5. Appendices

Appendix A. Delay Mechanism Pseudo-code

Table A1.: Pseudo-code for assigning delay propagation mechanism 2 - arrival backward propagation

```
Data: Darwin HSP

Result: Assign delay type 2 mechanism minutes

for All Data do

if Deviation from departure of primary train from station A = 0 then

| Next iteration
end
Filter secondary train journeys on the same day
Filter secondary train journeys that are arriving at station A
Filter secondary train journeys that are scheduled to arrive at station A after primary train is scheduled to depart from station A
Filter secondary train journeys that actually have scheduled arrival time at station A before primary train departs from station A

for Filtered journeys do

| Assign delay type 2 mechanism minutes
end
end
```

Table A2.: Pseudo-code for assigning delay propagation mechanism 3 - arrival forward propagation

```
Data: Darwin HSP

Result: Assign delay type 3 mechanism minutes

for All Data do

if Deviation from arrival of primary train at station B = 0 then

| Next iteration
| end
| Filter secondary train journeys on the same day
| Filter secondary train journeys that are arriving at station B
| Filter secondary train journeys that are scheduled to arrive at station B after primary train is
| scheduled to arrive at station B
| Filter secondary train journeys that actually have scheduled arrival time at station B before
| primary train arrives at station B
| for Filtered journeys do
| Assign delay type 3 mechanism minutes
| end
| end
```

Table A3.: Pseudo-code for assigning delay propagation mechanism 4 - departure backward propagation

```
Data: Darwin HSP
Result: Assign delay type 4 mechanism minutes
for All Data do
    if Deviation from departure of primary train from station A = 0 then
        Next iteration
    end
    Filter secondary train journeys on the same day
    Filter secondary train journeys that are departing from station A
    Filter secondary train journeys that are scheduled to depart from station A after primary train is
     scheduled to depart from station A
    Filter secondary train journeys that actually have scheduled departure time from station A before
     primary train departs from station A
    for Filtered journeys do
    | Assign delay type 4 mechanism minutes
    \mathbf{end}
end
```

Table A4.: Pseudo-code for assigning delay propagation mechanism 5 - departure forward propagation

```
Data: Darwin HSP

Result: Assign delay type 5 mechanism minutes

for All Data do

if Deviation from departure of primary train from station B = 0 then

| Next iteration
| end
| Filter secondary train journeys on the same day
| Filter secondary train journeys that are arriving at station B
| Filter secondary train journeys that are scheduled to depart from station B after primary train is
| scheduled to arrive at station B
| Filter secondary train journeys that actually have scheduled departure time from station B before
| primary train arrives at station B
| for Filtered journeys do
| Assign delay type 5 mechanism minutes
| end
| end
```

Appendix B. Data Preprocessing Pseudo-code

Table B1.: Pseudo-code for filling in missing actual train arrival time at current station

```
 \begin{array}{c|c} \textbf{Data: Darwin HSP} \\ \textbf{Result: Filled in missing arrival time of current station} \\ \textbf{while } \textit{Number of total null values change } \textbf{do} \\ \hline \textbf{for } \textit{All Data } \textbf{do} \\ \hline & \textbf{if } TD_{C_{i-1}} \neq \textit{null and } TD_{C_{i}} \neq \textit{null and } i \neq \textit{N then} \\ \hline & TA_{C_{i}} \leftarrow TD_{C_{i-1}} + \textit{Unique travel time between stations } C_{i-1} \textit{ and } C_{i} \\ \hline & \textbf{if } TA_{C_{i}} \leftarrow TD_{C_{i}} \textbf{ then} \\ \hline & TA_{C_{i}} \leftarrow TD_{C_{i}} \textbf{ then} \\ \hline & TA_{C_{i}} \leftarrow TD_{C_{i}} \textbf{ then} \\ \hline & TA_{C_{i}} \leftarrow TD_{C_{i-1}} \textbf{ then} \\ \hline & TA_{C_{i}} \leftarrow \textit{null} \\ \hline & \textbf{end} \\ \hline & \textbf{end} \\ \hline & \textbf{end} \\ \hline & \textbf{if } TD_{C_{i-1}} \neq \textit{null and } TD_{C_{i}} = \textit{null and } i = \textit{N then} \\ \hline & TA_{C_{i}} \leftarrow TD_{C_{i-1}} + \textit{Unique travel time between stations } C_{i-1} \textit{ and } C_{i} \\ \hline & \textbf{end} \\ \hline & \textbf{if } TD_{C_{i-1}} = \textit{null and } TD_{C_{i}} \neq \textit{null and } i \neq \textit{N then} \\ \hline & TA_{C_{i}} \leftarrow TD_{C_{i}} - \textit{Unique station dwell time of station } C_{i} \\ \hline & \textbf{end} \\ \hline & \textbf{end} \\ \hline & \textbf{end} \\ \hline & \textbf{calculate total null values} \\ \hline & \textbf{end} \\ \hline \end{array}
```

Table B2.: Pseudo-code for filling in missing actual train departure time at current station

```
 \begin{aligned} \textbf{Data:} & \text{Darwin HSP} \\ \textbf{Result:} & \text{Filled in missing departure time of current station} \\ \textbf{while} & \textit{Number of total null values change } \textbf{do} \\ & \textbf{for } & \textit{All Data } \textbf{do} \\ & \textbf{if } & TA_{C_i} \neq \textit{null and } & TA_{C_{i+1}} \neq \textit{null and } i \neq 0 \textbf{ then} \\ & & | & TD_{C_i} \leftarrow TA_{C_{i+1}} - \textit{Unique travel time between stations } C_i \textit{ and } C_{i+1} \\ & \textbf{if } & TD_{C_i} \leftarrow TA_{C_{i+1}} - \textit{Unique station dwell time of station } C_i \\ & \textbf{if } & TD_{C_i} \leftarrow TA_{C_i} + \textit{Unique station dwell time of station } C_i \\ & \textbf{if } & TD_{C_i} \leftarrow TA_{C_{i+1}} & \textbf{then} \\ & & | & TD_{C_i} \leftarrow \textit{null} \\ & \textbf{end} \\ & \textbf{end} \\ & \textbf{end} \\ & \textbf{if } & (TA_{C_{i+1}} \neq \textit{null and } i = 0) \textit{ or } (TA_{C_i} = \textit{null and } TA_{C_{i+1}} \neq \textit{null) \textbf{then}} \\ & & | & TD_{C_i} \leftarrow TA_{C_{i+1}} - \textit{Unique travel time between stations } C_i \textit{ and } C_{i+1} \\ & \textbf{end} \\ & \textbf{if } & TA_{C_i} \neq \textit{null and } & TA_{C_{i+1}} = \textit{null and } i \neq 0 \textbf{ then} \\ & & | & TD_{C_i} \leftarrow TA_{C_i} + \textit{Unique station dwell time of station } C_i \\ & \textbf{end} \\ & \textbf{end} \\ & \textbf{end} \\ & \textbf{calculate total null values} \\ & \textbf{end} \end{aligned}
```

Appendix C. Feature Engineering Process

Table C1.: Pre-processed data

Inpu	t Feat	ture																		
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
0	-1	Friday	0	-1	To Didcot Parkway	0	1.0	No	Yes	Feb	12	1	1	2	22.0	0	0	0	0	0
-3	-2	Friday	-3	-1	To Didcot Parkway	2	1.8	No	No	Feb	12	1	2	2	21.0	22	0	0	0	0
-5	-3	Friday	-2	-1	To Didcot Parkway	3	2.2	No	No	Feb	12	1	3	2	9.5	21	0	0	0	0
-7	-4	Friday	-2	-1	To Didcot Parkway	2	2.6	No	No	Feb	12	1	4	2	4.9	9	0	0	0	0
-9	-4	Friday	-2	0	To Didcot Parkway	3	2.0	No	No	Feb	12	1	5	2	9.9	5	0	0	0	0
-9	-5	Friday	0	-1	To Didcot Parkway	2	1.5	No	No	Feb	12	1	6	2	12.3	10	0	0	0	0
-9	-6	Friday	0	-1	To Didcot Parkway	1	2.3	No	No	Feb	12	1	7	2	10.9	12	0	0	0	0
-10	-6	Friday	-1	0	To Didcot Parkway	2	2.4	No	No	Feb	12	1	8	2	14.1	11	0	0	0	0
-10	4	Friday	0	10	To Didcot Parkway	11	3.4	No	No	Feb	12	1	9	2	17.2	15	0	0	0	0
1	22	Friday	11	18	To Didcot Parkway	10	3.7	No	No	Feb	12	1	10	2	12.4	18	0	0	0	11

Table C2.: Encoded pre-processed data

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 0 -1 4 0 -1 1 0 1.0 0 1 1 12 1 1 2 22.0 0 0 0 -3 -2 4 -3 -1 1 2 1.8 0 0 1 12 1 2 2 21.0 22 0 0 -5 -3 4 -2 -1 1 3 2.2 0 0 1 12 1 3 2 9.5 21 0 0 -7 -4 4 -2 -1 1 2 2.6 0 0 1 12 1 4 2 4.9 9 0 0 -9 -4 4 -2	Input	Featu	re																		
-3 -2 4 -3 -1 1 2 1.8 0 0 1 12 1 2 2 21.0 22 0 0 0 1 12 1 2 2 21.0 22 0 0 0 1 12 1 3 2 9.5 21 0 0 0 1 12 1 3 2 9.5 21 0 0 0 1 12 1 4 2 4.9 9 0 0 0 1 12 1 4 2 4.9 9 0 0 0 0 1 12 1 5 2 9.9 5 0 0 0 1 12 1 5 2 9.9 5 0 0 0 1 12 1 6 2 12.3 10 0 0 0 1 12 1 7 <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> <td>8</td> <td>9</td> <td>10</td> <td>11</td> <td>12</td> <td>13</td> <td>14</td> <td>15</td> <td>16</td> <td>17</td> <td>18</td> <td>19</td> <td>20</td> <td>21</td>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
-5 -3 4 -2 -1 1 3 2.2 0 0 1 12 1 3 2 9.5 21 0 0 0 1 12 1 3 2 9.5 21 0 0 0 1 12 1 4 2 4.9 9 0 0 0 1 12 1 4 2 4.9 9 0 0 0 1 12 1 4 2 4.9 9 0 0 0 1 12 1 5 2 9.9 5 0 0 0 1 12 1 5 2 9.9 5 0 0 0 1 12 1 6 2 12.3 10 0 0 0 1 12 1 7 2 10.9 12 0 0 0 1 12 1 1 1	0	-1	4	0	-1	1	0	1.0	0	1	1	12	1	1	2	22.0	0	0	0	0	0
-7 -4 4 -2 -1 1 2 2.6 0 0 1 12 1 4 2 4.9 9 0 0 0 -9 -4 4 -2 0 1 3 2.0 0 0 1 12 1 5 2 9.9 5 0 0 -9 -5 4 0 -1 1 2 1.5 0 0 1 12 1 6 2 12.3 10 0 0 -9 -6 4 0 -1 1 1 2.3 0 0 1 12 1 7 2 10.9 12 0 0 -10 -6 4 -1 0 1 2 2.4 0 0 1 12 1 8 2 14.1 11 0 0	-3	-2	4	-3	-1	1	2	1.8	0	0	1	12	1	2	2	21.0	22	0	0	0	0
-9 -4 4 -2 0 1 3 2.0 0 0 1 12 1 5 2 9.9 5 0 0 -9 -5 4 0 -1 1 2 1.5 0 0 1 12 1 6 2 12.3 10 0 0 -9 -6 4 0 -1 1 1 2.3 0 0 1 12 1 7 2 10.9 12 0 0 -10 -6 4 -1 0 1 2 2.4 0 0 1 12 1 8 2 14.1 11 0 0	-5	-3	4	-2	-1	1	3	2.2	0	0	1	12	1	3	2	9.5	21	0	0	0	0
-9 -5 4 0 -1 1 2 1.5 0 0 1 12 1 6 2 12.3 10 0 0 -9 -6 4 0 -1 1 1 2.3 0 0 1 12 1 7 2 10.9 12 0 0 -10 -6 4 -1 0 1 2 2.4 0 0 1 12 1 8 2 14.1 11 0 0	-7	-4	4	-2	-1	1	2	2.6	0	0	1	12	1	4	2	4.9	9	0	0	0	0
-9 -6 4 0 -1 1 1 2.3 0 0 1 12 1 7 2 10.9 12 0 0 -10 -6 4 -1 0 1 2 2.4 0 0 1 12 1 8 2 14.1 11 0 0	-9	-4	4	-2	0	1	3	2.0	0	0	1	12	1	5	2	9.9	5	0	0	0	0
-10 -6 4 -1 0 1 2 2.4 0 0 1 12 1 8 2 14.1 11 0 0	-9	-5	4	0	-1	1	2	1.5	0	0	1	12	1	6	2	12.3	10	0	0	0	0
	-9	-6	4	0	-1	1	1	2.3	0	0	1	12	1	7	2	10.9	12	0	0	0	0
-10 4 4 0 10 1 11 3.4 0 0 1 12 1 9 2 17.2 15 0 0	-10	-6	4	-1	0	1	2	2.4	0	0	1	12	1	8	2	14.1	11	0	0	0	0
	-10	4	4	0	10	1	11	3.4	0	0	1	12	1	9	2	17.2	15	0	0	0	0
1 22 4 11 18 1 10 3.7 0 0 1 12 1 10 2 12.4 18 0 0	1	22	4	11	18	1	10	3.7	0	0	1	12	1	10	2	12.4	18	0	0	0	11

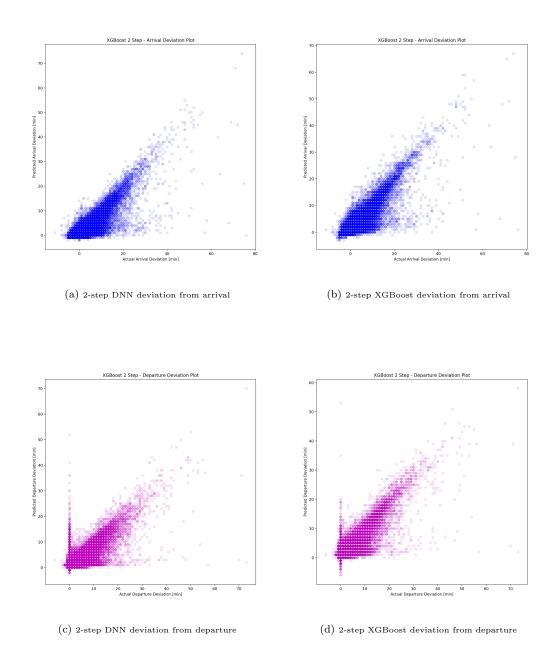
Table C3.: Encoded pre-processed data

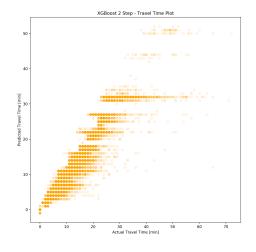
Input F	eature													
Tue	Wed	Thu	Fri	Feb	Mar	Apr	May	$_{ m Jun}$	$_{ m Jul}$	Aug	Sep	Oct	Nov	Dec
0	0	0	1	1	0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0	0	0	0	0	0	0

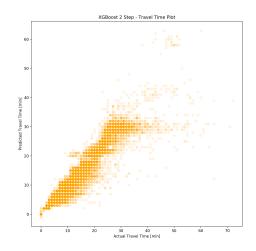
Table C4.: Input matrix

Input l	Feature																
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
-0.48	-0.50	-0.51	-0.51	1.99	-0.30	-0.31	-0.30	-0.31	-0.30	-0.30	-0.29	-0.31	-0.30	-0.31	-0.28	-0.36	-0.57
-0.48	-0.50	-0.51	-0.51	1.99	-0.30	-0.31	-0.30	-0.31	-0.30	-0.30	-0.29	-0.31	-0.30	-0.31	-0.28	-0.46	-0.60
-0.48	-0.50	-0.51	-0.51	1.99	-0.30	-0.31	-0.30	-0.31	-0.30	-0.30	-0.29	-0.31	-0.30	-0.31	-0.28	-0.54	-0.64
-0.48	-0.50	-0.51	-0.51	1.99	-0.30	-0.31	-0.30	-0.31	-0.30	-0.30	-0.29	-0.31	-0.30	-0.31	-0.28	-0.61	-0.67
-0.48	-0.50	-0.51	-0.51	1.99	-0.30	-0.31	-0.30	-0.31	-0.30	-0.30	-0.29	-0.31	-0.30	-0.31	-0.28	-0.68	-0.67
-0.48	-0.50	-0.51	-0.51	1.99	-0.30	-0.31	-0.30	-0.31	-0.30	-0.30	-0.29	-0.31	-0.30	-0.31	-0.28	-0.68	-0.70
-0.48	-0.50	-0.51	-0.51	1.99	-0.30	-0.31	-0.30	-0.31	-0.30	-0.30	-0.29	-0.31	-0.30	-0.31	-0.28	-0.68	-0.74
-0.48	-0.50	-0.51	-0.51	1.99	-0.30	-0.31	-0.30	-0.31	-0.30	-0.30	-0.29	-0.31	-0.30	-0.31	-0.28	-0.71	-0.74
-0.48	-0.50	-0.51	-0.51	1.99	-0.30	-0.31	-0.30	-0.31	-0.30	-0.30	-0.29	-0.31	-0.30	-0.31	-0.28	-0.71	-0.40
-0.48	-0.50	-0.51	-0.51	1.99	-0.30	-0.31	-0.30	-0.31	-0.30	-0.30	-0.29	-0.31	-0.30	-0.31	-0.28	-0.32	0.20
Input l	Feature																
19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	
-0.35	-0.78	0.93	-0.77	-0.44	-0.30	3.30	-0.51	-1.62	-1.31	0.38	2.04	-1.09	-0.16	-0.15	-0.15	-0.23	
-1.06	-0.78	0.93	0.24	0.28	-0.30	-0.30	-0.51	-1.62	-1.12	0.38	1.89	1.98	-0.16	-0.15	-0.15	-0.23	
-0.82	-0.78	0.93	0.74	0.59	-0.30	-0.30	-0.51	-1.62	-0.93	0.38	0.24	1.84	-0.16	-0.15	-0.15	-0.23	
-0.82	-0.78	0.93	0.24	0.99	-0.30	-0.30	-0.51	-1.62	-0.74	0.38	-0.43	0.17	-0.16	-0.15	-0.15	-0.23	
-0.82	-0.52	0.93	0.74	0.47	-0.30	-0.30	-0.51	-1.62	-0.55	0.38	0.29	-0.39	-0.16	-0.15	-0.15	-0.23	
-0.35	-0.78	0.93	0.24	0.01	-0.30	-0.30	-0.51	-1.62	-0.35	0.38	0.64	0.31	-0.16	-0.15	-0.15	-0.23	
-0.35	-0.78	0.93	-0.27	0.69	-0.30	-0.30	-0.51	-1.62	-0.16	0.38	0.44	0.59	-0.16	-0.15	-0.15	-0.23	
-0.59	-0.52	0.93	0.24	0.82	-0.30	-0.30	-0.51	-1.62	0.03	0.38	0.90	0.45	-0.16	-0.15	-0.15	-0.23	
-0.35	2.04	0.93	4.77	1.70	-0.30	-0.30	-0.51	-1.62	0.22	0.38	1.35	1.00	-0.16	-0.15	-0.15	-0.23	
2.24	4.10	0.93	4.27	1.92	-0.30	-0.30	-0.51	-1.62	0.41	0.38	0.65	1.42	-0.16	-0.15	-0.15	2.02	

Appendix D. DNN vs XGBoost Results

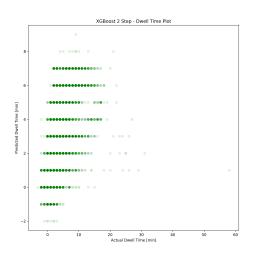


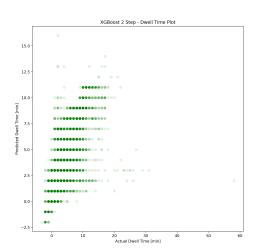




(e) 2-step DNN travel time

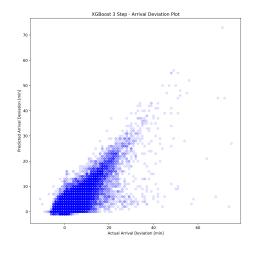


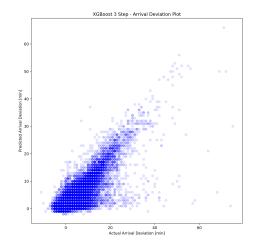




(g) 2-step DNN dwell time

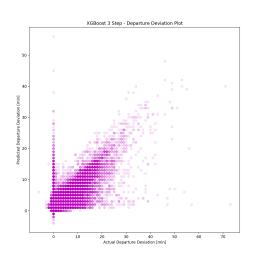
 $\hbox{$\left(h\right)$ 2-step XGBoost dwell time}$

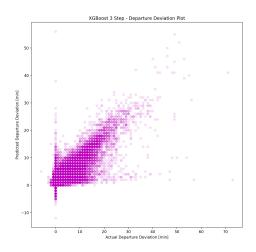




ig(iig) 3-step DNN deviation from arrival

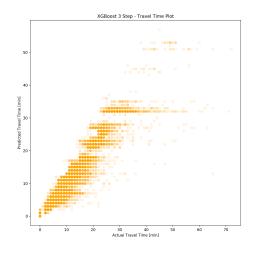


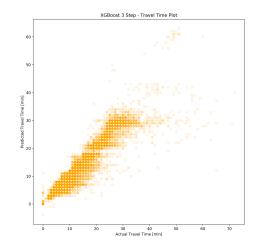




(k) 3-step DNN deviation from departure

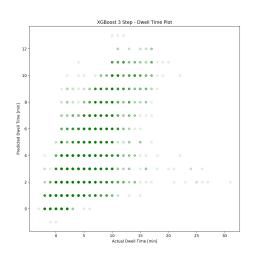
(l) 3-step XGBoost deviation from departure





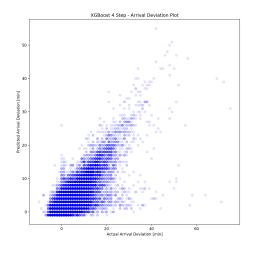
(m) 3-step DNN travel time

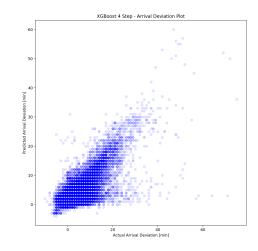




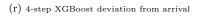
(o) 3-step DNN dwell time

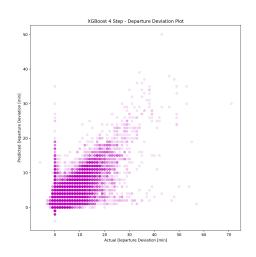
(p) 3-step XGBoost dwell time

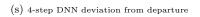


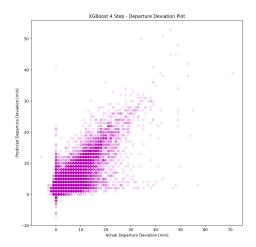


(q) 4-step DNN deviation from arrival

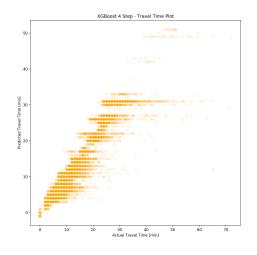


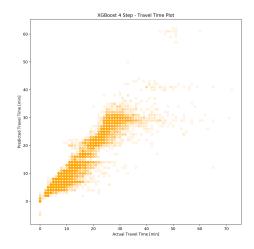






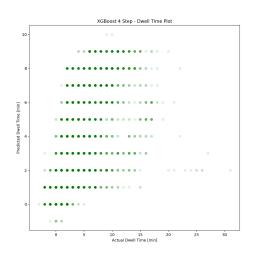
(t) 4-Step XGBoost Deviation from Departure





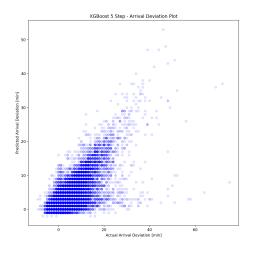
(u) 4-step DNN travel time

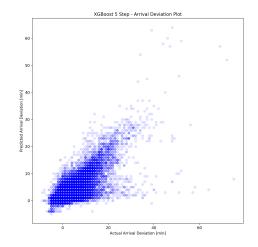




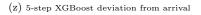
(w) 4-step DNN dwell time

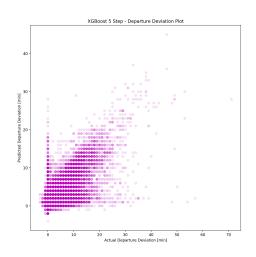
(x) 4-step XGBoost dwell time

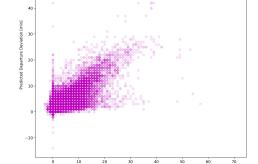




(y) 5-step DNN deviation from arrival

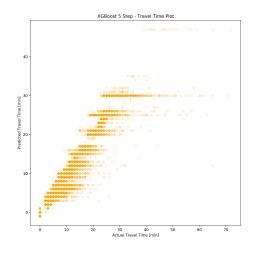


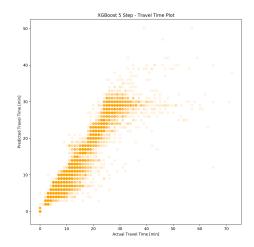




(aa) 5-step DNN deviation from departure

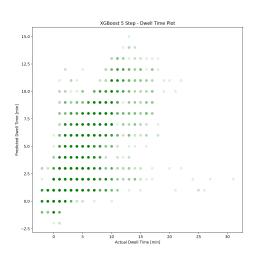
(ab) 5-step XGBoost deviation from departure

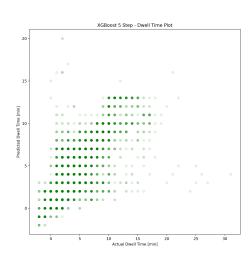




(ac) 5-step DNN travel time

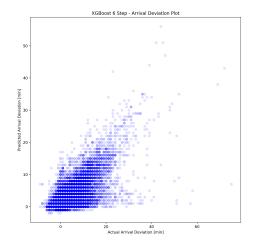


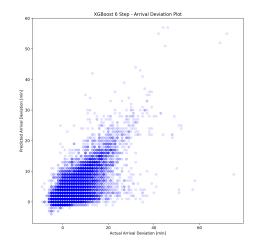




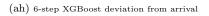
(ae) 5-step DNN dwell time

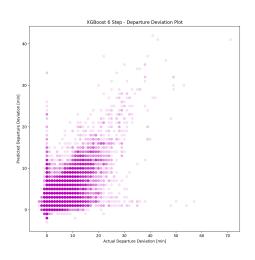
(af) 5-step XGBoost dwell time

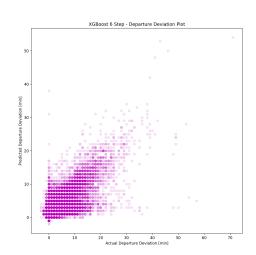




(ag) 6-step DNN deviation from arrival

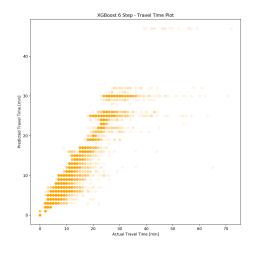


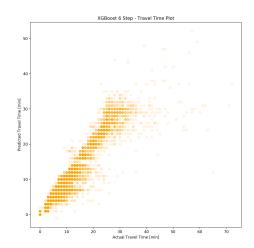




(ai) 6-step DNN deviation from departure

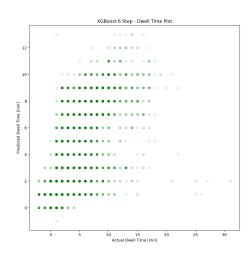
 $\left(aj\right) \text{ 6-step XGBoost deviation from departure}$



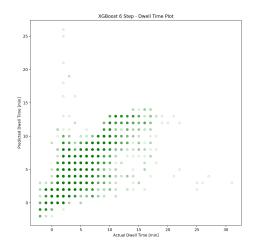


 $\left(ak\right) \text{ 6-step DNN travel time}$

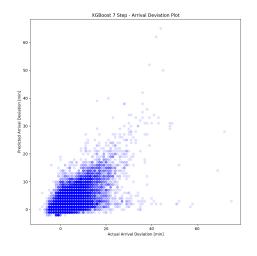


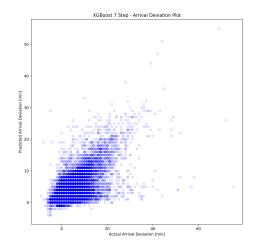


(am) 6-step DNN dwell time

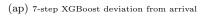


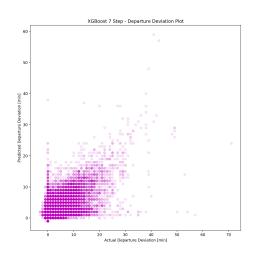
(an) 6-step XGBoost dwell time

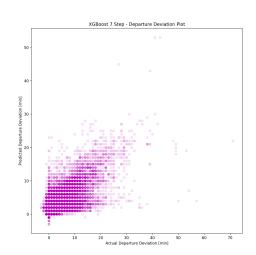




(ao) 7-step DNN deviation from arrival

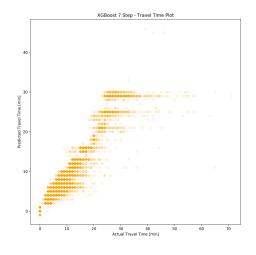


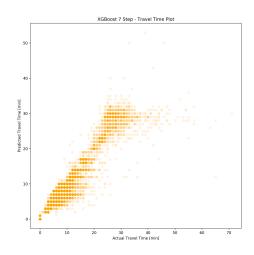




(aq) 7-step DNN deviation from departure

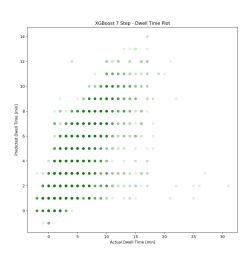
(ar) 7-step XGBoost deviation from departure

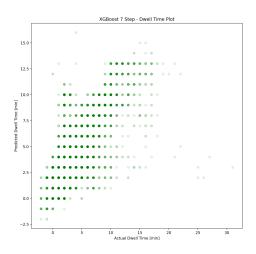




(as) 7-step DNN travel time

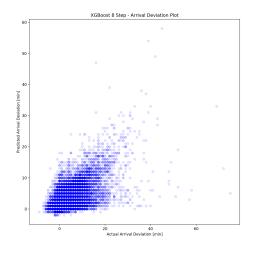


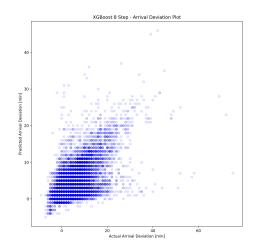




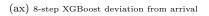
(au) 7-step DNN dwell time

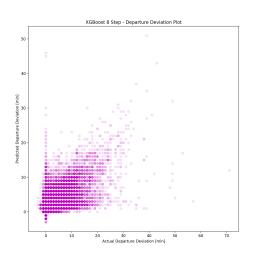
(av) 7-step XGBoost dwell time

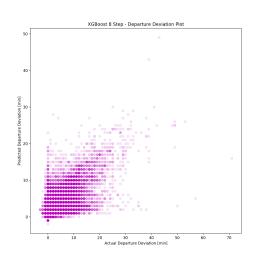




(aw) 8-step DNN deviation from arrival

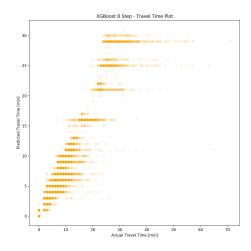


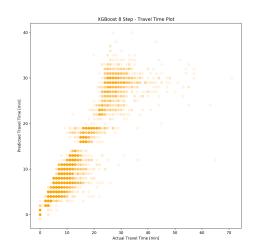




(ay) 8-step DNN deviation from departure

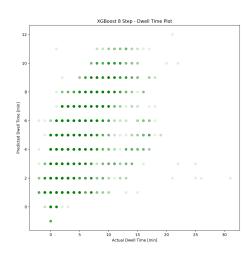
(az) 8-step XGBoost deviation from departure

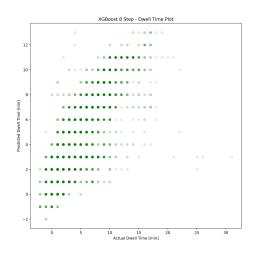




(ba) 8-step DNN travel time

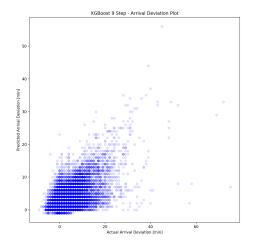


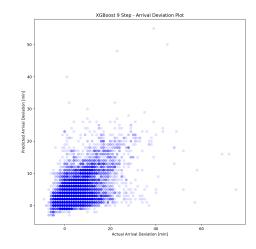




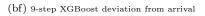
(bc) 8-step DNN dwell time

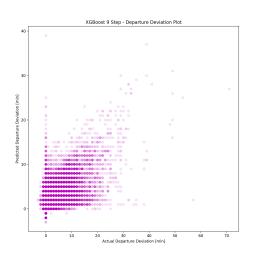
(bd) 8-step XGBoost dwell time

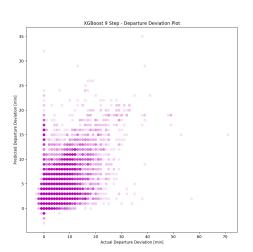




(be) 9-step DNN deviation from arrival

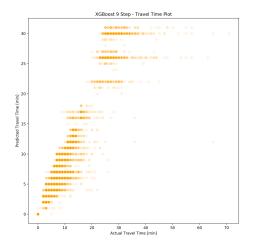


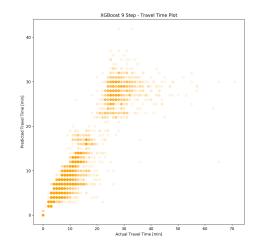




(bg) 9-step DNN deviation from departure

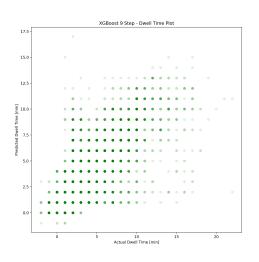
(bh) 9-step XGBoost deviation from departure

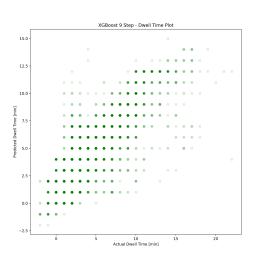




(bi) 9-step DNN travel time

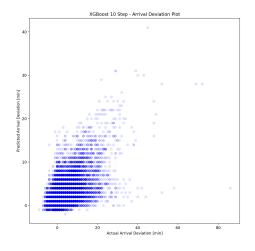


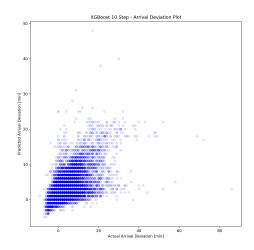




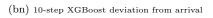
(bk) 9-step DNN dwell time

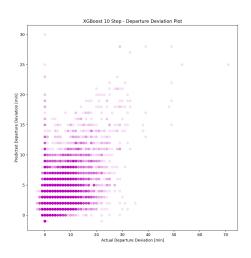
(bl) 9-step XGBoost dwell time

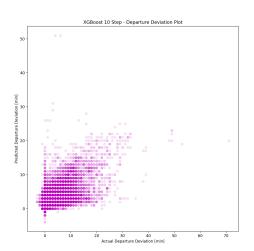




(bm) 10-step DNN deviation from arrival

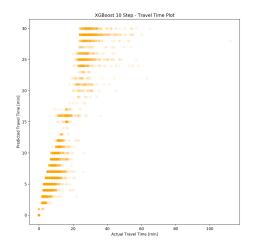


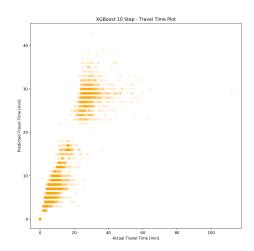




(bo) 10-step DNN deviation from departure

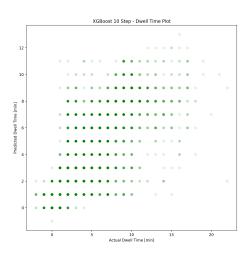
(bp) 10-step XGBoost deviation from departure

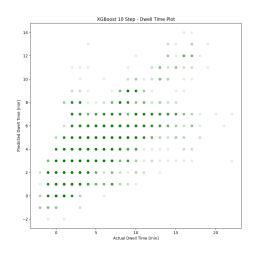




(bq) 10-step DNN travel time



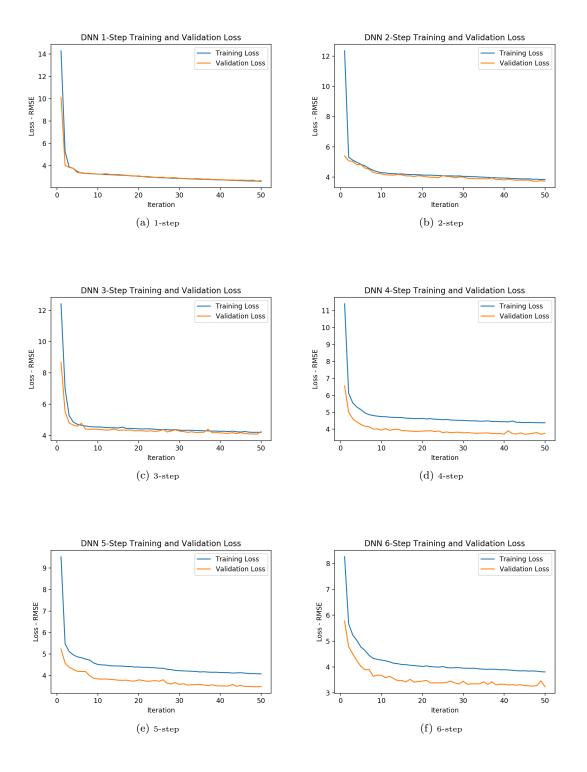


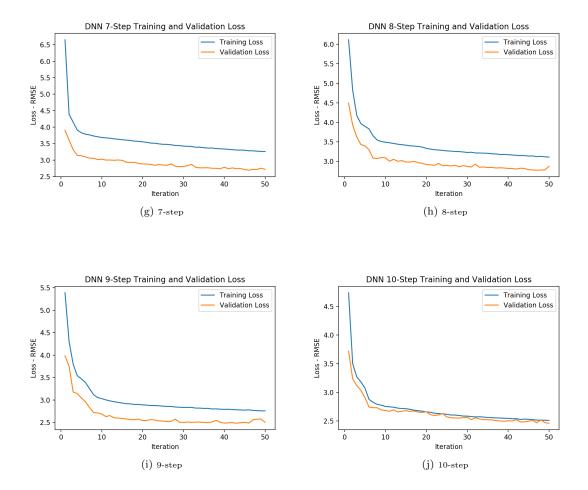


(bs) 10-step DNN dwell time

(bt) 10-step XGBoost dwell time

Appendix E. DNN Training and Validation Loss





Appendix F. XGBoost Training and Validation Loss

