheduled to arrive at station B
    Filter secondary train journeys that actually have scheduled arrival time at station B before
        primary train arrives at station B
    for Filtered journeys do
        | Assign delay type 3 mechanism minutes
    end
end
```

Table A3.: Pseudo-code for assigning delay propagation mechanism 4-departure backward propagation

```
Data: Darwin HSP
Result: Assign delay type 4 mechanism minutes
for All Data do
    if Deviation from departure of primary train from station A =0 then
    | Next iteration
    end
    Filter secondary train journeys on the same day
    Filter secondary train journeys that are departing from station A
    Filter secondary train journeys that are scheduled to depart from station A after primary train is
    scheduled to depart from station A
    Filter secondary train journeys that actually have scheduled departure time from station A before
        primary train departs from station A
    for Filtered journeys do
        Assign delay type 4 mechanism minutes
    end
end
```

Table A4.: Pseudo-code for assigning delay propagation mechanism 5-departure forward propagation

```
Data: Darwin HSP
Result: Assign delay type 5 mechanism minutes
for All Data do
    if Deviation from departure of primary train from station B}=0\mathrm{ then
    Next iteration
    end
    Filter secondary train journeys on the same day
    Filter secondary train journeys that are arriving at station B
    Filter secondary train journeys that are scheduled to depart from station B after primary train is
    scheduled to arrive at station B
    Filter secondary train journeys that actually have scheduled departure time from station B before
    primary train arrives at station B
    for Filtered journeys do
        Assign delay type 5 mechanism minutes
    end
end
```


## Appendix B. Data Preprocessing Pseudo-code

Table B1.: Pseudo-code for filling in missing actual train arrival time at current station

```
Data: Darwin HSP
Result: Filled in missing arrival time of current station
while Number of total null values change do
    for All Data do
        if \(T D_{C_{i-1}} \neq\) null and \(T D_{C_{i}} \neq\) null and \(i \neq N\) then
            \(T A_{C_{i}} \leftarrow T D_{C_{i-1}}+\) Unique travel time between stations \(C_{i-1}\) and \(C_{i}\)
            if \(T A_{C_{i}}>T D_{C_{i}}\) then
                \(T A_{C_{i}} \leftarrow T D_{C_{i}}\) - Unique station dwell time of station \(C_{i}\)
                if \(T A_{C_{i}}<T D_{C_{i-1}} \quad\) then
                    \(T A_{C_{i}} \leftarrow\) null
                end
            end
        end
        if \(T D_{C_{i-1}} \neq\) null and \(T D_{C_{i}}=\) null and \(i=N\) then
            \(T A_{C_{i}} \leftarrow T D_{C_{i-1}}+\) Unique travel time between stations \(C_{i-1}\) and \(C_{i}\)
        end
        if \(T D_{C_{i-1}}=\) null and \(T D_{C_{i}} \neq\) null and \(i \neq N\) then
            \(T A_{C_{i}} \leftarrow T D_{C_{i}}-\) Unique station dwell time of station \(C_{i}\)
        end
    end
    Calculate total null values
end
```

Table B2.: Pseudo-code for filling in missing actual train departure time at current station

```
Data: Darwin HSP
Result: Filled in missing departure time of current station
while Number of total null values change do
    for All Data do
        if \(T A_{C_{i}} \neq\) null and \(T A_{C_{i+1}} \neq\) null and \(i \neq 0\) then
            \(T D_{C_{i}} \leftarrow T A_{C_{i+1}}-\) Unique travel time between stations \(C_{i}\) and \(C_{i+1}\)
            if \(T D_{C_{i}}<T A_{C_{i}}\) then
                \(T D_{C_{i}} \leftarrow T A_{C_{i}}+\) Unique station dwell time of station \(C_{i}\)
                if \(T D_{C_{i}}>T A_{C_{i}}\) then
                    \(T D_{C_{i}} \leftarrow\) null
                end
            end
        end
        if \(\left(T A_{C_{i+1}} \neq\right.\) null and \(\left.i=0\right)\) or \(\left(T A_{C_{i}}=\right.\) null and \(T A_{C_{i+1}} \neq\) null \()\) then
            \(T D_{C_{i}}^{i+1} \leftarrow T A_{C_{i+1}} \quad-\) Unique travel time between stations \(C_{i}\) and \(C_{i+1}\)
        end
        if \(T A_{C_{i}} \neq\) null and \(T A_{C_{i+1}}=\) null and \(i \neq 0\) then
            \(T D_{C_{i}} \leftarrow T A_{C_{i}}+\) Unique station dwell time of station \(C_{i}\)
        end
    end
    Calculate total null values
end
```


## Appendix C. Feature Engineering Process

Table C1.: Pre-processed data

| Input Feature |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| 0 | -1 | Friday | 0 | -1 | To Didcot Parkway | 0 | 1.0 | No | Yes | Feb | 12 | 1 | 1 | 2 | 22.0 | 0 | 0 | 0 | 0 | 0 |
| -3 | -2 | Friday | -3 | -1 | To Didcot Parkway | 2 | 1.8 | No | No | Feb | 12 | 1 | 2 | 2 | 21.0 | 22 | 0 | 0 | 0 | 0 |
| -5 | -3 | Friday | -2 | -1 | To Didcot Parkway | 3 | 2.2 | No | No | Feb | 12 | 1 | 3 | 2 | 9.5 | 21 | 0 | 0 | 0 | 0 |
| -7 | -4 | Friday | -2 | -1 | To Didcot Parkway | 2 | 2.6 | No | No | Feb | 12 | 1 | 4 | 2 | 4.9 | 9 | 0 | 0 | 0 | 0 |
| -9 | -4 | Friday | -2 | 0 | To Didcot Parkway | 3 | 2.0 | No | No | Feb | 12 | 1 | 5 | 2 | 9.9 | 5 | 0 | 0 | 0 | 0 |
| -9 | -5 | Friday | 0 | -1 | To Didcot Parkway | 2 | 1.5 | No | No | Feb | 12 | 1 | 6 | 2 | 12.3 | 10 | 0 | 0 | 0 | 0 |
| -9 | -6 | Friday | 0 | -1 | To Didcot Parkway | 1 | 2.3 | No | No | Feb | 12 | 1 | 7 | 2 | 10.9 | 12 | 0 | 0 | 0 | 0 |
| -10 | -6 | Friday | -1 | 0 | To Didcot Parkway | 2 | 2.4 | No | No | Feb | 12 | 1 | 8 | 2 | 14.1 | 11 | 0 | 0 | 0 | 0 |
| -10 | 4 | Friday | 0 | 10 | To Didcot Parkway | 11 | 3.4 | No | No | Feb | 12 | 1 | 9 | 2 | 17.2 | 15 | 0 | 0 | 0 | 0 |
| 1 | 22 | Friday | 11 | 18 | To Didcot Parkway | 10 | 3.7 | No | No | Feb | 12 | 1 | 10 | 2 | 12.4 | 18 | 0 | 0 | 0 | 11 |

Table C2.: Encoded pre-processed data

| Input Feature |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| 0 | -1 | 4 | 0 | -1 | 1 | 0 | 1.0 | 0 | 1 | 1 | 12 | 1 | 1 | 2 | 22.0 | 0 | 0 | 0 | 0 | 0 |
| -3 | -2 | 4 | -3 | -1 | 1 | 2 | 1.8 | 0 | 0 | 1 | 12 | 1 | 2 | 2 | 21.0 | 22 | 0 | 0 | 0 | 0 |
| -5 | -3 | 4 | -2 | -1 | 1 | 3 | 2.2 | 0 | 0 | 1 | 12 | 1 | 3 | 2 | 9.5 | 21 | 0 | 0 | 0 | 0 |
| -7 | -4 | 4 | -2 | -1 | 1 | 2 | 2.6 | 0 | 0 | 1 | 12 | 1 | 4 | 2 | 4.9 | 9 | 0 | 0 | 0 | 0 |
| -9 | -4 | 4 | -2 | 0 | 1 | 3 | 2.0 | 0 | 0 | 1 | 12 | 1 | 5 | 2 | 9.9 | 5 | 0 | 0 | 0 | 0 |
| -9 | -5 | 4 | 0 | -1 | 1 | 2 | 1.5 | 0 | 0 | 1 | 12 | 1 | 6 | 2 | 12.3 | 10 | 0 | 0 | 0 | 0 |
| -9 | -6 | 4 | 0 | -1 | 1 | 1 | 2.3 | 0 | 0 | 1 | 12 | 1 | 7 | 2 | 10.9 | 12 | 0 | 0 | 0 | 0 |
| -10 | -6 | 4 | -1 | 0 | 1 | 2 | 2.4 | 0 | 0 | 1 | 12 | 1 | 8 | 2 | 14.1 | 11 | 0 | 0 | 0 | 0 |
| -10 | 4 | 4 | 0 | 10 | 1 | 11 | 3.4 | 0 | 0 | 1 | 12 | 1 | 9 | 2 | 17.2 | 15 | 0 | 0 | 0 | 0 |
| 1 | 22 | 4 | 11 | 18 | 1 | 10 | 3.7 | 0 | 0 | 1 | 12 | 1 | 10 | 2 | 12.4 | 18 | 0 | 0 | 0 | 11 |

Table C3.: Encoded pre-processed data

| Input Feature |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Tue | Wed | Thu | Fri | Feb | Mar | Apr | May | Jun | Jul | Aug | Sep | Oct | Nov | Dec |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Table C4.: Input matrix

| Input Feature |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| -0.48 | -0.50 | -0.51 | -0.51 | 1.99 | -0.30 | -0.31 | -0.30 | -0.31 | -0.30 | -0.30 | -0.29 | -0.31 | -0.30 | -0.31 | -0.28 | -0.36 | -0.57 |
| -0.48 | -0.50 | -0.51 | -0.51 | 1.99 | -0.30 | -0.31 | -0.30 | -0.31 | -0.30 | -0.30 | -0.29 | -0.31 | -0.30 | -0.31 | -0.28 | -0.46 | -0.60 |
| -0.48 | -0.50 | -0.51 | -0.51 | 1.99 | -0.30 | -0.31 | -0.30 | -0.31 | -0.30 | -0.30 | -0.29 | -0.31 | -0.30 | -0.31 | -0.28 | -0.54 | -0.64 |
| -0.48 | -0.50 | -0.51 | -0.51 | 1.99 | -0.30 | -0.31 | -0.30 | -0.31 | -0.30 | -0.30 | -0.29 | -0.31 | -0.30 | -0.31 | -0.28 | -0.61 | -0.67 |
| -0.48 | -0.50 | -0.51 | -0.51 | 1.99 | -0.30 | -0.31 | -0.30 | -0.31 | -0.30 | -0.30 | -0.29 | -0.31 | -0.30 | -0.31 | -0.28 | -0.68 | -0.67 |
| -0.48 | -0.50 | -0.51 | -0.51 | 1.99 | -0.30 | -0.31 | -0.30 | -0.31 | -0.30 | -0.30 | -0.29 | -0.31 | -0.30 | -0.31 | -0.28 | -0.68 | -0.70 |
| -0.48 | -0.50 | -0.51 | -0.51 | 1.99 | -0.30 | -0.31 | -0.30 | -0.31 | -0.30 | -0.30 | -0.29 | -0.31 | -0.30 | -0.31 | -0.28 | -0.68 | -0.74 |
| -0.48 | -0.50 | -0.51 | -0.51 | 1.99 | -0.30 | -0.31 | -0.30 | -0.31 | -0.30 | -0.30 | -0.29 | -0.31 | -0.30 | -0.31 | -0.28 | -0.71 | -0.74 |
| -0.48 | -0.50 | -0.51 | -0.51 | 1.99 | -0.30 | -0.31 | -0.30 | -0.31 | -0.30 | -0.30 | -0.29 | -0.31 | -0.30 | -0.31 | -0.28 | -0.71 | -0.40 |
| -0.48 | -0.50 | -0.51 | -0.51 | 1.99 | -0.30 | -0.31 | -0.30 | -0.31 | -0.30 | -0.30 | -0.29 | -0.31 | -0.30 | -0.31 | -0.28 | -0.32 | 0.20 |
| Input Feature |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |  |
| -0.35 | -0.78 | 0.93 | -0.77 | -0.44 | -0.30 | 3.30 | -0.51 | -1.62 | -1.31 | 0.38 | 2.04 | -1.09 | -0.16 | -0.15 | -0.15 | -0.23 |  |
| -1.06 | -0.78 | 0.93 | 0.24 | 0.28 | -0.30 | -0.30 | -0.51 | -1.62 | -1.12 | 0.38 | 1.89 | 1.98 | -0.16 | -0.15 | -0.15 | -0.23 |  |
| -0.82 | -0.78 | 0.93 | 0.74 | 0.59 | -0.30 | -0.30 | -0.51 | -1.62 | -0.93 | 0.38 | 0.24 | 1.84 | -0.16 | -0.15 | -0.15 | -0.23 |  |
| -0.82 | -0.78 | 0.93 | 0.24 | 0.99 | -0.30 | -0.30 | -0.51 | -1.62 | -0.74 | 0.38 | -0.43 | 0.17 | -0.16 | -0.15 | -0.15 | -0.23 |  |
| -0.82 | -0.52 | 0.93 | 0.74 | 0.47 | -0.30 | -0.30 | -0.51 | -1.62 | -0.55 | 0.38 | 0.29 | -0.39 | -0.16 | -0.15 | -0.15 | -0.23 |  |
| -0.35 | -0.78 | 0.93 | 0.24 | 0.01 | -0.30 | -0.30 | -0.51 | -1.62 | -0.35 | 0.38 | 0.64 | 0.31 | -0.16 | -0.15 | -0.15 | -0.23 |  |
| -0.35 | -0.78 | 0.93 | -0.27 | 0.69 | -0.30 | -0.30 | -0.51 | -1.62 | -0.16 | 0.38 | 0.44 | 0.59 | -0.16 | -0.15 | -0.15 | -0.23 |  |
| -0.59 | -0.52 | 0.93 | 0.24 | 0.82 | -0.30 | -0.30 | -0.51 | -1.62 | 0.03 | 0.38 | 0.90 | 0.45 | -0.16 | -0.15 | -0.15 | -0.23 |  |
| -0.35 | 2.04 | 0.93 | 4.77 | 1.70 | -0.30 | -0.30 | -0.51 | -1.62 | 0.22 | 0.38 | 1.35 | 1.00 | -0.16 | -0.15 | -0.15 | -0.23 |  |
| 2.24 | 4.10 | 0.93 | 4.27 | 1.92 | -0.30 | -0.30 | -0.51 | -1.62 | 0.41 | 0.38 | 0.65 | 1.42 | -0.16 | -0.15 | -0.15 | 2.02 |  |

Appendix D. DNN vs XGBoost Results

(a) 2-step DNN deviation from arrival

(c) 2-step DNN deviation from departure

(b) 2-step XGBoost deviation from arrival

(d) 2-step XGBoost deviation from departure


(i) 3-step DNN deviation from arrival

(k) 3-step DNN deviation from departure

(j) 3-step XGBoost deviation from arrival

(l) 3-step XGBoost deviation from departure


(q) 4-step DNN deviation from arrival

(s) 4-step DNN deviation from departure

(r) 4-step XGBoost deviation from arrival

(t) 4-Step XGBoost Deviation from Departure


(y) 5-step DNN deviation from arrival

(aa) 5 -step DNN deviation from departure

(z) 5-step XGBoost deviation from arrival

(ab) 5-step XGBoost deviation from departure


(ag) 6-step DNN deviation from arrival

(ai) 6-step DNN deviation from departure

(ah) 6-step XGBoost deviation from arrival

(aj) 6-step XGBoost deviation from departure


(ao) 7-step DNN deviation from arrival

(aq) 7 -step DNN deviation from departure

(ap) 7-step XGBoost deviation from arrival

(ar) 7-step XGBoost deviation from departure


(aw) 8-step DNN deviation from arrival

(ay) 8-step DNN deviation from departure

(ax) 8-step XGBoost deviation from arrival

(az) 8-step XGBoost deviation from departure

(ba) 8-step DNN travel time

(bc) 8-step DNN dwell time

(bb) 8-step XGBoost travel time

(bd) 8-step XGBoost dwell time

(be) 9-step DNN deviation from arrival

(bg) 9-step DNN deviation from departure

(bf) 9-step XGBoost deviation from arrival

(bh) 9-step XGBoost deviation from departure


(bm) 10-step DNN deviation from arrival

(bo) 10-step DNN deviation from departure

(bn) 10-step XGBoost deviation from arrival

(bp) 10-step XGBoost deviation from departure


## Appendix E. DNN Training and Validation Loss


(a) 1-step

(c) 3-step

(e) 5-step

(b) 2-step

(d) 4-step

(f) 6-step


## Appendix F. XGBoost Training and Validation Loss


(a) 1-step

(b) 2-step

(c) 3-step
(e) 5-step

(g) 7-step

(d) 4-step

(f) 6 -step

(h) 8 -step

(i) 9-step

(j) 10-step

