

Optimal Coordination of Variable Speed Limits to Suppress Shock Waves

Andreas Hegyi, Bart De Schutter, and J. Hellendoorn

Abstract—When freeway traffic is dense, shock waves may appear. These shock waves result in longer travel times and in sudden large variations in the speeds of the vehicles, which could lead to unsafe situations. Dynamic speed limits can be used to eliminate or at least to reduce the effects of shock waves. However, coordination of the variable speed limits is necessary in order to prevent the occurrence of new shock waves and/or a negative impact on the traffic flows in other locations. In this paper, we present a model predictive control approach to optimally coordinate variable speed limits for freeway traffic with the aim of suppressing shock waves. First, we optimize continuous valued speed limits, such that the total travel time is minimal. Next, we include a safety constraint that prevents drivers from encountering speed limit drops larger than, e.g., 10 km/h. Furthermore, to get a better correspondence between the computed and applied control signals, we also consider discrete speed limits. We illustrate our approach with a benchmark problem.

Index Terms—Coordinated control, model predictive control (MPC), safe speed limits, shock waves, traffic control, variable speed limits.

I. INTRODUCTION

A. Problem Description

AS THE number of vehicles grows and the need for mobility increases on a world-wide scale, the frequency and duration of traffic jams in and around major cities increases. In the short term, the most effective measures in the battle against traffic congestion seem to be a selective construction of new roads—an option that is often not viable due to lack of space and/or budgetary means—and a more efficient use of the existing infrastructure through dynamic traffic management and control. One of the strategies used in dynamic traffic control is traffic signal control to obtain a smoother or better circulation of traffic in urban areas or on freeways traffic conditions are improved by regulating access to freeways or main roads (ramp metering), influencing route choice (variable message signs), and reducing (the probability of) congestion by using speed limits. In this paper, we will concentrate on dynamic traffic control to fight congestion.

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The authors are with the Delft Center for Systems and Control, Delft University of Technology, 2628 CD, Delft, The Netherlands (e-mail: A.Hegyi@DCSC.TUdelft.nl; B.DeSchutter@DCSC.TUdelft.nl; J.Hellendoorn@DCSC.TUdelft.nl).

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In practice, ramp metering setups and other dynamic traffic-management installations usually operate based on local data only. However, considering the effects of the measures on the network level instead and computing the control signals based on network-wide measurements and predictions offers many advantages. Therefore, we will consider a network-wide *coordination* of control measures based on network-wide data. Since the effect of a control measure on more distant locations might only be visible after some time, a *prediction* of the network evolution is also necessary to achieve optimal network control. The model predictive control (MPC) approach to dynamic traffic management presented in this paper contains both elements: network-wide coordination and prediction.

In this paper, we consider a special case of traffic-control measures: variable speed limits to reduce or eliminate shock waves. Also in this case, prediction and coordination are necessary for an effective control strategy. Prediction is needed for two reasons: first, if the formation or arrival of a shock wave in the controlled area can be predicted, then preventive measures can be taken. Second, the positive effect of speed limits on the traffic flow cannot be observed instantaneously,¹ so prediction is necessary and should at least include the point when the improvement can be observed.

Another advantage of a predictive controller is that it may prevent a certain type of instability. In control systems theory, it is well known that the delay between the appearance of a disturbance and the action of the controller may cause instabilities. By using predictive control, the disturbance can be anticipated, which may prevent these kinds of instabilities.

Besides prediction and coordination, the speed-limit control problem has other characteristics that impose certain requirements on the control strategy.

- 1) There is a direct relation between the outflow of a network and the total time spent (TTS) in the network, assuming that the traffic demand is fixed. Papageorgiou *et al.* [1] showed that in a traffic network an increase of outflow of 5% may result in a decrease of the total time spent in the network of 20%.² Since the congestion after a breakdown usually has an outflow that is 5%–10% lower than the capacity,³ we can conclude that any control method that resolves (reduces) congestion will at best achieve a flow improvement of approx-

¹We will see that the speed limits have to slow down a part of the traffic first, in order to dissolve the shock wave.

²This result is specific to this example; in other situations, the decrease of TTS could be different. Nevertheless, the example clarifies that there is a strong relation between outflow and TTS in the case of congested networks.

³This is the so-called capacity-drop phenomenon (see, e.g., [2]).

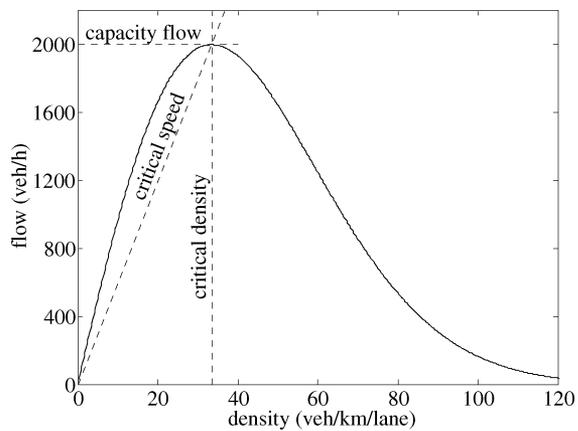


Fig. 1. Typical example of the fundamental diagram. The critical speed is the speed that corresponds to the maximum flow. The slope of the line connecting the origin and any point in the diagram represents the speed corresponding to that point.

imately 5%–10%, but this improvement can decrease the TTS significantly. This also means that the control strategy requires a high precision. For this reason and because there are always (unpredictable) disturbances present in a traffic network, *feedback control* is required.

- 2) Speed-limit signs used in practice display speed limits in increments of, e.g., 10 or 20 km/h. Therefore, the controller should produce discrete control signals.⁴
- 3) For safety, it is often required that drivers should not encounter a decrease in the displayed speed limit larger than a prespecified amount. The controller should be able to take this kind of constraints into account.

The control strategy presented in this paper takes these three requirements into account.

B. Literature Survey

In the literature, basically two views on the use of speed limits can be found. The first emphasizes the homogenization effect [4]–[8], whereas the second is more focused on preventing traffic breakdown by reducing the flow by means of speed limits [9]–[11].

The basic idea of homogenization is that speed limits can reduce the speed differences, by which a stabler (and safer) flow can be achieved. The homogenizing approach typically uses speed limits that are above the critical speed (i.e., the speed that corresponds to the maximal flow; see Fig. 1). Therefore, these speed limits do not limit the traffic flow, but only slightly reduce the average speed (and slightly increase the density). The homogenization approach can, in theory, increase the time to breakdown [12], but cannot suppress or resolve existing shock waves. According to field tests, homogenization results in a somewhat more stable and safer traffic flow, but no significant improvement of traffic volume measured [6], [8] (nor can be expected based on theory). Similar results are reported in the recently completed field test at Freeway A13 near Rotterdam, The

⁴In this paper, the main focus is on the procedure how discrete speed limits are found without solving a computationally demanding discrete optimization problem. A comparative study of different speed-limit step sizes can be found in [3].

Netherlands. The main effect of the homogenizing⁵ speed limits (in this case fixed 80 km/h) is the improvement of air quality and safety [13], [14]. An interesting feature of another field test performed on Freeway A1 near Deventer, The Netherlands, [8] is that the homogenizing speed limit was dynamically chosen according to a switching logic as a function of the prevailing traffic conditions. Also, this test resulted in similar findings regarding the effects on speed and flow. An extended overview of existing speed-limit systems that aim at reducing speed differentials is given by Wilkie [15].

The traffic breakdown prevention approach focuses more on preventing too high densities and also allows speed limits that are lower than the critical speed in order to limit the inflow to the jammed area. By resolving these high-density areas (bottle-necks), higher flow can be achieved in contrast to the homogenization approach.

Several control methodologies are used in the literature to find a control law for speed control, such as multilayer control [16], sliding-mode control [10], [11], and optimal control [17]. In [18], optimal control is approximated by a neural network in a rolling horizon framework. Other authors use (or simplify their control law to) a control logic in which the switching between the speed-limit values is based on traffic volume, speed, or density measurement [4]–[7], [11], [12]. In some cases, the switching between the speed-limit values is also based on special circumstances, such as weather and light conditions [4].

Some authors recognize the importance of anticipation in the speed control scheme. A pseudo-anticipative scheme is used in [11] by switching between speed limits based on the density of the neighboring downstream segment. Real predictions are used in [17], [18] and this is the only approach that results in a significant flow improvement.

Most application-oriented studies [5], [6], [8], [13], [14], [15] enforce speed limits, except for [4]. In [4], Zackor mentions that many drivers considered the speed limit as a recommendation, which has led to a slight increase of the mean speed. Enforcement is usually accepted by drivers if the speed-limit system leads to a more stable traffic flow.

Some approaches do explicitly model the effects of speed limits, but many of the models used in the literature represent the speed limits by a factor that downscales the fundamental diagram or assume that speed limits influence traffic states that have a lower speeds than the imposed speed limit (see, e.g., [10] and [17]). This can give too optimistic results (see Section III-B2). Therefore, we will propose a new macroscopic speed-limit model. We also introduce a model to express the difference in the drivers' anticipation to increasing or decreasing downstream densities in order to better reproduce shock waves.

C. Overview of this Paper

This paper extends the results of our conference papers [19], [20], in which we have already demonstrated the effectiveness of MPC with continuous speed limits against shock waves. In this paper, we include a safety constraint that prevents drivers from

⁵In this experiment, the main goal was to reduce noise and air pollution. However, the applied speed limits resulted in a more homogeneous traffic flow.

encountering speed limit drops larger than, e.g., 10 km/h. Furthermore, to get a better correspondence between the computed and applied control signals, we now consider discrete speed limits (see also [20]).

The organization of this paper is as follows. In Section II, we describe the problem of suppressing or reducing the effects of moving jams, as well as the basic idea behind our approach to solve this problem. In Section III, the basic ingredients of MPC for traffic-flow control are introduced and the prediction model including the extensions is presented. The proposed control method is applied to a benchmark problem in Section IV. Finally, the conclusion and topics for future research are stated in Section V.

II. PROBLEM STATEMENT

It is well known (see, e.g., [21]) that some type of traffic jams move upstream with approximately 15 km/h. These jams can remain stationary for a long time, so every vehicle that enters the freeway upstream of the jammed area will have to pass through the jammed area, which increases travel time. Besides the increased travel time, another disadvantage of the moving jams is that they are potentially unsafe.

To suppress shock waves, one can use speed limits in the following way. In some sections upstream of a shock wave, speed limits are imposed in order to reduce the inflow to the jammed area. When the inflow of the jammed area is reduced sufficiently, i.e., to a lower value than its outflow, the jam will eventually dissolve. In other words, the speed limits create a low-density wave (with a density lower than that in the uncontrolled situation) that propagates downstream. This low-density wave meets and compensates the high-density shock wave. As a result, the shock wave is reduced or eliminated.

The general idea of how dynamic speed limits can dissolve shock waves can also be explained in terms of the stable, metastable, and unstable traffic-flow states observed by Kerner and Rehborn [21]. Stable means that the traffic demand is such that any disturbance (no matter how large) will vanish without intervention. The metastable state corresponds with traffic demands in which both free-flow traffic and a shock wave can remain existent for a long time. In this state, in free flow, small disturbances will typically vanish, but large disturbances will create a shock wave. Unstable means that any disturbance (no matter how small) will trigger a shock wave. If speed limits are to dissolve the shock waves, the traffic flow must be in the metastable state, because in the stable state the disturbances will appear without control and in the unstable state any speed-limit change will initiate a new shock wave. In the metastable state, speed limits have the possibility (if the increment of the speed-limit values is sufficiently small) to spread out the shock wave into a disturbance that is small enough to vanish automatically.

Note that if the speed limits are optimized properly, they will never create a shock wave or an upstream queue that gives rise to delays that are higher than in the uncontrolled case. In this sense, “proper” optimization also means that the control objective includes all effects of the speed limits: the effects on the controlled freeway stretch and the (possible) upstream queues caused by the speed limits.

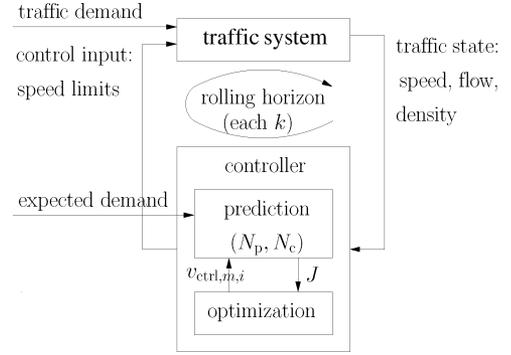


Fig. 2. Schematic view of the MPC structure.

In the following sections, we demonstrate how the proper speed limits can be found.

III. APPROACH

A. MPC

We use an MPC scheme to solve the problem of optimal coordination of speed limits (see Fig. 2). In MPC, at each time step k , the optimal control signal is computed (by numerical optimization) over a prediction horizon N_p . A control horizon N_c ($< N_p$) is selected to reduce the number of variables and to improve the stability of the system. (After the control horizon has been passed, the control signal is usually taken to be constant.) From the resulting optimal control signal, only the first sample $k + 1$ is applied to the process. In the next time step ($k + 1$), a new optimization is performed (with a prediction horizon that is shifted one time step ahead) and of the resulting control signal again only the first sample is applied and so on. This scheme, called rolling horizon, allows for updating the state from measurements or even for updating the model in every iteration step.

The advantage of updating the state is that this results in a controller that has a low sensitivity to prediction errors. Regularly updating the model results in an adaptive control system, which could be useful in situations in which the model significantly changes, such as in the case of incidents or changing weather conditions.

Besides the low sensitivity for prediction errors, this control scheme has another advantage that is a consequence of the prediction that is used. Prediction makes it possible to *perform temporarily suboptimally in order to gain more performance in the future*. In our case, we will see (what intuitively already can be expected) that, in order to suppress a shock wave, traffic flow has to be limited, but when the shock wave has dissolved, the traffic flow will be higher than otherwise.

For more information on MPC, see [22]–[24] and the references therein.

B. Prediction Model

The MPC procedure includes a prediction of the network evolution as a function of the current state and a given control input. For this prediction, we use an extended version of the destination-independent version of the macroscopic traffic-flow model METANET [25]–[27]. The extensions are introduced to model shock waves better and to include the effects of speed limits.

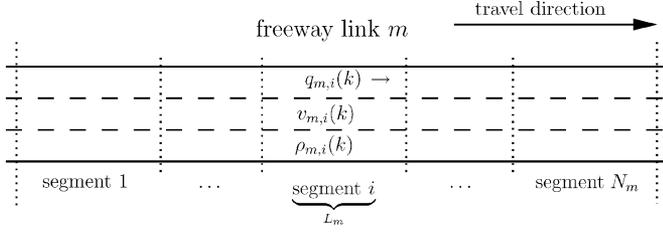


Fig. 3. In the METANET model, a freeway link is divided into segments. The main variables in the model are the average outflow of a segment $q_{m,i}(k)$, the average speed $v_{m,i}(k)$, the average density $\rho_{m,i}(k)$, and the segment length L_m .

Note that the MPC approach is generic; also other traffic models (that include the effect of the speed limit) could be used. The METANET model has been validated in several studies [28]–[30]. The reported validation results are satisfactory in general, except for the results in [29], which can be explained by the fact that the model in [29] was not calibrated before validation.

For the sake of brevity, we describe only those parts of the model that are relevant for interpreting and understanding the simulation results of our benchmark network (Section IV). See [25]–[27] for the complete METANET model (including lane drops and merging and weaving processes).

1) *Original METANET Model*: The METANET model represents a network as a directed graph with the links corresponding to freeway stretches. Each freeway link has uniform characteristics, i.e., no on- or off-ramps and no major changes in geometry. Each link m is divided into N_m segments of length L_m and has λ_m lanes (see Fig. 3). Each segment i of link m is characterized by the *traffic density* $\rho_{m,i}(k)$ (veh/lane/km), the *mean speed* $v_{m,i}(k)$ (km/h), and the *traffic volume* or *flow* $q_{m,i}(k)$ (vehicles/h), where k indicates the time instant $t = kT$ and T is the time step used for the simulation of the traffic flow (typically $T = 10$ s). The following equations describe the evolution of the network over time. The fundamental relationship between speed, flow and density is read as

$$q_{m,i}(k) = \rho_{m,i}(k) v_{m,i}(k) \lambda_m. \quad (1)$$

The conservation of vehicles is expressed by

$$\rho_{m,i}(k+1) = \rho_{m,i}(k) + \frac{T}{L_m \lambda_m} (q_{m,i-1}(k) - q_{m,i}(k)).$$

The mean speed equals the sum of mean speed at the previous time instance, a relaxation term, a convection term, and an anticipation term that expresses the speed decrease (increase) as drivers experience a density increase (decrease) downstream

$$\begin{aligned} v_{m,i}(k+1) = & v_{m,i}(k) + \frac{T}{\tau} (V(\rho_{m,i}(k)) - v_{m,i}(k)) \\ & + \frac{T}{L_m} v_{m,i}(k) (v_{m,i-1}(k) - v_{m,i}(k)) \\ & - \frac{\eta T}{\tau L_m} \frac{\rho_{m,i+1}(k) - \rho_{m,i}(k)}{\rho_{m,i}(k) + \kappa} \end{aligned} \quad (2)$$

where τ , η , and κ are model parameters and with

$$V(\rho_{m,i}(k)) = v_{\text{free},m} \exp \left[-\frac{1}{a_m} \left(\frac{\rho_{m,i}(k)}{\rho_{\text{crit},m}} \right)^{a_m} \right] \quad (3)$$

with a_m a model parameter and where the free-flow speed $v_{\text{free},m}$ is the average speed that drivers would assume if traffic would be flowing freely and the critical density $\rho_{\text{crit},m}$ is the density at which the traffic flow becomes unstable.

Origins are modeled with a simple queue model. The length of the queue $w_o(k)$ equals the previous queue length plus the demand $d_o(k)$, minus the outflow $q_o(k)$

$$w_o(k+1) = w_o(k) + T(d_o(k) - q_o(k)).$$

The outflow depends on the traffic conditions on the freeway and the capacity of the origin. The flow $q_o(k)$ is the minimum of the demand and the maximal flow that can enter the freeway given the mainstream conditions

$$q_o(k) = \min \left[d_o(k) + \frac{w_o(k)}{T}, Q_o \frac{\rho_{\text{max}} - \rho_{\mu,1}(k)}{\rho_{\text{max}} - \rho_{\text{crit},\mu}} \right] \quad (4)$$

where Q_o is the on-ramp capacity (vehicles/h) under free-flow conditions, ρ_{max} is the maximum density, and μ the index of the link to which the on-ramp is connected.

2) *Extensions*: Since the original METANET model does not explicitly describe the effect of speed limits, we have modified the equation for the desired speed (3) to incorporate speed limits. The second extension regards the modeling of a mainstream origin, which has a different nature than an on-ramp origin. The third extension describes the different effects of a positive or negative downstream density gradient on the speed [cf., the anticipation term in (2)].

In some publications, the effect of the speed limit is expressed by downscaling the desired speed–density diagram or using a model in which the speed limits influence traffic states that have a lower speeds than the imposed speed limit (see [10] and [17]). This changes the whole speed–density diagram, also for the states where the speed would otherwise be lower than the value of the speed limit. This means, e.g., that if the free-flow speed is 120 km/h and the displayed speed limit is 100 km/h, then the speed and flow of the traffic are reduced with the factor 100/120 even when the vehicles are traveling at 80 (< 100) km/h. An example of such a speed limit model is the one introduced by Cremer [31], shown in Fig. 4 (top), where the fundamental diagram is approximately scaled linearly by the speed limit. Furthermore, scaling down the desired speed also always reduces the capacity, while there is no reason to assume that a speed limit *above* the critical speed (speeds where the flow has not reached capacity yet) would reduce the capacity of the road [see Fig. 4 (top)].

The previous assumptions are rather unrealistic and exaggerate the effect of speed limits. To get a more realistic model for the effects of the speed limits, we assume that the desired speed is the minimum of the following two quantities: the desired speed based on the experienced traffic conditions (in the case of METANET: based on the experienced density) and the

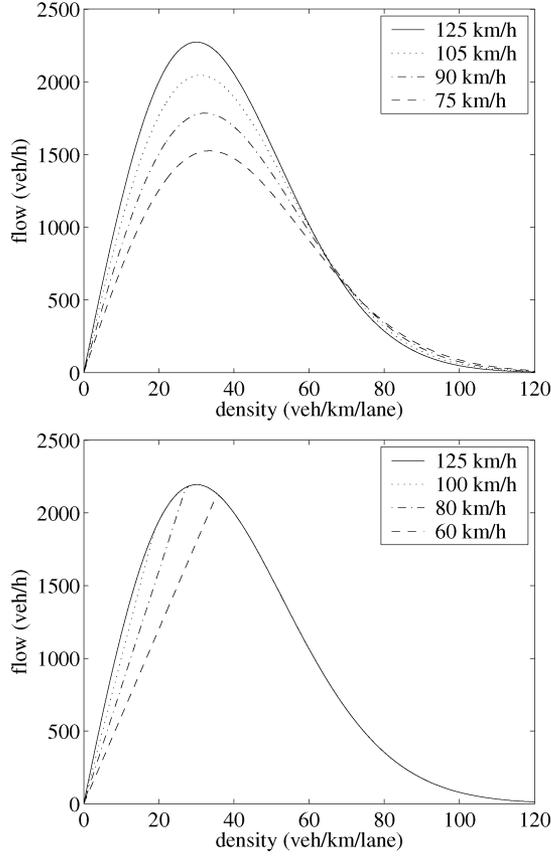


Fig. 4. Discussed speed limit models. Slopes correspond to speeds in these figures. Top: In the model proposed by Cremer [31], the flow-density relation is approximately scaled down linearly with the speed limit. This also influences traffic with a speed that is lower than the speed limit, which is unrealistic. Bottom: In the proposed speed limit model, the speed limit changes only the shape of the fundamental diagram for densities where the speed would have been higher (where the slope would have been steeper) than the applied speed limit. The straight lines represent the region where the speed limits do limit the traffic speed, for higher densities (corresponding to lower speeds than the speed limit) the new diagram coincides with the original one (solid line).

desired speed caused by the speed limit displayed on the variable message sign.⁶ A similar assumption has been made in [32]. The desired speed equation reads as shown in (5) at the bottom of the page, where $v_{\text{ctrl},m,i}(k)$ is the speed limit imposed on segment i , link m , at time k and the factor $(1 + \alpha)$ expresses the noncompliance, i.e., the factor that the desired speed is higher

⁶Although the quantitative validation would give a stronger confirmation of the correctness of this speed limit model, the quantitative arguments presented here and in [3] imply that the proposed model is more adequate than other existing ones. Model validation is a topic for future research.

than the displayed speed limit. See Fig. 4 (bottom) for an illustration. We refer the interested reader to [3] for a more extensive discussion of existing macroscopic speed-limit models.

The second extension is introduced to express the different natures of a mainstream origin link o and a regular on-ramp (the queue at a mainstream origin is in fact an abstraction of the sections upstream of the origin of the freeway network that we are modeling). To this end, we use a modified version of (4) with another flow constraint to model a mainstream origin link, because the inflow of a segment (and, thus, the outflow of the mainstream origin) can be limited by an active speed limit or by the actual speed in the first segment (when either of them is lower than the speed at critical density). Hence, we assume that the maximal flow equals the flow that follows from the speed-flow relationship from (1) and (3) with the speed equal to the speed limit or the actual speed in the first segment, whichever is smaller. So if o is the origin of mainstream link μ , then we have

$$q_o(k) = \min \left[d_o(k) + \frac{w_o(k)}{T}, q_{\text{lim},\mu,1}(k) \right]$$

where $q_{\text{lim},\mu,1}(k)$ is the maximal inflow determined by the limiting speed in the first segment of link μ (see the (6) at the bottom of the page) where $v_{\text{lim},\mu,1}(k) = \min(v_{\text{ctrl},\mu,1}(k), v_{\mu,1}(k))$ is the speed that limits the flow and $q_{\text{cap},\mu} = \lambda_\mu V(\rho_{\text{crit},\mu}) \rho_{\text{crit},\mu}$ is the capacity flow.

The third extension was introduced to be able to express the different reactions of drivers to varying downstream densities, since the effect of a higher downstream density is usually stronger than the effect of a lower downstream density. The sensitivity of the speed to the downstream density is expressed by parameter η . In (2), η is a global parameter and has the same value for all segments. However, here we take different values for $\eta_{m,i}(k)$, depending on whether the downstream density is higher or lower than the density in the actual segment

$$\eta_{m,i}(k) = \begin{cases} \eta_{\text{high}}, & \text{if } \rho_{m,i+1}(k) \geq \rho_{m,i}(k) \\ \eta_{\text{low}}, & \text{if } \rho_{m,i+1}(k) < \rho_{m,i}(k). \end{cases}$$

C. Objective Function

The objective function consist of two terms, a term for the TTS and a term that penalizes large control signal variations. In the TTS term, the total number of vehicle hours spent on the freeway segment and in the origin queue are summed. The control signal variation penalty term is included to express the preference for smooth signals. The tradeoff between these two

$$V(\rho_{m,i}(k)) = \min \left((1 + \alpha)v_{\text{ctrl},m,i}(k), v_{\text{free},m} \exp \left[-\frac{1}{a_m} \left(\frac{\rho_{m,i}(k)}{\rho_{\text{crit},m}} \right)^{a_m} \right] \right) \quad (5)$$

$$q_{\text{lim},\mu,1}(k) = \begin{cases} \lambda_\mu v_{\text{lim},\mu,1}(k) \rho_{\text{crit},\mu} \left[-a_\mu \ln \left(\frac{v_{\text{lim},\mu,1}(k)}{v_{\text{free},m}} \right) \right]^{1/a_\mu}, & \text{if } v_{\text{lim},\mu,1}(k) < V(\rho_{\text{crit},\mu}) \\ q_{\text{cap},\mu}, & \text{if } v_{\text{lim},\mu,1}(k) \geq V(\rho_{\text{crit},\mu}) \end{cases} \quad (6)$$

terms is expressed by the relative weighting of these terms in the objective function. Since the primary aim of the controller is to minimize the TTS, the weights are chosen such that the TTS term weighted to be more important.

Note that we distinguish between the controller time step length T_c and the simulation time step length T and between the controller time step counter k_c and the model time step counter k . We assume that the controller time step length is an integer multiple of the simulation time step length $T_c = MT$, with M a positive integer.

$$J(k_c) = T \sum_{k=Mk_c}^{M(k_c+N_p)-1} \left\{ \sum_{(m,i) \in I_{\text{links}}} \rho_{m,i}(k) L_m \lambda_m + \sum_{o \in I_{\text{orig}}} w_o(k) \right\} + \alpha_{\text{speed}} \sum_{l=k_c}^{k_c+N_c-1} \sum_{(m,i) \in I_{\text{ctrl}}} \left(\frac{v_{\text{ctrl},m,i}(\ell) - v_{\text{ctrl},m,i}(\ell-1)}{v_{\text{free},m}} \right)^2$$

where I_{links} is the set of indexes of all pairs of segments and links, I_{orig} is the set of all origins, and I_{ctrl} is the set of pairs of indexes (m, i) of the links and segments where speed control is applied. This objective function contains a term for the TTS and a term that penalizes abrupt variations in the speed-limit control signal. The variation term is weighted by the nonnegative weight parameter α_{speed} .

In conventional MPC, heuristic tuning rules have been developed to select appropriate values for N_p and N_c [23]. However, these rules cannot be straightforwardly applied to the traffic-flow control framework presented in this section. We will select appropriate values for N_p and N_c based on considerations discussed in [33].

D. Constraints

In general, for the safe operation of a speed-control system, it is required that the maximum decrease in speed limits that a driver can encounter (v_{maxdiff}) is limited. There are three situations in which a driver can encounter a different speed limit value:

- 1) when the speed limit changes in a given segment (and there are more speed limit signs on the same segment);
- 2) when a driver enters a new segment;
- 3) when the driver enters a new segment and the speed limit changes.

The maximum speed difference constraints for the three situations are formulated as follows:

$$v_{\text{ctrl},m,i}(l-1) - v_{\text{ctrl},m,i}(l) \leq v_{\text{maxdiff}} \\ \text{for all } m, i, l \text{ such that } (m, i) \in I_{\text{ctrl}} \text{ and} \\ l \in [k, \dots, k + N_c - 1]$$

$$v_{\text{ctrl},m,i}(l) - v_{\text{ctrl},m,i+1}(l) \leq v_{\text{maxdiff}} \\ \text{for all } m, i, l \text{ such that } (m, i) \in I_{\text{ctrl}} \\ (m, i+1) \in I_{\text{ctrl}} \text{ and } l \in [k, \dots, k + N_c - 1]$$

$$v_{\text{ctrl},m,i}(l-1) - v_{\text{ctrl},m,i+1}(l) \leq v_{\text{maxdiff}} \\ \text{for all } m, i, l \text{ such that } (m, i) \in I_{\text{ctrl}} \\ (m, i+1) \in I_{\text{ctrl}} \text{ and } l \in [k, \dots, k + N_c - 1].$$

In addition to the safety constraints, a minimum value v_{ctrlmin} for the speed limits could be imposed

$$v_{\text{ctrl},m,i}(l) \geq v_{\text{ctrlmin}} \quad \text{for all } (m, i) \in I_{\text{ctrl}}; \\ l \in [k, \dots, k + N_c - 1].$$

In practice, the variable speed limit signs display speed limits in increments of, e.g., 10 or 20 km/h. Therefore, the controller should produce discrete control signals. This is expressed by constraint

$$v_{\text{ctrl},m,i}(l) \in \mathcal{V}_{m,i} \quad \text{for all } (m, i) \in I_{\text{ctrl}}; \\ l \in [k, \dots, k + N_c - 1]$$

where $\mathcal{V}_{m,i}$ is the set of discrete speed limit values in segment i of link m .

IV. BENCHMARK PROBLEM

In order to illustrate the control framework presented before, we will apply it now to a benchmark problem.

A. Setup

The benchmark setup consists of an origin, a freeway link of 12 km and a destination, similar to Fig. 3. The mainstream origin has two lanes with a capacity of 2000 vehicles/h each. The freeway link has two lanes and consists of 12 segments of 1 km each. Segments 1–5 and segment 12 are uncontrolled, while segments 6–11 are equipped with a variable message sign where speed limits can be set. We use the same network parameters as in [25] $T = 10$ s, $\tau = 18$ s, $\kappa = 40$ vehicles/lane/km, $\rho_{\text{max}} = 180$ vehicles/lane/km, $\rho_{\text{crit}} = 33.5$ vehicles/lane/km, $a_m = 1.867$ and $v_{\text{free}} = 102$ km/h.

Furthermore, we take $\eta_{\text{high}} = 65$ km²/h, $\eta_{\text{low}} = 30$ km²/h, $\alpha = 0.05$ and $\alpha_{\text{speed}} = 2$. Note that these parameter values (and the speed limit and anticipation model) are not yet validated against real data.⁷

For the variable speed limits, we have assumed that they can change once per minute and that they cannot be less than $v_{\text{ctrlmin}} = 50$ km/h. This is imposed as a hard constraint in the optimization problem. For the cases in which there is a safety constraint present, $v_{\text{maxdiff}} = 10$ km/h.

The input of the system is the traffic demand at the upstream end of the link and the (virtual) downstream density at the downstream end of the link. The traffic demand (inflow) has a constant value of 3900 vehicles/h, close to capacity (4000 vehicles/h). The downstream density equals the steady-state value of 28 vehicles/km, except for the pulse that represents the shock wave. The pulse was chosen large enough to cause a back-propagating wave in the segments [see Figs. 5 and 6 (top)]. It is assumed that the upstream demand and downstream density is known or predicted by an external algorithm. In practice, a combination of traffic measurements outside the controlled area and historical data could be used for prediction.

⁷In the future, validation will be performed based on the data of the DYVERS experiment [8], where the speed limits were strictly enforced; this data is expected to give a good indication of the achievable flow limitation of dynamic speed limits. Nevertheless, the most relevant effect, namely the capacity drop, is reproduced.

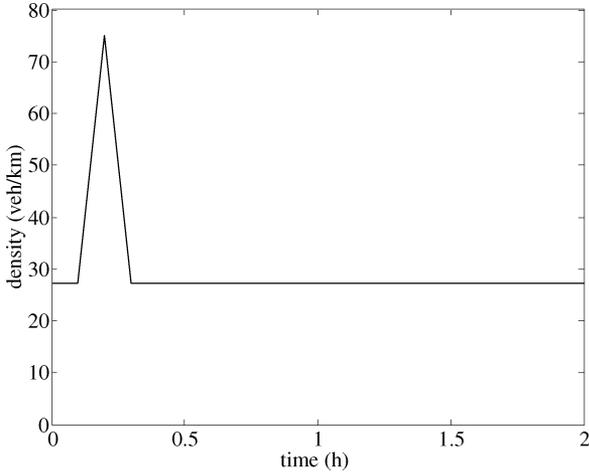


Fig. 5. Downstream density scenario considered in the experiments.

For this scenario N_p and N_c will be tuned and the performance (TTS) of the continuous and discrete controls with or without safety constraints are examined. In the discrete control case, the control values $v_{ctrl,m,i}$ are in the set $\mathcal{V}_{m,i} = \mathcal{V} = \{50, 60, 70, 80, 90, 100, 110\}$ for all $(m, i) \in I_{ctrl}$.

The solution of the continuous speed-control problem is calculated by the Matlab implementation of the sequential quadratic programming (SQP) algorithm `fmincon`. To get the discrete control signal, the continuous signal is rounded to a value in \mathcal{V} . Three different types of rounding are examined: The first (“round”) rounds the continuous control values to the nearest discrete value in \mathcal{V} , the second (“ceil”) rounds upward to the nearest discrete value in \mathcal{V} , and the third (“floor”) rounds downward to the nearest discrete value in \mathcal{V} .

This method of obtaining discrete control signals is heuristic but fast. It is also possible to use discrete optimization techniques such as tabu search, simulated annealing, or genetic algorithms, but since (as we will see) for this setup and input the discretization method results in a performance that is comparable to that of the continuous version, it is not necessary to do so.

Note that it is not difficult to prove that the result of all of the three types of rounding will satisfy the safety constraints if the continuous signal satisfies them and if $v_{maxdiff}$ is a multiple of the discretization step of the speed limits (here, multiple of 10 km/h). Since it does not make much sense to set $v_{maxdiff}$ to another value than a multiple of the discretization step, this condition should not be a limitation.

The rolling horizon strategy is now implemented as follows. After the discretization, the first sample of the control signal is applied to the traffic system and then the optimization–discretization steps are repeated. Note that this approach does not yield the same evolution and control signals as an approach in which first the continuous signal is computed (using the rolling horizon approach) for the entire simulation period at once, rounded, and then applied for the whole simulation period. This is because, in the first approach, the different traffic behavior caused by the discretization is already taken into account in the each subsequent MPC iteration.

In the next section, we will compare the performance of the discrete control to the performance achieved by the continuous

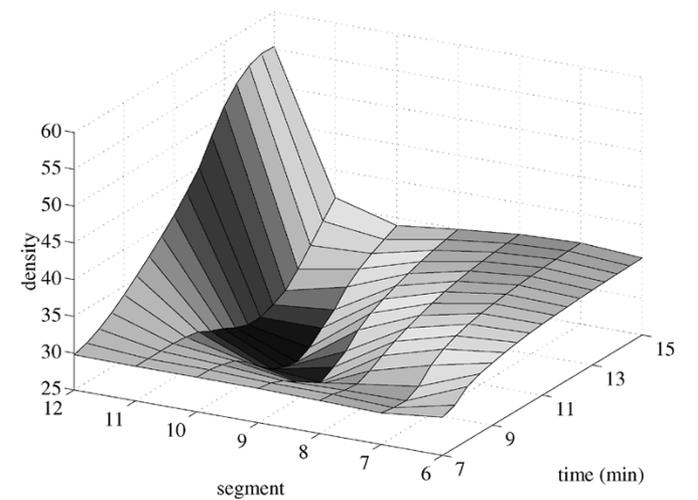
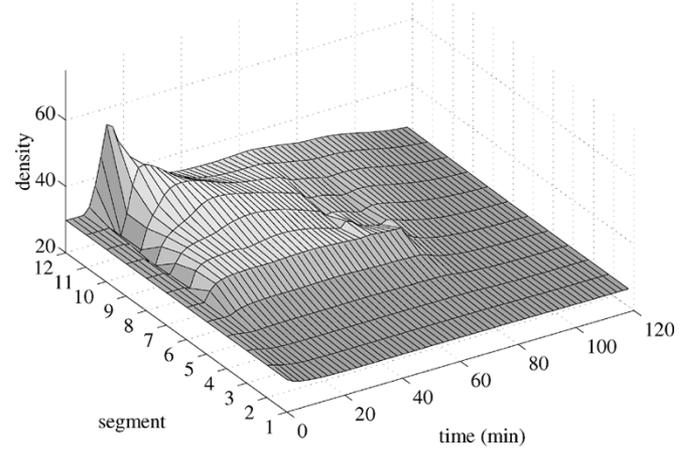
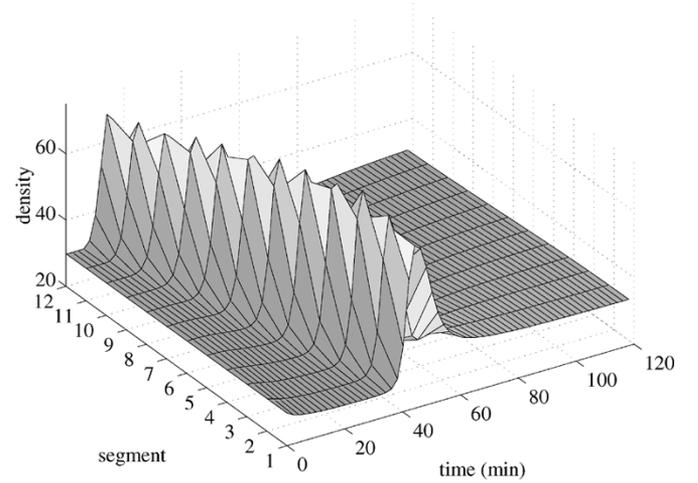


Fig. 6. (Top) Shock wave propagates through the link in the no-control case. In the coordinated control case, (middle) the shock wave disappears after approximately 90 min and (bottom) the zoom-in on the dip for the coordinated control case.

valued control without constraints and the effect of introducing the safety constraints is examined.

B. Results

The results of the simulations of the no-control and control cases with continuous speed limits without constraints is dis-

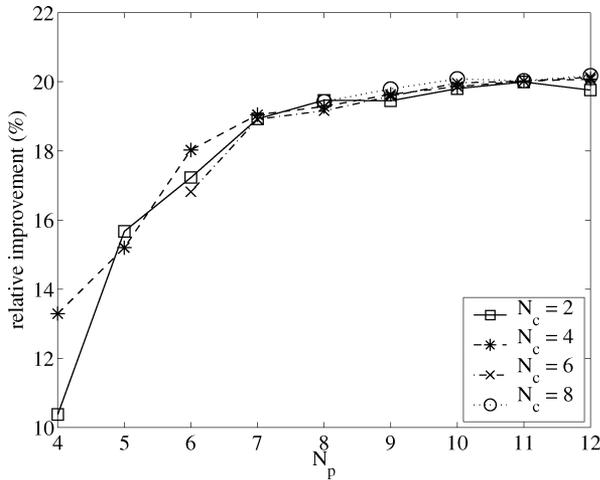


Fig. 7. Relative improvement of the performance (total time spent) in the continuous unconstrained case compared to the no-control case as a function of N_p for several values of N_c . The sensitivity to N_p is much higher than that to N_c .

played in Fig. 6 (top and middle). Since high densities correspond to low speeds and low densities to high speeds, the corresponding speeds plots (not shown here) have roughly the same shape as the plots in Fig. 6, but with the vertical axis flipped.

The propagation speed of the shock wave in the uncontrolled simulation is around 22 km/h (11 km/30 min), which is somewhat higher than the 15–20 km/h range reported in the literature⁸ [34], [21].

In the controlled case, the shock wave disappears after approximately 90 min, while in the no-control case, the shock wave travels through the whole link. The speed limits are active in segments 6–10; the speed limit in segment 11 has higher values than the critical speed and is not limiting the flow (see Fig. 8). The active speed limits start to limit the flow at $t = 5$ min and create a low-density wave traveling downstream [see the small dip in Fig. 6 (middle and bottom)]. This low-density wave meets the shock wave and reduces its density just enough to stop it. The tail of the shock wave has a fixed location while the head dissolves into free-flow traffic and the shock wave eventually dissolves completely.

The speed limits persist until the shock wave (to be precise, the high-density region) is completely dissolved. The speed limits in Fig. 8 start to increase after $t = 35$ min and return gradually to a high value that is not limiting the flow anymore. Since the shock wave is completely dissolved within the freeway stretch, traffic upstream the stretch will not be influenced by the control. Note, however, that in the uncontrolled situation the shock wave does propagate upstream and will impede the upstream traffic.

Note that the speed-limit values after 90–120 min are in the range of 70–100 km/h. These values do not limit the flow because they are higher than the critical speed (60 km/h in our

⁸This is probably the consequence of the chosen model parameters that are not calibrated in this study (e.g., η_{high} and η_{low}). The necessity of calibration is a topic for future research. What is relevant in this paper is the occurrence of the capacity drop: the outflow of the shock wave is less than the freeway capacity. Therefore, resolving the shock wave will result in a higher flow and an improvement of the total time spent.

TABLE I
RELATIVE IMPROVEMENT OF THE PERFORMANCE (TTS) FOR SEVERAL COMBINATIONS OF N_p AND N_c AND FOR THE CONTINUOUS SPEED LIMITS AND THE THREE DISCRETE SPEED LIMITS: “ROUND”, “CEIL”, AND “FLOOR”; WITHOUT SAFETY CONSTRAINTS

Horizon		Relative improvement (%)			
N_p	N_c	continuous	round	ceil	floor
9	4	19.6	17.5	17.9	-2.2
9	6	19.6	19.1	18.9	3.9
9	8	19.8	15.0	17.6	6.9
10	4	19.9	17.9	19.6	-1.1
10	6	20.0	19.6	19.3	2.9
10	8	20.1	15.2	18.3	5.9
11	4	20.0	18.0	19.8	-1.1
11	6	20.0	17.7	19.8	1.3
11	8	20.0	19.9	19.4	5.5
12	4	20.1	15.5	20.0	-2.2
12	6	20.1	19.7	20.0	1.3
12	8	20.2	19.8	20.0	5.7

TABLE II
RELATIVE IMPROVEMENT OF THE PERFORMANCE (TTS) FOR SEVERAL COMBINATIONS OF N_p AND N_c , AND FOR THE CONTINUOUS SPEED LIMITS AND THE THREE DISCRETE SPEED LIMITS: “ROUND”, “CEIL”, AND “FLOOR”; WITH SAFETY CONSTRAINTS

Horizon		Relative improvement (%)			
N_p	N_c	continuous	round	ceil	floor
9	4	19.4	16.4	18.0	0.2
9	6	19.5	19.3	19.0	12.3
9	8	19.4	18.4	11.4	11.9
10	4	19.5	15.5	18.5	1.4
10	6	19.6	19.4	18.0	9.0
10	8	19.7	19.1	17.2	11.0
11	4	19.6	15.4	18.2	0.4
11	6	19.7	19.8	19.6	7.3
11	8	19.9	19.7	19.3	5.5
12	4	19.7	14.7	19.3	1.8
12	6	19.9	19.9	19.7	12.5
12	8	19.9	19.3	19.6	13.4

case) and neither do they limit the traffic speed, because the traffic speeds (not shown here) were lower than the displayed speed limits.

The TTS was 1835.3 vehicles/h in the no-control case and 1466.7 vehicles/h in the controlled (continuous, unconstrained) case, which is an improvement of 20.1%.

The relative improvement of the performance as a function of N_p and N_c is shown in Fig. 7. The performance depends stronger on N_p , but for $N_p \geq 10$ (which corresponds to 10 min and is somewhat larger than the maximum travel time from segment 6 to the exit of the link), the graphs become nearly flat. We select $N_p = 10$ and $N_c = 8$ for further analysis.

The result of the several types of discretization is shown in Table I for the simulations without safety constraints and in Table II for the simulations with safety constraints. The performance loss caused by the discretization is small in the “round” and “ceil” cases, but large for “floor.” The cause for this performance degradation in the latter case is probably that rounding the speed limits downward limits the flow too much. This is also in accordance with the fact that the performance of “floor” is better in the constrained case than in the unconstrained case, because the constraints prevent too low speed limits, so the downward rounded version will on the average also be higher, resulting in a higher flow. In the other cases, the inclusion of the

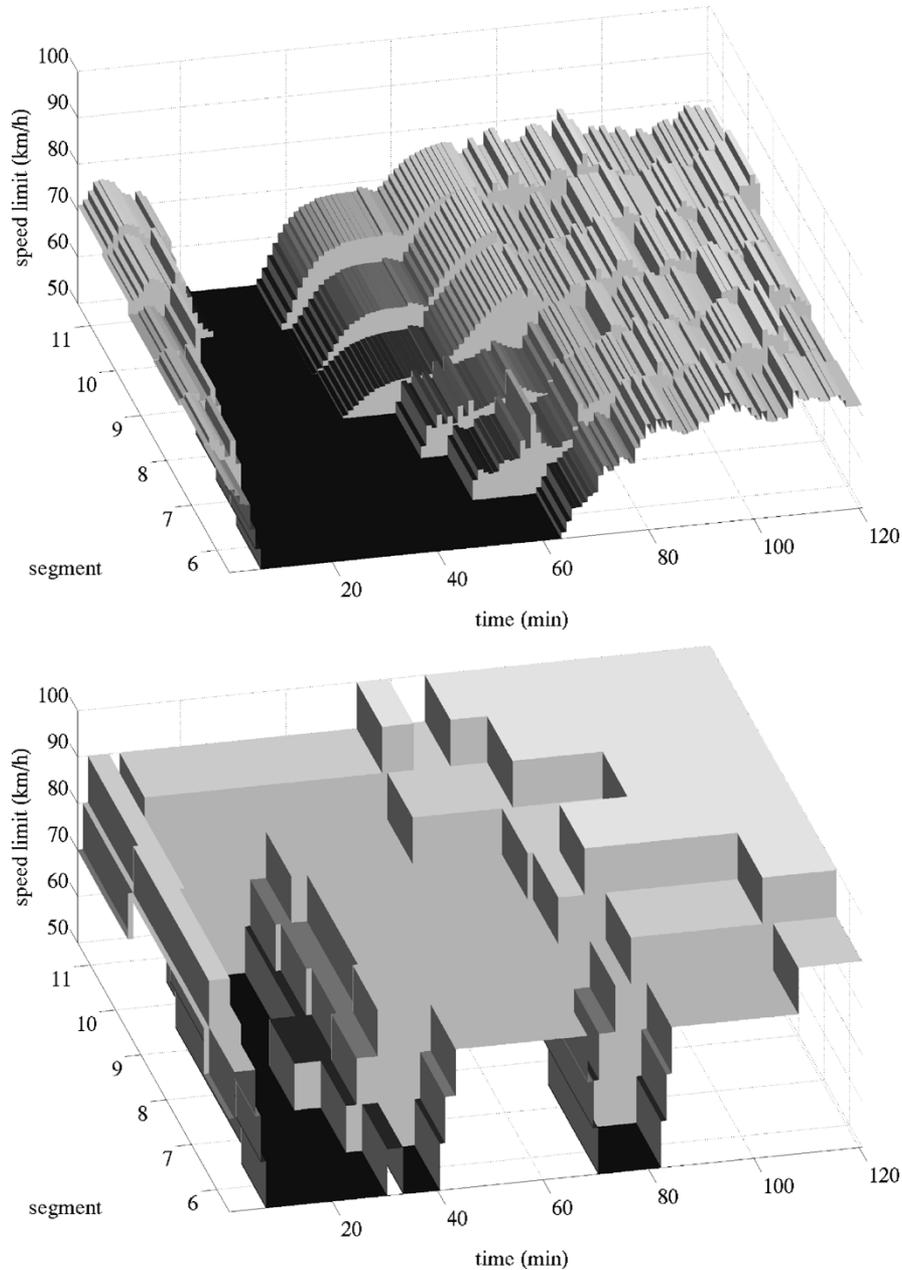


Fig. 8. Speed limits for the continuous case without safety constraints and $N_p = 10$, $N_c = 8$ (top). The speed limits for the discrete (“ceiling”) case with safety constraints and $N_p = 10$, $N_c = 8$ (bottom).

constraints result in a small performance loss, which is in accordance with the general expectation that the introduction of extra constraints usually results in lower performance.

The performance improvement for $N_p = 10$, $N_c = 8$ in the constrained “ceiling” case is 17.3%, which is close to the improvement of the unconstrained “ceiling” case (18.3%) and comparable to the improvement of 20.1% in the unconstrained continuous case. Fig. 8 (bottom) shows the values of the optimal speed limits in the discrete (“ceiling”) case with safety constraints and $N_p = 10$, $N_c = 8$.

The computation time varied between 3–25 min on a 500 MHz Pentium III PC, which is at least four times faster than real time. It is expected that the computation time varies linearly with the number of segments and the length of the prediction horizon and exponentially with the number of control inputs and the control horizon.

The fact that the same traffic-flow model was used as a prediction model and as the model for the controlled traffic system may have influenced (probably positively) the achievable improvement of the TTS. Nevertheless, the presented simulations give an indication that shock waves can be resolved by dynamic flow-limiting speed limits and that a significant improvement of traffic flow and travel times can be achieved. In case there is a mismatch between the process model and the controller model, several techniques exist to ensure robustness [35].

V. CONCLUSION AND FUTURE RESEARCH

We have applied MPC to optimally coordinate variable speed limits with the aim of suppressing shock waves. The purpose of the control was to find the control signals that minimize the total time that vehicles spend in the network.

We have applied the developed control framework to a benchmark network consisting of a link of 12 km, where six segments of 1 km are controlled by speed limits. It was shown that coordinated control with continuous speed limits (base case) is effective against shock waves.

The performance loss caused by discrete speed limits and the inclusion of safety constraints was examined. The performance of the discrete safety-constrained speed limits was comparable with the base case if the discrete speed limits were generated by “round” or “ceil.” In all of these cases, the coordination of speed limits eliminated the shock wave entering from the downstream end of the link. The coordinated case resulted in a network where the outflow was sooner restored to capacity and in an improvement (decrease) of the total time spent of 17.3%.

Topics for further research include the following:

- comparison of the discrete MPC approach with other existing approaches;
- further examination of the tradeoff between efficiency and optimality for rounding versus full discrete optimization;
- study of a real freeway stretch, including model calibration with real data, the examination of the necessity of online calibration, simulation of other setups and scenarios, and validation of the new modeling assumptions regarding the speed limits and the main stream origin;
- further investigation of the effectiveness of MPC for optimal coordination of speed limits for a wider range of scenarios, networks, traffic-flow models, and/or model parameters; explicit inclusion of modeling errors, different internal and external models, and unpredicted disturbances (demands);
- further study of the capacity drop and metastability phenomena;
- inclusion of extra control measures in addition to speed limits (such as ramp metering, dynamic lane assignment, route guidance, reversible lanes, etc.);
- investigation of issues relevant for real-life application, such as the extension of the control system with a traffic state estimation (for which a Kalman filtering approach could be followed similarly to [36]) and a traffic demand prediction module, investigation of the robustness of the control approach against unknown disturbances, state estimation errors, and a model mismatch; investigation of the requirements of the physical layout of the freeway stretch and the estimation of the expected improvement for a real scenario.

REFERENCES

- [1] M. Papageorgiou, J. Blosseville, and H. Hadj-Salem, “La fluidification des roclades de l’Ile de France: Un projet d’importance,” Tech. Rep., Dynamic Syst. Sim. Lab., Tech. Univ. Crete, Chania, Greece, Internal Rep. 1998-17, 1998.
- [2] M. J. Cassidy and R. L. Bertini, “Some traffic features at freeway bottlenecks,” *Transport. Res. B*, vol. B33, pp. 25–42, 1999.
- [3] A. Hegyi, “Model predictive control for integrating traffic control measures,” Ph.D., Delft Univ. Technol., Delft, The Netherlands, 2004.
- [4] H. Zackor, “Self-sufficient control of speed on freeways,” in *Proc. Int. Symp. Traffic Control Systems*, vol. 2A, Berkeley, CA, Aug. 1979, pp. 226–249.
- [5] S. Smulders, “Control by variable speed signs—The Dutch experiment,” in *Proc. Inst. Elect. Eng. Sixth Int. Conf. Road Traffic Monitoring and Control*, London, U.K., Apr. 1992, pp. 99–103.
- [6] E. v. d. Hoogen and S. Smulders, “Control by variable speed signs: Results of the Dutch experiment,” in *Proc. Inst. Elect. Eng. 7th Int. Conf. Road Traffic Monitoring and Control*, vol. 391, London, U.K., Apr. 1994, pp. 145–149.
- [7] E. J. Hardman, “Motorway speed control strategies using SISTM,” in *Proc. Road Traffic Monitoring and Control*, vol. 422, Apr. 1996, pp. 169–172.
- [8] “DHV Milieu en Infrastructuur BV, Eindevaluatie SlimRijden—Verkeerskundig—En Weggebruikersevaluatie (Final Evaluation of the Project SlimRijden (SmartDriving) —From a Traffic Engineering and a Road Users’ Point of View),” (in Dutch), AVV Traffic Res. Centre, Dutch Ministry of Transport, Public Works and Water Management, 2003.
- [9] C.-C. Chien, Y. Zhang, and P. A. Ioannou, “Traffic density control for automated highway systems,” *Automatica*, vol. 33, no. 7, pp. 1273–1285, 1997.
- [10] H. Lenz, R. Sollacher, and M. Lang, “Nonlinear speed-control for a continuum theory of traffic flow,” in *Proc. 14th World Cong. IFAC*, vol. Q, Beijing, China, 1999, pp. 67–72.
- [11] —, “Standing waves and the influence of speed limits,” in *Proc. Eur. Control Conf.*, Porto, Portugal, 2001, pp. 1228–1232.
- [12] S. Smulders, “Control of freeway traffic flow by variable speed signs,” *Transport. Res. B*, vol. 24B, no. 2, pp. 111–132, 1990.
- [13] “Evaluatie 80 km/uur-Maatregel A13 Overschie, Doorstroming and Verkeersveiligheid (Evaluation of the 80 km/h Measure on the A13 at Overschie, Traffic Flow and Safety),” (in Dutch), Rijkswaterstaat Directie Zuid-Holland, Tech. Rep., Ministry of Transport, Public Works and Water Management, Rijkswaterstaat, Directie Zuid-Holland – VIV, 2003.
- [14] J. Wesseling, K. Hollander, S. Teeuwisse, M. Keuken, H. Spoelstra, R. Gense, E. Burgwal, L. Hermans, J. Voerman, P. Kummu, and J. Elshout, “Onderzoek Naar de Effecten van de 80 km/h-Maatregel Voor de A13 op de Luchtkwaliteit in Overschie (Investigation of the Effects of the 80 km/h Measure at the A13 on the Air Quality in Overschie),” (in Dutch), Tech. Rep., TNO (on behalf of Rijkswaterstaat, Directie Zuid-Holland), 2003.
- [15] J. K. Wilkie, “Using Variable speed limit signs to mitigate speed differentials upstream of reduced flow locations,” Tech. Rep., Dept. Civil Eng., Texas A& M Univ., 1997.
- [16] P. Y. Li, R. Horowitz, L. Alvarez, J. Frankel, and A. M. Robertson, “Traffic flow stabilization,” in *Proc. Amer. Control Conf.*, Seattle, WA, Jun. 1995, pp. 144–149.
- [17] A. Alessandri, A. Di Febbraro, A. Ferrara, and E. Punta, “Nonlinear optimization for freeway control using variable-speed signaling,” *IEEE Trans. Veh. Technol.*, vol. 48, no. 6, pp. 2042–2052, Nov. 1999.
- [18] A. Di Febbraro, T. Parisini, S. Sacone, and R. Zoppoli, “Neural approximations for feedback optimal control of freeway systems,” *IEEE Trans. Veh. Technol.*, vol. 50, no. 1, pp. 302–312, Jan. 2001.
- [19] P. Breton, A. Hegyi, B. De Schutter, and H. Hellendoorn, “Shock wave elimination/reduction by optimal coordination of variable speed limits,” in *Proc. IEEE 5th Int. Conf. Intelligent Transportation Systems*, Singapore, Sep. 2002, pp. 225–230.
- [20] A. Hegyi, B. De Schutter, and H. Hellendoorn, “Optimal coordination of variable speed limits to suppress shock waves,” in *Proc. 82nd Ann. Meeting Transportation Research Board*, Jan. 2003.
- [21] B. S. Kerner and H. Rehborn, “Experimental features and characteristics of traffic jams,” *Phys. Rev. E*, vol. 53, no. 2, pp. R1297–R1300, 1996.
- [22] E. Camacho and C. Bordons, *Model Predictive Control in the Process Industry*. Berlin, Germany: Springer-Verlag, 1995.
- [23] J. Maciejowski, *Predictive Control with Constraints*. Harlow, U.K.: Prentice-Hall, 2002.
- [24] F. Allgöwer, T. Badgwell, J. Qin, J. Rawlings, and S. Wright, “Nonlinear predictive control and moving horizon estimation – An introductory overview,” in *Advances in Control: Highlights of ECC ’99*, P. Frank, Ed. London, U.K.: Springer, 1999, pp. 391–449.
- [25] A. Kotsialos, M. Papageorgiou, and A. Messmer, “Optimal coordinated and integrated motorway network traffic control,” in *Proc. 14th Int. Symp. Transport. Traffic Theory (ISTTT)*, Jerusalem, Israel, Jul. 1999, pp. 621–644.

- [26] M. Papageorgiou, J.-M. Blosseville, and H. Haj-Salem, "Modeling and real-time control of traffic flow on the southern part of Boulevard Périphérique in Paris: Part II: Coordinated on-ramp metering," *Transport. Res. A*, vol. 24A, no. 5, pp. 361–370, 1990.
- [27] A. Messmer, "METANET—A simulation program for motorway networks," *Dynamic Syst. Sim. Lab.*, Tech. Univ. Crete, Chania, Greece, 2001.
- [28] M. Papageorgiou, J.-M. Blosseville, and H. Hadj-Salem, "Modeling and real-time control of traffic flow on the southern part of Boulevard Périphérique in Paris: Part I: Modeling," *Transport. Res. A*, vol. 24A, no. 5, pp. 345–359, 1990.
- [29] "Validatie METANET, een rapport voor rijkswaterstaat AVV (Validation METANET, A report for directorate-general for public works and water management, transport research centre)," (in Dutch), Rand EUROPE, Leiden, The Netherlands, Tech. Rep. 0061, 2001.
- [30] D. Ngoduy and S. P. Hoogendoorn, "An automated calibration procedure for macroscopic traffic flow models," in *Proc. 10th IFAC Symp. Control in Transportation Systems (CTS'03)*, Tokyo, Japan, Aug. 2003, pp. 295–300.
- [31] M. Cremer, *Der Verkehrsfluss auf Schnellstrassen (Traffic Flow on Freeways)* (in German). Berlin: Springer-Verlag, 1979, vol. 3, Fachberichte Messen, Steuern, Regeln.
- [32] S. Hoogendoorn, "Multiclass continuum modeling of multiclass traffic flow," Ph.D. dissertation, Delft Univ. Technol., Delft, The Netherlands, 1999.
- [33] A. Hegyi, B. De Schutter, and J. Hellendoorn, "Optimal coordination of variable speed limits to suppress shock waves," *Transport. Res. Rec.*, no. 1852, pp. 167–174, 2004.
- [34] B. S. Kerner, "Empirical features of congested patterns at highway bottlenecks," in *Proc. 81st Annual Meeting Transportation Research Board*, Washington, DC, 2002.
- [35] D. Q. Mayne, J. B. Rawlings, C. V. Rao, and P. O. M. Scokaert, "Constrained model predictive control: Stability and optimality," *Automatica*, pp. 789–814, 2000.
- [36] Y. Wang, M. Papageorgiou, and A. Messmer, "RENAISSANCE: A real-time motorway network traffic surveillance tool," in *Preprints 10th IFAC Symp. Control in Transportation Systems*, Tokyo, Japan, Aug. 2003, pp. 235–240.



Andreas Hegyi was born in Leeuwarden, The Netherlands, in 1973. He received the M.Sc. degree in electrical engineering and the Ph.D. degree from Delft University of Technology, Delft, The Netherlands, in 1998 and 2004, respectively.

Currently, he is a Postdoctoral Researcher with the Delft Center for Systems and Control, Delft University of Technology. His current research interests include intelligent transportation systems, especially the integrated/coordinated control of freeway and urban traffic control measures in networks.



Bart De Schutter received the M.Sc. degree in electrotechnical/mechanical engineering and the Ph.D. degree in applied sciences (*summa cum laude* with congratulations of the examination jury) from K. U. Leuven, Leuven, Belgium, in 1991 and 1996, respectively.

Currently, he is an Associate Professor with the Delft Center for Systems and Control, Delft University of Technology, Delft, The Netherlands. His current research interests include traffic control, hybrid systems, multi-agent systems, control of large-scale transportation and infrastructure networks, and optimization.

Dr. De Schutter was awarded the 1998 SIAM Richard C. DiPrima Prize and the 1999 K. U. Leuven Robert Stock Prize for his Ph.D. dissertation.



J. Hellendoorn was born in Rotterdam, The Netherlands, in 1964. He studied computer science at Delft University of Technology, Delft, The Netherlands, where did research in fuzzy logic as well as at the National Aerospace Laboratory, Amsterdam, The Netherlands, resulting in a Ph.D. dissertation entitled "Reasoning with Fuzzy Logic" in 1990.

He joined the Siemens Research Laboratory, Munich, Germany, in 1991, in the fuzzy control group that he led until 1997. From 1997 to 2000, he was Department Head for training simulation at Siemens,

The Hague, The Netherlands. Since 2001, he has been responsible for innovation management. Since 1998, he has been a Part-Time Professor of control theory at the Delft University of Technology. He has written several books and a large number of publications on computational intelligence and control. He currently works on traffic control and hybrid and multi-agent systems.

Dr. Hellendoorn was President of the European Chapter of the International Fuzzy Set Association (IFSA) and coordinator of the "Fuzzy Sets" Working Group of the The Association of European Operational Research Societies (EURO).