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Subject Section

ATEN: And/Or Tree Ensemble for inferring accurate Boolean network topology and dynamics

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Abstract

Motivation: Inferring gene regulatory networks from gene expression time series data is important for gaining insights into the complex processes of cell life. A popular approach is to infer Boolean networks. However, it is still a pressing open problem to infer accurate Boolean networks from experimental data that are typically short and noisy.

Results: To address the problem, we propose a Boolean network inference algorithm which is able to infer accurate Boolean network topology and dynamics from short and noisy time series data. The main idea is that, for each target gene, we use an And/Or tree ensemble algorithm to select prime implicants of which each is a conjunction of a set of input genes. The selected prime implicants are important features for predicting the states of the target gene. Using these important features we then infer the Boolean function of the target gene. Finally, the Boolean functions of all target genes are combined as a Boolean network. Using the data generated from artificial and real-world gene regulatory networks, we show that our algorithm can infer more accurate Boolean network topology and dynamics from short and noisy time series data than other algorithms. Our algorithm enables us to gain better insights into complex regulatory mechanisms of cell life.

Availability: Package ATEN is freely available at https://github.com/ningshi/ATEN **Contact:** s.he@cs.bham.ac.uk

Supplementary information: Supplementary data are available at Bioinformatics online.

1 Introduction

Gene regulatory networks are important to elucidate complex processes of cell life (Karlebach and Shamir, 2008; Chai *et al.*, 2014). A gene regulatory network is composed of interactions among proteins, genes and metabolites in living cells, and models the regulation of gene expression based on the relationships among genes and their products (de Jong, 2002; Hecker *et al.*, 2009; Saadatpour and Albert, 2013; Chai *et al.*, 2014). To infer gene regulatory networks, computational approaches such as Bayesian networks (Friedman *et al.*, 2000; Sanchez-Castillo *et al.*, 2017), ordinary differential equations (Bansal *et al.*, 2007)) and Boolean networks (Kauffman, 1969; Liang *et al.*, 1998; Saadatpour and Albert, 2013) have been proposed.

In this paper, we focus on Boolean networks. Although Boolean networks are limited as the state of gene expression level can only be described using two states, they can capture some fundamental characteristics of signalling and gene regulatory mechanisms. They have been widely used to reveal both the gene regulatory network topology (i.e. the interactions between genes) and dynamics (i.e. the regulatory rules) (Lähdesmäki *et al.*, 2003; Hecker *et al.*, 2009; Gates and Rocha, 2016).

Most Boolean network inference algorithms focus on inferring network topology (Liang *et al.*, 1998; Maucher *et al.*, 2011; Pirkl *et al.*, 2015). There are only a few algorithms that can infer both the Boolean network topology and its dynamics. For example, the Best-Fit (Lähdesmäki *et al.*, 2003) algorithm can find Boolean functions by solving the consistency problem (Akutsu, 1999). Barman and Kwon (2017) proposed a Boolean inference algorithm named MIBNI based on mutual information. The

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algorithm REACT (Vera-Licona *et al.*, 2014) uses Boolean polynomials to infer Boolean networks.

However, despite these advances, it is still challenging to infer accurate Boolean networks from experimental data, which is typically short and noisy (Bar-Joseph, 2004). To address this challenge, we propose an And/Or tree ensemble (ATEN) algorithm for inferring both the Boolean network topology and its dynamics. For each target gene, our ATEN algorithm uses an And/Or tree ensemble to select prime implicants, i.e., the conjunction (AND) of non-redundant input genes. These prime implicants are important features for predicting the states of the target gene. Using these important features, ATEN infers the Boolean function of the target gene. Finally, ATEN combines the Boolean functions of all target genes as a Boolean network.

The advantages of our ATEN algorithm are as follows. First, ATEN is efficient because And/Or trees provide an efficient representation for inferring prime implicants using binary time series data. Second, by using an ensemble algorithm, ATEN can better handle the "large p small n" problem (Genuer *et al.*, 2010), i.e., the number of input genes p is larger than the number of time points n, to select more reliable important features (Huynh-Thu *et al.*, 2010), i.e., prime implicants. Third, based on the selected features, our algorithm can infer a minimal Boolean function without redundant input genes, which results in a more accurate Boolean network.

To summarize, our main contributions are:

- We propose the first And/Or tree ensemble algorithm. Although And/Or trees have been widely used to search for solutions in combinatorial and artificial intelligence (Marinescu and Dechter, 2009), no And/Or tree ensemble algorithm exists to search for robust consensus solutions. We are the first to bridge the gap between ensemble learning and And/Or trees.
- 2. We apply our And/Or tree ensemble algorithm to select important prime implicants as features, which is different from most existing algorithms, e.g., GENIE3 (Huynh-Thu *et al.*, 2010) that select individual input genes for each target gene.
- 3. We validate ATEN on both artificial and real-world gene regulatory networks. Our experimental results show that ATEN compares favourably with existing algorithms in terms of prediction accuracy of network topology and dynamics, even when the gene expression time series data is short and noisy.

2 Methods

2.1 Preliminaries

2.1.1 Boolean network model

A Boolean network G(X, F) is a set of nodes $X = \{x_1, ..., x_n\}$ representing genes and a set of Boolean functions $F = \{f_1, ..., f_n\}$ describing the regulatory rules between genes. Each node (i.e., gene) x_i is a Boolean variable taking 1 or 0 to describe its state, where 1 represents that the gene is expressed and 0 represents that the gene is not expressed. The directed edges, or the interactions between the target gene and input genes are associated with the regulatory rule, i.e., the Boolean function. The Boolean function consists of three basic Boolean operators (i.e. \lor , \land and \neg) and Boolean variables. The Boolean function f_i determines the dynamical changes of the state of gene x_i over time: $x_i(t+1) = f_i(x_{i_1}(t), ..., x_{i_k}(t)), \forall t$, where $x_i(t+1)$ represents the state of gene x_i at time point t + 1, and $x_{i_k}(t)$ represents the state of the kth input gene of gene x_i at time point t. All genes update their states synchronously. For each gene in a Boolean network, the goal of the network inference problem is to identify the underlying Boolean function



Fig. 1. And/Or tree example. An example of a three-level And/Or tree with 5 leaves that represents a DNF formula $(x_1 \land x_2) \lor (x_3 \land \neg x_4 \land x_5)$.

associated with input genes from the binary time series data by taking into account every time point.

To represent a Boolean function associated with input genes, we can use a logical formula in disjunctive normal form (DNF). A DNF formula is a disjunction (OR) of one or more implicants. An implicant p is the conjunction of literals (i.e., Boolean variables or their negations). An implicant p is called a prime implicant if the deletion of any literal from p results in a non-implicant. For example, a Boolean function $(x_1 \wedge x_2) \lor (x_3 \wedge \neg x_4 \wedge x_5)$ for the target gene x_1 represents two prime implicants $(x_1 \wedge x_2)$ and $(x_3 \wedge \neg x_4 \wedge x_5)$, where x_1, x_2, x_3, x_4, x_5 are input genes. We are interested in obtaining a minimal Boolean function which includes a minimum set of prime implicants by eliminating the redundant prime implicants. For example, a Boolean function $(\neg x_1 \wedge x_2 \wedge x_3) \lor (\neg x_1 \wedge x_2 \wedge \neg x_3) \lor (x_1 \wedge \neg x_2 \wedge \neg x_3) \lor (x_1 \wedge \neg x_2 \wedge x_3)$ can be minimized to $(\neg x_1 \wedge x_2) \lor (x_1 \wedge \neg x_2)$.

2.1.2 And/Or Trees representation of logic functions

A logic function, or more specifically, a DNF formula can be represented as a three-level And/Or tree, which provides an efficient data structure to fit the binary time series data. In such a tree, an internal node represents a Boolean operator \lor or \land , and a leaf denotes a Boolean variable or its negation. The output of a Boolean function is determined by the valuation of the And/Or tree with an assignment of "TRUE" or "FALSE" to each of the leaves. In Figure 1, we show an example of a three-level And/Or tree l which is equivalent to the DNF formula $(x_1 \land x_2) \lor (x_3 \land \neg x_4 \land x_5)$.

We can represent a Boolean function in DNF as a three-level And/Or tree as follows:

- (First Level) The root is labeled by the Boolean operator \lor ;
- (Third Level) A leaf is labeled by a Boolean variable, or by a negation (i.e., a Boolean variable associated with ¬);

2.2 Algorithm

Algorithm 1: ATEN for Boolean network inference
Data : A binary time series dataset with n genes.
Result: A Boolean network.
foreach target gene x_i , $1 \le i \le n$ do Infer a set of prime implicants using Algorithms 3; Select a set of important prime implicants using Algorithm 4; Infer the final associated Boolean function using Algorithm 2. Combine all Boolean functions of all target genes as a Boolean
network;

2.2.1 Algorithm overview

To infer an accurate Boolean network from short and noisy gene expression time series data, our And/Or tree ensemble (ATEN) algorithm consists of three key steps as summarized in Algorithm 1. For each target gene, the first step is to infer a set of prime implicants based on an And/Or tree ensemble. Each tree in the ensemble represents a putative Boolean function of the target gene. The second step is to select a set of prime implicants as important features using a recursive feature reconstruction and elimination procedure (see Algorithm 4). The third step is to infer a minimal Boolean function without redundant prime implicants using the selected features (see Algorithm 2). The Boolean functions of all target genes are combined to represent the Boolean network.

In addition, ATEN can incorporate prior knowledge (e.g., the number of input genes for target genes), which reduces the search space and might improve inference accuracy (Studham *et al.*, 2014).

2.2.2 And/Or tree inference

We summarize the And/Or tree inference algorithm in Algorithm 2. Given binary time series data including N time points and n genes, ATEN infers an And/Or tree that best predicts the state of the target gene x_i , $1 \le i \le n$. The inference is achieved by searching the optimal input features (i.e., genes or prime implicants) and Boolean operators of the And/Or tree using a simulated annealing (SA) algorithm (van Laarhoven and Aaris, 1987).

Specifically, the And/Or tree of a target gene is initialized with an input feature (e.g., a random gene, or a random prime implicant, or known prime implicants). Then at each iteration k of the SA algorithm, a new tree l_k is proposed by randomly executing a permissible move based on the old tree l_{k-1} , e.g., adding a leaf, deleting a leaf, etc (for the fully permissible move set, see the Supplementary Data). The acceptance probability for the new tree l_k is determined by the misclassification rates of l_{k-1} and l_k and the temperature T specified in the SA cooling scheme, i.e., $Pr_{l_k} = min\{1, exp((E_{l_{k-1}} - E_{l_k})/T)\}$, where $E_{l_{k-1}}$ and E_{l_k} are the misclassification rates of l_{k-1} and l_k is calculated by

$$E_{l_k} = \frac{1}{N-1} \sum_{t=2}^{N} I(y_{l_k}(t-1) \neq x_i(t)),$$

where $I(\cdot)$ is an indicator function $I(\cdot) = \begin{cases} 1, & if y_{l_k}(t-1) \neq x_i(t) \\ 0, & if y_{l_k}(t-1) = x_i(t) \end{cases}$ and $y_{l_k}(t-1)$ is the output state predicated by l_k based on the states of the input genes at time point t-1, and $x_i(t)$ is the true state of the target gene at time point $t, 2 \leq t \leq N$. The acceptance probability indicates: 1) if l_k is better than l_{k-1} (i.e., $E_{l_k} < E_{l_{k-1}}$), then l_k is always accepted; 2) if l_k is not better than l_{k-1} (i.e., $E_{l_k} > E_{l_{k-1}}$), then l_k is accepted with a very small probability which gradually converges to zero as the temperature decreases. The maximum number of iterations is predefined to stop the searching scheme. The tree size which is defined as the number of input genes in the tree can be set according to prior knowledge, i.e., the maximum in-degree of the network, or determined experimentally or empirically. In addition, if the interactions as fixed prime implicants when inferring the tree.

Algorithm 2: And/Or tree inference for a target geneData: Binary time series data.Result: An And/Or tree l_k of the target gene.k = 0;Initialize an And/Or tree l_0 using an input feature;repeat $k \leftarrow k + 1$; $l_k \leftarrow$ Update l_{k-1} to propose a new tree;if l_k is rejected according to the probability Pr_{l_k} then $\lfloor l_k \leftarrow l_{k-1}$;

until k reaches the maximum iteration ;

The finally accepted And/Or tree may contain redundant regulatory interactions (i.e., prime implicants) between the target gene and input



Fig. 2. Illustration of bootstrap samples and the corresponding out-of-bag (oob) samples. Each column represents an expression vector $\mathbf{x}^{j}(t)$. Each row denotes an input feature (i.e., a gene or a prime implicant). For each target gene, we generate a set of pairs of a bootstrap and an oob sample. Bootstrap samples are used to infer ensembles of trees. Oob samples are used to compute the importances of prime implicants based on the tree ensemble.

genes that are unnecessary for predicting the state of the target gene. Thus we introduce a Boolean minimization method aimed at obtaining a minimal And/Or tree (i.e., a minimal DNF) based on the Quine-McCluskey algorithm (Quine, 1955; McCluskey, 1956), where the Quine-McCluskey algorithm tries to find essential prime implicants and other necessary prime implicants to simplify Boolean functions.

Algorithm 3: Compute the importances of prime implicants of a
target gene
Data : A binary time series dataset D.
Result: The prime implicants with their importances
Initialization : The number of bootstrap samples B;
Generate bootstrap samples S_b by drawing B samples ;
foreach S_b in $B, 1 \leq b \leq B$ do
$l_b \leftarrow$ Infer an And/Or tree using Algorithm 2;
$O_b \leftarrow \text{Generate an oob sample;}$
$PI \leftarrow \text{Extract all distinct prime implicants } p_i, i = 1, 2,;$
foreach $p_i \in PI$ do
foreach l_b do
$E_{l_b} \leftarrow \text{Compute the misclassification of } l_b \text{ using } O_b;$
$l_b^-/l_b^+ \leftarrow \text{Remove/Append } p_i \text{ from/to } l_b;$
$\begin{bmatrix} E_{l_b^-} / E_{l_b^+} \leftarrow \text{Compute the misclassification of } l_b^- / l_b^+ \text{ using} \\ O_b; \end{bmatrix}$
Determine the importance of p_i by $VI(p_i) =$
$\sum_{b=1}^{B} \left(\sum_{p_i \in l_b} \left(E_{l_b^-} - E_{l_b} \right) + \sum_{p_i \notin l_b} \left(E_{l_b} - E_{l_b^+} \right) \right).$

2.2.3 Prime implicant importance measure

We compute the importances of prime implicants as shown in Algorithm 3 based on logicFS (Ruczinski *et al.*, 2003; Schwender and Ickstadt, 2008). The main idea is to construct an And/Or tree ensemble to quantify how much a prime implicant improves the predictive accuracy of the state of the target gene. As shown in Figure 2, given a binary time series dataset D, for a target gene, we draw B pairs of a bootstrap sample S_b and an out-of-bag (oob) sample O_b , $1 \le b \le B$ for inferring ensembles of trees and computing the importances of prime implicants, respectively.

Formally, given J time series covering N time points each, the jth $(1 \leq j \leq J)$ time series can be presented as a matrix of states of all genes, denoted as $\mathbf{X}^j = (\mathbf{x}^j(1), \cdots, \mathbf{x}^j(t), \cdots, \mathbf{x}^j(N))$, where $\mathbf{x}^j(t) = (x_1^j(t), x_2^j(t), \cdots, x_n^j(t))^{\mathrm{T}}$ is a vector containing the states of all n genes at time point t. We then construct the binary time series dataset matrix D by concatenating the J time series, i.e.,

$$D = \{\mathbf{X}^1, \cdots, \mathbf{X}^j, \cdots, \mathbf{X}^J\}$$

We draw a bootstrap sample by random sampling D with replacement, which is done by randomly selecting a column from D. This sampling procedure stops when the the bootstrap samples S_b reaches the size of J * (N - 1). We also obtain a corresponding oob sample O_b , i.e., $O_b = \{\mathbf{x}^j(t) | \mathbf{x}^j(t) \in D, \mathbf{x}^j(t) \notin S_b, t \neq N\}$. Note that vectors $\mathbf{x}^j(N), \forall j$ are not included in both bootstrap samples and oob samples, because the true states of the target gene recorded in $\mathbf{x}^j(N + 1)$ are unknown for estimating the misclassification rate of an inferred tree.

We use the *B* bootstrap samples in S_b as inputs of Algorithm 2 to get ensembles of *B* And/Or trees. From the And/Or trees, we then extract all distinct prime implicants *PI*. For each prime implicant p_i in *PI*, we compute its importance based on p_i 's presence or absence over every l_b in the ensemble. If p_i is present in l_b , we compute the misclassification rate $E_{l_b^-}$ of the new tree l_b^- obtained by removing p_i from l_b . On the other hand, if p_i is absent in the l_b , we compute the misclassification rate $E_{l_b^+}$ of the new tree l_b^+ obtained by appending p_i to l_b as a prime implicant. In the end, the importance of p_i is determined by $VI(p_i) = \sum_{b=1}^{B} \left(\sum_{p_i \in l_b} (E_{l_b^-} - E_{l_b}) + \sum_{p_i \notin l_b} (E_{l_b} - E_{l_b^+}) \right)$.

2.2.4 Recursive feature reconstruction and elimination

We propose a recursive feature reconstruction and elimination (RFRE) procedure for selecting a set of important prime implicants as features, which will be used for inferring Boolean functions. The main idea is to recursively reconstruct the selected important prime implicants, and eliminate the non-important ones. We summarize RFRE in Algorithm 4.

Initially, we apply Algorithm 3 to a binary time series dataset matrix D containing J time series covering N time points each, which results in a set of prime implicants PI_0 with their importances. We then eliminate the least important prime implicants, i.e., prime implicants with negative importance and the 20% of prime implicants with the lowest importances.

Algorithm 4: RFRE for prime implicants selection
Data : A binary time series dataset D.
Result: A small set of prime implicants.
$PI_0 \leftarrow$ Apply Algorithm 3 to D and eliminate the non-important
prime implicants
$r \leftarrow 1;$
repeat
$D_{r-1} \leftarrow$ Update a dataset matrix based on PI_{r-1} ;
$PI_r \leftarrow$ Apply Algorithm 3 to D_{r-1} and eliminate the
non-important prime implicants;
$PI_{new} \leftarrow PI_r \setminus PI_{r-1};$
$PI_{old} \leftarrow PI_r \setminus PI_{new};$
$r \leftarrow r+1;$
until $VI(p_v) > VI(PI_w)$, $\forall p_v \in PI_{old}, \forall p_w \in PI_{new}$;

Then at each recursion, we first update the time series dataset matrix D_{r-1} based on the important prime implicants:

$$D_{r-1} = \{ \mathbf{P}_{r-1}^1, \cdots, \mathbf{P}_{r-1}^j, \cdots, \mathbf{P}_{r-1}^J \},\$$

where \mathbf{P}_{r-1}^{j} denotes the *j*th time series dataset matrix of all prime implicants, i.e., $\mathbf{P}_{r-1}^{j} = (\mathbf{p}_{r-1}^{j}(1), \cdots, \mathbf{p}_{r-1}^{j}(t), \cdots, \mathbf{p}_{r-1}^{J}(N))$. $\mathbf{p}_{r-1}^{j}(t)$ is a vector containing the states of all prime implicants in PI_{r-1} at time point *t*. We then apply Algorithm 3 to D_{r-1} to reconstruct the prime implicants. This step results in a set of important prime implicants, i.e., PI_r , which possibly contain some new ones (i.e., PI_{new}) that are reconstructed from input prime implicants.

The RFRE procedure stops when the newly reconstructed prime implicants are not important. Specifically, we compare $VI(p_v)$ to $VI(p_w)$, where $p_v \in PI_{old}$ and $PI_w \in PI_{new}$. If we cannot find



Fig. 3. Part of the topology of a single parasegment primordium network. The whole network is an interconnected network of four identical cells. Nodes located inside the dashed rectangle are in one cell. Nodes 16-21 are in the adjacent cells. The directed edges represent the existence of regulation without implying the activation or inhibition.

any new prime implicants (i.e., p_w) that are more important than the input prime implicants remained in PI_r (i.e. p_v), we terminate the recursion.

2.3 Datasets

2.3.1 Artificial network

We first validated the performance of ATEN by inferring three artificial Boolean networks generated by BoolNet (Müssel *et al.*, 2010), where three networks include 50 nodes, 100 nodes, and 150 nodes, respectively. The maximum in-degree of each network is 5. For each network we generated 12 datasets D_i , $1 \le i \le 12$ where each dataset includes 10 time series. Each time series in $D_i(i = 1, 2, 3)$, $D_i(i = 4, 5, 6)$, $D_i(i = 7, 8, 9)$ and $D_i(i = 10, 11, 12)$ has 5, 10, 15, 20 time points, respectively. Additionally, we added 1% and 5% noise to $D_i(i = 2, 5, 8, 11)$ and $D_i(i = 3, 6, 9, 12)$, respectively. The noise was introduced by randomly flipping the state of each node with the probability of 1% or 5%.

2.3.2 Real-world network

We also applied ATEN to infer a real-world gene regulatory network using experimentally-observed gene expression data. The network is derived from a well-studied Drosophila segment polarity gene regulatory network (Albert and Othmer, 2003) and modified by REACT (Vera-Licona *et al.*, 2014). It is considered as a single parasegment primordium of four identical cells (Albert and Othmer, 2003; Laubenbacher and Stigler, 2004). As shown in Figure 3 and Supplementary Data Table 12, we present part of the network topology and its dynamic model (i.e., Boolean functions), respectively. The network of one cell consists of 15 nodes and 6 extracellular nodes, where the 6 extracellular nodes are connected with other nodes (not shown in Figure 3) in the adjacent cells. In the experiment, the whole network of a single parasegment primordium which consists of 15*4=60 nodes was used for network inference.

For the dataset used for inference, we introduced three datasets that were used in REACT. The datasets were initialized using experimentally observed gene expression data (Albert and Othmer, 2003) and knockout perturbations. These three datasets included 0%, 1%, 5% data noise, respectively. Each dataset has 24 time series containing 202 time points in total. Moreover, we used the same initialization to generate 9 additional datasets D_i , $1 \le i \le 9$, where each dataset has 10 time series. Each time series in D_i (i = 1, 2, 3), D_i (i = 4, 5, 6) and D_i (i = 7, 8, 9) has 5, 10, 15 time points, respectively. We also added 1% and 5% noise into D_i (i = 2, 5, 8) and D_i (i = 3, 6, 9), respectively.

2.4 Computational experiments

We compared ATEN with the other three existing network inference algorithms, i.e., MIBNI (Barman and Kwon, 2017), Best-Fit (Lähdesmäki *et al.*, 2003) and REACT (Vera-Licona *et al.*, 2014). Because ATEN uses a

Table 1. ATEN inferred more accurate artificial network topology from short and noisy data. Experimental results of ATEN, MIBNI and Best-Fit for the networks with 100 nodes inferred from the datasets including 1% noise and 5% noise. The maximum in-degree of each target gene inferred by ATEN, MIBNI and Best-fit was limited to 8. The results of ATEN are presented using average and standard deviation values. The best result among three algorithms is highlighted in boldface. The symbol '-' indicates that the results of Best-Fit cannot be obtained due to the walltime limit (8 days).

Number of Time Points	Algorithm		Noise 1%		Noise 5%			
		Recall	FPR	F-score	Recall	FPR	F-score	
50	ATEN	0.898±0.010	0.009±0.001	$0.702{\pm}0.016$	0.827±0.018	$0.022{\pm}0.001$	0.468±0.012	
	MIBNI	0.758	0.071	0.209	0.758	0.071	0.209	
	Best-Fit	0.797	0.018	0.499	0.664	0.031	0.327	
100	ATEN	0.950±0.010	$0.007 {\pm} 0.001$	0.765±0.020	$0.922{\pm}0.017$	$0.016{\pm}0.002$	0.579±0.019	
	MIBNI	0.773	0.071	0.213	0.766	0.071	0.211	
	Best-Fit	0.906	0.027	0.458	0.781	0.046	0.293	
150	ATEN	0.953±0.010	$0.008 {\pm} 0.001$	0.755±0.018	$0.913 {\pm} 0.013$	$0.011 {\pm} 0.002$	0.667±0.016	
	MIBNI	0.758	0.071	0.209	0.766	0.071	0.211	
	Best-Fit	0.930	0.029	0.447	-	-	-	
200	ATEN	0.901±0.009	$0.007 {\pm} 0.001$	0.735±0.019	$0.881 {\pm} 0.015$	$0.013 {\pm} 0.001$	0.615±0.010	
	MIBNI	0.766	0.071	0.211	0.773	0.071	0.213	
	Best-Fit	-	-	-	-	-	-	

heuristic algorithm, we executed ATEN 30 times with B = 100 on every dataset. Due to the unavailable implementation of REACT, we adopted the results from the literature (i.e., Vera-Licona *et al.* (2014)) for comparison. We present the details of computing resources in the Supplementary Data.

For inferring the artificial network, we compared the performance of ATEN with that of Best-Fit and MIBNI. For inferring the real-world gene regulatory network, we compared ATEN with MIBNI, Best-Fit and REACT.

One important control parameter of ATEN is the upper limit on tree size, i.e., the maximum number of input genes of a target gene. This parameter essentially defines the search space of the problem, which affects not only the prediction accuracy but also the computational time of ATEN. However, finding a suitable value of this parameter is challenging not only for ATEN but also for other algorithms (Barman and Kwon, 2017). To determine the value of this parameter, we executed experiments on an artificial network with 150 nodes (See Supplementary Data). Based on the experimental results, we set the upper limit on tree size to 8. For fair comparison, MIBNI and Best-Fit were limited to infer up to 8 input genes for each target gene. Additionally, we also presented the results with known maximum number of input genes of the artificial and real-world networks in the Supplementary Data.

2.5 Performance matrices

To quantify the quality of the inferred network topology, we used the performance metrics used in Maucher *et al.* (2011), namely, Recall= $\frac{TP}{TP+FN}$, False Positive Rate (FPR)= $\frac{FP}{FP+TN}$ and F-score= $\frac{2TP}{2TP+FP+FN}$, where TP denotes the number of inferred interactions that are present in the ground truth network; FP denotes the number of inferred interactions that are absent in the ground truth network; TN denotes the number of absent interactions in the inferred network that are also absent in the ground truth network; FN denotes the number of absent in the ground truth network that are absent in the ground truth network that are absent in the ground truth network.

To evaluate the quality of the dynamic model of the inferred networks, we used 6 steady states that have been investigated in existing literature as detailed in (Vera-Licona *et al.*, 2014) and Supplementary Data Table 13. We checked whether the Boolean functions inferred by each algorithm can retrieve these steady states.

3 Results

3.1 Performance on artificial network

We summarize experimental results from ATEN, Best-Fit and MIBNI on the artificial networks with 100 nodes inferred from noisy data (with 1% and 5% noise) where we set the upper limit on tree size to 8 in Table 1 (The results from the noise-free data are detailed in Supplementary Data Table 3.). We summarize the results of inferring the networks with 50 and 150 nodes without known maximum in-degree in Supplementary Data Tables 1-2 and 4-5. In addition, the results of inferring all artificial networks using known maximum in-degree are detailed in Supplementary Data Tables 6-11.

From Table 1, we can see that ATEN always obtained the best Recall, FPR and F-score when the datasets are noisy (i.e., 1% and 5% noise). We can also see that since Best-Fit uses exhaustive search, it cannot successfully infer the networks from the datasets including 200 time points with 1% and 5% noise within the walltime. When the data is noise-free, from Supplementary Data Table 3, Best-Fit outperformed than other algorithms. For the networks consisting of 50 and 150 nodes, from Supplementary Data Tables 1-2 and 4-5, we can observe that ATEN inferred the best results from noisy data and Best-Fit obtained the best results from noise-free data.

3.2 Performance on real-world network

We used the real-world gene regulatory network to evaluate ATEN's performance of inferring network topology and its dynamic model (i.e., Boolean functions), in comparison with other three algorithms (i.e., MIBNI, Best-Fit and REACT).

3.2.1 Inference of network topology

Overall, ATEN outperformed the other three algorithms for inferring the network topology from short and noisy data. We present their performance among the datasets including 1% and 5% noise with setting the maximum in-degree of target genes to 8 in Figure 4. (The results from the noise-free data are detailed in Supplementary Data Table 14.) We also discuss the experimental results where we set the upper limit on tree size to 4, the exact maximum in-degree of the network.

In Figure 4, the average and standard deviation values of Recall and FPR obtained from ATEN were used for comparison. From Figure 4, among all these four algorithms ATEN always obtained the best FPR and F-score values. Compared with the performance of MIBNI, it can be seen

Table 2. ATEN inferred more accurate real-world dynamic model from short and noisy data. The maximum in-degree of each target gene inferred by ATEN, MIBNI and Best-fit was limited to 8. The numbers indicate the number of steady states that was successfully retrieved. The best result among three algorithms is highlighted in boldface. Note that the experimental results of REACT was collected from Vera-Licona et al. (2014) and the symbol '*' indicates that the corresponding results cannot be collected.

Number of Time Points	50			100			150			202		
Algorithms	Noise 0%	1%	5%									
ATEN	5	5	3	4	5	5	4	4	6	4	4	5
MIBNI	0	0	0	0	0	0	0	0	0	0	0	0
Best-Fit	3	2	2	4	1	1	5	2	2	5	2	2
REACT	*	*	*	*	*	*	*	*	*	5	3	5

that ATEN was significantly better. With respect to the network inferred from the dataset including 50 time points and 1% noise, ATEN achieved similar experimental results with Best-Fit. However, when the datasets including 5% noise, we can find that ATEN achieved significantly better recall, FPR and F-score values than Best-Fit. Compared with the best recall and FPR values of REACT, ATEN achieved similar but more stable results. Moreover, from Figure 4, it can be concluded that ATEN outperformed the other three algorithms when the data was shorter (i.e., 50 time points) with higher noise level (i.e., 5% noise). When we inferred the network from noise-free data (see Supplementary Data Table 14), Best-Fit achieved better results than other algorithms.

3.2.2 Inference of dynamic model

The overall performance of ATEN for predicting the dynamic model was better than MIBNI, Best-Fit and similar to REACT. Table 2 presents the number of steady states that can be retrieved by ATEN and other algorithms when the maximum in-degree of inferred network is unknown.

From Table 2, We can observe that ATEN always retrieved at least 50% steady states even when the input data was short and noisy (i.e., 50 time points and 5% noise). The MIBNI did not find any steady states, since MIBNI can infer only conjunctive or disjunctive Boolean functions. Compared with Best-Fit and MIBNI, we can see that ATEN was significantly better than both the compared algorithms among all datasets. Compared with REACT, ATEN correctly retrieved the same number of steady states. The experimental results also show that ATEN was more robust to different levels of noise and different numbers of time points for inferring the network dynamic model.

4 Discussion

Inferring topological structure and network dynamics of gene regulatory networks from gene expression time series data is a major challenge in systems biology. To tackle this challenge, we propose ATEN, which is the first algorithm that combines ensemble learning and And/Or trees.

Our experimental results (Tables 1 and 2, Supplementary Data Tables 2, 5, 7, 9, 11 16 and 17) show that, when the data was noisy, ATEN performed better than the other three algorithms in terms of the prediction accuracy. When the data was noise-free, Best-Fit achieved the best results. We therefore recommend using ATEN for inferring Boolean networks from noisy data, while Best-Fit for noise-free data.

We used Simulated Annealing algorithm to infer And/Or trees because of its simplicity and good search performance. Any other heuristic algorithms such as Genetic Algorithms could be suitable for this task. It would be interesting to investigate whether other heuristic algorithms could improve the performance. Another reason that we used heuristic algorithm is because it is faster than exhaustive search method (e.g. Best-Fit). However it cannot guarantee that the inferred network is optimal. To find the optimal solution, it is possible to introduce mathematical programming (Knijnenburg *et al.*, 2016) into ATEN. ATEN has been evaluated on Boolean networks with synchronous updating scheme due to its computational efficiency. However, asynchronous updates is more biological plausible although the inference is more difficult. It will be our future work to utilize Boolean state space scoring function (Lim *et al.*, 2016) for inferring asynchronous Boolean networks.

Another interesting direction is to extend ATEN to infer Probabilistic Boolean networks (PBNs) (Shmulevich *et al.*, 2002a,b) which improves Boolean networks for handling noise and uncertainty. The PBN allows each target gene to be associated with multiple Boolean functions with corresponding selection probabilities. We expect to extend our ATEN algorithm to infer probabilistic Boolean networks from the gene expression time series data in the future.

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Fig. 4. ATEN inferred more accurate real-world network topology from short and noisy data. Experimental results of ATEN, MIBNI, Best-Fit and REACT for the inferred network from the datasets including 1% noise and 5% noise. The maximum in-degree of each target gene inferred by ATEN, MIBNI and Best-Fit was limited to 8. The results of ATEN are presented using average and standard deviation values. The experimental results of REACT, i.e., the maximum and minimum Recall and FPR values were collected from the literature (i.e., Vera-Licona et al. (2014)), and the F-score values cannot be collected.

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