CREPE: Can Vision-Language Foundation Models Reason Compositionally?

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Abstract

A fundamental characteristic common to both human vision and natural language is their compositional nature. Yet, despite the performance gains contributed by large vision and language pretraining, we find that—across 7 architectures trained with 4 algorithms on massive datasets-they struggle at compositionality. To arrive at this conclusion, we introduce a new compositionality evaluation benchmark, CREPE, which measures two important aspects of compositionality identified by cognitive science literature: systematicity and productivity. To measure systematicity, CREPE consists of a test dataset containing over 370K image-text pairs and three different seen-unseen splits. The three splits are designed to test models trained on three popular training datasets: CC-12M, YFCC-15M, and LAION-400M. We also generate 325K, 316K, and 309K hard negative captions for a subset of the pairs. To test productivity, CREPE contains 17K image-text pairs with nine different complexities plus 183K hard negative captions with atomic, swapping and negation foils. The datasets are generated by repurposing the Visual Genome scene graphs and region descriptions and applying handcrafted templates and GPT-3. For systematicity, we find that model performance decreases consistently when novel compositions dominate the retrieval set, with Recall@1 dropping by up to 12%. For productivity, models' retrieval success decays as complexity increases, frequently nearing random chance at high complexity. These results hold regardless of model and training dataset size.

1. Introduction

Compositionality, the understanding that "the meaning of the whole is a function of the meanings of its parts" [13], is held to be a key characteristic of human intelligence. In language, the whole is a sentence, made up of words. In vision, the whole is a scene, made up of parts like objects, their attributes, and their relationships [37, 41].

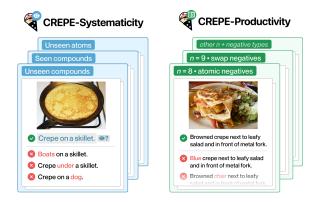


Figure 1. We introduce CREPE, a benchmark to evaluate whether vision-language foundation models demonstrate two fundamental aspects of compositionality: systematicity and productivity. To evaluate systematicity, CREPE utilizes Visual Genome and introduces three new test datasets for the three popular pretraining datasets: CC-12M, YFCC-15M, and LAION-400M. These enable evaluating models' abilities to systematically generalize their understanding to seen compounds, unseen compounds, and even unseen atoms. To evaluate productivity, CREPE introduces examples of nine complexities, with three types of hard negatives for each.

Through compositional reasoning, humans can understand new scenes and generate complex sentences by combining known parts [7, 32, 35]. Despite compositionality's importance, there are no large-scale benchmarks directly evaluating whether vision-language models can reason compositionally. These models are pretrained using large-scale imagecaption datasets [75, 77, 88], and are already widely applied for tasks that benefit from compositional reasoning, including retrieval, text-to-image generation, and open-vocabulary classification [12, 68, 73]. Especially as such models become ubiquitous "foundations" for other models [6], it is critical to understand their compositional abilities.

Previous work has evaluated these models using imagetext retrieval [38,67,98]. However, the retrieval datasets used either do not provide controlled sets of negatives [53,88] or study narrow negatives which vary along a single axis

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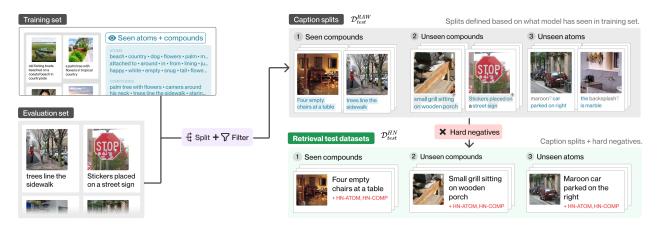


Figure 2. An overview of the **systematicity** retrieval set generation process. First, a model's image-caption training set is parsed to identify what atoms and compounds the model has seen. Then, an evaluation set is divided into three compositional splits according to whether the model has seen all the compounds (Seen Compounds), only all the atoms of the caption (Unseen Compounds), or neither (Unseen Atoms). Finally, hard negative captions HN-ATOM and HN-COMP are generated for the hard negatives retrieval set \mathcal{D}_{test}^{HN} .

(*e.g.* permuted word orders or single word substitutions as negative captions) [24, 61, 78, 89]. Further, these analyses have also not studied how retrieval performance varies when generalizing to unseen compositional combinations, or to combinations of increased complexity.

We introduce CREPE (Compositional REPresentation Evaluation): a new large-scale benchmark to evaluate two aspects of compositionality: systematicity and productivity (Figure 1). Systematicity measures how well a model is able to represent seen versus unseen atoms and their compositions. Productivity studies how well a model can comprehend an unbounded set of increasingly complex expressions. CREPE uses Visual Genome's scene graph representation as the compositionality language [41] and constructs evaluation datasets using its annotations. To test systematicity, we parse the captions in three popular training datasets, CC-12M [10], YFCC-15M [88], and LAION-400M [75], to identify atoms (objects, relations, or attributes) and compounds (combinations of atoms) present in each dataset. For each training set, we curate corresponding test sets containing 385K, 385Kand 373K image-text pairs respectively, with splits checking generalization to seen compounds, unseen compounds, and unseen atoms. To test productivity, CREPE contains 17Kimage-text pairs split across nine levels of complexity, as defined by the number of atoms present in the text. Examples across all datasets are paired with various hard negative types to ensure the legitimacy of our conclusions.

Our experiments—across 7 architectures trained with 4 training algorithms on massive datasets—find that vision-language models struggle at compositionality, with both systematicity and productivity. We present six key findings: first, our systematicity experiments find that models' performance consistently drops between seen and unseen compositions; second, we observe larger drops for models trained on

LAION-400M (up to a 12% decrease in Recall@1); third, our productivity experiments indicate that retrieval performance degrades with increased caption complexity; fourth, we find no clear trend relating training dataset size to models' compositional reasoning; fifth, model size also has no impact; finally, models' zero-shot ImageNet classification accuracy correlates only with their absolute retrieval performance on the systematicity dataset but not systematic generalization to unseen compounds or to productivity. ¹

2. Related Work

Our work lies within the field of evaluating foundation models. Specifically, we measure visio-linguistic compositionality. To do so, we create a retrieval benchmark with hard negatives.

Contrastive Image-Text Pretraining. The recently released contrastively trained CLIP model [67] has catalyzed a wide array of work at the intersection of Computer Vision and Natural Language Processing. Since its release, CLIP has enabled several tasks, ranging from semantic segmentation to image captioning, many of which have remarkable zero-shot capability [14, 18, 45, 67, 84, 87]. CLIP has been used as a loss function within image synthesis applications [34, 52, 54, 64, 95, 100], acted as an automated evaluation metric [25, 62], used successfully as a feature extractor for various vision and language tasks [79], and incorporated into architectures for various tasks including dense prediction and video summarization [51, 60, 65, 69, 80, 81]. This success has also encouraged the design of other contrastive vision and language pretraining algorithms for image [17, 21, 47, 48, 50, 56, 82, 96, 97] and video do-

¹We release our datasets, and code to generate and evaluate on our test sets at https://github.com/RAIVNLab/CREPE.

mains [46,91,94]. Our work evaluates how well such contrastively trained models capture a fundamental property present in human vision and language: compositionality.

Compositionality. Compositionality allows us to comprehend an infinite number of scenes and utterances [43]. For an AI model, compositionality would not only allow for systematic, combinatorial generalization, but would also confer benefits such as controllability [6]. This promise prompted a wealth of work on both designing [2, 28, 30] and evaluating [20, 22, 31, 42, 85] compositional models. In our work, we focus on two aspects of compositionality: systematicity and productivity. While there is a plethora of benchmarks for systematic generalization within Computer Vision [3, 5, 22, 39] and Machine Learning [40, 42, 72], the subject has been almost unexplored for vision-language models, largely due to lack of benchmarks complementary to the different largescale training datasets. To address this, CREPE provides a benchmark with three different datasets to evaluate the compositional generalization of vision-language models. Productivity, on the other hand, has been studied only for specialized tasks [22] or toy domains [32, 42, 72]. CREPE evaluates productivity by using an image-text retrieval task featuring captions of varying compositional complexity.

Evaluation with hard negatives. Like us, past work evaluating models has commonly designed tasks featuring hard negatives to isolate particular model capabilities while overcoming the limitations of prior evaluation tasks. Using atomic foils that replace an atom in the image or text with a distractor has been the most common strategy [5, 11, 24, 29, 61, 63, 78]. Notably, Park et al. [63] targets verbs and person entities in videos; COVR [5] studies question answering with distractor images; VALSE [61] targets linguistic phenomena such as existence, cardinality and the recognition of actions and spatial relationships. Another strategy has been to swap atoms within a caption to test whether models behave akin to a bag-of-words [1,61,89]. In particular, Winoground [89] introduces a set of 800 human edited negatives to evaluate compositionality; it is the closest related work to us. We complement Winoground by scaling it up by three orders of magnitude, by decomposing compositionality into systematicity and productivity, and by studying a variety of different types of hard negatives.

3. Compositional evaluation

The following section builds from the formally vacuous principle of compositionality to a well-defined evaluation scheme [32]. First, we establish the syntax and semantics of the composed language (Section 3.1). Then, we define expected behaviors from a model that achieves comprehension of said language (3.2, 3.3). Finally, we establish how to empirically measure those behaviors via retrieval (3.4).

3.1. Compositional language of visual concepts

To evaluate vision-language models, we find that a compositional language consisting of *scene graph* visual concepts is an appropriate foundation [41]. Accordingly, an *atom* A is defined as a singular visual concept, corresponding to a single scene graph node. Atoms are subtyped into *objects* A_o , *relationships* A_r , and *attributes* A_a . A *compound* C is defined as a primitive composition of multiple atoms, which corresponds to connections between scene graph nodes. Visual concepts admit two compound types: the attachment of attribute to objects ("black dog") C_{ao} , and the attachment of two objects via a relationship ("man hugs child") C_{oro} .

The composition of these compounds form subgraphs S, which can be translated to natural language captions T. Conversely, captions T derived from image-text datasets \mathcal{D} can be parsed to become scene graphs S. This extensible language is capable of capturing a number of linguistic phenomena identified in existing literature [61,85], including the existence of concepts ("a photo with *flowers*"), spatial relationships ("a grill *on the left of* a staircase"), action relationships ("A bird with *green* wings"), and negation ("There are *no* trucks on the road"). Furthermore, while this study focuses on visual concepts, scene graphs featuring common-sense relationships or other more abstract concepts can be designed; therefore, our methodology is widely applicable [74].

3.2. Systematicity

With our compositional language in place, we now define two dimensions of compositionality-systematicity and productivity-which we adapt to vision-language representations. Systematicity evaluates a model's ability to systematically recombine seen atoms in compounds. Concretely, let SEEN(A, D) denote if an atom is seen in a training dataset \mathcal{D} , namely $\exists (I,S) \in \mathcal{D} : A \in S$, and SEEN(C, D) denote if a compound is seen in a dataset \mathcal{D} , namely $\exists (I,S) \in \mathcal{D} : C \subseteq S$. To evaluate systematicity, we define three compositional splits: Seen Compounds (SC), Unseen Compounds (UC) and Unseen Atoms (UA). SC is the split where all compounds (and thus all atoms) of every caption have been seen in the training dataset, *i.e.* $\mathcal{D}_{SC} = \{ (I, S) \in \mathcal{D}_{test} | \forall C \subseteq S : SEEN(C, \mathcal{D}_{train}) \}.$ UC is the split where, for each caption, all atoms have been seen but at least one compound has NOT, *i.e.* $\mathcal{D}_{UC} =$ $\{(I,S) \in \mathcal{D}_{test} \mid (\forall A \in S : SEEN(A, \mathcal{D}_{train}) \land (\exists C \subseteq$ $S : \neg \text{Seen}(C, \mathcal{D}_{train}))$. UA is the split where each caption contains at least one atom that has NOT been seen, *i.e.* $\mathcal{D}_{UA} = \{ (I, S) \in \mathcal{D}_{test} \mid \exists A \in S : \neg SEEN(A, \mathcal{D}_{train}) \}.$

3.3. Productivity

Productivity refers to a capacity to comprehend an unbounded set of expressions. Since the set of atoms in any dataset is finite, a reasonable substitute for testing unbounded

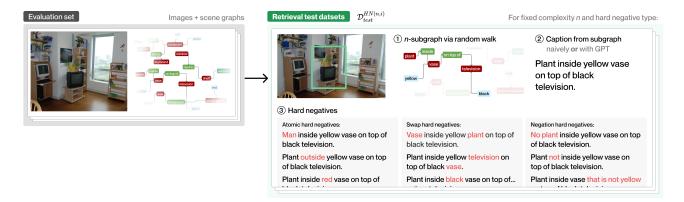


Figure 3. An overview of the **productivity** retrieval set generation process. By performing random walks on the scene graphs of an evaluation dataset, we generate subgraphs of various complexities. Then, for complexities $n \in \{4, 5..., 12\}$ and three hard negative types, we populate the retrieval set \mathcal{D}_{test}^{HN} by generating a ground truth caption for each *n*-subgraph and hard negatives for each caption.

Table 1. We summarize the sizes of the eight evaluation datasets we create for systematicity and productivity evaluation.

Systematicity								ctivity	
\mathcal{D}_{test}^{RAW} (# of image-text pairs)					\mathcal{D}_{test}^{HN} (# of te	exts)	$\mathcal{D}_{test}^{RAW} = \mathcal{D}_{test}^{HN}$		
Training data	CC-12M	YFCC-15M	LAION-400M	CC-12M	YFCC-15M	LAION-400M	Any	Any	
Dataset size	385,777	385,777	373,703	325,523	316,668	309,342	17,553	183,855	

comprehension is testing comprehension over increasingly complex scenes. Now, an image I does not have a notion of complexity, since it is theoretically infinitely describable; on the other hand, we can define a notion of complexity for a caption T: the number of atoms in its corresponding scene graph $|S_T|$.² Therefore, a *productive* vision-language model should be able to match a given image to the correct corresponding caption, regardless of that caption's complexity. To evaluate productivity, we define a range of productivity complexity (in our case, n = 4, 5, ..., 12). We need splits of the evaluation dataset based on these complexities, where image-text pairs in a given split have a fixed complexity n, and evaluate a model's performance over each split.

3.4. Compositional evaluation via retrieval

We evaluate compositional reasoning using zero-shot image-to-text and text-to-image retrieval. This formulation probes the representation space as directly as possible and is already the most common evaluation method for visionlanguage foundation models [67]. Theoretically, any existing image-text dataset can be used as retrieval sets for our evaluation. However, one challenging limitation in existing datasets renders the metrics evaluated on them inaccurate. Consider using an image query of a "plant inside a yellow vase on top of a black television." Retrieving unintended alternative positives (*e.g.* "a black television") is not necessarily incorrect. Similarly, if no other texts in the retrieval set contain a "plant" and a "television", retrieving the correct text doesn't suggest that the model comprehends the image. Ideally, to properly evaluate a model, the retrieval dataset should contain *hard negatives* for every query. A hard negative is a caption that does not faithfully represent the corresponding image, and differs from the ground truth caption by some minimal atomic shift. A example hard negative for the query above is "*man* inside a yellow vase on top of a black television." By erring in a single, granular syntactic or semantic fashion, hard negatives allow for variations in retrieval performance to be attributable to a specific failure mode of a model's compositional comprehension (see Appendix). We address this need for a new benchmark dataset to evaluate the systematicity and productivity of vision-language models.

4. **CREPE:** a large-scale benchmark for vision-language compositionality

There are several challenges to creating image-text retrieval datasets that evaluate compositional systematicity and productivity. For systematicity, the primary challenge lies in parsing the training dataset for seen atoms and compounds in order to split the data into the three compositional splits. For productivity, the major challenge is generating imagetext pairs across different text complexities for the retrieval sets. For both datasets, it is crucial to enumerate different types of hard negatives, and to design an automated hard negative generator which ensures the incorrectness of the

 $^{^{2}}$ By avoiding captions with redundant objects ("... a lamb and a lamb and...") and abstract modifiers ("there are many lampposts"), we ensure atom count is tightly coupled with caption complexity.

negatives it generates. We detail our methods for tackling these challenges for future efforts that attempt to create similar benchmarks for other training datasets.

4.1. Creating systematicity datasets

To create the three systematicity splits—SC, SA, UA—we parse a given training dataset \mathcal{D} into its constituent atoms and compounds, filter low-quality data, and generate hard negatives (Figure 2).

Parsing a dataset into atoms and compounds Since we utilize the scene graph representation as our compositional language, we use the Stanford Scene Graph Parser [76,93] to parse texts in \mathcal{D}_{train} into their corresponding scene graphs with objects, attributes and relationships. Since the parser only parses for objects and relationships, we further extract the attributes from the text via spaCy's natural language processing parser by identifying adjective part-of-speech tags. These connected objects, attributes, and relationships constitute our seen atoms and compounds. Similarly, we parse a given \mathcal{D}_{test} and divide all the image-text pairs into the three splits based on the presence of unseen atoms and/or compounds in the parser can be found in the Appendix.

Filtering low-quality data We perform the following filtering steps on the image-text pairs in all splits: we only keep region crops which have an area greater than or equal to 40K pixels, occupy at least 10% of the whole image, and whose width-to-height ratio is between 0.5-2.0. We only include text which have at least 2 atoms and 1 compound and de-duplicate text using their corresponding scene graphs.

Generating hard negatives We introduce two types of hard negatives: HN-ATOM and HN-COMP. HN-ATOM replaces A_a, A_o , or A_r in the text with an atomic foil. For example, for the caption "a grill on top of the porch", one HN-ATOM can be "a grill *underneath* the porch", where the A_r "on top of" is replaced by "underneath". Since captions and scene graphs are not exhaustive, this replacement must be done carefully. For example, if a dog is white and furry, but only "white" is annotated, replacing the atom "white" with "furry" would result in a correct caption. To minimize errors, we employ WordNet [59] to pick replacement atoms that are either antonyms ("black dog") or share the same grand-hypernym ("pink dog") with respect to the original atom. Furthermore, we use BERT to select the most sensical negatives for each ground truth caption [15,61]. HN-COMP concatenates two compound foils where each contains an atomic foil. For instance, one HN-COMP of the caption "a pink car" can be "a blue car and a pink toy", where "blue" and "toy" are the atomic foils in the two compounds foils "blue car" and "pink toy". We only generate negatives for one-compound examples for systematicity evaluation, as productivity covers complex captions with more atoms.

4.2. Creating productivity datasets

We first generate ground truth captions for scene graphs of varying complexity, filter for data quality, and then generate hard negatives for each example (Figure 3).

Generating captions We systematically generate captions of different atom counts for each image. Given a scene graph, we perform a random walk of length n through the graph to generate a subgraph. Each subgraph corresponds to a specific region of the image, determined by the union of the bounding boxes of the subgraph atoms. We filter out lowquality regions using the same process as systematicity with additional deduplication on patches that overlap by > 75%. For simple subgraphs (n = 4), we produce captions using handcrafted templates. For larger subgraphs $(n \ge 5)$, we leverage GPT-3 [8] (text-davinci-002) to generate captions based on a text description of the scene graph, which lists all objects and relationships. We prompt GPT-3 using 5 manually written captions per complexity, filtering out captions where GPT-3 errs and omits atoms from the subgraph during generation (see more details in Appendix).

Generating hard negatives For productivity, we employ three hard negatives types (HN-ATOM from systematicity, HN-SWAP, and HN-NEG) corresponding to three hypothesized model error modes. First, as a caption's complexity increases, a model may begin to ignore individual atoms. HN-ATOM randomly selects an atom from the caption and replaces it with an incorrect atom. Second, as a caption's complexity increases, a model may treat captions as "bags of words", ignoring syntactic connections built out of word order. A swap hard negative (HN-SWAP) accordingly permutes atoms of the same subtype in a caption. This hard negative is similar to Winoground [89], but in the context of varying caption complexity. On top of Wordnet, we use entailment with RoBERTa to further filter errant HN-SWAP hard negatives [55]. Finally, as a caption's complexity increases, a model may begin to lose comprehension of negations. A negation hard negative (HN-NEG) either negates the entire caption or a specific atom. Refer to the Appendix for details on generating HN-SWAP and HN-NEG.

4.3. The final benchmark datasets

For both productivity and systematicity, we generate two test datasets: \mathcal{D}_{test}^{HN} , which contains image-ground truth text pairs along with all generated hard negatives, and D_{test}^{RAW} , which contains only image-ground truth text pairs. To measure the data quality, we randomly sample 2% of productivity ground truth captions generated by GPT-3 and 1% of the queries in the productivity and systematicity \mathcal{D}_{test}^{HN} sets for manual human verification. We assign 2 annotators to each set and measure both generated quality and intraannotator agreement. 87.9% of sampled productivity ground truth captions generated by GPT-3 are rated as faithful to the image, with an average pairwise annotator agreement of

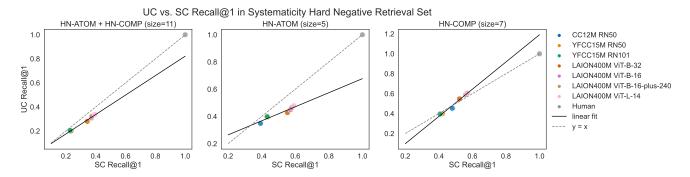


Figure 4. *Systematicity analysis*. We plot models' recall@1 on the Seen Compounds vs. Unseen Compounds split of the systematicity retrieval set with hard negatives HN-ATOM, HN-COMP and both types. We observe a consistent drop in models' performance from the SC to UC split when the retrieval set contains HN-ATOM or both types, and little to no difference when it contains only HN-COMP.

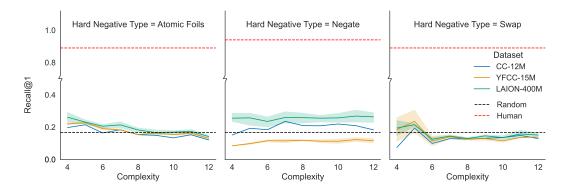


Figure 5. *Productivity Analysis.* We plot models' Recall@1 on the hard negatives retrieval set against complexity, averaged across all models pretrained on all three training datasets. We find that models' ability to retrieve the ground-truth degrades as complexity increases.

88.8%. 83.7% of productivity and 86.0% of systematicity hard negatives were rated as genuine negatives (*i.e.* made factually incorrect statements about the image), with pairwise annotator agreements of 84.3% and 83.7% respectively.

5. Experiments

We present our experimental setup and results with six takeaways. First, our systematicity experiments show performance decreases consistently on compounds unseen in training. Second, the greatest drop between splits occurs for models trained on LAION-400M. Third, our productivity results reveal models' retrieval performance decays with increasing complexity. Fourth, we find that dataset size has no impact on compositionality. Fifth, we find no clear trend relating model size to compositionality. Finally, models' zero-shot ImageNet classification accuracy correlates with retrieval performance on the systematicity dataset but not systematic generalization to the UC split or productivity.

Datasets. We utilize Visual Genome to create our test datasets. For systematicity, image patches and corresponding spelling-corrected region descriptions are used. We provide three different splits for \mathcal{D}_{test}^{HN} , for three training datasets:

CC-12M, YFCC-15M and LAION-400M. For productivity, Visual Genome's image-scene graph pairs are used to create captions and hard negatives for \mathcal{D}_{test}^{RAW} and \mathcal{D}_{test}^{HN} (Table 1). Models. We firstly evaluate seven vision-language models pretrained with contrastive loss [83] across three commonly used image-text datasets: Conceptual Captions 12M (CC-12M) [10], a subset of the YFCC100M dataset (YFCC-15M) [67, 88] and LAION-400M [75]. We limit our evaluation to models openly released in the OpenCLIP repository [33] for systematicity evaluation. These include ResNet (RN) [23] and Vision Transformer (ViT) [16] encoders of different sizes: RN50, RN101, ViT-B-16, ViT-B-16-plus-240, ViT-B-32 and ViT-L-14. Additionally, since productivity evaluation is not restricted to models that were trained on publicly released datasets, we conduct productivity evaluation on other foundation vision-language models as well. Specifically, we consider OpenAI's CLIP [67] with ResNet and ViT backbones, CyCLIP [21] (a variant of CLIP introducing auxiliary losses that regularize the gap in similarity scores between mismatched pairs, trained on Conceptual Captions 3M [77] with a ResNet-50 [23] backbone), AL-BEF [48] (additionally trained with a masked language modeling and image-text matching loss) and FLAVA [82] (which

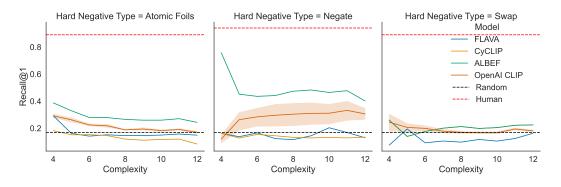


Figure 6. *Productivity Analysis on Additional Foundation Vision-language Models*. We plot models' Recall@1 on the productivity hard negatives retrieval set against complexity, where OpenAI CLIP's performance is averaged across five models RN50, RN101, ViT-B-16, ViT-B-32 and ViT-L-14. We find that all models' retrieval performance decreases as complexity increases in both the HN-ATOM and HN-SWAP retrieval sets. For the HN-NEG set, all models except for CLIP either drop in performance or remain at random chance.

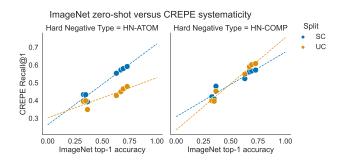


Figure 7. A plot of ImageNet zero-shot top-1 accuracy vs. Recall@1 on CREPE's systematicity hard-negative sets. We observe a strong correlation for both splits on HN-ATOM and HN-COMP.

further adds unimodal losses for image and text domains). **Retrieval.** For \mathcal{D}_{test}^{HN} , we perform image-to-text retrieval and stratify results by split and hard negative type. For systematicity, the splits are SC, UC, and UA; for productivity, the splits are by caption complexity n (denoted $\mathcal{D}_{test}^{HN,n}$). Each retrieval task is between one image and its ground truth caption plus h hard negatives of a single type (see Appendix). We adopt commonly used retrieval metrics Recall@1, 3, 5 and Average Recall@K. For \mathcal{D}_{test}^{RAW} , retrieval experiments are described in the Appendix.

5.1. Systematicity evaluation

Model performance on the \mathcal{D}_{test}^{HN} dataset for systematicity decreases monotonically when compounds are unseen. We first observe a monotonic decrease in recall@1 from the Seen Compounds to the Unseen Compounds split on the systematicity \mathcal{D}_{test}^{HN} set consisting of both HN-ATOM and HN-COMP (Figure 4 left). This drop is relatively small (2 - 4%) for the CC-12M and YFCC-15M trained models and the most pronounced for models trained on the largest dataset LAION-400M [75], with the decrease reaching 6% for the ViT-B-32 model. However, CC-12M and YFCC-15M models also significantly underperform LAION-400M models in general, meaning that small drops between sets may be due to overall poor performance rather than improved systematic generalization. In comparison, human oracle experiments generalize with 100% accuracy to \mathcal{D}_{test}^{HN} .

Similar to the overall results, there is also a consistent discrepancy between the SC and UC split on the \mathcal{D}_{test}^{HN} subset consisting of HN-ATOM only (Figure 4 center). This drop is consistently smaller (3–5%) for models trained on CC-12M and YFCC-15M, but pronounced (higher than 10%, reaching 12.5% drop for ViT-B-32) for LAION-400M models.

On the HN-COMP subset (Figure 4 right), we find little (1 - 3%) to no difference in performance between the two splits. We hypothesize that this is due to the lower difficulty of the HN-COMP hard negatives, as they introduce more foils to the caption, are always longer than the ground truth, and thus offer more opportunities for the model to correctly distinguish the ground truth. This hypothesis is supported by the fact that Recall@1 values on HN-COMP are overall higher than the ones on HN-ATOM even though the HN-COMP retrieval set size is larger than that of HN-ATOM.

5.2. Productivity evaluation

Models' performance decreases with complexity on HN-ATOM and HN-SWAP negatives. At small complexities such as n = 4, we observe that model retrieval quality is well above random chance (Figure 5). However, as caption complexity increases, we observe a steady decrease in performance, nearing random chance for HN-ATOM and dipping below it for HN-SWAP negatives. Similarly, we find that the same downward trend persists for other vision-language foundation models (Figure 6) on HN-ATOM, and these models also perform near random chance on HN-SWAP. Importantly, the downward trend occurs for FLAVA and ALBEF even though their training set contains Visual Genome images. We note that for HN-NEG negatives, the OpenAI CLIP

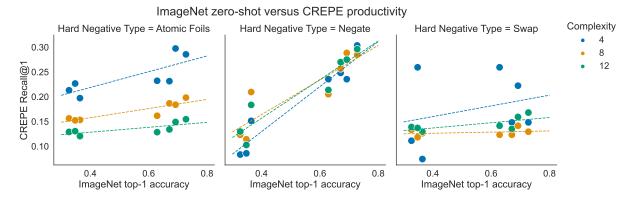


Figure 8. A plot showing the correlation between zero-shot top-1 accuracy on ImageNet and Recall@1 on CREPE's productivity hard negative sets for complexities of 4, 8, and 12. Overall, we find a strong correlation between ImageNet accuracy and Recall@1 on our productivity HN-NEG ($R^2 > 0.78$) and HN-ATOM ($R^2 > 0.54$) sets and weak to no correlation on HN-SWAP.

models do not adhere to the downward trend, achieving their lowest scores for the lowest complexity. Their performances on higher complexities, however, show great variation. Overall, we find that all vision-language foundation models in our evaluation struggle at the productivity hard negative retrieval sets, demonstrating near-random chance performance and/or worse performance at higher caption complexity.

We see no effect of dataset size on productivity. We do not observe a clear advantage for larger pretraining datasets in our productivity evaluation. For atomic and swapping foils, we see similar performance for models trained on the three datasets, with slightly worse performance on atomic foils for the CC-12M trained models. However, on negation hard negatives (Figure 5), we see variable performance across training sets, with CC-12M models outperforming larger models trained on larger datasets YFCC and LAION.

5.3. Effect of model size

We find no trends relating compositionality to model size. Overall, we note that the LAION trained models (which are both larger models and trained on larger datasets) achieve *significantly* better absolute performances than smaller models. However, model's systematicity and productivity remain indifferent to the size of the model itself (Figures 4 and 5).

5.4. Correlation with ImageNet performance

We find that zero-shot ImageNet accuracy strongly correlates with models' Recall@1 on the hard negative retrieval sets except for productivity HN-SWAP. Specifically, we acquire R^2 scores of 0.95, 0.80 for the systematicity SC and UC split on HN-ATOM, and 0.91, 0.97 on HN-COMP (Figure 7). On productivity datasets, we obtain R^2 scores of 0.60, 0.79, 0.55 for HN-ATOM, 0.92, 0.78, 0.88 for HN-NEG and 0.07, 0.08, 0.47 for HN-SWAP negatives on complexity n = 4, 8, 12 respectively (Figure 8). However, this correlation does not imply that models' zero-shot

ImageNet performance correlates with systematic or productive generalization, which is indicated by small or no *difference* between the SC and UC and complexity splits.

6. Discussion

Limitations. First, although our data validation protocols verified our generated hard negatives for productivity as highquality, approximately 70% of HN-SWAP and of HN-NEG negatives were rated as correct. While this does not invalidate our key productivity result, this noise is a limitation of CREPE and could hinder future evaluations once foundation models begin performing better. Second, our evaluation only covers a limited set of vision-language foundation models that were trained with contrastive loss. Additionally, given the computational requirements associated with training a foundation model, our experiments centered around model architectures that were already available publicly. We hope that future foundation models are evaluated with our publicly available CREPE benchmark. Third, while we observe textto-image and image-to-text retrieval to have similar trends for our systematicity experiments, we lack text-to-image datasets with hard negatives. Future work can explore mechanisms to generate counterfactual negative images.

Conclusion. We present CREPE, a collection of imageto-text retrieval datasets with hard negative texts for evaluating pretrained vision-language models' systematicity and productivity. We demonstrate that models struggle with compositionality along both axes, with performance drops across compositional splits and complexities. We expect that CREPE will provide a more systematic evaluation to benchmark the emergence of compositionality as future models improve. Finally, researchers can leverage our hard-negative generation method to create training batches with hard negatives to improve vision-language compositionality.

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A. Additional details on dataset generation

A.1. Hard negative types

In both our productivity and systematicity experiments, we rely on hard negatives to ensure that the retrieval sets we construct meaningfully probe a model's comprehension. Specifically, to *granularly* probe a model's comprehension, we identify a set of common failure modes of noncompositional models and design hard negative types that address each of these failure modes. Examples of each failure mode and hard negative type are outlined in Table 2.

A.2. Scene graph parser verification

To generate data splits for our systematicity experiments, we employed a rule-based implementation of the Stanford Scene Graph Parser [76, 93]. To verify its performance, we randomly sample 20 captions from each of CC-12M, YFCC-15M and LAION-400M and manually annotate scene graphs for the captions. We report precision and recall values for object, attribute and relationship atoms and object-relationship-object triplets on Table 3. For CC-12M, YFCC-15M and LAION-400M, the object precision was 88.14, 96.24, 70.00%, attribute precision was 93.00, 94.44, 72.22% and triplet precision was 91.67, 92.31 and 87.00% respectively. For recall values, on the other hand, we found that object recall was 83.06, 93.33, 60.68%, attribute recall was 56.51, 75.56, 36.11% and triplet recall was 64.04, 81.11 and 39.55% respectively. The precision values help determine whether the atoms the parser identifies are valid, while the recall values help determine whether the parser can identify the atoms and triplets present in the caption, important for the validity of our seen compounds (SC) and unseen compounds (UC) splits.

We find that the parser's precision values are high throughout for each dataset. Recall values are lower compared to precision, particularly for the LAION dataset, where captions can be more similar to bags of words rather than well structured sentences. We note, however, that if compounds were incorrectly placed into the UC set due to poor recall, our systematicity task would become easier. As all models experience drops in performance between SC and UC splits, we do not observe this.

A.3. Productivity caption generation

As discussed in the main text, each instance in the productivity test dataset is a image-text pair of complexity n with a set of hard negative captions. To generate such examples, we begin by sampling a n-node subgraph from a scene graph in Visual Genome [41]. We sample this subgraph using a random walk (see the paragraph titled **Random walk**). This subgraph is then transformed into a caption either using a template or GPT-3 (see the paragraph titled **Caption generation**). Finally, we crop the original image to the union of Table 2. A list of the potential failure modes a vision-language model may encounter when parsing increasingly complex scenes, and the corresponding hard negatives generated in our test datasets.

Dataset	Label	Error Mode	Hard Negative	Example
Sys	НМ-Атом	Ignoring incorrect atoms.	Atomic foils. Replace a single atom with a mutually exclusive or antonymic atom, enforced by WordNet.	A grill on top of the porch. \rightarrow : A grill underneath the porch.
Sys	НN-Сомр	Ignoring proper binding of atoms into compounds.	Compound foils . Split the correct atoms of a single compound over two compounds; fill in the partial compounds with atomic foils (see above).	A pink car. \rightarrow : A blue car and a pink toy. \rightarrow : A pink flower and a black car.
Prod	НМ-Атом	Ignoring incorrect atoms.	Atomic foils. Replace a single atom with a mutually exclusive or antonymic atom, enforced by WordNet.	Yellow vase on top of television. \rightarrow : Red vase on top of television. \rightarrow : Yellow vase underneath television. \rightarrow : Yellow vase on top of shelf.
Prod	HN-SWAP	Ignoring proper binding of atoms.	Swapping foils . Swap two atoms of the same type – or permute several atoms of the same type.	Yellow vase on top of television. \rightarrow : Yellow television on top of vase. \rightarrow : Television on top of yellow vase.
Prod	HN-NEG	Disregarding incorrect nega- tions.	Negation foils . Negate the entire caption <i>or</i> an individual atom with a grammatically correct "not" modifier.	Yellow vase on top of television. →: There is no yellow vase on top of television. →: Vase that is not yellow on top of television.

Table 3. *Scene Graph Parser Validation:* We report precision and recall values the Stanford Scene Graph parser obtains on the CC-12M, YFCC-15M and LAION-400M datasets. For each dataset, we compute values for object, attribute and relationship atoms as well as object-relationship-object triplets. Overall, the scene graph obtains high precision values but lower recall scores. The parser performs the poorest on LAION-400M due its noisier captions.

	CC-12M		YFCC-15M	М	LAION-400M		
	Precision	Recall	Precision	Recall	Precision	Recall	
Object	88.14	83.06	96.24	93.33	69.91	60.68	
Attribute	93.00	56.51	94.44	75.56	72.22	36.11	
Relationship	92.86	70.18	93.59	83.33	88.33	40.15	
Triplet	91.67	64.04	92.31	81.11	87.00	39.55	

all object bounding boxes in the subgraph (see main text). We describe these details below.

Random walk Given a scene graph G, we generate an n-atom subgraph ($n \leq |G|$). We initialize a subgraph S with a single random object in G. While this subgraph contains less than n atoms, a compound C consisting of at least one unadded atom is added to S. If C is a relationship compound (C_{oro}), the walk continues from the newly added object; otherwise, the walk is continued from the same object. If the entire connected component of the scene graph is exhausted, another object is selected at random from a different connected component. This process ends when n atoms are added to the subgraph. We discard all walks that result in insufficient number of atom.

Caption generation To generate captions, we either utilize hand crafted templates or use GPT-3. For subgraphs of complexity n > 4, we use GPT-3 to generate a coherent caption for each prompt; otherwise, we use the templates. When prompting GPT-3 to produce captions, we populate the the first line of the prompt with a list the objects in the subgraph, prepended with their attributes. If multiple instances of an object type occur (e.g., we have two objects both with name "window" in the graph), we append a numerical suffix to distinguish between then (e.g. "window1" from "window2."). On the second line of the prompt, we list all the relationships between objects in the graph, in the form subject relationship object. Additionally, we manually generate 5 caption examples per complexity from random subgraphs and prepend both the random subgraph and the manually generated caption to the prompt above, as few-shot training examples for GPT-3. We provide examples of graphs, prompts, and their generated captions in Figure 9.

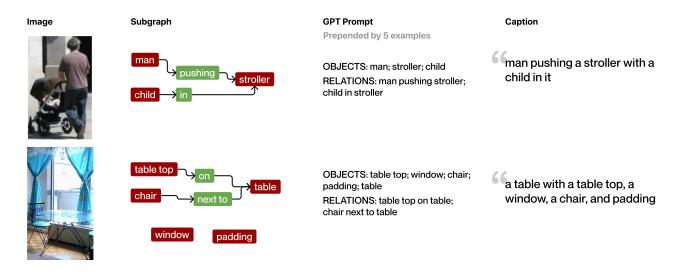


Figure 9. Examples of image-text pairs we generate for our productivity evaluation. The image is the union of the objects bounding boxes in the subgraphs. We also showcase the GPT-3 prompt associated with the subgraph and their corresponding generated ground-truth captions.

For examples of complexity n = 4, we found that stringing together a simple templated prompt was sufficient to produce fluent captions. This was done by prepending attributes in front of objects and stringing together subjects, relations, and objects in the correct order. For example, a subgraph containing boy=(tall,blue); grass=(green); (boy, on, grass) would be templated as tall and blue boy on green grass. Any disconnected atoms are appended with the prefix "and a."

Table 4. Productivity ground truth captions' faithfulness to their paired images, split by caption complexity. Overall, the generated captions' faithfulness is stable and consistently high across different complexities.

Complexity	Avg faithfulness
n = 7	88.7 ± 10.8
n = 8	85.7 ± 7.0
n = 9	90.0 ± 6.0
n = 10	87.7 ± 9.3
n = 11	88.1 ± 7.8
n = 12	89.1 ± 2.9

Data verification. We manually verify the accuracy of our produced productivity dataset. We provide a breakdown of annotators' scores for GPT-3 caption faithfulness across complex subgraphs with $n \ge 7$ in Table 4. We see that scores are consistently high for ground-truth captions across complexities.

A.4. Hard negative generation details

We provide additional detail for the procedure of generating a hard negative of types HN-SWAP and HN-NEG. Suppose throughout that for a given image and its annotated scene graph G, we seek to generate a hard negative caption for caption t associated with the subgraph $S \subseteq G$.

HN-SWAP The following pairs of atoms could be swapped to create a hard negative for *S*:

- The subject A_o and object A'_o of a relationship compound C_{oro} ∈ S.
- Two attributes A_a and A'_a attached to distinct objects A_o, A'_o, such that one attribute is not present for the other object in G and vice versa. ((A_a, A'_o) ∉ G and (A'_a, A_o) ∉ G).
- Two objects A_o , A'_o not connected by a relationship such that their swapping within G does not create an identical graph.

Additionally, some swap hard negatives generated are *permutations* rather than a swapped pair:

- One attribute A_a can be transferred from one object A_o to another object A'_o, so long as that attribute doesn't apply to the new object ((A_a, A'_o) ∉ G).
- For low complexities (n = 4), any permutation of atoms of the same type are allowed. For example: ("There is a dog on the bed and also a nightstand" → "There is a *nightstand* on the *dog* and also a *bed*")

HN-NEG We verify with G to ensure that negating an atom results in an incorrect caption. If an attribute A_a connected with A_o is negated, we ensure that there does not exist an object of A'_o that doesn't have an attribute A_a but shares all the other attributes of A_o . For example, if we negate "black" in "Black dog on a building", we ensure there doesn't exist another dog on the building that isn't black. Similar checks are performed for negating relationships and objects. When a relationship A_r connecting A_o and A'_o is negated, there cannot exist another identical subject and object pair connected by a different relationship A'_r . When an object is negated, there cannot exist any other object with the same attributes and relationships.

A.5. Test dataset sizes, examples, and additional verification

Table 5 expands on Table 1 from the main paper to provide a breakdown of the number of image-text pair per hard negative type and, for productivity, for each sentence complexity. We remark that \mathcal{D}_{test}^{RAW} , which contains only imageground-truth caption pairs, is a superset of the ground-truth captions in \mathcal{D}_{test}^{HN} . This is because, for some ground truth captions in \mathcal{D}_{test}^{RAW} , a sufficient number of hard negatives to perform retrieval in \mathcal{D}_{test}^{HN} could not be generated. Additionally, due to the prevalence of rare atoms, we could only generate valid hard negatives for very few captions in the UA split. Therefore, we omit the evaluation on the UA split with hard negatives and focus on the analysis of results between the SC and UC split, which is more interesting as models have seen all the atoms in both splits. Table 6 summarizes the text retrieval set size of each image query for both \mathcal{D}_{test}^{raw} and \mathcal{D}_{test}^{HN} in our systematicity and productivity evaluation. Figures 10 and 11 present examples of ground truth captions and hard negative captions in our test datasets for systematicity and productivity, respectively.

We provide a breakdown of annotators' scores for the accuracy of productivity hard negatives in Table 7. A hard negative caption is accurate if it contains incorrect facts about the image. We find that the accuracy and pairwise agreement of the HN-ATOM is the highest and much higher than those of HN-SWAP and HN-NEG.

A.6. Systematicity hard negative dataset details

Table 8 summarizes the number of unique atoms and compounds in the SC and UC split of the systematicity hard negative set. Additionally, we plot the atom count in the systematicity test set vs. the training set (on a log scale). As shown in Figure 12, we see that the atom count in the training set is always on the same scale across both splits for the same training dataset (x-axis in each row). We further observe that the atom distributions are similar in the SC and UC splits. These suggest that the atoms appearing in the UC split are not substantially rarer or more difficult than the ones in the SC split.

B. Additional evaluation results

B.1. Full retrieval results on hard negative datasets

Systematicity We additionally include the full retrieval results on \mathcal{D}_{test}^{HN} with both HN-ATOM and HN-COMP, HN-ATOM only and HN-COMP only in Tables 9, 10 and 11. We note that as we relax the metric from R@1 to R@3, the difference between models' performance in the SC and UC split decreases.

Productivity We report the full retrieval results on productivity \mathcal{D}_{test}^{HN} sets in Tables 12, 14 and 13.

B.2. Retrieval results on raw datasets

In addition to \mathcal{D}_{test}^{HN} retrieval experiments, we perform retrieval experiments with \mathcal{D}_{test}^{RAW} .

We perform *both* image-to-text and text-to-image retrieval within splits of \mathcal{D}_{test}^{RAW} . Each retrieval task is between one image and every caption in the split, or vice versa. We report the mean and standard deviation of Recall@1 across K-fold retrievals (where $K = \min(20, \lfloor \frac{|\mathcal{D}_{test}^{RAW}|}{N} \rfloor)$), and $N = \min\{|SC|, |UC|, |UA|\} = 1855$ for systematicity and $N = \min_{n \in \{4...12\}} |\mathcal{D}_{test}^{RAW,n}| = 1508$ for productivity), as the data size varies across compositional splits and complexities.

Systematicity We present the systematicity retrieval results on \mathcal{D}_{test}^{raw} in Table 15, where each retrieval set for an image consists of the captions of the other images. We continue to observe a monotonic decrease in performance when compounds are unseen. Additionally, we continue to observe a drop in performance for larger training datasets. In particular, we see a similar drop in performance for LAION-trained models across both the image-to-text and text-to-image tasks. We also observe larger drops on LAION-trained models than for \mathcal{D}_{test}^{HN} when moving across the SC \rightarrow UC, and across UC \rightarrow UA splits, with LAION models dropping as much as 13% for ViT-L/14.

Productivity We additionally present the productivity retrieval results on \mathcal{D}_{test}^{raw} in Table 16. We observe that models' Recall@1 generally increases as the caption complexity increases. We hypothesize that models' low performance in the low-complexity subset is caused by false negatives in the original dataset: since the captions are simple and likely true for multiple images, there are multiple false negatives in the retrieval set, making these numbers unreliable. As the captions become more complex, however, the chance of such false negatives is lower. This means there are more true negatives in the higher-complexity subsets, making retrieval easier for these models.

Table 5. We report the ground truth caption counts in \mathcal{D}_{test}^{raw} and hard negative counts in \mathcal{D}_{test}^{HN} s for systematicity and productivity, separated by hard negative type and split.

Systematicity				Productivity	ý			
Split	Ground Truth	НN-Атом	НИ-Сомр	Split	Ground Truth	НМ-Атом	HN-SWAP	HN-NEG
CC-12M SC	262,541	104,024	156,036	n = 4	1,508	6,290	135	2,510
CC-12M UC	113,659	14,348	21,522	n = 5	1,734	7,270	180	3,425
CC-12M UA	9,577	-	-	n = 6	1,905	9,025	1,310	6,565
YFCC SC	194,502	75,948	113,922	n = 7	2,171	10,410	2,525	7,845
YFCC UC	172,469	39,204	58,806	n = 8	2,247	11,205	4,955	10,210
YFCC UA	18,806	-	-	n = 9	1,969	9,485	4,420	8,310
LAION SC	170,253	62,884	94,326	n = 10	2,246	11,325	6,465	10,460
LAION UC	201,595	49,604	74,406	n = 11	1,895	8,620	5,380	7,925
LAION UA	1,855	-	-	n = 12	1,878	10,005	7,890	9,710

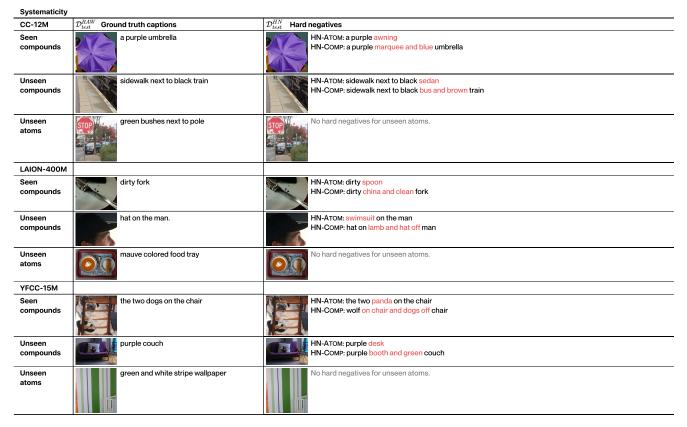


Figure 10. A sample of image-caption pairs in the **systematicity** retrieval sets. One ground truth caption is shown for each split of each training dataset, each of which lie in both \mathcal{D}_{test}^{RAW} and \mathcal{D}_{test}^{HN} . Additionally, one example of each hard negative type is shown for each ground truth caption.

B.3. Retrieval results with all hard negatives at once

Productivity We present models' retrieval performances over the whole productivity \mathcal{D}_{test}^{HN} dataset, where each retrieval set contains one ground truth caption and fifteen hard negatives, five for each of the three types HN-ATOM, HN-SWAP and HN-NEG. We find in Figure 13 that models'

Recall@1 performance decreases with complexity, which aligns with the findings on the separate retrieval sets for HN-ATOM, HN-SWAP and HN-NEG.

Productivity	\mathcal{D}_{test}^{RAW} Ground truth captions	\mathcal{D}_{test}^{HN} Hard negatives
n = 4	speaker beside pope. there is a stand	HN-ATOM: speaker beside mistress. There is a stand. HN-SWAP: pope besides speaker, there is a stand HN-NEG: there is no speaker beside pope.
n = 5	tree on a sidewalk next to a meter	HN-ATOM • tree on a catwalk next to a meter • pineapple on a sidewalk next to a meter HN-Swap • meter on a tree next to a sidewalk • meter on a sidewalk next to a tree HN-NEG • there is no tree on a sidewalk next to a meter • tree not on a sidewalk next to a meter
n = 6	a dog behind a surfboard and water with splashes	HN-ATOM: a dog behind a foil and water with splashes HN-SWAP: a surfboard behind a dog and water with splashes HN-NEG: a dog behind an object which is not a surfboard and water with splashes
n = 7	chairs in a row with umbrellas above them; there are also tables and chairs	HN-ATOM: chairs in a row with umbrellas below them; there are also tables and chairs HN-SWAP: chairs in a tables with umbrellas above them; there are also row and chairs HN-NEG: chairs in a row with umbrellas not above them; there are also tables and chairs
n = 8	a person wearing a cap and another person standing on the sidewalk, and another person on the sidewalk	HN-ATOM: a person wearing a coverall and another person standing on the sidewalk, and another person on the sidewalk HN-SWAP: a person wearing a sidewalk and another person standing on the cap, and another person on the sidewalk HN-NEC: a person wearing a cap and another person standing not on the sidewalk, and another person on the sidewalk
n = 9	a laptop and paper on a table. a man is standing by the table with his hands on it.	HN-ATOM: a laptop and paper on a matrix. a man is standing by the table with his hands on it HN-SWAP: a laptop and paper on a hands. a man is standing by the hands with his table on it. HN-NEG: a laptop and paper on a table. a man is not standing by the table with his hands on it
n = 10	a black chair with wheels in front of a desk, with a laptop and lamp on it	HN-ATOM: a black chair with wheels in front of a console, with a laptop and lamp on it HN-SWAP: a black chair with desk in front of a wheels, with a laptop and lamp on it HN-NEG: a black chair with wheels not in front of a desk, with a laptop and lamp on it
n = 11	a cardboard under a pan, and a deep dish pizza in the pan. the pan is filled with the deep dish pizza and there is a spatula in the deep dish pizza.	HN-ATOM: A cardboard under a pan, and a deep dish pizza not in the pan. the pan is filled with the deep dish pizza and there is a spatula not in the deep dish pizza. HN-SWAP: a pan under a cardboard, and a deep dish pizza in the pan. the pan is filled with the deep dish pizza and there is a spatula in the deep dish pizza. HN-NEC: a cardboard under a pan, and a deep dish pizza in the pan. the pan is filled with the deep dish pizza and there is an object that is not a spatula in the deep dish pizza.
n = 12	stand with handles and advertisements, with a tv resting on top of three drawers. the surface of the tv has a reflection, and there is a sign on top of the stand.	 HN-ATOM Stand with handles and advertisements, with a tv resting on top of three drawers. The surface of the tv has a rendering, and there is a sign on top of the stand. wing with handles and advertisements, with a tv resting on top of three drawers. the surface of the tv has a reflection, and there is a sign on top of the stand HN-SwaP sign with handles and advertisements, with a tv resting on top of three drawers. the surface of the tv has a reflection, and there is a stand on top of the sign. stand with handles and advertisements, with a tv resting on top of three drawers. the surface of the tv has a reflection, and there is a stand on top of the sign. stand with handles and advertisements, with a tv resting on top of three drawers. the surface of the tv has a advertisements, and there is a sign on top of the stand. HN-NEG an object which is not a stand with handles and advertisements, with a tv not resting on top of three drawers. the surface of the tv has a reflection, and there is a sign on top of the an object which is not a stand. stand with handles and advertisements, with a tv not resting on top of three drawers. the surface of the tv has a reflection, and there is a sign on top of the an object which is not a stand.

Figure 11. A sample of image-caption pairs in the **productivity** retrieval sets. One ground truth (GT) caption is shown for each complexity n. These GT captions lie in both \mathcal{D}_{test}^{RAW} and \mathcal{D}_{test}^{HN} . One example of each hard negative type is shown for each GT caption. For two highlighted example captions (n = 5, 12), we show 2 hard negatives per type for comprehensiveness.

Table 6. We summarize the retrieval set sizes for both \mathcal{D}_{test}^{HN} and \mathcal{D}_{test}^{Raw} in our systematicity and productivity evaluation.

Retrieval set size		\mathcal{D}_{test}^{HN}		\mathcal{D}_{test}^{RAW}
Systematicity	HN-ATOM 5	НN-Сомр 7		1,855
Productivity	HN-Атом 6	HN-SWAP 6	HN-NEG 6	1,508

Table 7. Accuracy of our generated hard negatives for productivity, split by type, in our data verification. While HN-ATOM atoms receive strong human evaluation scores, we find that HN-SWAP and HN-NEG negatives are noisier.

Туре	Acc. mean \pm std	Pairwise agreement
HN-ATOM	91.6 ± 4.2	83.1
HN-SWAP	70.1 ± 9.1	58.5
HN-NEG	72.4 ± 0.0	59.5

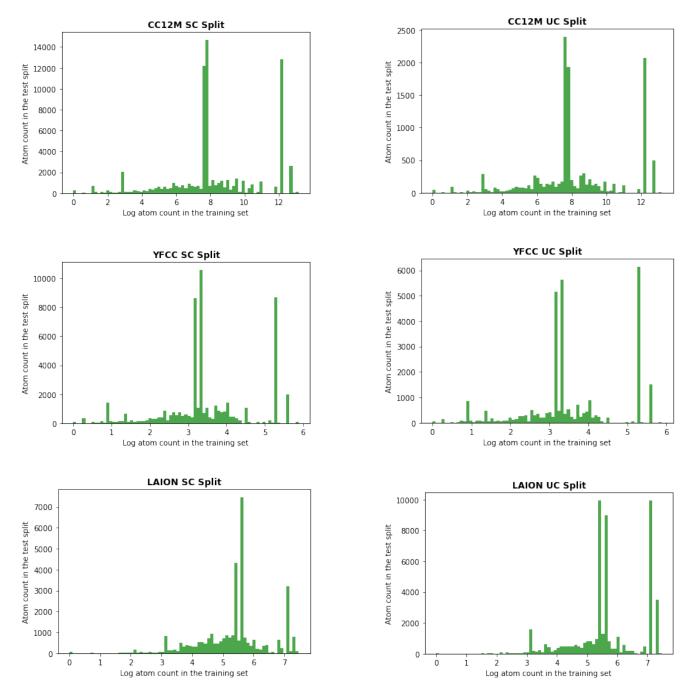


Figure 12. We plot the atom count in training vs. in the systematicity hard negative test set. We observe that the atoms in the SC and UC test splits have similar counts in the training dataset.

B.4. Qualitative analysis on systematicity evaluation

We perform a qualitative analysis to better understand why the LAION-400M trained models ViT-B-16 and ViT-L-14 show a large versus small performance drop from the Seen to Unseen Compounds split respectively. Table 17 presents examples where both ViT-B-16 and ViT-L-14 retrieve the correct caption successfully in the SC split and where VT-B-16 fails in the UC split. Through this analysis, we find that the SC split for LAION-400M trained models is dominated by simple two-atom examples such as "purple couch". The UC split, however, contains more complex examples that involve relationships such as "curtains on the window". In

Table 8. We summarize the unique atom and compound counts in the SC and UC split of the systematicity hard negative set.

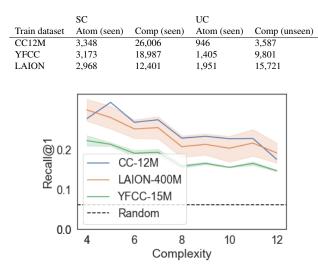


Figure 13. *Productivity Analysis on Hard Negatives of All Types*. We plot models' Recall@1 on the overall hard negatives retrieval set against complexity, where each retrieval set contains hard negatives of all types. We find that models' ability to correctly retrieve the ground-truth caption drops as complexity increases.

particular, we find that the ViT-B-16 model struggles with the relationship "on" and often retrieves a wrong caption where "on" is replaced with "off" or where the object is replaced with an atomic foil. For example, ViT-B-16 retrieves "plants on bob and plants off building" incorrectly when the groundtruth caption is "plants on a building". Nevertheless, the rank of the groundtruth caption is often still within the top three. This explains the narrower gap in ViT-B-16' Recall@3 between Seen Compounds and Unseen Compounds. On the other hand, we see that ViT-L-14 continues to retrieve the correct caption even on the more challenging Unseen Compounds split, suggesting that a larger model size could improve compositional systematicity.

C. Additional Related Work

Evaluating learned representations By analyzing the properties of pretrained representations, our work continues a tradition of research in Computer Vision [19,49,57,58,71,90] and Natural Language Processing [26, 36, 66, 70, 86, 92] that probes characteristics of representations themselves rather than their performance on downstream tasks. Instead of learning probes, we use retrieval for zero-shot evaluation in order to avoid scenarios where the learned probe compensates for the characteristics deficient in the original representations [4, 9, 27, 44, 99].

Table 9. Systematicity HN-ATOM + HN-COMP Dataset Analysis. We report Recall@1,3,5 and Avg R@K results for all models on the D_{test}^{HN} hard-negative datasets with both HN-ATOM + HN-COMP. Model performance decreases from the Seen all compounds (SC) to the Unseen Compounds (UC) split, particularly for LAION-400M models.

	Training dataset	Model	R@1		R@3		Avg R@K	
	Training Galaset	Widdel	SC	UC	SC	UC	SC	UC
		Random	9.09	9.09	27.27	27.27	18.18	18.18
	CC12M	RN50	23.26	19.96	62.44	59.52	42.85	39.74
	YFCC15M	RN50	23.38	20.08	60.09	56.61	41.74	38.34
	ITCCI5W	RN101	22.74	20.50	59.15	57.59	40.94	39.04
Image-to-text		ViT-B-32	34.28	28.00	70.74	68.74	52.51	48.37
	LAION400M	ViT-B-16	37.01	30.81	73.92	72.85	55.46	51.83
		ViT-B-16+240	37.32	32.26	75.03	73.46	56.17	52.86
		ViT-L-14	39.44	33.81	74.31	73.47	56.87	53.64

Table 10. Systematicity HN-ATOM Dataset Analysis. We report Recall@1,3 and Avg R@K results for all models on the D_{test}^{HN} subset with HN-ATOM. Model performance decreases from the Seen Compounds (SC) to the Unseen Compounds (UC) split, particularly for LAION-400M models.

	Training dataset	Model	R@1 R@3		Avg R@K			
	Training Galaset	Widdel	SC	UC	SC	UC	SC	UC
		Random	20.00	20.00	60.00	60.00	40.00	40.00
	CC12M	RN50	39.26	34.88	88.81	88.10	64.04	61.49
	YFCC15M	RN50	43.35	39.50	90.55	90.07	66.95	64.78
	ITCCI5W	RN101	43.26	39.85	90.33	90.30	66.79	65.08
Image-to-text		ViT-B-32	55.32	42.75	93.38	91.92	74.35	67.34
	LAION400M	ViT-B-16	57.18	44.93	94.01	92.95	75.59	68.94
		ViT-B-16+240	57.95	46.53	94.36	93.40	76.16	69.97
		ViT-L-14	59.11	47.86	94.39	93.66	76.75	70.76

Table 11. Systematicity HN-COMP Dataset Analysis. We report Recall@1,3 and Avg R@K results for all models on the D_{test}^{HN} subset with HN-COMP. We observe little to no difference in performance between the SC and UC split.

	Training dataset	Model	R@1 R@3		@3	Avg R@K		
	framing dataset	Widdei	SC	UC	SC	UC	SC	UC
		Random	14.29	14.29	42.86	42.86	28.57	28.57
	CC12M	RN50	48.02	45.27	80.24	79.59	64.13	62.43
	YFCC15M	RN50	42.07	39.83	75.06	73.66	58.56	56.74
	ITCCIJNI	RN101	40.72	39.56	74.71	74.16	57.72	56.86
Image-to-text		ViT-B-32	52.29	54.80	82.40	83.25	67.35	69.02
	LAION400M	ViT-B-16	56.00	59.00	84.64	86.24	70.32	72.62
	LAION400M	ViT-B-16+240	56.57	60.19	85.28	85.69	70.92	72.94
		ViT-L-14	57.10	60.78	84.17	85.69	70.64	73.24

	Training dataset	Model	4	5	6	7	8	9	10	11	12
		Random	16.67	16.67	16.67	16.67	16.67	16.67	16.67	16.67	16.67
	CC-12M	RN50	19.71	21.46	16.40	18.35	15.31	14.92	13.38	15.26	12.04
	YFCC-15M	RN50	21.30	23.31	19.94	18.11	15.62	16.03	14.97	15.14	12.89
	Tree-ISM	RN101	22.66	22.21	18.17	18.44	15.22	16.34	15.85	17.34	13.04
		ViT-B-32	23.21	21.25	19.06	18.59	16.15	13.92	15.76	15.49	12.84
	LAION-400M	ViT-B-16	23.13	22.83	19.89	21.09	18.65	15.92	16.42	17.00	13.39
	LAION-400M	ViT-B-16+240	29.73	23.31	21.72	21.81	18.38	18.08	17.62	18.39	14.89
Image-to-text		ViT-L-14	28.54	25.10	21.55	24.06	19.81	18.61	17.88	18.68	15.44
inage-to-text		CyCLIP RN50	18.20	15.13	15.24	14.46	11.91	11.12	11.70	11.95	8.35
		FLAVA	29.17	16.23	14.13	15.08	14.46	14.55	14.88	15.72	14.79
		ALBEF	38.71	32.94	27.87	27.76	26.51	25.94	25.92	27.03	24.34
		RN50	26.79	26.41	21.83	21.09	18.38	19.40	17.40	19.14	15.49
	CLIP's dataset	RN101	28.46	26.34	22.22	22.33	18.56	19.14	19.16	18.56	17.94
	CLIF S dataset	ViT-B-32	28.70	23.31	21.33	19.79	18.61	18.13	17.66	18.10	16.69
		ViT-B-16	30.68	26.41	23.93	23.15	19.19	19.19	18.76	20.19	16.44
		ViT-L-14	31.00	28.47	22.71	22.48	19.01	21.09	18.01	19.14	18.24

Table 12. *Productivity* HN-ATOM *Dataset Analysis*. We report mean Recall@1 results for all models across all complexities. We find that models' Recall@1 values decrease as caption complexity increases.

Table 13. *Productivity* HN-SWAP *Dataset Analysis*. We report mean Recall@1 results for all models across all complexities. We find that models' Recall@1 values are near or even below random chance across all complexities.

	Training dataset	Model	4	5	6	7	8	9	10	11	12
		Random	16.67	16.67	16.67	16.67	16.67	16.67	16.67	16.67	16.67
	CC-12M	RN50	7.41	19.44	9.92	12.87	12.61	13.12	13.53	14.87	12.93
	YFCC-15M	RN50	11.11	16.67	14.50	15.25	13.32	14.14	10.75	13.48	13.88
	IFCC-ISM	RN101	25.93	30.56	8.40	12.67	11.81	11.76	12.30	13.85	13.69
	LAION-400M	ViT-B-32	25.93	19.44	12.98	13.86	12.31	14.37	11.60	12.08	14.13
		ViT-B-16	14.81	22.22	10.31	14.85	12.31	14.03	13.77	14.87	13.50
		ViT-B-16+240	22.22	22.22	14.12	15.05	14.13	14.48	13.69	18.31	15.91
Image-to-text		ViT-L-14	14.81	22.22	12.60	14.06	12.92	15.61	15.00	17.84	16.79
inage-to-text		CyCLIP RN50	11.11	5.56	11.07	14.46	11.81	12.56	13.23	13.75	11.79
		FLAVA	7.41	19.44	9.16	10.50	9.69	11.65	10.44	12.36	16.22
		ALBEF	25.93	13.89	17.56	20.00	21.19	19.80	20.42	22.12	22.43
	CLIP's dataset	RN50	22.22	19.44	19.47	20.20	17.66	17.99	17.71	18.49	18.12
		RN101	29.63	25.00	16.79	17.62	17.15	15.38	17.40	19.61	18.06
		ViT-B-32	25.93	22.22	22.90	15.64	15.14	16.63	16.24	20.91	18.95
		ViT-B-16	33.33	22.22	20.99	18.42	17.86	16.40	15.78	19.42	16.79
		ViT-L-14	11.11	13.89	19.08	16.83	17.05	16.86	16.01	18.49	18.06

Table 14. *Productivity* HN-NEG *Dataset Analysis*. We report mean Recall@1 results for all models across all complexities. We find that models' Recall@1 values either stay near random chance or decrease as caption complexity increases except for some of OpenAI's CLIP models.

	Training dataset	Model	4	5	6	7	8	9	10	11	12
		Random	16.67	16.67	16.67	16.67	16.67	16.67	16.67	16.67	16.67
	CC-12M	RN50	15.13	19.28	18.41	23.59	20.94	20.83	21.95	20.90	18.34
	YFCC-15M	RN50	8.32	10.29	12.18	12.64	12.30	12.23	12.65	13.49	12.96
	IFCC-ISM	RN101	8.56	9.30	10.96	10.35	11.41	10.36	9.88	11.08	10.25
	LAION-400M	ViT-B-32	23.53	18.75	18.08	21.01	20.50	21.88	21.32	20.78	21.36
		ViT-B-16	24.80	26.91	23.47	23.89	25.67	25.88	24.59	25.54	26.98
		ViT-B-16+240	23.53	28.20	26.36	29.12	28.83	27.03	28.30	30.30	27.49
Image-to-text		ViT-L-14	30.35	29.04	26.14	29.92	28.48	27.41	28.70	30.72	29.60
image-to-text		CyCLIP RN50	16.24	12.65	15.35	14.39	13.19	12.77	13.23	12.77	13.27
		FLAVA	16.16	13.72	16.52	12.29	11.54	14.42	20.25	16.81	12.86
		ALBEF	75.83	45.12	43.55	44.05	47.28	48.19	46.45	47.71	40.05
	CLIP's dataset	RN50	14.10	34.83	37.10	41.76	41.18	40.90	39.61	40.06	31.41
		RN101	8.72	12.88	15.57	14.73	15.91	18.20	17.34	20.66	25.83
		ViT-B-32	15.85	30.56	34.09	35.99	38.99	40.13	39.87	41.33	38.94
		ViT-B-16	7.13	26.22	28.64	32.11	33.16	31.41	34.29	36.51	31.56
		ViT-L-14	13.79	26.91	26.36	23.05	22.37	24.07	24.05	27.17	24.92

Table 15. *Systematicity Raw Dataset Analysis.* We report mean Recall@1 results for all models across k-fold evaluations. Model performance consistently decreases from Seen all Compounds (SC) to Unseen Compounds (UC) and from Unseen Compounds to Unseen Atoms (UA) splits, particularly for LAION-400M models.

	Training dataset	Model	SC	UC	UA
		Random	0.05 ± 0.00	0.05 ± 0.00	0.05 ± 0.00
	CC-12M	RN50	19.92 ± 0.94	17.82 ± 0.99	15.02 ± 0.85
	YFCC-15M	RN50	16.30 ± 0.70	14.57 ± 0.69	12.80 ± 0.90
	TPCC-15M	RN101	17.10 ± 0.90	15.58 ± 1.04	13.62 ± 0.84
Image-to-text		ViT-B-16	35.61 ± 0.92	30.04 ± 1.42	25.88 ± 0.00
	LAION-400M	ViT-B-16+240	36.80 ± 0.90	31.10 ± 1.37	26.25 ± 0.00
	LAION-400M	ViT-B-32	33.86 ± 0.97	29.00 ± 1.40	23.99 ± 0.00
		ViT-L-14	38.24 ± 0.70	32.70 ± 1.30	26.42 ± 0.00
	CC-12M	RN50	20.85 ± 0.98	18.15 ± 0.84	15.46 ± 1.10
	YFCC-15M	RN50	15.60 ± 0.79	14.05 ± 0.84	12.17 ± 0.64
	TPCC-15M	RN101	16.11 ± 0.84	14.47 ± 0.87	12.54 ± 0.66
Text-to-image		ViT-B-16	35.74 ± 0.76	29.58 ± 1.39	23.29 ± 0.00
	LAION-400M	ViT-B-16+240 37.25 ± 0.97		30.57 ± 1.33	24.26 ± 0.00
	LAION-400101	ViT-B-32	33.66 ± 1.03	29.00 ± 1.40	22.10 ± 0.00
		ViT-L-14	38.69 ± 0.86	32.00 ± 0.90	25.61 ± 0.00

	Training dataset	Model	4	5	6	7	8	9	10	11	12
		Random	0.06	0.06	0.06	0.06	0.06	0.06	0.06	0.06	0.06
	CC-12M	RN50	13.19	14.23	16.20	19.02	21.17	19.26	22.70	24.29	25.77
	YFCC-15M	RN50	9.08	10.92	12.09	14.23	14.17	15.40	14.54	16.75	19.02
	IFCC-ISM	RN101	11.10	11.47	11.90	14.60	15.34	16.50	16.99	18.90	20.67
Image-to-text	LAION-400M	ViT-B-16	20.80	20.00	25.89	27.30	29.63	29.02	30.31	34.11	37.36
		ViT-B-16+240	22.39	21.53	26.93	28.10	30.61	30.18	32.88	36.50	38.83
		ViT-B-32	20.49	20.37	23.50	26.93	29.20	28.22	29.94	32.58	35.40
		ViT-L-14	22.09	23.07	27.67	29.69	33.13	31.04	35.09	37.12	40.25
	CC-12M	RN50	12.52	15.03	15.52	17.85	17.30	19.75	21.66	22.52	25.58
	YFCC-15M	RN50	8.04	9.82	9.82	12.15	12.94	13.62	13.37	14.97	15.15
		RN101	9.39	11.10	11.10	13.31	13.74	15.03	14.48	16.07	18.40
Text-to-image		ViT-B-16	18.16	19.26	23.62	24.85	27.85	27.79	28.77	31.53	33.93
	LAION-400M	ViT-B-16+240	18.96	20.67	25.46	26.13	28.83	29.02	31.41	32.88	37.24
	LAION-400M	ViT-B-32	17.55	18.65	22.21	23.50	26.20	26.13	27.36	28.83	32.21
		ViT-L-14	19.88	20.43	24.97	26.63	30.37	30.00	32.76	34.42	36.99

Table 16. *Productivity Raw Dataset Analysis*. We report mean Recall@1 results for all models across all complexities. We find that models' Recall@1 increases as the caption complexity increases.

Table 17. *Systematicity Qualitative Analysis*. We present examples where LAION-400M trained ViT-B-16 and ViT-L-14 both perform well on the Seen Compounds (SC) split, and where ViT-B-16 performs poorly on the Unseen Compounds (UC) split.

			ViT-B-16			ViT-L-14
	Image	GT caption	R@1	Top 3 captions	R@1	Top 3 captions
SC		purple couch	1	purple couch purple altar and brown couch purple commode and red couch	1	purple couch purple altar and brown couch purple desk and brown couch
		a white parked car	1	a white parked car a green parked car a white bike	1	a white parked car a green parked car a orange parked car
	Part of	a fully grown brown horse	1	a fully grown brown horse a fully grown brown mule and red horse a fully grown brown mule and yellow horse	1	a fully grown brown horse a fully grown brown mule and red horse a fully grown brown zebra and blue horse
UC		a cat on the sofa.	0	a cat on the console. a cat on the sofa. cat on counter and cat off sofa	1	a cat on the sofa. a cat on the console. badger on sofa and cat on console
		boat on the water	0	boat on the polish boat on the soda boat on the water	1	boat on the water boat on the lime ship on water and boat on rubber
		plants on a building	0	plants on bob and plants off building plants on a building court on building and plants off building	1	plants on a building park on a building billboard on building and plants off building