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2 **A Reproducibility Analysis-based Statistical Framework for Residue-Residue**

3 **Evolutionary Coupling Detection**

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Abstract

25 Direct coupling analysis (DCA) has been widely used to infer evolutionary coupled residue
 26 pairs from the multiple sequence alignment (MSA) of homologous sequences. However,
 27 effectively selecting residue pairs with significant evolutionary couplings according to the
 28 result of DCA is a non-trivial task. In this study, we developed a general statistical
 29 framework for significant evolutionary coupling detection, referred to as IDR-DCA, which
 30 is based on reproducibility analysis of the coupling scores obtained from DCA on manually
 31 created MSA replicates. IDR-DCA was applied to select residue pairs for contact
 32 prediction for monomeric proteins, protein-protein interactions and monomeric RNAs, in
 33 which three different versions of DCA were applied. We demonstrated that with the
 34 application of IDR-DCA, the residue pairs selected using a universal threshold always
 35 yielded stable performance for contact prediction. Comparing with the application of
 36 carefully tuned coupling score cutoffs, IDR-DCA always showed better performance. The
 37 robustness of IDR-DCA was also supported through the MSA down-sampling analysis.
 38 We further demonstrated the effectiveness of applying constraints obtained from residue
 39 pairs selected by IDR-DCA to assist RNA secondary structure prediction.

40 **Key words:** direct coupling analysis, quality control, statistical methods, contact prediction

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45 Introduction

46 Contacting residues in monomeric proteins/RNAs or between interacting
 47 proteins/RNAs often show covariance in the process of evolution to maintain
 48 the architectures and the interactions of these macromolecules, which allows
 49 us to infer the intra- or inter-protein/RNA residue-residue contacts through
 50 co-evolutionary analysis [1]. Direct coupling analysis (DCA) is a class of widely
 51 used methods for co-evolutionary analysis, which quantifies the direct coupling
 52 strength between two residue positions of a biological sequence through
 53 global statistical inference using maximum entropy models learned from large
 54 alignments of homologous sequences [2]. Comparing with local statistical
 55 methods like mutual information (MI) and correlated mutation analysis, DCA is
 56 able to disentangle direct couplings from indirect transitive correlations, thus
 57 showing much better performance in predicting residue-residue contacts [3,4].
 58 A wide variety of algorithms at different levels of approximation for
 59 implementing DCA have been developed in recent years, with the focus being
 60 on improving the accuracy of DCA and increasing the computational efficiency.
 61 The developed algorithms for DCA include message passing DCA (mpDCA)
 62 [3], mean-field DCA (mfDCA) [4] and pseudo-likelihood maximization DCA
 63 (plmDCA) [2]. Among these developed algorithms, PlmDCA is currently the
 64 most popular algorithm for implementing DCA because of its high accuracy
 65 and moderate computational cost, which has been successfully applied to
 66 directly acquire contact constraints to assist the prediction of protein/RNA

67 structures, interactions and dynamics [5–14], or been used to provide major
68 feature components for deep learning-based contact/distance prediction
69 methods [15–19].

70 Comparing with so many efforts made on improving DCA algorithms and
71 applying DCA to obtain structural information from sequence data, relatively
72 less attention has been made on how to quantify the number of residue pairs
73 with significant evolutionary couplings and select the predictive residue pairs
74 from the result of DCA. Generally, residue pairs with higher coupling scores
75 obtained from DCA tend to have higher probabilities to form contacts.
76 Therefore, in most previous studies, often a certain number (e.g. top 10 or top
77 $L/5$, L as the sequence length) of residue pairs with the highest coupling
78 scores were selected for contact prediction, or a coupling score cutoff was set
79 empirically to select residue pairs with coupling scores higher than the cutoff.
80 However, both the number of predictive residue pairs and the coupling score
81 values are influenced by many factors including the number and the length of
82 the homologous sequences forming the MSA, the detailed settings of the DCA
83 algorithm, the functional characteristics of the macromolecule [6,7]. Therefore,
84 neither applying a “number” cutoff nor a “coupling score” cutoff is an ideal
85 protocol for selecting predictive residue pairs from the result of DCA. In a
86 previous work, for predicting residue-residue contacts between interacting
87 proteins, Ovchinnikov *et al.* first rescaled the raw coupling scores from Gremlin
88 (a software for implementing plmDCA) with an empirical model to consider the

89 influence of the number and the length of the homologous sequences forming
90 the MSA on the coupling scores, then determined an optimal score cutoff
91 based on the inter-protein residue-residue contacts in the crystal structure of
92 the 50S ribosome complex [6]. For the same purpose, Hopf *et al.* did
93 something similar but rescaled the coupling scores from EVcouplings (another
94 software for implementing plmDCA) with a different empirical model [7]. Both
95 the two methods achieve success in selecting inter-protein residue pairs for
96 contact prediction. However, since the parameters of these empirical models
97 were tuned on only a limited number of cases, whether they are applicable for
98 more general cases is questionable. Besides, Xu et al. proposed a statistical
99 approach referred to as inverse finite-size scaling (IFSS) to estimate the
100 significance of DCA results, which was later applied in epistasis detection of
101 microbial genomes [20–22]. However, to the best of our knowledge, the
102 effectiveness of this approach has never been shown in selecting evolutionary
103 coupled residue pairs. The lack of a general approach for detecting significant
104 evolutionary couplings from the result of DCA limits the appropriate application
105 of this method. For example, when applying DCA to infer inter-protein residue
106 pairs with significant evolutionary couplings to assist the protein-protein
107 interaction prediction at large scale, without appropriately measuring the
108 coupling significance, we may introduce false positive couplings or miss
109 significant couplings.

110 In this study, we develop a general statistical framework for significant

111 residue-residue coupling detection. The development of this statistical
 112 framework is inspired by the quality control protocols in functional genomic
 113 experiments, in which often reproducible signals in multiple experimental
 114 replicates are considered as the genuine functional signal [23,24]. Here, given
 115 an MSA of homologous sequences, two MSA (pseudo) replicates are created
 116 by randomly assigning the sequences in the MSA into two groups. DCA is then
 117 performed on both the original full MSA and the two MSA replicates. We
 118 assume that the significant couplings are reproducible from DCA on the two
 119 MSA replicates. Therefore, we perform reproducibility analysis on the coupling
 120 scores obtained from DCA on the two MSA replicates, from which we assign
 121 each residue pair an irreproducible discovery rate (IDR) calculated with the
 122 Gaussian copula mixture modelling described in Li *et al.* [25], with the lower
 123 the IDR, the more reproducible the residue-residue coupling. Then, we create
 124 an IDR signal profile for the residue pairs under consideration, which
 125 represents the IDR variation with the ranking of the residue pairs sorted
 126 descendingly according to the coupling scores obtained from DCA on the full
 127 MSA. The residue pairs before the IDR signal profile reaching a certain
 128 threshold are considered to be with significant evolutionary couplings. This
 129 statistical framework, referred to as IDR-DCA, was applied to select residue
 130 pairs for contact prediction for 150 monomeric proteins, 30 protein-protein
 131 interactions and 36 monomeric RNAs, in which the DCA were performed with
 132 three different versions of DCA including EVcouplings [26], Gremlin [5] and

CCMpred [27]. The result shows that IDR-DCA can effectively select evolutionary coupled residue pairs with a universal threshold (IDR cutoff=0.1), for that the numbers of residue pairs selected by IDR-DCA vary dramatically for cases across the three datasets, but the accuracies of the selected residue pairs for contact prediction are kept stable. Comparing with the application of the DCA tool specific coupling score cutoffs carefully tuned on each dataset to reproduce the overall accuracies of the residue pairs selected by IDR-DCA, IDR-DCA is always able to select more residue pairs, and provide effective contact predictions for more cases. We further evaluated the robustness of IDR-DCA through the MSA downsampling analysis. The result shows that as the numbers of homologous sequences forming the MSAs getting smaller and smaller, generally IDR-DCA would select fewer and fewer residue pairs to keep the accuracy of the selection, but the advantage of IDR-DCA over the application of coupling score cutoffs are always kept at different levels of the MSA down-sampling. Therefore, IDR-DCA provides an effective and robust statistical framework for selecting evolutionary coupled residue pairs.

Results

1. Overview of IDR-DCA

IDR-DCA includes three major stages: creating pseudo-replicates, performing reproducibility analysis and detecting significant couplings, which are described in detail in the following subsections (See Figure 1).

1.1 Creating pseudo-replicates

As it is shown in Figure 1A, given an MSA of homologous sequences, we first perform DCA on the full MSA, from which we can obtain a coupling score x_i for each residue pair. The residue pairs are then sorted descendingly according to the coupling scores, in which the residue pairs with higher rankings (n_i) are more likely to be with significant evolutionary couplings. After that, the aligned sequences in the MSA are randomly grouped into two subsets without realignment, and we then perform DCA on the two MSA subsets separately, from which we can obtain a coupling score tuple $(x_{i,1}, x_{i,2})$ and a ranking tuple $(n_{i,1}, n_{i,2})$ for each residue pair, with $x_{i,1}$, $x_{i,2}$ representing the coupling scores for the residue pair i from the DCA on the two MSA subsets, and $n_{i,1}$, $n_{i,2}$ representing the rankings of residue pair i sorted according to the coupling scores descendingly. Since the two MSA subsets can be considered as (pseudo) biological replicates, the significant couplings are expected to be reproducible from the DCA on the two MSA replicates. Therefore, we perform reproducibility analysis on the coupling scores obtained from the replicated DCA to evaluate the reproducibility of each residue-residue coupling. It should be noted that if the provided MSA contains a large number of redundant sequences (including extremely similar sequences), insignificant couplings may also show a certain level of reproducibility. To avoid reproducible couplings caused by the issue of sequence redundancy, redundant sequences in the MSA should be filtered.

1.2 Performing reproducibility analysis

177 Since the scale and the distribution of the coupling scores obtained from
178 DCA are case dependent, it is not appropriate to measure the reproducibility of
179 the residue-residue coupling through the direct comparison of the coupling
180 score values from the two MSA replicates. In this study, we measure the
181 reproducibility of each residue-residue coupling through calculating the
182 irreproducible discovery rate (IDR) for each residue-residue coupling with the
183 Gaussian copula mixture modelling described in Li *et al* [25], in which the
184 rankings rather than the coupling score values from the two MSA replicates
185 were employed in the statistical modeling. Specifically, we assume that there
186 are two types of residue pairs (i.e. evolutionary coupled residue pairs and
187 evolutionary uncoupled residue pairs), for which the observed coupling score
188 tuples $(x_{i,1}, x_{i,2})$ are generated by a latent variable tuple (unobserved) (z_1, z_2)
189 following the Gaussian mixture distribution $(\pi_0 h_0(z_1, z_2) + \pi_1 h_1(z_1, z_2))$, with
190 $h_0 \sim N\left(\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}\right)$ and $h_1 \sim N\left(\begin{pmatrix} \mu_1 \\ \mu_1 \end{pmatrix}, \begin{pmatrix} \sigma_1^2 & \rho_1 \sigma_1^2 \\ \rho_1 \sigma_1^2 & \sigma_1^2 \end{pmatrix}\right)$ ($\mu_1 > 0$, $\rho_1 > 0$) (1).
191 Where h_0 and h_1 correspond to the uncoupling component and the coupling
192 component respectively, and π_0 and π_1 are the corresponding weights of the
193 two components. Since evolutionary coupled residue pairs generally have
194 higher and more reproducible coupling scores, we require ($\mu_1 > 0$, $\rho_1 > 0$).
195 Because (z_1, z_2) are not observable, and the relationship between (z_1, z_2)
196 and the observable coupling score tuples $(x_{i,1}, x_{i,2})$ is unknown, the
197 association parameters $\theta = (\pi_1, \mu_1, \sigma_1^2, \rho_1)$ of the Gaussian mixture model are

198 determined through maximizing the likelihood function of corresponding copula
199 mixture model:

$$200 \quad L(\theta) = \prod_{i=1}^N [\pi_0 h_0(G^{-1}(u_{i,1}), G^{-1}(u_{i,2})) + \pi_1 h_1(G^{-1}(u_{i,1}), G^{-1}(u_{i,2}))] \quad (2).$$

201 Where $(u_{i,1}, u_{i,2}) = \left(n_{i,1}/N, n_{i,2}/N \right)$ is the normalized ranking tuple of residue

202 pair i , with $n_{i,1}, n_{i,2}$ corresponding to the rankings of residue pair i according

203 to the coupling scores from replicated DCA, and N representing the total

204 number of residue pairs; $G(z_*) = \frac{\pi_1}{\sigma_1} \Phi\left(\frac{z_* - \mu_1}{\sigma_1}\right) + \pi_0 \Phi(z_*)$ is the cumulative

205 marginal distribution of z_1 and z_2 , with z_* representing either z_1 or z_2 , and

206 Φ representing the standard normal cumulative distribution function. As we

207 can see from Equation (2) that only the rankings obtained from the two MSA

208 replicates are employed in the parameter determination.

209 Given a set of parameters θ , the probability that a residue pair with the

210 normalized ranking tuple $(u_{i,1}, u_{i,2})$ being an evolutionary uncoupled residue

211 pair (local IDR) can be computed as:

$$212 \quad \text{idr}(u_{i,1}, u_{i,2}) = \frac{\pi_0 h_0(G^{-1}(u_{i,1}), G^{-1}(u_{i,2}))}{\sum_{k=0,1} \pi_k h_k(G^{-1}(u_{i,1}), G^{-1}(u_{i,2}))} \quad (3).$$

213 The local IDR are then converted to (global) IDR for the multiple hypothesis

214 correction. The IDR of each residue pair represents the reproducibility of the

215 corresponding residue-residue coupling, with the lower the IDR value, the

216 higher the reproducibility (See Figure 1B).

217 1.3. Detecting significant couplings

218 The rankings (n_i) and the reproducibilities (IDRs) of residue-residue

219 couplings are unified for the significant coupling detection. Specifically, we
 220 build an IDR signal profile for all residue pairs under consideration, which
 221 represents the IDR variation with the ranking of the residue pairs sorted
 222 descendingly according the coupling scores obtained from DCA on the full
 223 MSA. Generally, the IDR of each residue-residue coupling increases
 224 ($-\log_{10}(\text{IDR}) \downarrow$) with fluctuation when its ranking goes down. After smoothing
 225 the IDR signal profile using a moving average filter with a window size 5, the
 226 residue pairs before the IDR signal reaching a specified cutoff are considered
 227 to be with significant evolutionary couplings (See Figure 1C).

228 2. Detecting significant evolutionary couplings with variable IDR cutoffs

229 IDR-DCA was used to detect intra-protein residue-residue couplings for the
 230 150 monomeric proteins in the original PSICOV contact prediction dataset [28],
 231 inter-protein residue-residue couplings for 30 protein-protein interactions from
 232 Ovchinnikov *et al.* [6], and intra-RNA residue-residue couplings for 36
 233 monomeric RNAs from Pucci *et al.* [13], in which the DCA were performed with
 234 three widely used plmDCA-based DCA software including EVcouplings [26],
 235 Gremlin [5] and CCMpred [27]. We first applied variable IDR cutoffs to select
 236 evolutionary coupled residue pairs. The percentage of contacting residue pairs
 237 in the selected residue pairs was used to evaluate the accuracy of the
 238 selection. Two intra-protein residues were considered to be in contact if their
 239 C β -C β distance (C α - C α distance in the case of glycine) is smaller than 8Å.
 240 For the inter-protein residues, the distance cutoff was relaxed to 12 Å

241 considering that the inter-protein residues have much lower contact probability
242 than the intra-protein residues. For the intra-RNA residues, a contact was
243 defined if their C1'-C1' distance is smaller than 12 Å. In Figure 2A-2C, we
244 show the overall accuracies of the selected residue pairs from each dataset
245 with the application of variable IDR cutoffs. As we can see from Figure 2A-2C
246 that independent on the DCA tools, for all the three datasets, the accuracies
247 drop at a relative slow speed when increasing IDR cutoff until reaching 0.1,
248 and after that the accuracies drop dramatically. Therefore, 0.1 can be
249 considered as a natural IDR cutoff for selecting residue pairs for contact
250 prediction when using the IDR-DCA statistical framework.

251 For the purpose of comparison, we also selected residue pairs based on the
252 coupling score values. In Figure 2D-2F, we show the overall accuracies of the
253 residue pairs selected from each dataset with the application of variable
254 coupling score cutoffs. As we can see from Figure 2D-2F, the accuracy of the
255 selected residue pairs varies with the choice of the coupling score cutoff in
256 DCA tool specific and dataset dependent ways. Therefore, a universal
257 coupling score cutoff is not applicable for selecting residue pairs for contact
258 prediction. For each dataset, we can set empirical DCA tool specific coupling
259 score cutoffs for the residue pair selection, with which the selected residue
260 pairs reproduce the accuracies of the residue pairs selected by IDR-DCA with
261 0.1 as the IDR cutoff. Specifically, for the monomeric protein dataset, the
262 coupling score cutoffs for EVcouplings, Gremlin and CCMpred were set as

0.42, 0.29 and 0.73; for the protein-protein interaction dataset, the coupling score cutoffs were set as 0.16, 0.09 and 0.24; and for the monomeric RNA dataset, the coupling score cutoffs were set as 0.29, 0.30 and 0.41. The dramatic variations of the coupling scores cutoffs between different DCA tools and different datasets show that the coupling score is not a good metric for the predictive residue pair selection.

It is easy to explain that the obtained coupling score cutoffs are tool dependent. Since all the three versions of DCA use some sort of regularizations to avoid the model overfitting, if the parameters of the regularizations are set differently, or the regularizations are done in different ways, the scales of the obtained coupling score values will vary. This is also the reason that the standard practice in the DCA application relies more on the order of the prediction than numeric values of the coupling scores. Besides, it is also reasonable that different datasets show different scales of coupling scores, since the different types of biophysical interactions can have different strengths. For example, the intra-protein residue-residue interactions are generally stronger and more conserved than the inter-protein residue-residue interactions, and may also show different evolutionary characteristics from the RNA residue-residue interactions.

3. The performance of IDR-DCA with a universal IDR cutoff (0.1) on evolutionary coupled residue pair selection

We analyzed the performance of IDR-DCA on selecting evolutionary

285 coupled residue pairs with 0.1 as the IDR cutoff. In Figure 3A-3C, we show the
 286 accuracies, the numbers and the corresponding coupling score cutoffs (i.e. the
 287 smallest coupling score) of the selected residue pairs for each case in the
 288 three datasets. As we can see from Figure 3A-3C, the selected residue pairs
 289 yield quite stable accuracies across cases in the three datasets independent
 290 on the DCA tools (e.g. for most of the cases, the accuracies of selected
 291 residue pairs are higher than 50%), although the numbers of the selected
 292 residue pairs vary dramatically. We can also see that the corresponding
 293 coupling score cutoffs of the selected residue pairs vary dramatically not only
 294 between DCA tools, but also across cases in the three datasets. This further
 295 supports that it is not appropriate to apply a universal coupling score cutoff to
 296 select residue pairs for contact prediction.

297 We further analyzed the distance distribution of non-contacting intra-protein
 298 residue pairs ($C\beta - C\beta$ distance $\geq 8 \text{ \AA}$) selected by IDR-DCA from the
 299 monomeric protein dataset. The analysis was focused on the intra-protein
 300 residue pairs for which have the largest sample size. We found that the
 301 distances of most of the non-contacting residue pairs selected by IDR-DCA are
 302 just slightly larger than 8 \AA (e.g. $< 12 \text{ \AA}$), as it is shown in Figure S1A.
 303 Therefore, we suspect that many of these “non-contacting” residue pairs by
 304 definition may also be “truly” evolutionary coupled. We also noticed a tiny
 305 fraction of the selected residue pairs are in long distance (e.g. $\geq 12 \text{ \AA}$) in the
 306 crystal structure. These residue pairs can be evolutionary coupled with the

307 long distances caused by protein conformational changes, as it is shown by
308 Anishchenko et al., in which they found that most of the evolutionary coupled
309 residue pairs not in repeat proteins are actually in spatial proximity in at least
310 one biologically relevant conformation [11]. Besides, the alignment errors in
311 MSA and the approximations made in DCA can also be responsible for these
312 exceptions.

313 We also noticed that for several cases in the protein-protein interaction
314 dataset and the monomeric RNA dataset, IDR-DCA was not able to find any
315 evolutionary coupled residue pairs. The scatter plot of the coupling scores of
316 all residue pairs for these cases is shown in Figure S1B, in which the
317 contacting residue pairs are colored red, and the non-contacting residue pairs
318 are colored black. As we can see from the plot, for all the cases, very few
319 top-ranked residue pairs based the coupling scores from DCA are in contacts
320 in the 3D crystal structure. This means that the DCA on these cases failed to
321 correctly model the residue-residue couplings, which might be caused by the
322 lack of effective sequences in their MSAs.

323 Therefore, it is encouraging that IDR-DCA can avoid selecting false positive
324 residue pairs from these cases. This phenomenon did not happen to our
325 monomeric protein dataset, for the monomeric proteins used in our study are
326 all single domain proteins with large number of homologous sequences in their
327 MSAs, thus the DCA on these cases can always successfully identify a certain
328 number of evolutionary coupled residue pairs.

329 4. The performance comparison between the application of IDR-DCA and 330 coupling score cutoffs on evolutionary coupled residue pair selection

331 We compared the performance of IDR-DCA on evolutionary coupled residue
332 pair selection with the application of the DCA tool specific coupling score
333 cutoffs tuned on each dataset. As we have described in section 2, the coupling
334 score cutoffs were determined to reproduce the accuracies of the residue pairs
335 selected by IDR-DCA. As we can see from Figure 4A-4C, for all the three
336 datasets, IDR-DCA with a universal IDR cutoff (0.1) is always able to select
337 more residue pairs than the application of the carefully tuned DCA tool specific
338 coupling score cutoffs, although the accuracies of the selected residue pairs
339 are almost the same.

340 Besides, IDR-DCA also shows a more stable performance across cases in
341 each dataset. For example, for most of the cases, the numbers of residue pairs
342 selected by IDR-DCA are very similar between different DCA tools, but the
343 numbers of residue pairs selected by applying the coupling score cutoffs are
344 highly dependent on the choice of the DCA tools (See Figure S2). Since the
345 differences between the three DCA tools are only on the detailed settings of
346 the plmDCA algorithm (e.g. the initial values for the optimization, the criterion
347 for the convergence, the ways of regularizations, etc.), DCA implemented with
348 the three DCA tools on the same MSA should provide similar number of
349 evolutionary coupled residue pairs.

350 An effective contact prediction should provide enough residue pairs above a

certain level of accuracy to assist the structure prediction. Here, as rules of thumb, for monomeric proteins or RNAs, we defined a prediction providing not fewer than $L/5$ (L as the sequence length) residue pairs with an accuracy not lower than 50% as an effective contact prediction; for protein-protein interactions, an effective contact prediction was defined if it can provide at least one residue pairs with an accuracy not lower than 50%, considering even one inter-protein residue contact constraint can significantly reduce the configuration space of the protein-protein interactions. It should be noted that the “effective contact prediction” defined here is only to make performance comparison between the application of the universal IDR cutoff and the variable coupling score cutoffs quantitatively, thus other reasonable criteria can also be used in the analysis. In Figure 4D-4F, we show the comparison of the numbers of cases with effective contact predictions provided by applying IDR-DCA and by applying the coupling score cutoffs from the three datasets respectively. As we can see that IDR-DCA is always able to provide effective contact predictions for much more cases than the application of the coupling score cutoffs. Besides, we can also see that the performance gap for the protein-protein interaction dataset is much larger than those for the monomeric protein dataset and the monomeric RNA dataset. This is mainly because the coupling scales of DCA methods are also highly dependent on the sequence length. For the monomeric protein and monomeric RNA dataset, the variations of the sequence lengths (51~267 and 24~492) are significantly smaller than

373 that for the protein-protein interaction dataset (181~1453).

374 5. Evaluating the robustness of IDR-DCA through the MSA downsampling 375 analysis

376 We further evaluated the robustness of IDR-DCA through the MSA
377 down-sampling analysis on the monomeric protein dataset. Specifically, for
378 each protein in monomeric protein dataset, $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{8}$ and $\frac{1}{16}$ of sequences in
379 the original MSA were randomly selected to form the MSAs with different
380 levels of downsampling, and then we applied IDR-DCA on the downsampled
381 MSAs with 0.1 as the IDR cutoff to select evolutionary coupled residue pairs.
382 EVcouplings, Gremlin and CCMpred were still applied respectively to perform
383 the DCA.

384 In Figure 5A-5C, we show the accuracies, the numbers of residue pairs
385 selected by IDR-DCA for each case in the monomeric protein dataset with the
386 application of the three tools for DCA respectively. As we can see from the
387 Figure 5A-5C, as the size of MSA getting smaller and smaller, the numbers of
388 the selected residue pairs are also getting smaller and smaller, however, the
389 accuracies of the selected residue pairs for contact prediction are kept stable
390 (See Figure S3 for an example). Since DCA on MSA with fewer sequences
391 tends to have lower statistical power to accurately model the residue-residue
392 couplings, it is reasonable that IDR-DCA selected fewer residue pairs as we
393 kept downsampling the MSA.

394 For the purpose of comparison, we also applied the previous determined

395 coupling score cutoffs to select residue pairs according to the coupling scores
 396 obtained from DCA on the MSA with different levels of downsampling (See
 397 Figure S4). In Figure 6A-6C, we show the comparison of the numbers and the
 398 accuracies of the residue pairs selected by applying IDR-DCA and by applying
 399 the coupling scores cutoffs for the three DCA tools respectively. As we can see
 400 from Figure 6A-6C, the accuracies of the residue pairs selected by the two
 401 approaches are kept comparable across different levels of the MSA
 402 downsampling, however, IDR-DCA is always able to select more residue pairs.
 403 Besides, we also compared the numbers of proteins with effective contact
 404 predictions provided by the two approaches, which is shown in Figure 6D-6F.
 405 The definition of an effective contact prediction for the monomeric protein is
 406 the same as before. As we can see from Figure 6D-6F, for all the three DCA
 407 tools, IDR-DCA is always able to provide effective contact predictions for more
 408 proteins across different levels of the MSA downsampling.

409 6. Applying constraints obtained from IDR-DCA to assist RNA secondary 410 structure prediction

411 We used RNA secondary structure prediction as an application example to
 412 show the benefit of leveraging IDR-DCA statistical framework. Specifically, the
 413 webserver 2dRNAAdca [29] (<http://biophy.hust.edu.cn/new/2dRNAAdca/>) was
 414 applied for the RNA secondary structure prediction, which first applied a
 415 remove-and-expand algorithm to refine residue pairs selected by IDR-DCA
 416 (0.1 as the IDR cutoff) to form the prior constraints for RNA secondary

structure prediction, and then the prior constraints were further used to guide RNAfold [30] (a minimum free energy based RNA secondary structure prediction method) to predict the RNA secondary structure. 26 RNAs without broken strands were selected from the RNA dataset for testing the protocol. Since the result of IDR-DCA is not that dependent on the specific DCA tools, only the IDR-DCA results based on CCMpred were employed in our study. Besides, the prediction performances by RNAfold without prior constraints, with prior constraints refined by the remove-and-expand algorithm from the top $L/5$ (L as the sequence length) residue pairs and from residue pairs selected according to the coupling scores (CCMpred coupling score cutoff: 0.41) were also evaluated as the references. In Figure 7, we show the Matthews Correlation Coefficients (MCC) between the experimental RNA secondary structure and the predicted secondary structures by the four protocols for each of the 26 RNAs (the RNAs are ordered according to the sequence length ascendingly). As we can see from the figure that the introduction of prior constraints by the three protocols all dramatically improves the prediction performance for most of the cases. However, the prediction protocol using the constraints refined from the residue pairs selected by IDR-DCA yields a more stable performance, especially for large RNAs. We also noticed that for short RNAs (e.g. sequence length < 80), the secondary structure prediction with the three types of prior constraints almost makes no difference. This is mainly because that for short RNAs, the number of residue pairs selected by the three

approaches are very similar. However, for long RNAs, IDR-DCA can more effectively select the residue pairs with significant evolutionary couplings, thus for which the RNA secondary structure prediction with the IDR-DCA constraints shows better performance (see Table S1). It should be noted that since the variations of the RNA sizes and MSA qualities (the numbers of effective sequences for all the MSAs are larger than 70) of RNA dataset used in our study are not that large, selecting residue pairs according to the coupling scores or trivially selecting the top $L/5$ residue pairs to some extent can also produce reasonable results. This is also the reason that the predicted RNA secondary structures using the prior constraints from IDR-DCA only achieved slightly higher accuracies. It is reasonable to expect that performance gaps can be enlarged if a more diverse RNA dataset is applied here.

Discussion

DCA has been widely used to obtain residue-residue contact information to assist the protein/RNA structure, interaction and dynamics prediction. Besides, the coupling score matrices obtained from DCA also provide major feature components for most of the deep learning methods for the protein residue-residue contact/distance prediction, which has revolutionized the field of protein structure prediction [15]. Given the MSA of homologous sequences, DCA can be easily implemented with the state-of-art DCA software to provide the residue-residue coupling scores. However, it is not easy to quantify the number of residue pairs with significant evolutionary couplings and select

461 these predictive residue pairs from the result of DCA, because the number of
462 predictive residue pairs and the coupling score values from DCA are
463 influenced by many factors including the number and the length of the
464 homologous sequences forming the MSA, the detailed settings of the DCA
465 algorithm, the functional characteristics of the macromolecule, etc.

466 In this study, we presented a general statistical framework named IDR-DCA
467 for selecting residue pairs with significant evolutionary couplings.
468 Benchmarked on datasets of monomeric proteins, protein-protein interactions
469 and monomeric RNAs, we showed that IDR-DCA can effectively select
470 predictive residue pairs with a universal IDR cutoff (0.1). Comparing with the
471 application of the DCA tool specific coupling score cutoffs carefully tuned on
472 each dataset to reproduce the accuracies of the residue pairs selected by
473 IDR-DCA, IDR-DCA is always able to select more residue pairs and provide
474 effective contact predictions for more cases. Therefore, IDR-DCA provides an
475 effective statistical framework for the evolutionary coupled residue pair
476 detection, which can also be considered as a general approach for controlling
477 the quality of the result of DCA. Besides, we also used RNA secondary
478 structure prediction as application example of IDR-DCA. Of course, IDR-DCA
479 can also be used in other application scenarios. Since the statistical framework
480 of IDR-DCA is not dependent on any detailed implementation of the DCA
481 algorithm, this statistical framework is also expected to be applicable to
482 performing quality control for other data-driven contact prediction methods

483 including deep learning.

484 **Materials and Methods**

485 **1. Preparing the three datasets**

486 **1.1 The protein dataset**

487 The PSICOV contact prediction dataset [28] which contains 150 proteins
488 was used to evaluate the performance of IDR-DCA on detecting intra-protein
489 residue-residue couplings. The structures of the 150 proteins were obtained
490 from <http://bioinfadmin.cs.ucl.ac.uk/downloads/PSICOV/suppdata/>. The MSAs
491 of homologous proteins for the 150 proteins were built through searching the
492 whole-genome sequence databases Uniclust30 [31] and UniRef90 [32] and
493 the metagenome database (Metaclust) [33] using DeepMSA [34]. The
494 redundant sequences with sequence identity higher than 90% in the MSA were
495 removed with HHfilter [35].

496 **1.2 The protein-protein interaction dataset**

497 The PDB benchmark from Ovchinnikov *et al.* was used to evaluate the
498 performance of IDR-DCA on detecting inter-protein residue-residue
499 couplings[6].

500 The complex structures of the 30 protein-protein interactions were downloaded
501 direct from the Protein Data Bank [36]. The MSAs of non-redundant
502 protein-protein interologs for the 30 protein-protein interactions were obtained
503 from the supplementary data of Ovchinnikov *et al* [6]. The original PDB
504 benchmark contains 32 protein-protein interactions, however, 1IXR_B-1IXR_C

was removed due to the interacting region of 1IXR_B was missing in the MSA of protein-protein interologs; and 2Y69_B-2Y69_C was removed for the two chains do not directly interact with each other in the crystal structure.

1.3 The RNA dataset

The D^{High} dataset from Pucci *et al.* [13] containing 36 RNAs associated to RNA families with the number of effective sequences larger than 70 was used to evaluate the performance of IDR-DCA on detecting intra-RNA residue-residue couplings. The structures and MSAs of the 36 RNAs were obtained from <https://github.com/KIT-MBS/RNA-dataset>. For each MSA, the columns with more than 50% gaps were first removed, and then the redundant sequences with sequence identity higher than 95% were removed with HHfilter.

2. Performing the DCA

The three DCA tools: EVcouplings, Gremlin and CCMpred were applied respectively in this study to perform the DCA. Evcouplings (only the plmc module) was obtained from <https://github.com/debbiemarkslab/plmc>; Gremlin was obtained from <https://github.com/sokrypton/GREMLIN>; and CCMpred was obtained from <https://github.com/soedinglab/CCMpred>. CCMpred and Gremlin were run with their default settings, and EVcouplings was run with parameters “-le 16.0 -lh 0.01 -m 100” for proteins and protein-protein interactions, and with parameters “-a .ACGU -le 20.0 -lh 0.01 -m 50” for RNAs according to the recommendations from the website.

527 3. Performing the reproducibility analysis

528 The R package 'idr' obtained from
 529 <https://cran.r-project.org/web/packages/idr/index.html> was employed for the
 530 reproducibility analysis with the set of parameters “mu=1.0, sigma=1.0,
 531 rho=0.2, p=0.1, eps=1e-5, max.iter=1000”. For the monomeric proteins and
 532 RNAs, the residue pairs separated by less than 6 residues were not
 533 considered in the IDR estimation. For the protein-protein interactions,
 534 considering the contact probability of inter-protein residues is much lower than
 535 that of intra-protein residues, the intra- and inter-protein residue pairs were
 536 mixed together for the IDR calculation for the purpose of better parametrization
 537 of the statistical model. However, only the IDRs of inter-protein residue-residue
 538 couplings were used to build the IDR signal profile for the inter-protein
 539 evolutionary coupling detection. For the purpose of reducing the computational
 540 cost, we only perform the reproducibility analysis for the top $10 \times L$ (L as the
 541 sequence length) couplings ranked based the coupling score obtained from
 542 the DCA on the full MSA, since the number of evolutionary coupled residue
 543 pairs is generally much smaller than this value.

544 4. Determining the coupling score cutoffs

545 For the purpose of comparison, we determined a DCA tool specific coupling
 546 score cutoff on each dataset to reproduce the accuracy of the residue pairs
 547 selected by IDR-DCA with 0.1 as the IDR cutoff. Specifically, for each DCA tool,
 548 starting from 0, we kept increasing the coupling score cutoff for selecting

residue pairs from the corresponding dataset with a step size 0.01, until the accuracy of the selected residue pairs exceeded the accuracy of the residue pairs selected by IDR-DCA (0.1 as the IDR cutoff). Then the coupling score cutoff which yielded an accuracy closest to accuracy of IDR-DCA was chosen as the empirical coupling score cutoff for this DCA tool on the corresponding dataset.

5. Predicting RNA secondary structure

The 2dRNAdca webserver (<http://biophy.hust.edu.cn/new/2dRNAdca/>) were employed to perform the constraints assisted RNA secondary structure prediction. Ten RNAs with broken strands were removed from the RNA dataset in the secondary structure prediction. The experimental secondary structure of each RNA was calculated with X3DNA [37] without pseudoknotted base pairs. The predicted secondary structures were evaluated by calculating the Matthews Correlation Coefficient (MCC) between the predicted structure and the experimental structure, which was calculated using the following formula:

$$MCC = \frac{TP \times TN - FP \times FN}{\sqrt{(TP + FP)(TP + FN)(TN + FP)(TN + FN)}} \quad (4)$$

Where TP is the number of true positive base pairs; FP is the number of false positive base pairs; TN is the number of true negative base pairs and FN is the number of false negative base pairs.

Key points:

- 570 ● A novel statistical framework is proposed to control the quality of the result
- 571 of DCA.
- 572 ● Our method allows to effectively select residue pairs with significant
- 573 evolutionary couplings using a universal threshold.
- 574 ● Our method with a universal threshold consistently achieves better
- 575 performance than carefully tuned coupling score cutoffs.
- 576 ● Prior constraints obtained from our method has a robust performance in
- 577 assisting RNA secondary structure prediction.

578 **Availability**

579 The script for IDR calculation was provided in
 580 <https://github.com/ChengfeiYan/IDR-DCA>.

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584 **Yunda Si** is a PhD student in the School of Physics at Huazhong University of Science
 585 and Technology. His research interests include protein structure prediction,
 586 protein-protein interaction prediction and deep learning.

587 **Chengfei Yan** is an associate professor in the School of Physics at Huazhong University
 588 of Science and Technology. His research interests include molecular docking,
 589 protein-protein interaction prediction and biological data mining.

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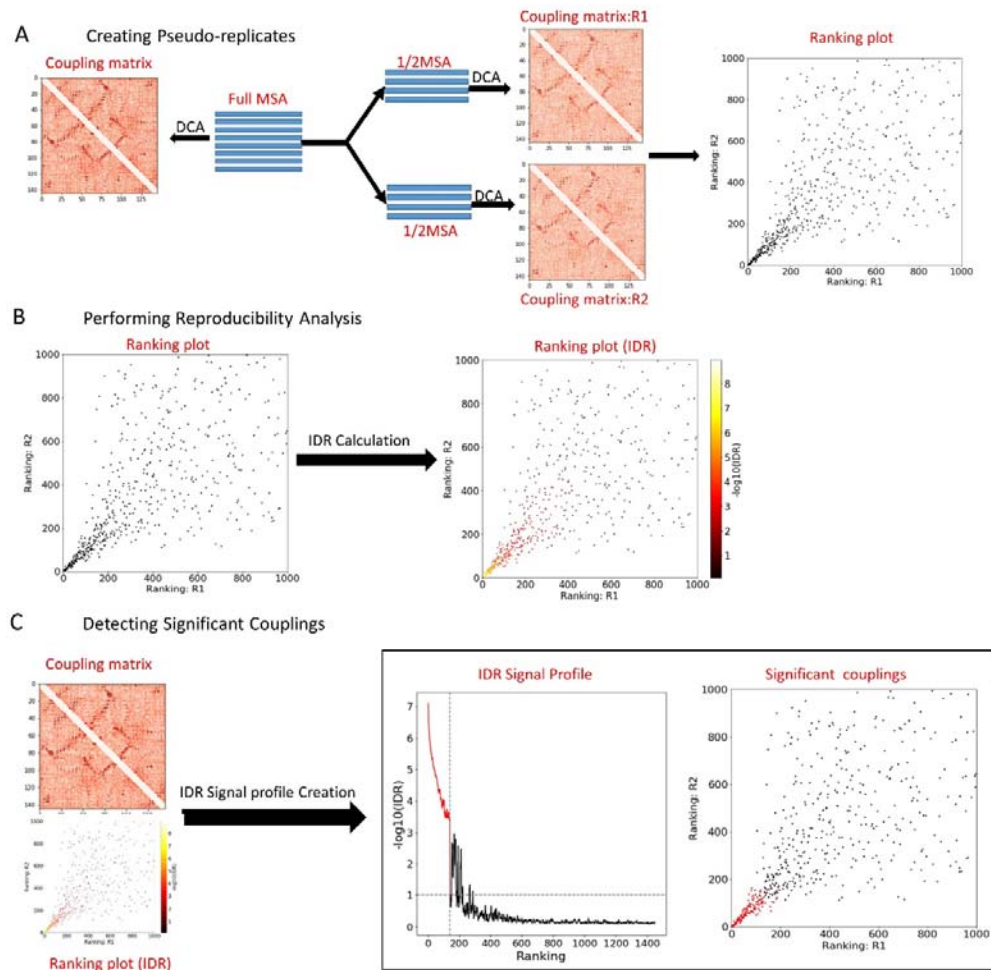


Figure 1. The flowchart of IDR-DCA. (A) Creating pseudo MSA replicates for DCA; (B) Performing reproducibility analysis; (C) Detecting significant couplings.

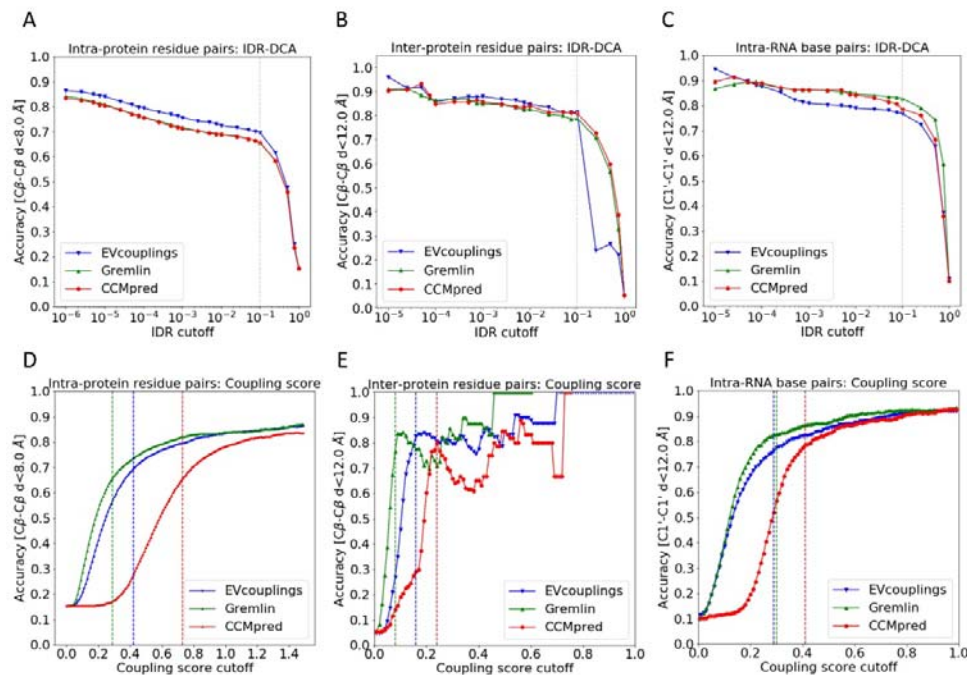


Figure 2. The overall accuracies of residue pairs selected from each dataset based on IDR-DCA and coupling scores with the application of variable IDR and coupling score cutoffs. (A)-(C) The overall accuracies of residue pairs selected by IDR-DCA with the application of variable IDR cutoffs from the three datasets: (A) The monomeric protein dataset; (B) The protein-protein interaction dataset; (C) The monomeric RNA dataset. (D)-(F) The overall accuracies of residue pairs selected based on coupling scores with the application of variable coupling score cutoffs from the three datasets: (D) The monomeric protein dataset; (E) The protein-protein interaction dataset; (F) The monomeric RNA dataset. EVcouplings, Gremlin and CCMpred were applied to perform the DCA for each case in the three datasets respectively. The grey vertical dashed lines in (A)-(C) represent the natural IDR cutoff (0.1) for IDR-DCA. The blue, green and red vertical dashed lines in (D)-(F) represent the empirical coupling score cutoffs for EVcouplings, Gremlin and CCMpred respectively, which were tuned on each dataset to reproduce the accuracies of residue pairs selected by IDR-DCA with 0.1 as the IDR cutoff.

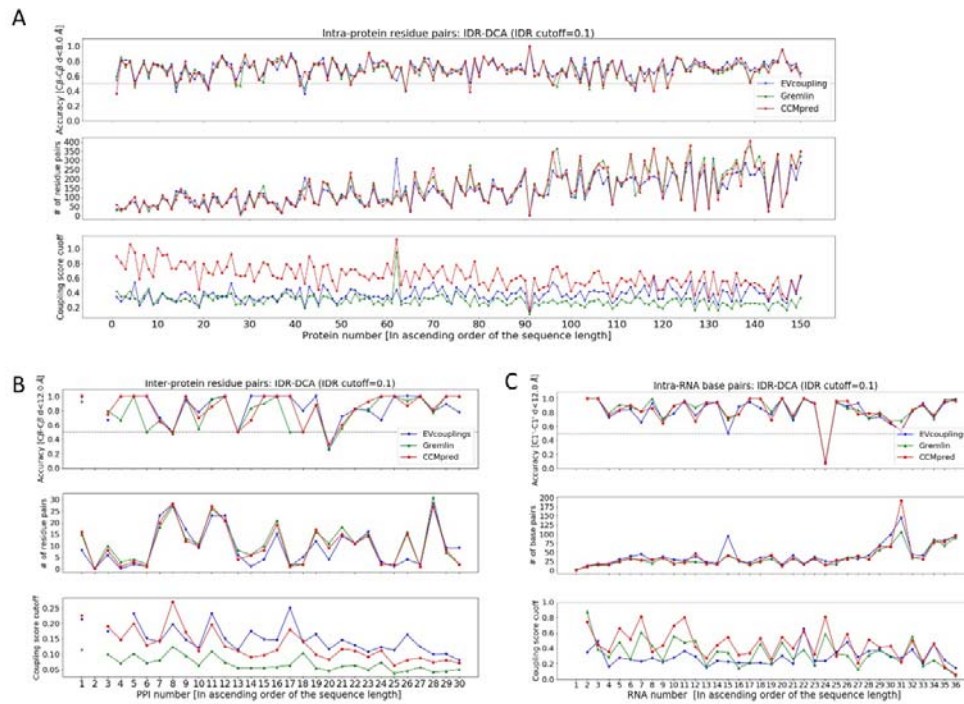


Figure 3. The performance of IDR-DCA on evolutionary coupled residue pair selection with 0.1 as the IDR cutoff. (A)~(C) The accuracies, the numbers and the corresponding coupling score cutoffs of the residue pairs selected by IDR-DCA with 0.1 as the IDR cutoff for each case in the three datasets: (A) The monomeric protein dataset; (B) The protein-protein interaction dataset; (C) The monomeric RNA dataset. For each case, EVcouplings, Gremlin and CCMpred were applied to perform the DCA respectively. In the case that no residue pair is selected by IDR-DCA, the corresponding accuracy and the corresponding score cutoff is not shown. For each dataset, the cases (proteins, protein-protein interactions, RNAs) are ordered ascendingly in the plot according to their sequence lengths.

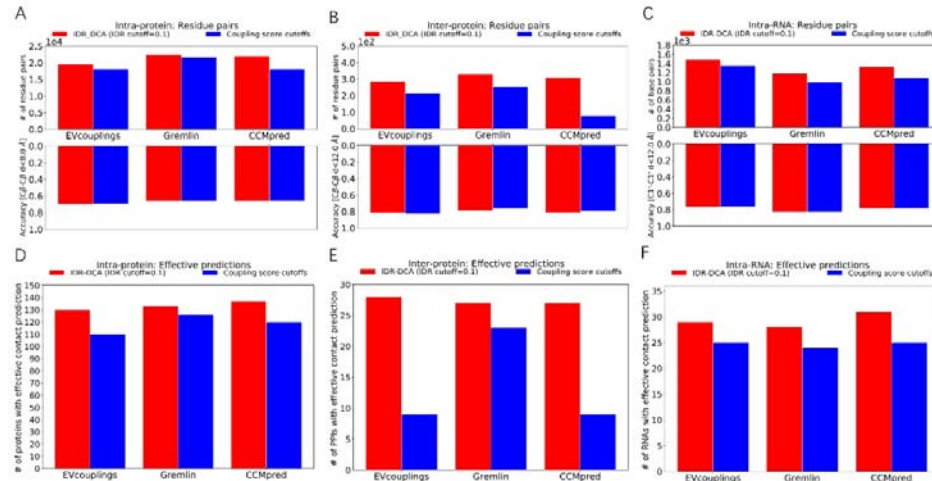


Figure 4. The performance comparison between the application of IDR-DCA (0.1 as the IDR cutoff) and the coupling score cutoffs for the evolutionary coupled residue pair selection. (A)-(C) The comparison of the numbers of the residue pairs selected by applying IDR-DCA with 0.1 as the IDR cutoff and by applying the DCA tool specific coupling score cutoffs from the three datasets: (A) The monomeric protein dataset; (B) The protein-protein interaction dataset; (C) The monomeric RNA dataset. The coupling score cutoffs for the EVcouplings, Gremlin and CCMpred were tuned on each dataset respectively to reproduce the accuracies of residue pairs selected by IDR-DCA with 0.1 as the IDR cutoff. (D)-(F) The comparison of the numbers of cases with effective contact predictions provided by applying IDR-DCA with 0.1 as the IDR cutoff and by applying the DCA tool specific coupling score cutoffs for residue pair selection on the three datasets: (D) The monomeric protein dataset; (E) The protein-protein interaction dataset; (F) The monomeric RNA dataset.

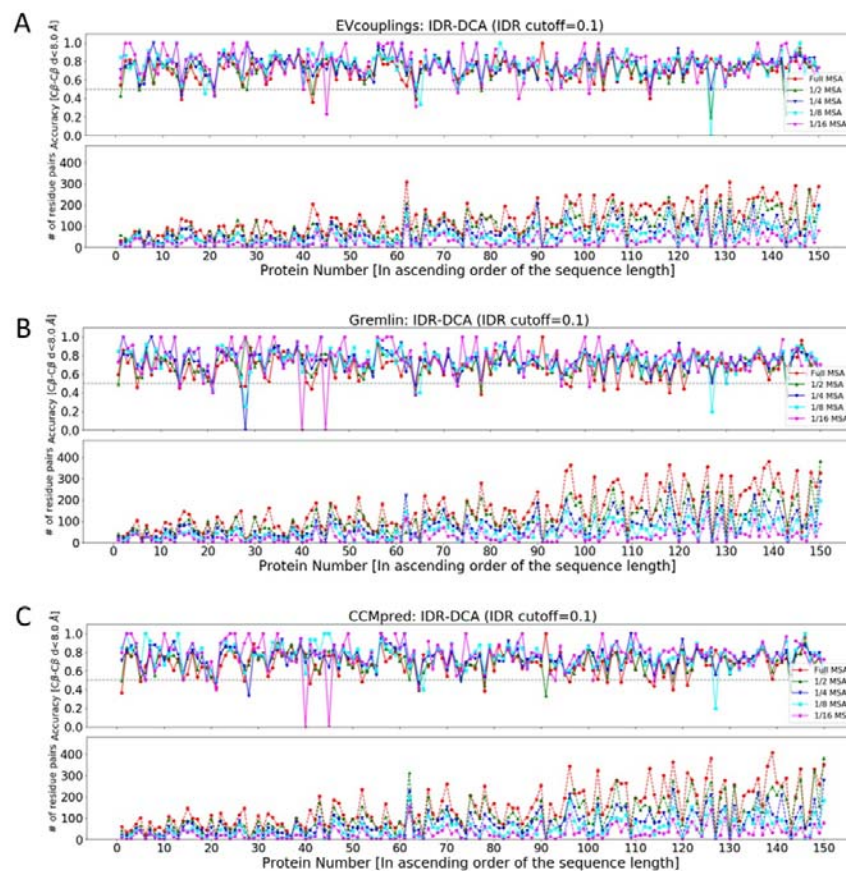


Figure 5. The robustness evaluation of IDR-DCA (0.1 as the IDR cutoff) on evolutionarily coupled residue pair selection through the MSA downsampling analysis. (A)-(C) The accuracies and the numbers of the

758 residue pairs selected by IDR-DCA (0.1 as the IDR cutoff) for each protein in the monomeric protein
759 dataset, in which the DCA were performed on the MSAs with different levels of downsampling with the
760 application of the three DCA tools: (A) EVcouplings; (B) Gremlin; (C) CCMpred. In the case that no
761 residue pair is selected, the corresponding accuracy is not shown in the plot. The proteins are ordered
762 ascendingly in each plot according to their sequence lengths.

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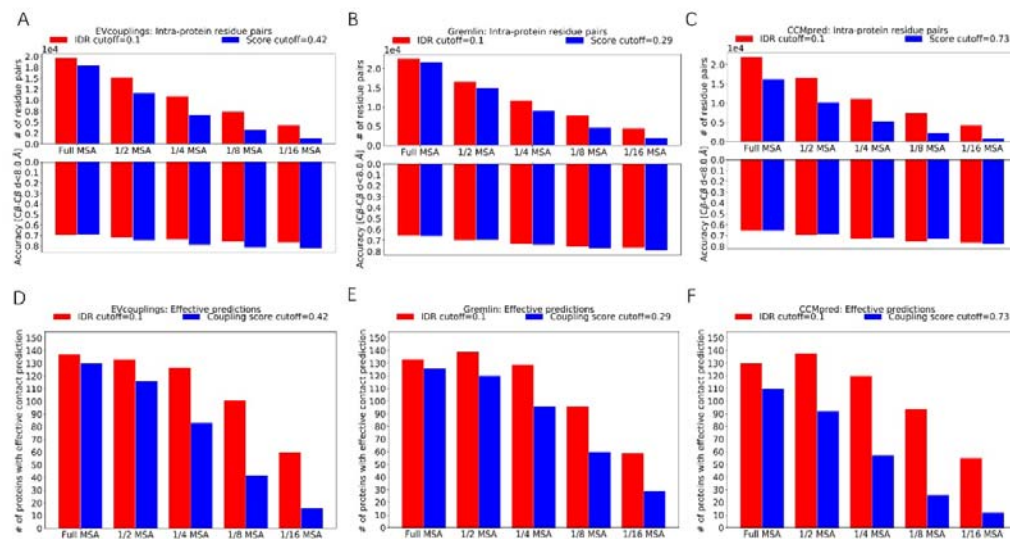
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770 Figure 6. The performance comparison between the application of IDR-DCA (0.1 as the IDR cutoff) and

771 the coupling score cutoffs for the evolutionary coupled residue pair selection from the monomeric protein

772 dataset on the MSAs with different levels of downsampling. (A)-(C) The comparison of the numbers and

773 the accuracies of residue pairs selected by applying IDR-DCA (0.1 as the IDR cutoff) and by applying the
774 coupling score from the monomeric protein dataset, in which the DCA were performed on the MSAs with
775 different levels of downsampling with the three DCA tools: (A) EVcouplings; (B) Gremlin; (C) CCMpred.
776 (D)-(F) The comparison of the numbers of cases with effective contact predictions provided by applying
777 IDR-DCA(0.1 as the IDR cutoff)and by applying the coupling score cutoffs for residue pair selection from
778 the monomeric protein dataset on the MSAs with different levels of downsampling, in which the DCA
779 were performed with the three DCA tools: (D) EVcouplings; (E) Gremlin; (F) CCMpred.

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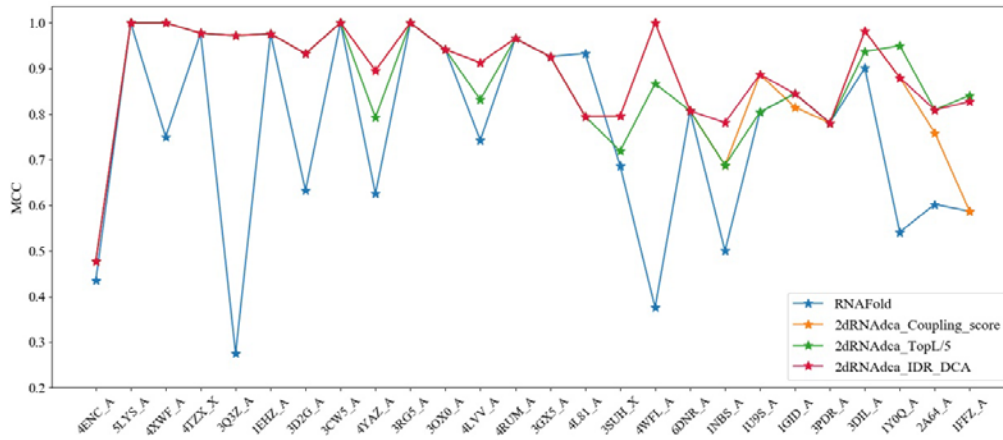


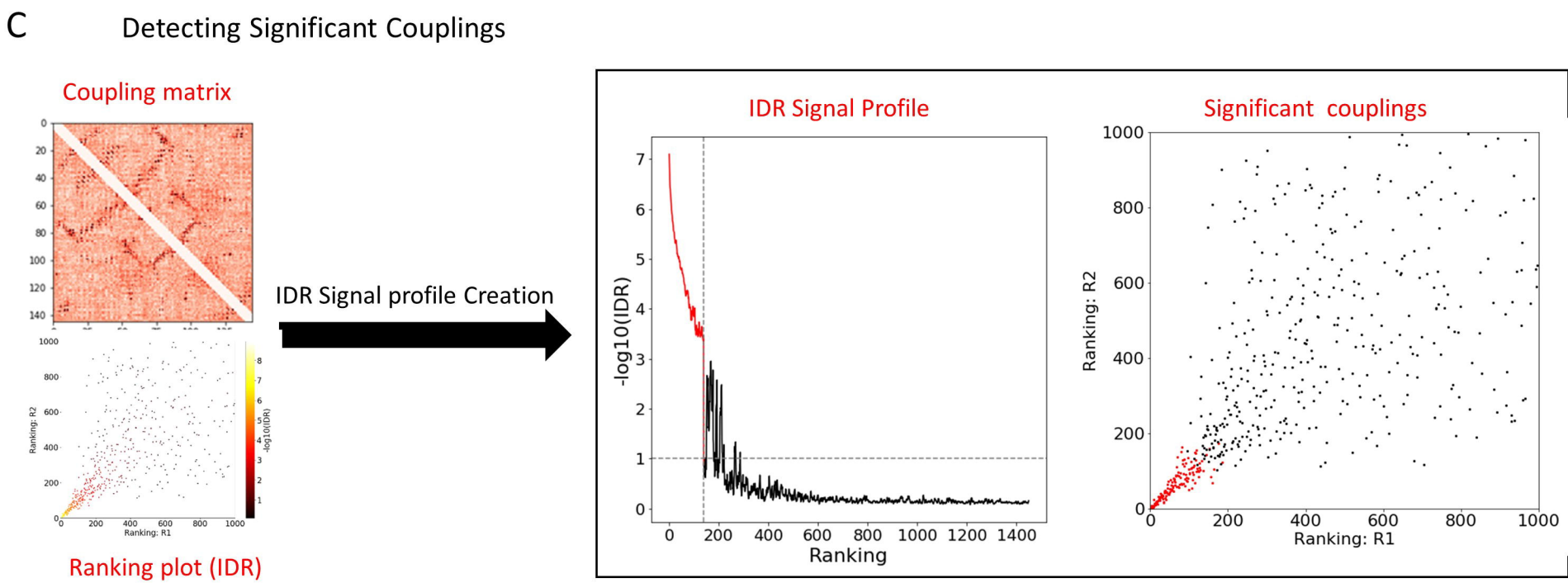
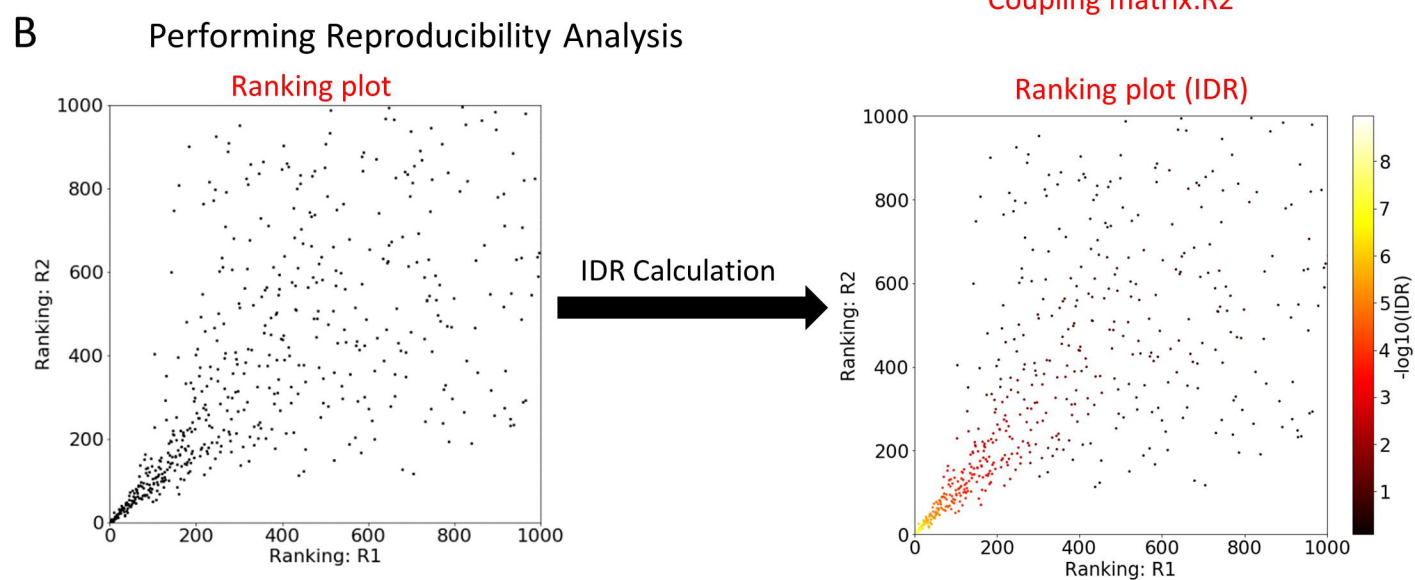
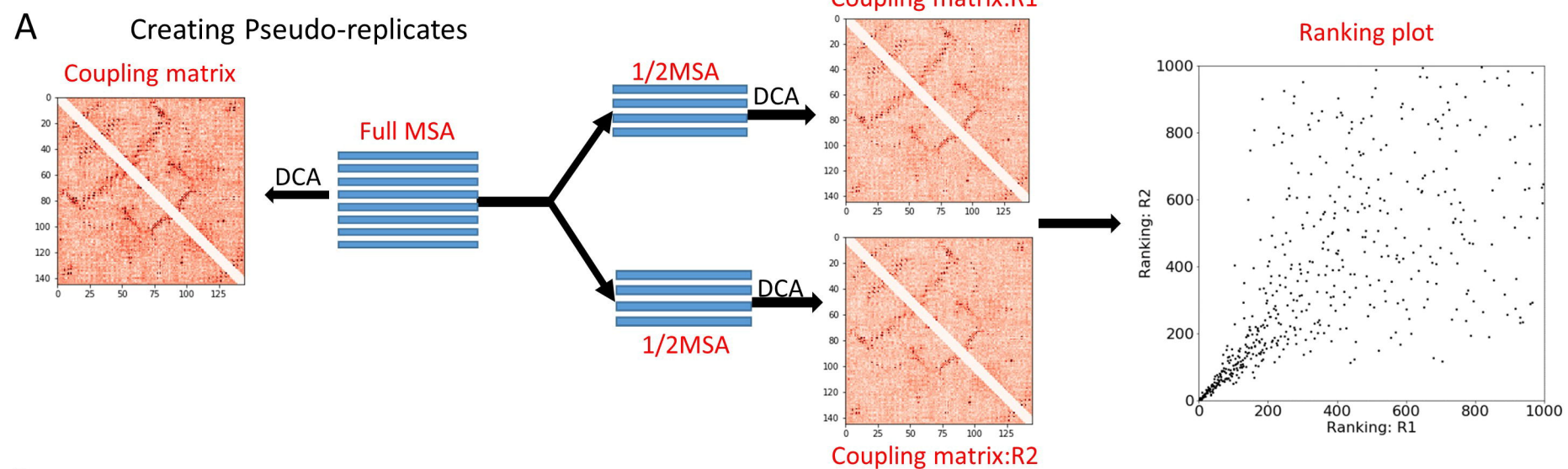
Figure 7. The Matthews Correlation Coefficients (MCC) between the experimental RNA secondary structure and the predicted RNA secondary structures by the four protocols for each of the 26 RNAs. The RNAs are ordered ascendingly according to their sequence lengths.

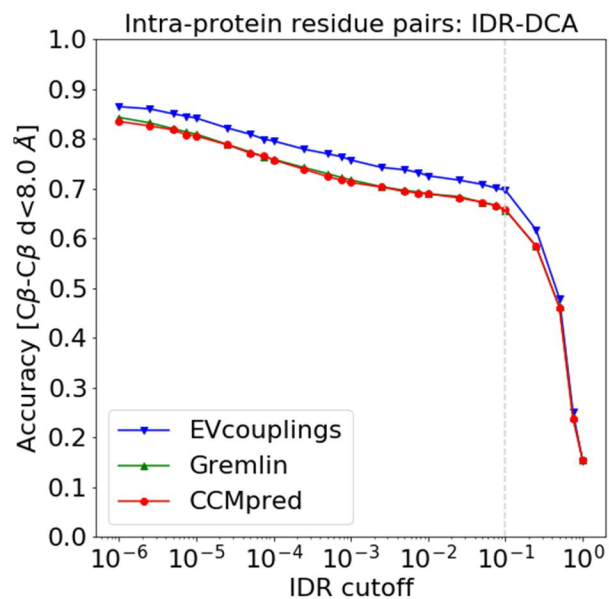
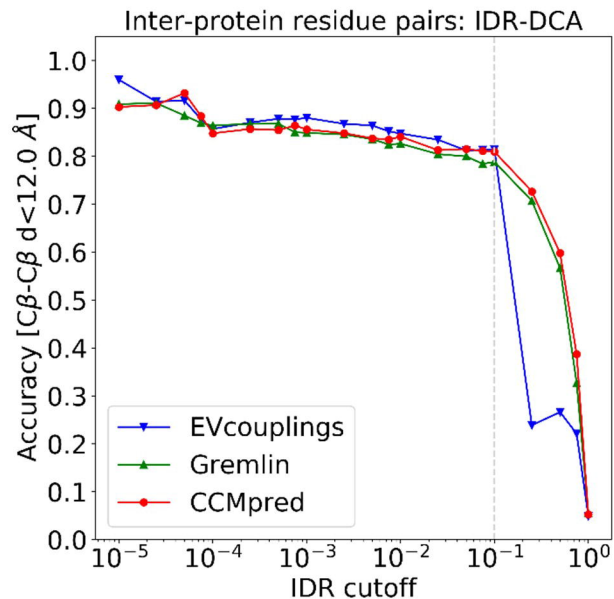
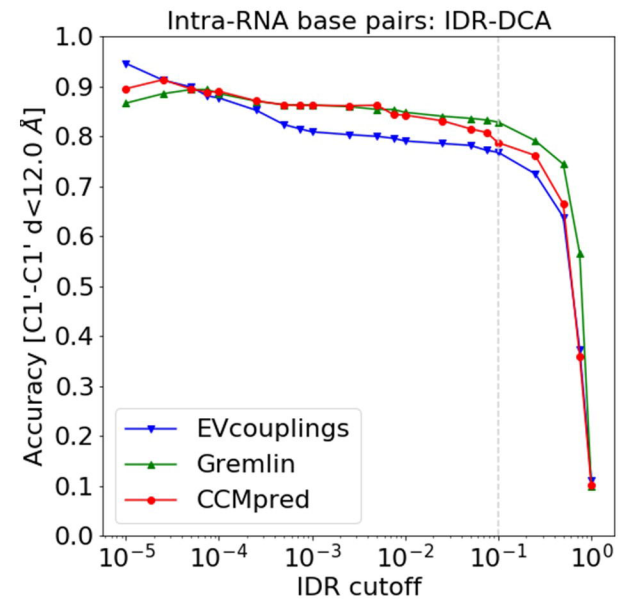
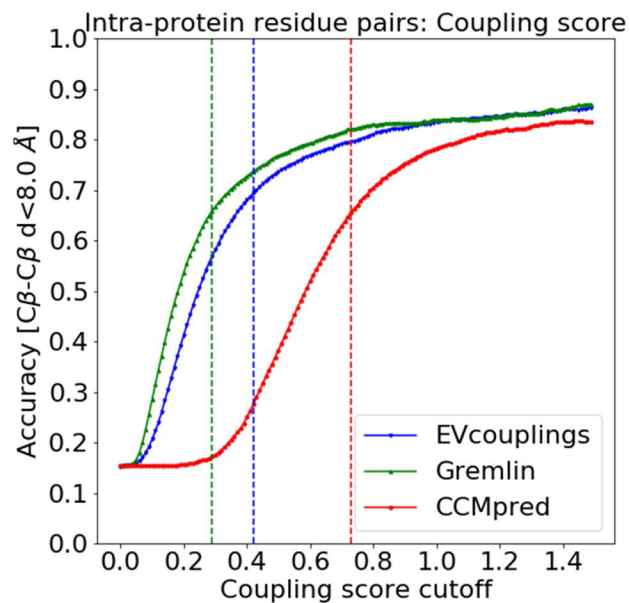
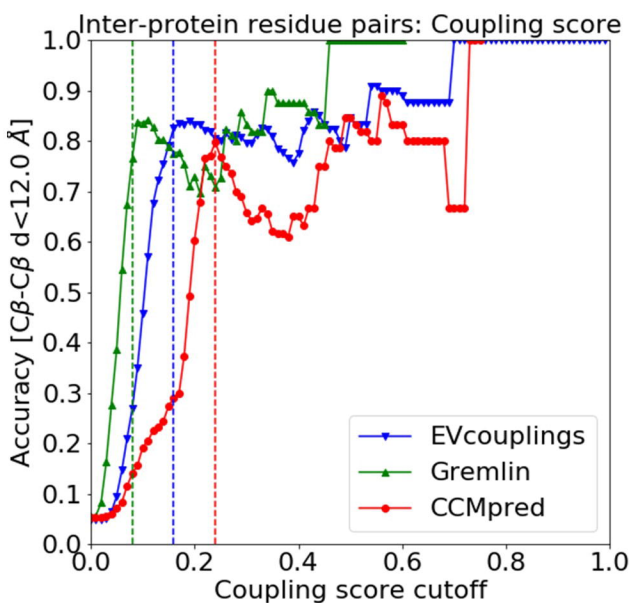
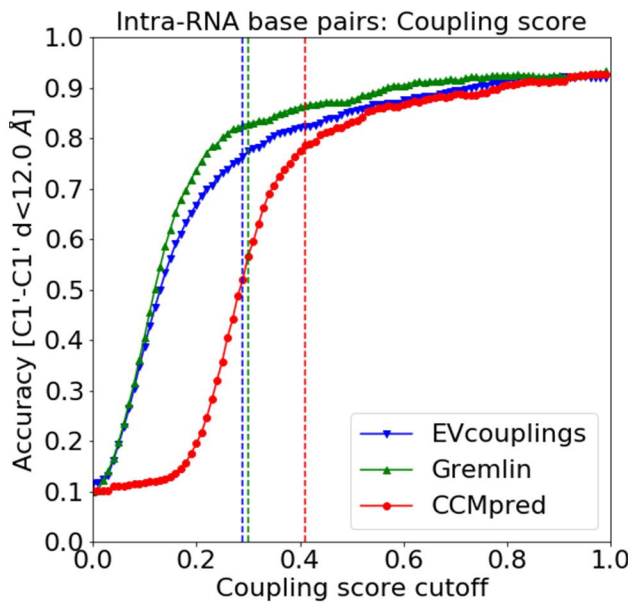
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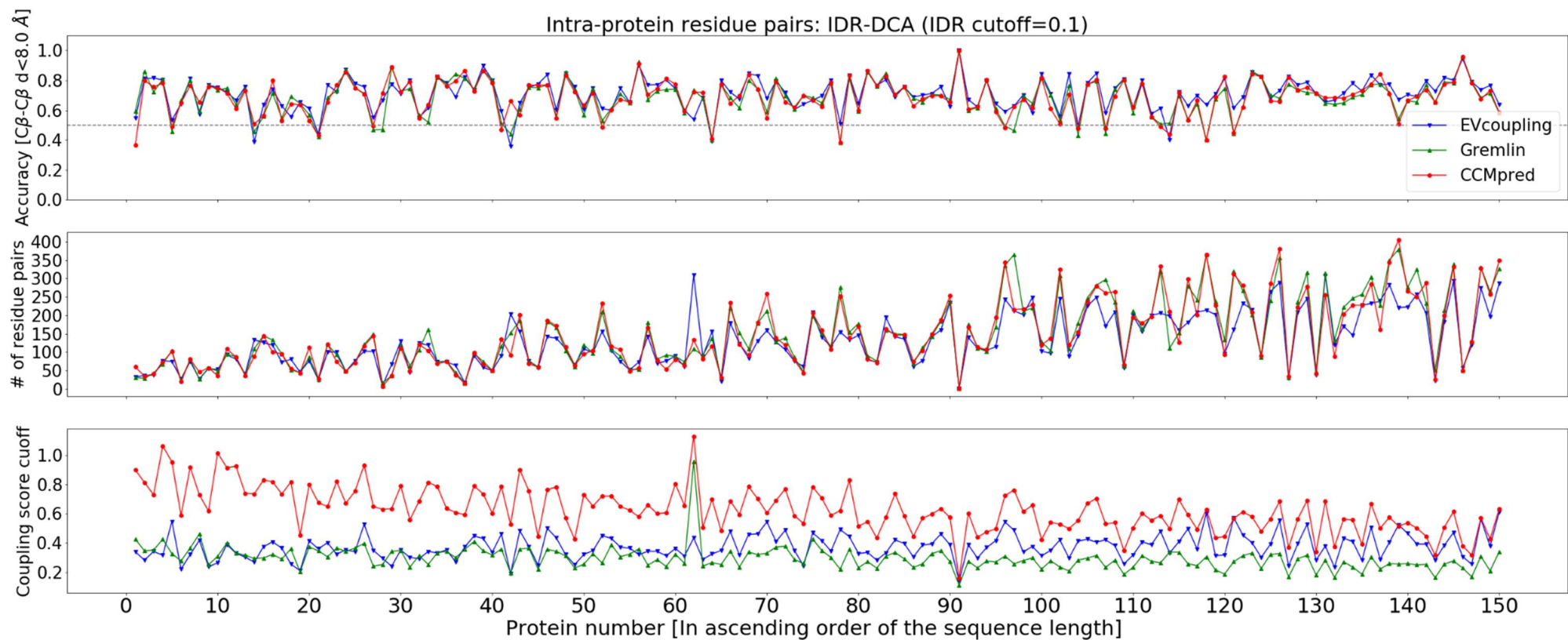
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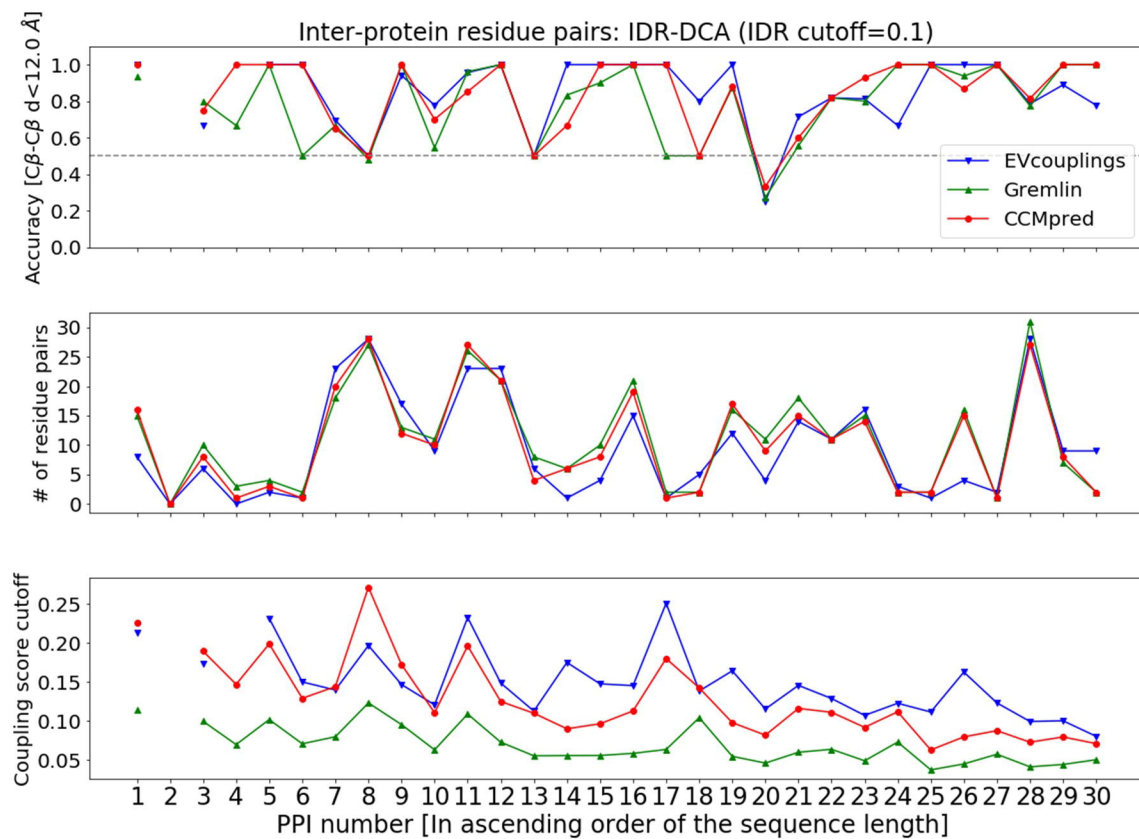


A**B****C****D****E****F**

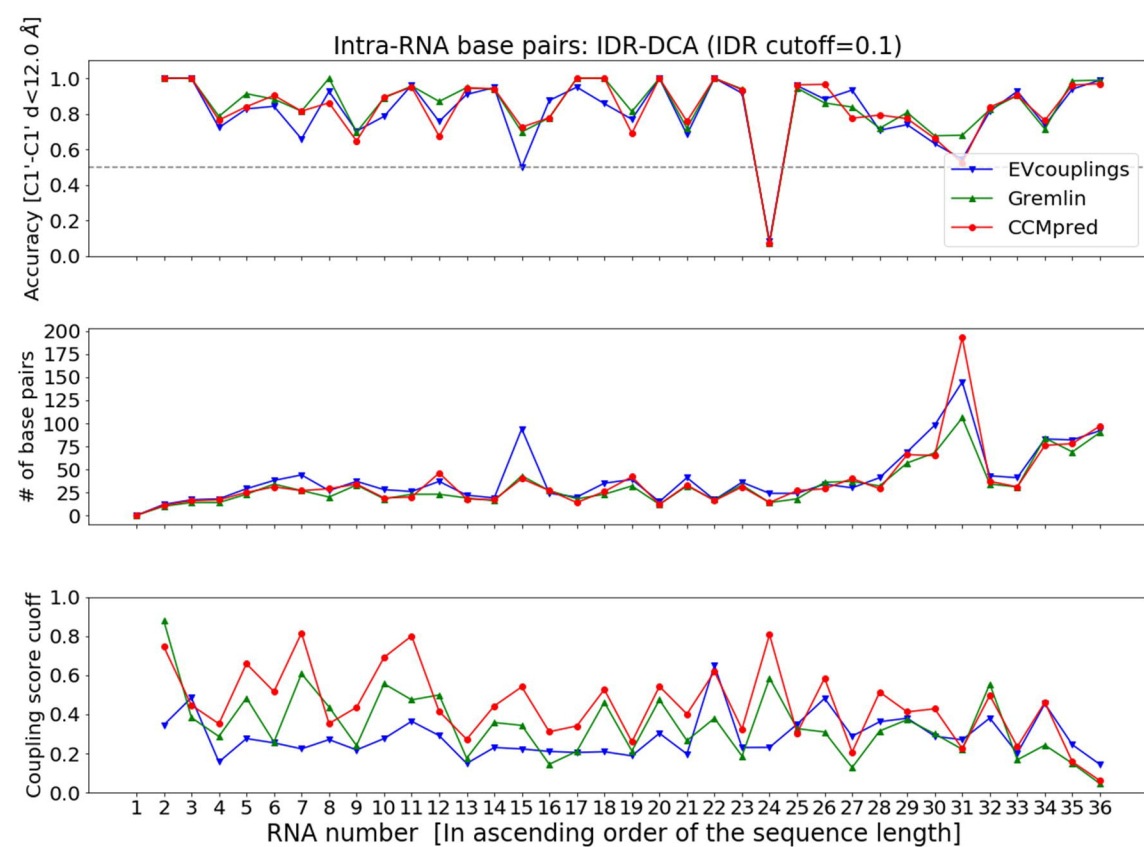
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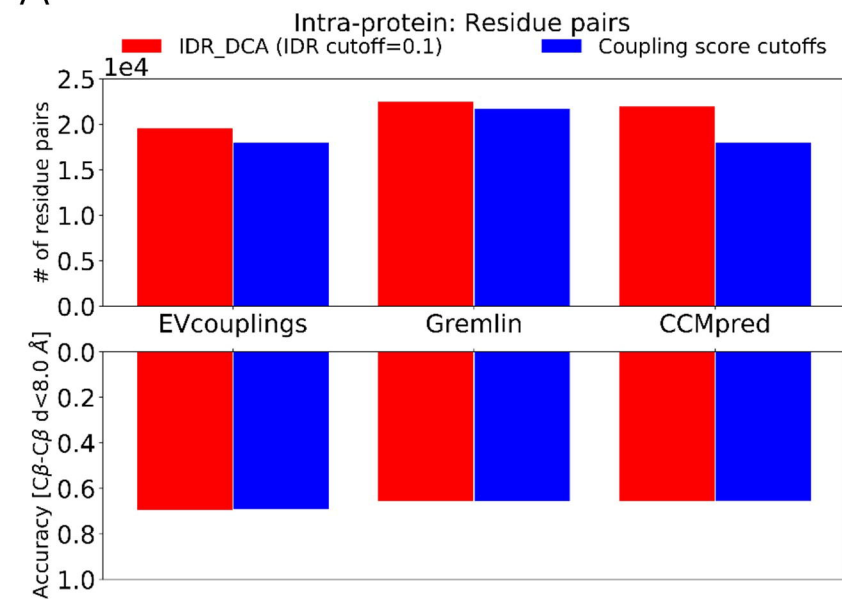
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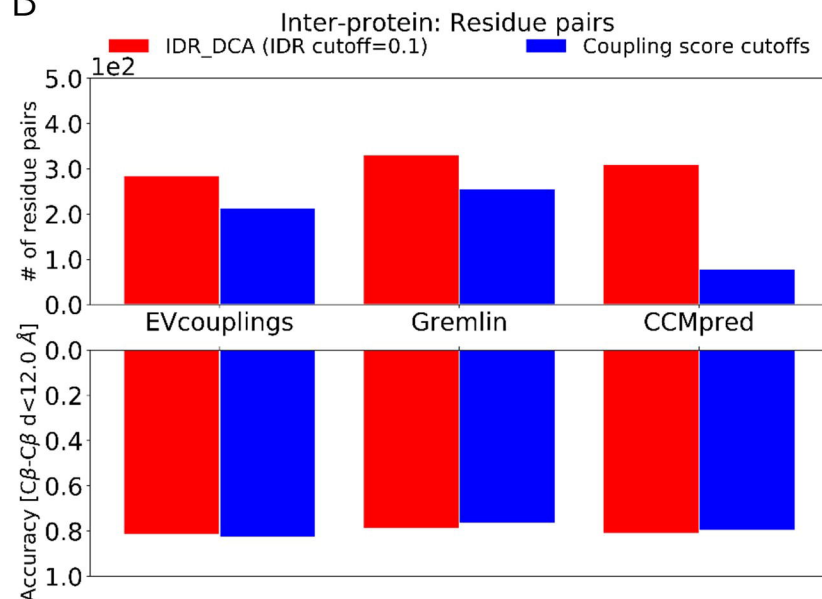
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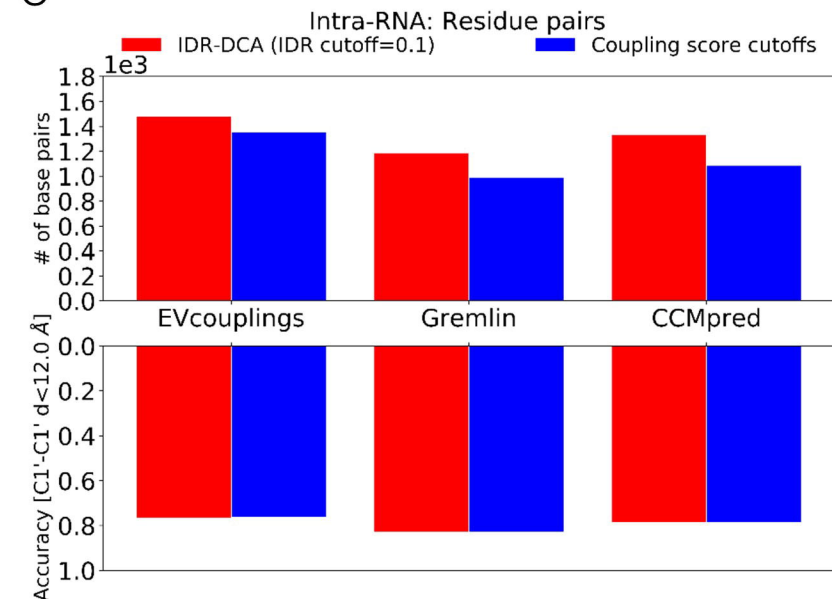
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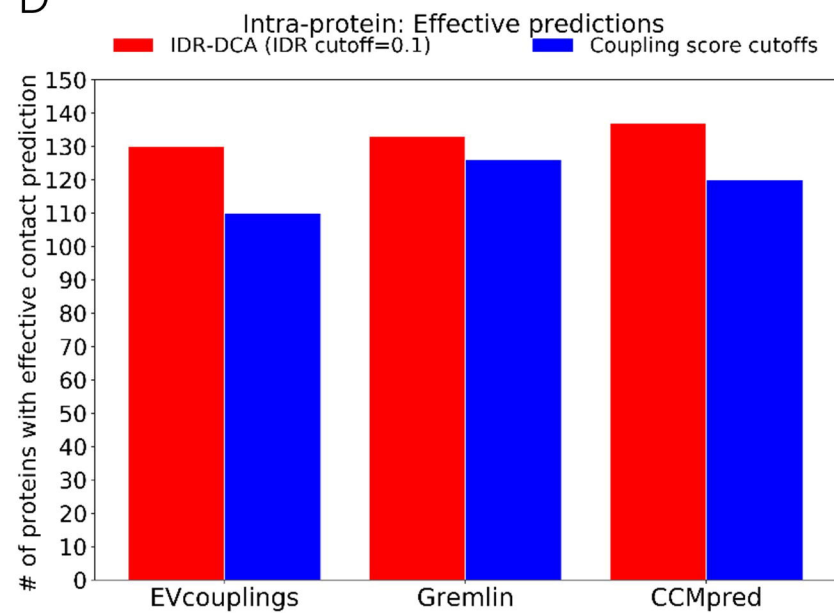
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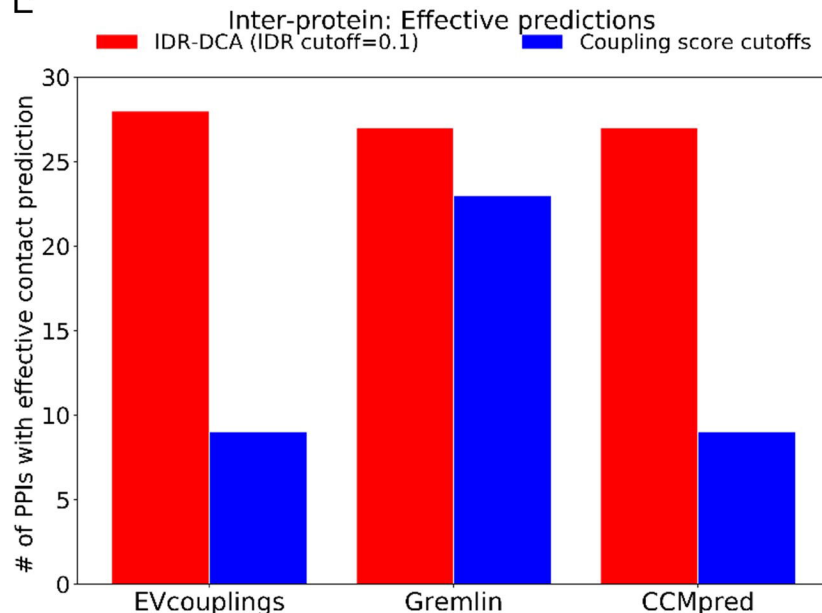
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