Survivable Robotic Control through Guided Bayesian Policy Search with Deep Reinforcement Learning

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Abstract-Many robot manipulation skills can be represented with deterministic characteristics and there exist efficient techniques for learning parameterized motor plans for those skills. However, one of the active research challenge still remains to sustain manipulation capabilities in situation of a mechanical failure. Ideally, like biological creatures, a robotic agent should be able to reconfigure its control policy by adapting to dynamic adversaries. In this paper, we propose a method that allows an agent to survive in a situation of mechanical loss, and adaptively learn manipulation with compromised degrees of freedom- we call our method Survivable Robotic Learning (SRL). Our key idea is to leverage Bayesian policy gradient by encoding knowledge bias in posterior estimation, which in turn alleviates future policy search explorations, in terms of sample efficiency and when compared to random exploration based policy search methods. SRL represents policy priors as Gaussian process, which allows tractable computation of approximate posterior (when true gradient is intractable), by incorporating guided bias as proxy from prior replays. We evaluate our proposed method against off-the-shelf model free learning algorithm (DDPG), testing on a hexapod robot platform which encounters incremental failure emulation, and our experiments show that our method improves largely in terms of sample requirement and quantitative success ratio in all failure modes. A demonstration video of our experiments can be viewed at: https://sites.goog iew/survivalr

Index Terms—Survivable Robotic Control, Bayesian Learning, Guided Policy Search

I. INTRODUCTION

Reinforcement learning (RL) have recently demonstrated promising performance in domain of robotic learning, solving problems like robot manipulation [1], motion planning [2] and robot control [3]. Moreover, RL methods for robotics are expected to shift the automation paradigm by exhibiting high tolerance or error resilience, thus capable of autonomously accomplishing tasks under complex environments. However, such overwhelming vision equally demands reduced training overhead and tractable computational requirements. One of the key challenges for RL algorithms is there requirement of extensive interaction with the environment, gathering experience to train policies that solve new tasks [4]. This requirement, in particular grows significantly in domain of high-dimensional robotic systems where gathering experience from interactions is slow and expensive. Moreover, the gathered experience could also become less relevant if the composition of robotic system varies over time—hence requiring to regather the samples [5], [6]. Intuitively, a possible approach to address this challenge could be defined by representing past gathered samples as a generative representation of the model being learnt, allowing the agent to reproduce or bootstrap parameters from past experiences to alleviate sample requirements for learning



Fig. 1: (a):18-DoF Hexapod used for experiments (b):Failure shown as reduction in one DoF (c):Failure case where entire limb is amputated, reducing three DoFs as well as the mass.

policy for future tasks. We study about how efficiently an agent can adapt its learning towards task completion, when encountered with adversaries like physical damage to joints or random loss in degrees of freedom, mimicking mechanical failure. Our proposed Survivable Robotic Learning (SRL) framework enables the robot to learn and update its future policy by inducing bias from prior behavioral samples. Given a learned policy π for a deterministic robotic agent Fig.1.a, our method aims at quickly adapting to sudden changes in system dynamics or robotic agent itself as shown in Fig.1.b and Fig.1.c respectively; for example, an agent in Fig.1.a is deterministically trained, and is equipped with control policy π assuming complete functionality, but unexpectedly looses certain portion of its mobility or faces with unforeseen occurrences; now would need to relearn a policy separately in case of Fig.1.b and Fig.1.c. Mathematically, all these scenarios can be formally abstracted as the loss in state space S or action space A. As such, the goal of our SRL is to compute a new optimal policy π_{new} considering the changes in S and A, while doing generative exploitation of previously learned samples from past policies.

Our key idea is to use parametric posterior estimation (Bayesian RL) to guide the search direction of new policy while exploiting the base policy as much as possible inspired by [7]. Technically, our proposed SRL exploits Bayesian exploration strategy to wisely guide the exploration of on-going learning policy by integrating the past learned knowledge through prior distributions. Bayesian learning not only stabilizes exploration-exploitation dilemma during

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gradient estimation, but also tackles the central challenges of the explosion of sample-complexity imposed by off-theshelf Monte-Carlo based policy gradient approaches ([3], [5], [8]). Thus, we can compute policy gradient and policy integral (posterior) with Bayesian gradient estimation [9] and the samples of its integrand distributions(a priori), while avoiding the high parametric divergence of MC based update.

II. RELATED WORK

In this section, we will briefly discuss about existing work that utilize RL methods for robotic applications, specially achieving robotic control using probabilistic methods for learning control policy through Bayesian estimation methods that use prior distributions to bias parametric updates in posterior inference.

Bayesian Reinforcement Learning— Bayesian methodology, which incorporates prior information into inference algorithms, has been extensively studied to augment the conventional reinforcement learning (RL) [10]. Such integration provides an elegant approach to account for prior knowledge and learning uncertainty while effectively trading between exploration and exploitation during action-selection. Although the majority of recent literature on Bayesian RL is model-based [10] (priors are expressed over the value function or policy class), in robotics, because prior information rarely can be accurately expressed as a parameterized Markov model [7], [9], this paper will exclusively focus on Bayesian methods for model-free RL, where priors are expressed over the value function or policy class. Specifically, the study in [9] proposed a new actor-critic learning model consisting of a Bayesian class of non-parametric critics using Gaussian process temporal difference learning. Recently in [7], Bayesian framework has been shown that modeling the policy gradient as a Gaussian process can significantly improve the efficiency of sample usage and acquire uncertainty measurements almost free.

Damage recovery and sudden perturbation planning in robotics- Previously, to mitigate the adverse effect due to sudden malfunction, most robotics systems were preloaded multiple contingency planes constructed beforehand. As such, as soon as robotic damage occurs, the robot would first conduct self-diagnosis, quickly assess its damage, and subsequently select the best recovery plan [11]. Unfortunately, such self-diagnosing robots are overly challenging to design, because foreseeing all possible failure modes is extremely difficult and providing all backup plans can be prohibitively expensive. For example, in [12], a 4-leg robot has been demonstrated to recover from a disabled leg autonomously without pre-stored contingent policies by continuous self-modeling. The main algorithm used in [12] is based on the basic stochastic optimization that attempts to explain the observed sensory-actuation causal relationship, therefore largely heuristic-based. More recently, in [13], an evolutionary algorithm has been developed that allows a sixlegged robot to adapt to unforeseen changes. The six-legged mobile robot investigated used an intelligent trial-and-error algorithm to tap into the experiences previously accumulated and quickly find optimal compensating behaviours.

Key SRL differences— Compared with the prior studies, our proposed SRL algorithm has at least two fundamental distinctions. First, both [12] and [13] applied control systembased methodology to tackle damage recovery in robotics and these methods have been quite successful in various domains, but here we wanted to exploit the most recent development in deep RL for robotics. This is critical because deep RL is proved not only to provide a mathematically rigorous machine learning framework, but also is more accurate to account for the continuous state and action space for robotic control. Second, although the study [13] did utilize a Bayesian-inspired prediction scheme, our proposed methodology tightly incoorperate the Bayesian learning algorithm with the most recent off-model and off-policy deep reinforcement learning, thus much more capable and more sophisticated. In many aspects, the Intelligent Trial and Error algorithm (IT&E) proposed in [13] represent a rudimentary form of basic tabular-based Q-learning [14],which is typically used for finite state and action spaces, while most of the robotic platforms deal with continuously varying spaces.

III. PRELIMINARIES

We consider the standard RL setting represented as an MDP (Markov decision process). We represent MDP node as a tuple $(s, a, p_0, r, p, \gamma)$. An agent interacts with an stochastic environment consisting of a set of states $s \in S$, a set of actions $a \in A$, a distribution of initial states $p(s_0)$, a reward function $r : S \times A \to \mathbb{R}$, transition probabilities $p(s_{t+1}|s_t, a_t) : s \times a \to s'$, and a discount factor $\gamma \in [0, 1]$. The agent interacts with the environment to learn a policy $\pi(a_t|s_t)$ which is actually a mapping function representing probability distribution function (PDF) of reward, taking state and action as input random variables. An agent chooses an action according to $\pi(a_t|s_t) : S \to \mathcal{P}(A)$ such that long-term expected sum of rewards, $J = \mathbf{E}_{\pi}[\sum_{t=0}^{\infty} \gamma^t r(s_t, a_t)]$, can be maximized.

The quality of each action a_t sampled by current policy π in a state s_t can be measured by a function $Q(s_t, a_t) = \mathbb{E}_{\pi}[J|s_t, a_t]$. The sequence of state-action pairs in an episode creates a trajectory $\xi = (s_0, a_0, s_1, a_1, \dots, s_{T-1}, a_{T-1}, s_g)$ in form of a Markov chain. The PDF of such Markov chain followed by policy π is represented as $P(\xi_{\pi}) = p(s_0) \prod_{t=0}^{T-1} \pi(a_t|s_t) p(s_{t+1}|s_t, a_t)$, which is generated by Monte-Carlo sampling. Also, the expected return for a given ξ can be expressed as, $\eta(\pi) = \mathbf{E}[J(\xi_{\pi}))] = \int J(\xi_{\pi}) P(\xi_{\pi}) d\pi$.

A. Bottlenecks in Monte-Carlo Simulation

The policy search is performed by estimating the gradient over expected return from a class of parameterized stochastic policies $\{\pi(\cdot|s,\theta), s \in S, \theta \in \Theta\}$ w.r.t policy parameters θ from observed system trajectories and then improve the policy by adjusting the parameters in the direction of gradient. For, any given set of trajectories $\xi_1, \xi_2, \ldots, \xi_M$ we can state Monte-Carlo (MC) esti-mator as $\widehat{\nabla}\eta_{MC}(\pi_{\theta}) = \frac{1}{M} \sum_{i=1}^M J(\xi_i) \nabla \log P(\xi_i | \pi_{\theta}) = \frac{1}{M} \sum_{i=1}^M J(\xi_i) \sum_{t=0}^{T_{i-1}} \nabla \log \pi(a_{t,i} | s_{t,i}, \theta)$, where gradients are defined as likelihood ratio. So, in MC based estimation, policy gradients are defined over the expected values of trajectories and the samples are drawn according to their probability values. This policy gradient can be an unbiased estimate of true gradient $\eta(\cdot)$ only when number of drawn samples tend to infinity i.e $M \to \infty$ and thus, variance between $\nabla \eta_{MC}(\pi_{\theta})$ and true gradient $\nabla \eta(\pi_{\theta})$ diminishes to zero. This condition makes MC based policy modeling infeasible for robotic platforms, because gathering experiences in robot learning is slow and expensive. Moreover, MC estimation is fundamentally unsound as explained in [5], because the estimator only depends on the values of sampling

distribution which are arbitrary choices, and are dependent on stationary reward distributions. This dependence violates the likelihood principle because the estimated gradient becomes irrelevant if the reward distribution is likely to evolve with time [9]. Therefore, for problems with temporally varying distribution, classical policy gradient alone would yield nonoptimal performance.

B. Gradient Computation by Bayesian Quadrature

RL for robotic control typically deals with continuous state and action spaces with extremely high dimensionality, and environments and the associated robotic agent are largely susceptible to uncertain changes due to inherent nonstationarity in work-space and unwanted malfunction in the agent's structure itself. In Bayesian RL, the distribution of unknown function $f(\cdot)$ which can be a representative for robust control policy $\pi(\cdot|s_t)$ to tackle uncertainty mentioned earlier, is modelled as a Gaussian Process (GP) by defining a Gaussian distribution as prior distribution over functions. The inferred posterior distribution from this prior will also be a Gaussian normal. Therefore, the gradient of expected return in terms of Bayesian quadrature is given by $\eta_B(\pi_{\theta}) =$ $\int J(\xi_{\pi}) P(\xi_{\pi}, \theta) d\xi$. We consider $\eta_B(\pi_{\theta})$ as a random variable due to high variance (Bayesian uncertainty) in $J(\xi_{\pi})$. As such, the expected mean of a posterior distribution of gradient is computed as

$$\nabla \mathbf{E}[\eta_B(\theta) \mid \mathcal{D}_M] = \mathbf{E}[\nabla \eta_B(\theta) \mid \mathcal{D}_M]$$

= $\mathbf{E}[\int J(\xi_\pi) \frac{\nabla P(\xi_\pi, \theta)}{P(\xi_\pi, \theta)} P(\xi_\pi, \theta) d\xi \mid \mathcal{D}_M]$ (1)

where the set of samples $\mathcal{D}_M = \{(s_i, \hat{s}_i)\}_{i=1}^M$ are provided and \hat{s} is the noisy observation of $f(s) : s \times a \to s'$. The integrand in Eq. (1) can be decomposed into a GP prior function $f(\xi_{\pi}, \theta)$ and its probability distribution $p(\xi_{\pi}, \theta)$. When computing posterior, the quadrature assumes p to be known.

Despite of addressing the issue of high variance, calculating the gradient in Eq. (1) implicitly assumes that (i) the behavior of prior moments can be aggregated into a policy distribution which is a normal Gaussian process and (ii) the parameter θ of prior can be embedded for determining direction of posterior gradient. Therefore, we augmented the policy learning with Bayesian optimization for exploiting the past experiences and prior policy gradient updates to guide new policy search in order to handle sudden perturbations in state-space or action-space of the robotic agent.

IV. PROPOSED APPROACH

The major objective of our proposed SRL is enabling a robotic agent to inherit, partially or entirely, a previously learned motion policy in order to quickly evolve or adapt to a new policy that optimally tackles unexpected sudden changes in state dynamics, such as joint damages during run time. The key intuition behind our SRL, which has been biologically confirmed as well [12], is that, even if a robot is damaged, its prior motion policy π_B can still be partially utilized to characterize behavior for both initializing the parameter vector for π_{new} and determining the direction for making gradient updates $\nabla \pi_{new}$. Abstractly, to formalize our SRL formulation, we defined two separate domain of operation–*healthy domain* and *unhealthy domain*. At the beginning, our SRL agent was assumed to be equipped with a well-learned policy π_B and a healthy model \mathcal{M}_B , where the

subscript *B* represents *behavior*— as we will use behavior policy to learn target (new) policy. In our case, the robot was initially intact with all available degree of freedoms (DoFs) and zero malfunction. The knowledge learned in this *healthy domain* can be encoded as a heuristic ensemble guide that directs the exploration and parameter updates for future *unhealthy domain*. Hence, learning in a new domain need not to be initiated from absolute scratch, rather our SRL agent strives to learn unknown tasks through performing a guided exploration to explore states unknown to *healthy domain*. When our SRL agent suffered from unknown functionality



Fig. 2: Overall learning framework of SRL.

loss in terms of its mobility remarked as unhealthy model \mathcal{M}^+ , naturally the previous healthy policy π_B would underperform in \mathcal{M}^+ due to sudden changes in state space and action-space. However, instead of totally disregarding the learning trends in previous \mathcal{M}_B , our SRL agent can exploit its prior locomotion policy by estimating state value similarity between known \mathcal{M}_B and unknown \mathcal{M}^+ to quickly plan new locomotion plans for maneuvering in new unhealthy domain. Fig. 2 depicts the overall learning strategy for our SRL agent. As such, we view the SRL problem as an incremental estimation, where a new trajectory is suggested by the π_{new} considering the old behaviors of the agent as a set of advise to plan locomotion in the \mathcal{M}^+ domain. In short, the objective of the SRL state estimation is to find a continuous-valued posterior trajectory for \mathcal{M}^+ given an ensemble prior distribution optimized by policy in \mathcal{M}_B .



Fig. 3: Algorithmic details for parametric updates in SRL

A. Behavior Policy: Healthy Ensembles

To formalize healthy ensemble attributes, we consider infinite-horizon MDPs with stochastic transition dynamics $p(s_{t+1}|s_t, a_t)$, a set of terminal states $\mathcal{G}_B \subset \mathcal{S}$, and a sparse reward function $r_{\mathcal{G}_B}(s_B) = \mathbb{1}(s_B \in \mathcal{G}_B)$. For any stochastic behavior policy π_B , the state value function is

$$V_{\mathcal{G}_{B}}^{\pi_{B}}\left(s_{(0,B)}\right) = \mathbf{E}\left[\sum_{t=1}^{\infty}\gamma^{t}r_{\mathcal{G}_{B}}\left(s_{t,B}\right)\right]$$

B superscript specifies that these information are collected from prior domain \mathcal{M}_B . By following behavior policy π_B , the agent creates a trajectory of state-action pairs as, $\xi_{\pi_B} = (s_0, a_0, s_1, a_1, ...)$ where $a_t \sim \pi_B(\cdot|s_t)$ and $s_{t+1} \sim p(\cdot|s_t, a_t)$. Each trajectory either ends by reaching a goal state s_g or exhausts all allowed steps and fails to reach a goal state. All trajectories can be clustered into two sets \mathcal{X}_g and \mathcal{X}_g^C such as, all successful trajectories $\xi_{i_{\pi_B}} \in \mathcal{X}_g$ and all failure states $\xi_{j_{\pi_B}} \in \mathcal{X}_g^C$ (where *C* represents *cancelled* trajectories). For any goal state $s_{g_B} \in \mathcal{G}_B$, s_{g_B} is absorbing with reward 1, then the value for s_{g_B} , is $V^{\pi_B}(s_{g_B}) = \frac{1}{1-\gamma}$. Now, any trajectory $\xi_{i_{\pi_B}} \in \mathcal{X}_g$ that ends being successful within allowed time-steps t_g , generates a return of $\frac{\gamma^{t_g-1}}{1-\gamma}$ and all trajectories belonging to \mathcal{X}_g^C returns always 0. Therefore, the expected value function expression can be written as expected discount sum of rewards for a trajectory ξ_{π_B} as,

$$V_{\mathcal{G}_B}^{\pi_B}\left(s_{(0,B)}\right) = \mathbf{E}_{\xi}[R(\xi_{\pi_B})]$$
$$= P(\xi_{\pi_B} \in \mathcal{X}_g)\mathbf{E}_{t_g}\left[\frac{\gamma^{t_g-1}}{1-\gamma}\right]$$

The above expression of value function contains two important attributes: (1) reaching a goal state from state $s_{(0,B)}$ with higher certainty and (2) reaching the goal state quickly [4], [15].

So when we build the prior healthy ensembles taking into consideration the actions taken by policy π_B and the effects of those actions while computing the value functions for any state *s*, we are taking two-fold advantages from prior domains—how much probable this trajectory is for reaching a goal state and how fast it converges to optimal solution, i.e completion of task with highest return possible. Thus, the value functions can be utilized to extend the ensemble attributes, since value functions implicitly carry information about past successful trajectories the agent created.

B. Behavior Policy: Partially Guidance

Based on the goal reaching probability and time based healthy ensemble setting discussed above, the prior behavior policy, in some known regions, would transit from one state to another state as an optimal policy would reach quickly the goal state from the new state. Thus, in that known region, the behavior policy would offer partially useful advice for the target policy π^+ to tackle unhealthy domain \mathcal{M}^+ . Let π^{*+} denote the optimal policy and $V_{\mathcal{G}}^{*+}(s)$ denote the optimal state value function, with respect to a fixed set of goals \mathcal{G}^+ . Then the behavior policy can only guide partially, if in some non-empty strict subset $s_g \subset S, \forall s_g \in S$, we have that $V_{\mathcal{G}}^{*+}(\xi_B(s_g, a)) > V_{\mathcal{G}}^{*+}(s_g)$, where ξ_B denotes the transition generated with behavior policy π_B . This is also visually depicted in Fig. 3, showing that the partial guidance from π_B acts as behavior ensemble and helps the agent to model the future policy fast by utilizing partial information of behavior samples and computing $\nabla \pi_{new}$ gradient in direction of prior ensembles.

C. Thompson Sampling

Exploitation of healthy ensemble needs to be balanced between those states whose utility is non-stationary or unknown to behavior policy π_B . We adapt Thompson Sampling [16], which is widely accepted Bayesian method for maintaining balance between exploration and exploitation, by modeling the uncertainty as a posterior distribution for each policy. Inspired by [4], we use Thompson sampling to model posterior distribution over expected state-action values within the critic network. The reason behind maintaining posterior distribution, instead of $q \forall Q_{\phi}$ estimates, the distribution is maintained over network weights (parameters) and consequently over Bayesian confidence. The weights are forward passed to the controller (as shown in Fig. 3), which then decides what action to take by evaluating action proposals and corresponding values.

D. Controller

It is potentially possible that the behavior policy π_B can distract our SRL agent from optimal learning, especially in those state-action choices which are unseen by π_B . Additionally, there is also a chance that our SRL agent formulates a virtual local minima, and switches excessively between $V(\phi) \sim \pi_B$ and $V(\theta) \sim \pi_{\theta}^{*+}$. To mitigate these risks, we setup a controller (see Fig. 3), that compare the policy parameters for both θ_i and ϕ_i , selected at timestep t_i , by performing Thompson sampling process between (θ_i, ϕ_i) and $(\theta_{i-i}, \phi_{i-i})$. The controller also utilizes posterior sampling to estimate the probabilistic state-action values of actions suggested by prior healthy ensemble as $\arg \max_{i \in 1,...,N} Q(s, a_i)$, if this value is larger than actor's action proposal value, the behavioral policy acts as the new policy at timestep *i*, otherwise the agent acts with the previous policy. We present more algorithm details in Algorithm 1

Algorithm 1: SRL Bayesian Inference Algorithm				
Require: π_B : Behaviour Policy S_t : Current Observation \mathcal{A} : Action Proposal				
while epoch $< maxEpoch$ do for $episode = \{1, 2,, n_{episodes}\}$ do for $steps = \{1, 2,, n_{steps}\}$ do $A \leftarrow [\pi_{\theta}(S_t), \pi_{\theta}^{-}(S_t)]$ #Observe Action Proposal $\theta_{t+1} \sim q(\phi)$ # Posterior dist sampling $TS(a_t) \leftarrow \arg\max_{i \in 1,N} Q_{\phi}(s, a)$ # Thompson # Get probability of higher expected value b/w two timsteps $p_a \leftarrow P[Q_{\phi}(S_t, TS(a_t)) > Q_{\phi}(S_t, TS(a_{t-1}))]$ if P_a then CNTRL : accept proposed action $choose a_t \leftarrow A$ else $ $ $V(s_t) \leftarrow value update E[G_t s_t]choose arg max_{\pi_{\theta}}(V(s, a))CNTRL Update:Loss: \phi \leftarrow \phi - \nabla_{\phi}L_{actor}(\phi)V(S_t) \leftarrow value updatereturn (a_t) to agentendend$				

V. SYSTEM OVERVIEW AND EXPERIMENTS

In this section we describe our simulation and physical frameworks that were utilized to conduct comparative testing of SRL and DDPG [3].

A. Hardware Platform

As shown in Fig. 1, we used a Phantomx® AX Metal Hexapod Mark III crawler robot to conduct our experiments. It consists of six legs and each leg comprises of three individually controlled joints named as "coxa", "femur", and "tibia". Altogether this crawler robot comprises 18 degrees of freedom (DOF), which make it versatile and robust for conducting our experiments. To read and write 18 joint angles of all 6 legs of our hexapod, we opted to use an U2D2 USB communication converter instead of a more conventional Arduino compatible Arbotix controller because the U2D2 allows faster data communication with the dynamixel motors attached at each joint. We also integrated a PID based position controller for each joint in order to

follow closed-loop feedback commands and shift within predetermined operating ranges.

B. Experiments overview

Video demo of our experiments can be viewed at: https://sites.google.com/view/survivalrl. Two pointers were placed in the workspace of our experiments and were marked as "start" and "finish". At first, to define the baseline of our crawler's movement, our hexapod was programmed to crawl from the start pointer to the finish pointer while following the tripod gait movement pattern of a six-legged insect. Afterwards, as depited in Fig. 1, the "tibia" joint of right middle leg was removed manually to evaluate how the robot adapts to its new structure and how well our proposed SRL learning algorithm performs in completing its defined trajectory. At last, the full right-middle leg of our hexapod was removed from the body. As a result, our algorithm tried to discover optimal policy to complete the full trajectory in a more complicated circumstance of losing 3 DOF. The same length trajectory was designed in the simulation profile for the hexapod to follow. A similar tripod gait pattern was implemented in the simulation profile to move the robot. Eventually, one tibia joint and one full leg was disconnected gradually from the simulation profile to evaluate the overall performance and reward-return of our designed controller. To testify the robustness and generalization of our algorithm and implementation, later, different legs were kept as a disconnected leg from the controller.

Along with random physical damage, we tested and validated SRL on three different categories of test-cases, (i) **Task_X**, (ii) **Task_XY** and (iii)**Task_P2P**.

- **Task_X**. In this easy mode, the agent's goal is to cover maximum distance along only X-axis, while its tibia joint is inoperable, i.e the robotic agent loses 1 degree of freedom as depicted in Fig. 4(b).
- **Task_Y**. This is the medium difficulty mode where the agent targets to exert smooth locomotion in 2-D environments and travels maximum distance while the one leg becomes totally damaged i.e it loses 3 DOF randomly as shown in Fig.4(c).
- **Task P2P** In this hard difficulty mode, the objective is to arrive at specific cordinates on a planar surface, overcoming the maneuvering hindrance due to missing one full leg randomly.

C. Simulation Environment

The algorithm was trained over generative sampling of state-action sequences from simulation environment. We utilized an integrated robot simulator that combines the 3D simulator Gazebo and the ROS robotic interface for all of our high-fidelity simulations. We adopted an open-source gazebo simulation model for Phanomx AX Metal Hexapod Mark III crawler robot (as shown in Fig. 4) that accurately models both the mechanical structure and the system dynamics of our target robot. Finally, the inter-process communication protocol (IPC) was based on ROS ecosystem to control parallel operation and ensure low latency feedback among simulation platform, physical robot and our SRL controller. The Gazebo model has been spawned as an independent ROS node while its communication was synced at the minimum rate of 20Hz to maintain handshaking message passing protocol.

D. Algorithmic Implementation

We presented SRL technique that leverages past experience as probabilistic bias towards on-going learning. The algorithmic implementation of our proposed method was significantly inspired by DDPG learning method [3] which is considered as one of well-established policy learning techniques for continuous robotic control. Moreover, our approach combines a probabilistic bias with conventional DDPG and computes posterior out of behavior sampleshence representing policies as Gaussian process instead of parametric mapping function. This bias enables the agent to exploit its existing policy as prior behavior ensemble and quickly learns a target policy to adapt to unforeseen domain setting. Technically, we introduced Bayesian posterior conditioned over behavior policy, that can incrementally estimate relevance between two domains, resulting in lesser exploration requirement and faster gradient updates over fewer samples.

We tested our approach on a hexapod robot with 18-DOF as shown in Fig.1. The robot learns its behavior policy π_B in a healthy or undamaged domain and this well-learned policy serves as the *healthy ensemble* to guide learning in *unhealthy* domain. π_B is generic tripod gait locomotion policy which enables the agent to travel very smoothly according to three different task trajectories mentioned in section V-B. In the next step, we explicitly introduce adversary by amputating random joints from the robot body to emulate random unhealthy domain settings. Such random perturbations in statespace or action-space is totally unknown to π_B . In brief, the robot gets damaged and loses its maneuvering capabilitiesturning π_B into a sub-optimal policy modeling in damaged domain. Both actor and critic network comprises of 4x1200 dense hidden layers, 1x600 hidden layer and a Bayesian dropout layer [17]. We list additional training parameters in the Table I below:

 TABLE I: Training Parameters

Training Parameters				
Max Episodes	7,000	Variance	$(0.9999)^t$	
Steps/Episode	2500	Learning Rate	$3e^{-2}$	
Replay Buffer	1600	Optimizer 1	ADAM	
MiniBatch Size	300	Optimizer 2	RMSProp	

E. Result Analysis

Our experiments are developed to empirically investigate following questions:

- 1) How SRL can utilize the behavior policy and healthy ensemble knowledge to infer posterior distribution as target policy?
- 2) How efficient SRL is when new domain differs significantly from prior ensemble settings?

As shown in Fig. 5, our proposed SRL methodology shows improved performance w.r.t sample efficiency (lesser episodic requirements), depicted as episodic returns in all three task scenarios compared to the baseline method. It can also be observed by looking at the Fig. 5 that standalone DDPG not only struggles to achieve optimality, but also it dips as exploration, in turn learning rate, narrows down with increasing number of episodes, trapping the baseline trend into local minima. Moreover, our Bayesian augmented SRL promisingly stabilizes the learning and exhibits less variance than the baseline. The dotted line in the plots define oracle reward threshold. This threshold can be marked as a finishing point, if reached, then an episode ends with success. We



(a) Hexapod Simulation Profile

(b) Right middle leg joint 'tibia' removed from body

(c) Right middle leg removed fully from body

Fig. 4: Simulation model of hexapod robot and level of damages by reducing numbers of DOF.



Fig. 5: Comparison between SRL and baseline for (a) Difficulty mode: Easy, Task: **Task_X**; (b) Difficulty mode: Medium, Task: **Task_Y**; Difficulty mode: Hard, Task: **Task_P2P**. 10 random seeds are used for each test.

can observe from the Fig. 5 that the SRL method is more effective than the baseline for handling sudden disturbances occurred to state-space of a robotic agent learning optimal policy to preserve functionality.

VI. CONCLUSION

Robotic systems suffer from so called "policy fragility", meaning that a learned robotic control policy typically can not effectively adapt to sudden changes in working environment or robotic agent itself. In sharp contrast, most living animals can quickly recover and find a compensatory behaviour when they are injured. Partially inspired by this observation, we propose the Survivable Reinforcement Learning (SRL) framework in order to construct optimized motion policy for a robotic agent, through integrating Bayesian priors as guided bias for future policy learning. We demonstrate promising performance of our proposed approach as an application for robotic agents working in a dynamically constrained environment and encountering random failures. In future research, we would like to apply the proposed SRL algorithm for multi-robot agents with high DoFs operating in same workspace with dynamic constraints and investigate their autonomous adaptive capability with uncertain physical damages to any agent operating in the environment.

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