

Heuristic Distribution of Latency-Sensitive Tasks in Multi-Access Edge Computing Systems

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Abstract—Multi-Access Edge Computing (MEC) paradigm has been widely studied as a potential solution to cope with the challenges emerging from new generations of mobile networks. By processing applications' data closer to the users, service providers are able to offload origin servers and their underlying network infrastructure, which consequently reduces users' experienced latency. In this paper, we consider internet-based applications with strict latency tolerance which are primarily enabled by the MEC architecture. Moreover, nodes at the edge may host application-related tasks as well as assist in their provision. We address the Task Distribution Problem (TDP), where the objective is to maximize the overall Quality of Service (QoS) based on the achieved throughput while ensuring that tasks' latency requirements are satisfied. The TDP is modeled as an Integer Programming problem, taking into account three components: (i) tasks' priority assignment, (ii) placement and (iii) routing through the MEC network. We propose to approach the problem through two different heuristics: a greedy replacement algorithm and a streaming algorithm. In our experiments, we evaluate the algorithms' performance by showing numerical results across different experimental settings. We observe that, for the tested scenarios, our techniques provide a good trade-off between run time and high performance.

Index Terms—Edge Computing, Resource Allocation, Quality of Service, Operations Research, Combinatorial Optimization, Greedy Algorithm, Streaming Algorithm

I. INTRODUCTION

The increasing trend in terms of mobile connectivity and the evolution of data consumption profiles have imposed a series of challenges to the next generation of mobile networks. Not only must their infrastructure be able to handle intense traffic and data processing, it must also accommodate an immense and heterogeneous number of connected devices [1]. Additionally, in order to enable disruptive technologies and innovative applications, they should be designed to have a flexible architecture and support applications and services with different requirements, e.g., in terms of latency and bandwidth. It has been widely discussed in the literature that shifting from the classic Cloud Computing paradigm to the Multi-Access Edge Computing (MEC) paradigm may significantly contribute to address such challenges [2].

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Roughly speaking, the idea is to move data processing and storage from remote cloud servers to network nodes that are located at the “edge”, closer to the application's users. The distribution of computation across different network agents offers the possibility to offload both origin servers and the underlying network infrastructure. In the context of Industry 4.0, Smart Warehouse (SW) systems combine all the aforementioned challenges in an effort to promote digitization and automation of industrial processes. They have been considered an important use case in most envisioned next generation architecture designs, e.g., the EU-funded DED-ICAT 6G project [3]. In particular, SW systems must provide real-time human-machine interaction services with strict latency requirements, e.g., automatically guided vehicles, timely computer-aided industrial operations (e.g., assisted with virtual and augmented reality technologies), etc. A MEC-powered network design is a key enabler of such a system through back-end computation offload and opportunistic networking.

A. Related Work

MEC architectures and applications are comprehensively summarized in [4], [5], [6]. Resource allocation on MEC systems has been addressed in numerous variants, e.g., joint minimization of task completion time and energy cost [7], cross-layer multiple resource allocation [8], auction-based blockchain applications [9], and QoS for vehicular systems [10]. Some industrial solutions include, for example, efficient routing for energy-balanced consumption in heterogeneous Industrial IoT (IIoT) [11] and energy-efficient scheduling guaranteeing delay requirements [12]. Authors in [13] propose a full model for joint optimization of service placement and routing capabilities targeting low latency applications. Moreover, in [14], the authors propose an optimization model and greedy algorithm to perform resource allocation in MEC network for the edge-gaming application, considering energy saving and high intensity computation. The model considered in [15] for the cost minimization problem in OFDM two-layer networks share many similarities to the modeling proposed in this paper. The streaming optimization framework [16] is the foundation of one of our proposed techniques. A seminal work in this area was proposed in [17], which discusses streaming algorithms for the optimization of submodular functions under cardinality constraints.

B. Main Contributions

We outline our main contributions and present the paper organization as follows:

- We propose a model for a MEC network operating under latency-sensitive requirements in Section II. We model tasks' latency as a linear function of the network's links rate in order to characterize such requirements.
- We introduce the Task Distribution Problem (TDP) in Section III as a throughput maximization problem. We provide theoretical results on its complexity and discuss practical aspects of its exact solution.
- In Section IV, we propose two replacement algorithms to address the problem. The first one is based on greedy decisions and, even though it is more computationally demanding, it has optimality guarantees under uniform scenarios. The second one has a shorter run time and it demands a single pass over the problem's input.
- We discuss experimental results in Section V, showing the algorithms' relative performance in practice.

II. SYSTEM MODEL AND ASSUMPTIONS

Consider a mobile network consisting of a set \mathcal{U} of user equipment (UEs), where each UE is associated with a single mobile Base Station (BS) from a set \mathcal{B} . Each BS is equipped with a MEC host for application-oriented data storage, processing, and routing. For simplicity, we assume that BSs are able to perfectly handle all transmissions from and to their associated UEs, such that UE-BS communication will be transparent to our model. In the transport network, BSs' traffic often converges at sink nodes/gateways also equipped with MEC hosts, which we refer to as "near-edge" nodes (NENs). We represent the set of NENs by \mathcal{N} . MEC hosts may be interconnected (e.g. via Mp3 interface), forming the *MEC network*. The logical topology of the MEC network is represented by a graph $G = (\mathcal{H}, \mathcal{E})$, where nodes $\mathcal{H} = \mathcal{B} \cup \mathcal{N}$ are the MEC hosts (BSs and NENs) and there is an edge in $\mathcal{E} \subseteq \mathcal{H} \times \mathcal{H}$ for each connected pair of MEC hosts.

We refer to applications and services indistinguishably as *tasks*. As in some related work (e.g., [18]), we consider a fixed catalog \mathcal{T} of tasks that are pre-installed at every MEC host. Each UE may place requests for tasks to its associated BS, which will, in turn, forward the request to the *Multi-Access Edge Orchestrator* (MEO), a centralized control intelligence aware of the entire network's infrastructure and available resources. The system has a periodic operation split into *setup* phase and *main* phase. In the setup phase, the MEO, upon receiving the set of requests $\mathcal{R} \subseteq \mathcal{U} \times \mathcal{T}$, determines how resources should be allocated for their provision. It also assigns one MEC host to be the *provider* of each request and the route through which tasks' data will be forwarded. Then, in the main phase, tasks' data is effectively exchanged between UEs and providers and eventual new requests are placed to be handled on the setup phase of the next period.

A. System Operation

In the setup phase, the MEO must determine a *provision plan*, which consists of three components.

1) *Priority assignment*: Consider a set \mathcal{P} of priorities. One priority must be assigned to each request, which is associated to a specific transmission performance level (and, consequently, to the demanded amount of resources). We measure performance in terms of the achieved average throughput, which is responsible for providing UEs with a smoother, uninterrupted experience [19]. When priority p is assigned to request r , the associated task's data transmission will achieve an average throughput of T_p^r .

2) *Request allocation*: Each request r must be allocated to a MEC host (its provider). The provision of each request consumes a portion of the host's computational resources, e.g. in terms of RAM or CPU cycles, and it depends of the request's assigned priority. Each MEC host may be the provider of multiple requests (at different priorities) as long as it has enough available resources. When a request r is assigned to a MEC host h at a priority p , it consumes D_p^r of host h 's total available computational resources C_h .

3) *Request routing*: If the MEO allocates a request to a NEN, then it must also provide a route on the MEC network connecting the request's UE's BS and the actual NEN provider. We represent a request route simply as a path $\{(s, h), \dots, (h', d)\}$ on G , i.e., a cycle-free sequence of distinct edges connecting a source node s to a destination node d , which we henceforth refer to as a *flow*. We define the set of (equivalent) $s - d$ flows, denoted by $\mathcal{F}_{s,d}$, as a set of all flows sharing source and destination nodes. For the MEC network, we define the set of all considered flows as $\mathcal{F} = \{\mathcal{F}_{s,d} : \forall s \in \mathcal{B}, \forall d \in \mathcal{H}\}$.

In order to determine the provision plan, we capture each of its three components with the decision variable

$$\lambda \in \{0, 1\}^{\mathcal{R} \times \mathcal{F} \times \mathcal{P}}, \quad (1)$$

indicating whether request $r \in \mathcal{R}$ is assigned to flow $f \in \mathcal{F}$ at priority $p \in \mathcal{P}$ (i.e., $\lambda_{f,p}^r = 1$) or not (i.e., $\lambda_{f,p}^r = 0$).

B. Latency Model

MEC-network routing naturally produces a *latency* overhead in the tasks' data transmissions due the potential multiple hops. This latency may be an obstacle for some sensitive tasks and must be avoided in the provision plan. In this work, we consider a latency model based on the end-to-end delay definition [20], i.e., the time to transmit application packets from the request's UE's BS to its provider. We assume that a request's latency consists uniquely of its queuing delay component¹, which is fundamentally impacted by the total throughput at each routing link.

¹As introduced in [20], the end-to-end delay has four components: transmission, propagation, processing, and queuing delays. We justify this assumption by considering a roughly homogeneous network (e.g., packets with the same size, links with equal capacity, etc.), so, in order to simplify our analysis, we can disregard sources of delay other than the queuing delay.

Consider that the total rate over a link $e \in \mathcal{E}$ is simply given by the sum of the average throughput over all requests routed through it, i.e.,

$$\text{RATE}_e(\lambda) \triangleq \sum_{r \in \mathcal{R}} \sum_{f \in \mathcal{F}} \sum_{p \in \mathcal{P}} \mathbb{1}_{e \in f} T_p^r \lambda_{f,p}^r, \quad (2)$$

where $\mathbb{1}_x$ indicates the occurrence of event x . As in some related work (e.g., [21]), we approximate the latency (i.e., the queuing delay) of a request r by a linear function of the rate² on its routing links, i.e.,

$$\text{LATENCY}^r(\lambda) \triangleq \sum_{f \in \mathcal{F}} \sum_{p \in \mathcal{P}} \lambda_{f,p}^r \sum_{e \in f} \alpha_e \text{RATE}_e(\lambda) + \beta_e \quad (3)$$

where $\text{RATE}_e(\cdot)$ is given by (2) and $\alpha_e, \beta_e \in \mathbb{R}_+$ are the line coefficients for edge e . In summary, latency is impacted by two factors: (i) The number of links forwarding the request's data and (ii) the rate over all requests traversing each link.

III. THE TASK DISTRIBUTION PROBLEM

Considering the system model presented in Section II, the Task Distribution Problem (TDP) aims at determining a provision plan that (i) maximizes the system's performance and (ii) meets the requests' latency tolerance. In Problem 1, we present the TDP as an Integer Programming (IP) problem.

Problem 1 (Task Distribution Problem – TDP).

$$\underset{\lambda}{\text{maximize}} \quad \text{QoS}(\lambda) \triangleq \frac{1}{|\mathcal{R}|} \sum_{r \in \mathcal{R}} \sum_{f \in \mathcal{F}} \sum_{p \in \mathcal{P}} T_p^r \lambda_{f,p}^r \quad (4)$$

subject to

$$\sum_{f \in \mathcal{F}} \sum_{p \in \mathcal{P}} \mathbb{1}_{s(f)=b(r)} \lambda_{f,p}^r = 1, \quad \forall r \in \mathcal{R} \quad (5)$$

$$\sum_{r \in \mathcal{R}} \sum_{f \in \mathcal{F}} \sum_{p \in \mathcal{P}} \mathbb{1}_{d(f)=h} D_p^r \lambda_{f,p}^r \leq C_h, \quad \forall h \in \mathcal{H} \quad (6)$$

$$\text{LATENCY}^r(\lambda) \leq L^r, \quad \forall r \in \mathcal{R} \quad (7)$$

$$\lambda \in \{0, 1\}^{\mathcal{R} \times \mathcal{F} \times \mathcal{P}} \quad (8)$$

The elements of Problem 1 are described as follows:

- **Objective function:** The QoS function (4) is defined in terms of the average throughput over all requests.
- **Singularity constraints:** In (5), to every request $r \in \mathcal{R}$, we assign exactly one flow and one priority. Notice that, by multiplying by $\mathbb{1}_{s(f)=b(r)}$, we are enforcing that the chosen flow f has its source node $s(f) \in \mathcal{B}$ coinciding with the BS $b(r) \in \mathcal{B}$ associated with request r 's UE.
- **Computational capacity constraints:** Constraints (6) ensure that the computational limitation of each host is met. We multiply by $\mathbb{1}_{d(f)=h}$ in order to guarantee that we are considering only if flow f 's destination host $d(f)$ consumes resources of host h .
- **Latency requirement constraints:** In constraints (7), we ensure that request r 's latency, as defined in (3), meets its threshold L^r .

²The system is stable if the total throughput over every link is bounded by the link's capacity [20]. We assume that all links have enough capacity to accommodate the maximum priority throughput.

Proposition III.1. Problem 1 is \mathcal{NP} -Hard.

Due to space limitations, we present the full proof of Proposition III.1 in our technical report [22]. The idea is to reduce the Multiple Knapsack Problem, which is \mathcal{NP} -Hard [23], to a particular instance of Problem 1, where requests enjoy sufficiently high latency tolerance such that routing can be disregarded in the problem's solution. A corollary of such a reduction is that TDP's decision version is \mathcal{NP} -Complete in the strong sense, so it does not admit a polynomial time approximation scheme (PTAS).

Remark III.1. Because latency constrains (7) can be “linearized” through a succession of substitutions, we can find its exact solution through traditional integer programming methods. Moreover, we can obtain an upper bound to the linear version of Problem 1 if we solve its continuous relaxation, i.e., relaxing the integrality of variables λ . Then, Problem 1's relaxation can be translated to a Linear Programming (LP) problem, which can be efficiently solved.

The setup time for the MEO to determine the provision plan should be as short as possible, which makes most IP exact solution methods unfeasible to be used in practice. In the next section, we propose to tackle the TDP with approximate algorithms and discuss some theoretical optimality results.

IV. APPROXIMATE ALGORITHMS

In this section, we introduce two heuristic methods to approach Problem 1: (1) the Greedy Replacement Algorithm and (2) the Streaming Replacement Algorithm.

A. Set Formulation

We build a ground set $V = \mathcal{R} \times \mathcal{F} \times \mathcal{P}$, which each element $v = (r, f, p) \in V$ is a tuple indicating that flow f is assigned to request r at priority p . From now on, we consider that \mathcal{F} consists uniquely of the shortest flows between each pair s, d . Now, consider a solution set $X \subseteq V$ which holds a candidate setup to solve a given instance of Problem 1. We denote by V^r the partition of the ground set V related to assignments for request r , such that $V = (V^1, \dots, V^{|\mathcal{R}|})$.

The translation of Problem 1 to an equivalent problem in the set-function framework is rather straightforward and we introduce its formulation in Problem 2.

Problem 2 (TDP - Set Formulation).

$$\underset{X \subseteq V}{\text{maximize}} \quad \text{QoS}(X) \triangleq \frac{1}{|\mathcal{R}|} \sum_{v \in X} T_{p(v)}^{r(v)} \quad (9)$$

subject to

$$|V^r \cap X| = 1, \forall r \in \mathcal{R} \quad (10)$$

$$\sum_{v \in X} \mathbb{1}_{d(v)=h} D_{p(v)}^{r(v)} \leq C_h, \forall h \in \mathcal{H} \quad (11)$$

$$\sum_{v \in X \cap V^r} \sum_{e \in f(v)} \alpha_e \left[\sum_{v' \in X} \mathbb{1}_{e \in f'} T_{p'}^{r'} \right] + \beta_e \leq L^r, \forall r \in \mathcal{R} \quad (12)$$

The objective function is given by (9). We ensure in (10) that there is only one element in X for each request. The

computational capacity constraints are presented in (11), where we represent the destination node of the flow associated to element v by $d(v)$. Finally, the latency requirement constraints are depicted in (12).

In what follows, we use function $\text{ISVALID} : 2^V \rightarrow \{0, 1\}$, to indicate whether a set X is a valid solution, in terms of constraints (10), (11), and (12), or not. We also define the *implementation cost* of a provision plan X as

$$W(X) \triangleq \frac{1}{2|\mathcal{H}|} \sum_{h \in \mathcal{H}} \frac{\sum_{v \in X} \mathbb{1}_{d(v)=h} D_p^{r(v)}}{C_h} + \frac{1}{2|\mathcal{R}|} \sum_{r \in \mathcal{R}} \frac{\text{LATENCY}^r(X)}{L^r}, \quad (13)$$

where, for a valid solution X , the values of $W(X)$ are limited within the interval $[0, 1]$. Finally, inspired by [24], we propose to measure flows' centrality by the sum of their composing edges' *betweenness*³, i.e.,

$$B_f \triangleq \sum_{e \in f} \frac{1}{|\mathcal{F}|} \sum_{f' \in \mathcal{F}} \mathbb{1}_{e \in f'} \quad (14)$$

As the rate (2) primarily affects the latency, choosing less central shortest flows provides solution candidates with less chances to violate latency constraints.

B. Greedy Replacement Algorithm

In our first approach, we propose a greedy replacement algorithm, which, at every iteration, replaces element $v \in X$ with another element $v' \in V \setminus X$, of the same request (i.e., $r(v) = r(v')$), that provides the largest cost-benefit, i.e., marginal performance gain over the implementation cost. We describe its detailed operation in Algorithm 1.

Algorithm 1 has a simple implementation and runs in $\mathcal{O}(|V|^2)$, because the ground set update in line (26) enforces that replaced elements are not reconsidered. Even though we can not provide a PTAS (as discussed in Section III), we provide optimality guarantees under special cases.

Proposition IV.1. If requests' latency is independent of other requests, i.e., $\forall e \in \mathcal{E}, \alpha_e = 0$, then a provision plan X_{GREEDY} provided by Algorithm 1 enjoys $(1-1/e)$ optimality guarantee.

The objective function (9) is a monotone, submodular function and, in this case, the latency constraints can be converted into an additional set of knapsack constraints. Then, we reduce the submodular multiple knapsack problem to Problem 2 and, consequently, it holds that Algorithm 1's results are at most $(1 - 1/e)$ far from the optimal [26]. We refer to our technical report [22] for a complete proof.

Proposition IV.2. If, $\forall r \in \mathcal{R}, \forall p \in \mathcal{P}$, (i) $T_p^r = pT$ and (ii) $D_p^r = pD$, for some $T, D \in \mathbb{R}_+$, then a provision plan X_{GREEDY} provided by Algorithm 1 is optimal.

Due to space limitations, we present the detailed proof of Proposition IV.2 in our technical report [22]. In summary, the

³Edge Betweenness [25] is a centrality in networks which assigns a score to an edge based on the fraction of shortest paths traversing it.

Algorithm 1: GREEDY

input : $G = (\mathcal{H}, \mathcal{E}), \mathcal{F}, \mathcal{R}, \mathcal{P}, V = (V^1, \dots, V^{|\mathcal{R}|})$,
Functions $\text{QoS}(\cdot), W(\cdot), \text{ISVALID}(\cdot)$, and
Parameters $\mathbf{D}, \mathbf{C}, \mathbf{T}, \mathbf{L}, \alpha, \beta, \mathbf{B}$.

output: Valid Provision Plan X

```

1  $X \leftarrow \emptyset$ 
2 repeat
3    $v_{\text{IN}} \leftarrow \text{NONE}$ 
4    $\Delta \text{QoS}^* \leftarrow 0$ 
5    $\Delta W^* \leftarrow 2$ 
6   for  $v \in V \setminus X$  do
7      $X_{\text{REP}} \leftarrow (X \setminus V^{r(v)}) \cup \{v\}$ 
8     if  $\text{ISVALID}(X_{\text{REP}})$  then
9        $\Delta \text{QoS} \leftarrow \text{QoS}(X_{\text{REP}}) - \text{QoS}(X)$ 
10       $\Delta W \leftarrow B_{f(v)}(W(X_{\text{REP}}) - W(X) + 1)$ 
11      if  $\frac{\Delta \text{QoS}}{\Delta W} > \frac{\Delta \text{QoS}^*}{\Delta W^*}$  then
12         $v_{\text{IN}} \leftarrow v$ 
13         $\Delta \text{QoS}^* \leftarrow \Delta \text{QoS}$ 
14         $\Delta W^* \leftarrow \Delta W$ 
15      else if  $\Delta \text{QoS} = \Delta \text{QoS}^* = 0$  then
16        if  $\Delta W < \Delta W^*$  then
17           $v_{\text{IN}} \leftarrow v$ 
18           $\Delta \text{QoS}^* \leftarrow \Delta \text{QoS}$ 
19           $\Delta W^* \leftarrow \Delta W$ 
20        end
21      end
22    end
23  end
24   $v_{\text{OUT}} \leftarrow X \cap V^{r(v_{\text{IN}})}$ 
25   $X \leftarrow X \setminus \{v_{\text{OUT}}\} \cup \{v_{\text{IN}}\}$ 
26   $V \leftarrow V \setminus \{v_{\text{OUT}}\}$ 
27 until  $\Delta \text{QoS}^* = 0$  and  $\Delta W^* = 2$ 
28 return  $X$ 

```

proof is based on the fact that the objective function of a solution X is simply given by the total assigned priority, i.e.,

$$\text{QoS}(X) = \frac{1}{|\mathcal{R}|} \sum_{v \in X} T_p^{r(v)} = \frac{T}{|\mathcal{R}|} \sum_{v \in X} p(v) = \frac{T}{|\mathcal{R}|} P(X), \quad (15)$$

where $P(X)$ is solution X 's priority level, i.e., the sum of the assigned priorities. This provides an instance of Problem 2 with optimal sub-structure, so we can gradually build the final solution by moving from a current solution X , in a priority level $P(X)$, to a new solution X' , in an immediately higher priority level $P(X') = P(X) + 1$, until it reaches the optimal level $P(X_{\text{GREEDY}}) = P(X^*)$.

C. Streaming Replacement Algorithm

We propose to solve the TDP using an algorithm based on the streaming framework, which consists in finding a solution with a single pass over the input set (see [17] for a thorough explanation). It evaluates each element in V and replaces the element of the same request in the current solution set X if it (i) provides a better QoS or (ii) provides equal QoS but

at a smaller implementation cost. We describe the detailed procedure in Algorithm 2.

Algorithm 2: STREAMING

input : $G = (\mathcal{H}, \mathcal{E}), \mathcal{F}, \mathcal{R}, \mathcal{P}, V = (V^1, \dots, V^{|\mathcal{R}|}),$
 Functions $\text{QoS}(\cdot), W(\cdot), \text{ISVALID}(\cdot),$ and
 Parameters $\mathbf{D}, \mathbf{C}, \mathbf{T}, \mathbf{L}, \alpha, \beta, \mathbf{B}.$

output: Valid Provision Plan X

```

1  $X \leftarrow \emptyset$ 
2 for  $v \in V$  do
3    $X_{\text{REP}} \leftarrow X \setminus V^{r(v)} \cup \{v\}$ 
4   if  $\text{ISVALID}(X_{\text{REP}})$  then
5     if  $\text{QoS}(X_{\text{REP}}) > \text{QoS}(X)$  then
6        $X \leftarrow X_{\text{REP}}$ 
7     else if  $\text{QoS}(X_{\text{REP}}) = \text{QoS}(X)$  then
8       if  $W(X_{\text{REP}}) < W(X)$  then
9          $X \leftarrow X_{\text{REP}}$ 
10      end
11    end
12  end
13 end
14 return  $X$ 

```

Remark IV.1. The immediate replacement may quickly exhaust the available resources, stopping the algorithm from achieving better results. Let the *individual cost* of $v \in V$ be defined as

$$w_v \triangleq D_{p(v)}^{r(v)} + |f(v)| T_{p(v)}^{r(v)}.$$

In order to improve Algorithm 2's performance, we propose a 2-pass variant: Before effectively running the algorithm, we sort the elements in ascending order of individual cost.

V. EXPERIMENTAL RESULTS

In this section, we first study the performance of our algorithms for different number of requests and network sizes. Then, we study how parameters α and β affect the optimal solution and the performance of the proposed approximate techniques. In our experiments, we consider a random MEC network consisting of 10 BSs and 20 NENs. We control the density of edges in the network with parameter $\rho \in (0, 1]$, such that $\rho = 1$ means a fully connected network. BSs and NENs have $C_h = 32.0$ GB and $C_h = 64.0$ GB of RAM, respectively. We consider 3 priorities, such that, $\forall r \in \mathcal{R}$, computational demands are $D_1^r = 1.0$ GB, $D_2^r = 2.0$ GB, and $D_3^r = 4.0$ GB, and the throughput levels are $T_1^r = 10.0$ Mbps, $T_2^r = 20.0$ Mbps, and $T_3^r = 30.0$ Mbps. Requests source hosts are chosen uniformly at random among the BSs and the related latency is also uniformly selected from the interval $[50.0, 150.0]$ ms. All these values are consistent with the literature (e.g., [14]).

Given the described experimental setup, we generate the request set such that BSs can provide all their UEs' requests at the lowest priority possible. This guarantees that the optimization problem always have a feasible solution, which we refer to

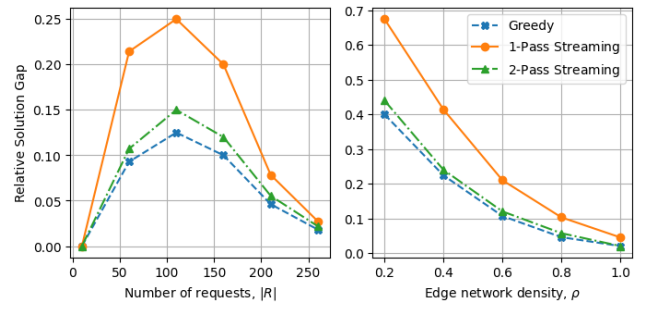


Fig. 1. Relative gap (left) versus the number of request $|\mathcal{R}|$ for $\rho = 0.6$ and (right) versus network density ρ for $|\mathcal{R}| = 110$.

as the *trivial solution*. We propose to compare the performance of Algorithm 1 and Algorithm 2 single- and double-pass with Problem 1's upper bound (UB), provided by its continuous relaxation.

In the first set of experiments, we show the solution gap relative to the UB versus the number of requests $|\mathcal{R}|$, in Figure 1 (left), and versus the density ρ of the MEC network, in Figure 1 (right). In Figure 1 (left), we observe that all techniques start at zero, which means that the network can accommodate all requests in the highest priority. They all lose performance as we increase the number of requests and reach a peak in the solution gap at $|\mathcal{R}| = 100$. Interestingly, after that point, both curves seem to decrease asymptotically converging to zero. We assign this trend to the fact that, at some point, we reach the maximum number of requests the network can prioritize. Then, no matter how many additional requests we include, they will all get the lowest priority. For bigger request sets, the contribution of the excess of minimum-priority requests dominates the performance gain of the optimally assigned requests, making the relative solution gap approaching zero. In Figure 1 (right), we observe that the relative solution gap has its maximum value at $\rho = 0.2$, which means that flows tend to overshare the network edges, resulting in a solution close to the trivial one. The relative solution gap reduces as ρ increases, until it reaches $\rho = 1$, where the network is a complete graph and the flows are simply direct links. In this case, the problem's bottleneck is only the computational capacity of the hosts.

Now, consider that $\alpha_e = \alpha, \forall e \in \mathcal{E}$ and $\beta_e = \beta, \forall e \in \mathcal{E}$. In the second set of experiments, we show the relative solution gap versus parameters α , in Figure 2 (left), and versus the density β , in Figure 1 (right). In Figure 1 (left), we observe that, if $\alpha = 0$, the rate does not affect the latency and, thus, the problem is reduced to the computational constraints (in this setup, the hosts can provide all requests at the highest priority). The solution gap for the algorithms reach their peaks at $\alpha = 1$ and converge to zero, where only the trivial solution is feasible. Figure 1 (right) shows an abrupt decrease towards zero where only the trivial solution is feasible. Note that STREAMING had its performance increased significantly by considering a pre-processing step, with results closer to the GREEDY's ones.

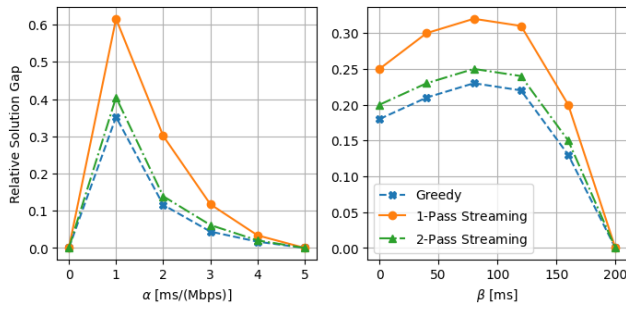


Fig. 2. Relative gap (left) versus the number of request α for $\beta = 80$ and (right) versus β for $\alpha = 1.5$.

VI. CONCLUSIONS AND FUTURE WORK

The TDP captures the primary requirements of latency-sensitive applications on top of MEC architectures. In this paper, we propose to approach the TDP with a flow-based optimization model. We also propose to approximate the latency through a linear model based on the classic end-to-end queuing delay. We approach the problem using two different replacement algorithms. The first one is based on greedy updates and, even though it is more computationally costly, it enjoys optimality guarantees under specific assumptions (e.g., see Proposition IV.2). The second one is designed within the streaming framework, which is able to quickly provide a feasible solution. In our experiments, we could observe our techniques' performance. Our proposed streaming algorithm is simple and, if considering two passes, may provide solutions with similar results to the greedy one. This framework can be expanded to consider a mathematical modeling for the robust optimization of the expected QoS under random requests and accounting for uncertainties.

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