# Analysis of Intelligent Vehicular Relaying in Urban 5G+ Millimeter-Wave Cellular Deployments 

Vitaly Petrov*, ${ }^{*}$, Dmitri Moltchanov*, Sergey Andreev*, and Robert W. Heath Jr. ${ }^{\dagger}$<br>*Unit of Electrical Engineering, Tampere University, Finland<br>${ }^{\dagger}$ Department of Electrical and Computer Engineering, The University of Texas at Austin, USA<br>\{vitaly.petrov, dmitri.moltchanov, sergey.andreev\}@tuni.fi, rheath@utexas.edu


#### Abstract

The capability of smarter networked devices to dynamically select appropriate radio connectivity options is especially important in the emerging millimeter-wave (mmWave) systems to mitigate abrupt link blockage in complex environments. To enrich the levels of diversity, mobile mmWave relays can be employed for improved connection reliability. These are considered by 3GPP for on-demand densification on top of the static mmWave infrastructure. However, performance dynamics of mobile mmWave relaying is not nearly well explored, especially in realistic conditions, such as urban vehicular scenarios. In this paper, we develop a mathematical framework for the performance evaluation of mmWave vehicular relaying in a typical street deployment. We analyze and compare alternative connectivity strategies by quantifying the performance gains made available to smart devices in the presence of $\mathbf{m m W a v e}$ relays. We identify situations where the use of $\mathbf{m m W a v e}$ vehicular relaying is particularly beneficial. Our methodology and results can support further standardization and deployment of mmWave relaying in more intelligent 5G+ "all-mmWave" cellular networks.


## I. Introduction

Millimeter-wave (mmWave) communications is one of the key solutions introduced by the fifth-generation (5G) wireless networks. Adopted by 3GPP for New Radio (NR) technology, mmWave communications enable transmissions with the data rates considerably higher than those offered by 4G microwave solutions [1]. In contrast, the coverage range of a mmWave access point (AP) is expected to be smaller than that offered by sub- 6 GHz cellular systems and will remain within a few hundred meters [2]. The highly directional mmWave transmissions are also susceptible to blockage - occlusion of the signal path by buildings, vehicles, and even human bodies [3]. Dense deployments of mmWave APs are a natural solution, but may incur capital and operating expenditures [4].

Millimeter-wave relays are an alternative to backhauled APs. Static mmWave relays can densify the network at lower costs than full-fledged APs without compromising its performance [5], [6]. The use of static mmWave relays has been ratified by 3GPP as part of 5G NR Rel. 15 [7]. Currently, 3GPP continues to investigate this area by targeting a possible adoption of mobile mmWave relays mounted on vehicles and drones as part of NR Rel. 17 and beyond [8]. That work is currently at an early stage focused primarily on identifying the target setups, where the deployment of mobile mmWave relays is especially beneficial. For this purpose, a holistic

[^0]methodology is required, which accounts for a realistic city deployment, features of vehicular and drone-carried relay operation, and complex propagation of mmWave signal.

In this paper, we develop a mathematical framework for the performance evaluation of a cellular network with mmWave APs, intelligent mmWave users, and mmWave vehicular relays. Our framework accounts for the specifics of a realistic urban (street) deployment, 3GPP-compatible mmWave signal propagation model with blockage caused by humans and vehicles, and alternative relaying strategies. We apply our framework to quantifying the realistic performance gains that mmWave vehicular relays may bring to an average user. We highlight the conditions where the use of mmWave vehicular relays leads to a more than two-fold increase in the spectral efficiency. Our methodology and numerical results can be used to justify the system design choices for the mmWave vehicular relaying in complex and dynamic mmWave-based networks.

## II. System Model

## A. Scenario and Deployment

We consider a straight segment of a street with four traffic lanes and two sidewalks (see Fig. 1]. The lane width is $w_{\mathrm{L}}$ and the width of the sidewalk is $w_{\mathrm{S}}$. Static mmWave APs are deployed on the lampposts between the central lanes at a height $h_{\mathrm{A}}$. The separation distance between the APs is $d_{\mathrm{I}}$. On each sidewalk, there are two human paths representing a typical bidirectional flow. A human body is modeled as a cylinder with a radius $r_{\mathrm{P}}$ and a height $h_{\mathrm{P}}$. The pedestrians on the same path are separated by a random distance $\ell$, where $L$ is a generally-distributed random variable (RV) with the cumulative distribution function (CDF) $F_{L}(x)$. Each pedestrian carries a mmWave user equipment (UE) at a height of $h_{\mathrm{U}}$.

Two types of vehicles are deployed in our scenario: (i) regular vehicles termed cars and modeled as parallelepipeds with the dimensions of $\ell_{\mathrm{C}} \times w_{\mathrm{C}} \times h_{\mathrm{C}}$, and (ii) large vehicles representing city buses and trucks termed buses and modeled as parallelepipeds with the dimensions of $\ell_{\mathrm{T}} \times w_{\mathrm{T}} \times h_{\mathrm{T}}$. Buses and cars are deployed randomly along the centers of all the traffic lanes with a random distance $d$ between their bumpers, where $D$ is a generally-distributed RV with the mean $\mathrm{E}[D]$. Each vehicle is a bus with probability $p_{\mathrm{T}}$ independently of other vehicles. A fraction of cars, $p_{\mathrm{R}}$, are also equipped with mmWave relaying capabilities and can act as "cells on wheels" (COWs). The COW coverage range is $R$.


Fig. 1. Our considered urban street deployment for mmWave vehicular relaying with the regular placement of static mmWave APs, random locations of pedestrians, cars, and buses. A fraction $p_{\mathrm{R}}$ of cars are also equipped with mmWave relaying capabilities and can forward traffic between UEs and mmWave APs.

## B. Propagation Model

The mmWave signal propagation is modeled following the recent 3GPP considerations [9] and accounts for both humanand vehicle-body blockage. In case where the line-of-sight (LoS) path between the communicating nodes is occluded by either a human or a vehicle body, the nodes use an alternative non-line-of-sight (nLoS) path by utilizing one of the reflected or scattered mmWave signal components [10].

Following [9], the pathloss, $T$, is given by

$$
T=\left\{\begin{array}{l}
32.4+21.0 \log _{10}\left(d_{3 \mathrm{D}}\right)+20 \log _{10} f_{\mathrm{c}}, \operatorname{LoS}  \tag{1}\\
32.4+31.9 \log _{10}\left(d_{3 \mathrm{D}}\right)+20 \log _{10} f_{\mathrm{c}}, \mathrm{nLoS}
\end{array}\right.
$$

where $f_{c}$ is the carrier frequency and $d_{3 \mathrm{D}}$ is the 3 D separation distance between the nodes.

The communicating entities in our model (APs, UEs, and COWs) set their transmit powers as $P_{\mathrm{A}}, P_{\mathrm{U}}$, and $P_{\mathrm{C}}$, respectively. All the nodes also utilize directional antenna radiation patterns with the corresponding gains of $G_{\mathrm{A}}, G_{\mathrm{U}}$, and $G_{\mathrm{C}}: G_{\mathrm{U}} \leq G_{\mathrm{C}} \leq G_{\mathrm{A}}$. For simplicity, we assume perfect beam alignment between the communicating entities.

## C. Connectivity Models

We analyze and compare three UE connectivity strategies:

- Baseline. All the UEs always utilize the infrastructure link to the nearest static mmWave AP. No relays are used.
- Conservative Relay. COWs can assist UEs within their coverage. The radio resources occupied by UE-COW connections do not overlap with those utilized for UE-AP and COW-AP links. This strategy primarily reflects the implementation of mobile relays in 3G and 4G systems by providing a pessimistic estimate for the performance gains of mmWave vehicular relays in our scenario.
- Agressive Relay. COWs can assist UEs within their coverage. The radio resources occupied by UE-COW
connections may overlap with those utilized for UE-AP and COW-AP links, thus exploiting better spatial diversity of narrow-beam 5G mmWave communications [11]. This strategy offers an optimistic estimate for the performance gains of mmWave vehicular relays in our scenario.
For both relay-aided strategies, each of the UEs continiously selects the path currently characterized by the highest signal-to-noise ratio (SNR) out of those provided by the static APs and COWs. UE is assumed to instantaneously switch to the best available link via multi-connectivity mechanisms [12].

In the following sections, we develop a mathematical framework for evaluating the introduced connectivity strategies. We particularly focus on a dense deployment of mmWave APs that do not permit outages. Therefore, the UE mean spectral efficiency (SE) is selected as a primary performance indicator.

## III. Analysis of Baseline Model

## A. Human-Body Blockage Modeling

In this subsection, we derive the probability that the link between UE and AP is blocked by a pedestrian, where the UE is separated from the AP by a fixed distance of $x_{0}$. Following [13], the link is considered blocked if there is at least a single pedestrian center in the "blockage zone", see Fig. 2. The width of this rectangle is $2 r_{\mathrm{P}}$, while its length, $\ell_{\mathrm{B}}$, can be derived as $\ell_{\mathrm{B}}=r_{\mathrm{P}}+d_{2 \mathrm{D}}\left(h_{\mathrm{P}}-h_{\mathrm{U}}\right) /\left(h_{\mathrm{A}}-h_{\mathrm{U}}\right)$, where $d_{2 \mathrm{D}}=\sqrt{\left(3 w_{\mathrm{S}} / 4+2 w_{\mathrm{L}}\right)^{2}+x_{0}^{2}}$ is the AP-UE distance.

Observe that the link can be blocked by the pedestrians on both paths. From the scenario geometry, the blockage probability for the pedestrians on the same path, $p_{\mathrm{B}, \mathrm{H}_{1}}$, equals the probability that at least a single cylinder base center is within the interval of length $z=r_{\mathrm{P}} / \sin (\alpha)$. Hence, we have

$$
\begin{equation*}
p_{\mathrm{B}, \mathrm{H}_{1}}=\operatorname{Pr}\{\ell \leq z\}=F_{L}\left(r_{\mathrm{P}} / \sin \alpha\right), \tag{3}
\end{equation*}
$$

$$
p_{\mathrm{B}}= \begin{cases}F_{L}(z)+\frac{1-F_{L}(z)}{\mathrm{E}[L]}\left(2 z-\int_{0}^{2 z} F_{L}(x) d x\right), & h_{\mathrm{T}}<h_{\mathrm{T}}^{\star} \cap w_{\mathrm{S}} \leq 2 r_{\mathrm{P}}+\frac{\left(h_{\mathrm{P}}-h_{\mathrm{U}}\right)\left(8 w_{\mathrm{L}}+3 w_{\mathrm{S}}\right)}{2\left(h_{\mathrm{A}}-h_{\mathrm{U}}\right)}  \tag{2}\\ F_{L}(z), & h_{\mathrm{T}}<h_{\mathrm{T}}^{\star} \cap w_{\mathrm{S}}>2 r_{\mathrm{P}}+\frac{\left(h_{\mathrm{P}}-h_{\mathrm{U}}\right)\left(8 w_{\mathrm{L}}+3 w_{\mathrm{S}}\right)}{2\left(h_{\mathrm{A}}-h_{\mathrm{U}}\right)} \\ 1-\frac{\left(\ell_{\mathrm{C}}-p_{\mathrm{T}} \ell_{\mathrm{C}}+\mathrm{E}[D]\right)\left(1-F_{L}(z)-\frac{1-F_{L}(z)}{\mathrm{E}[L]}\left(2 z-\int_{0}^{2 z} F_{L}(x) d x\right)\right)}{p_{\mathrm{T}} \ell_{\mathrm{T}}+\left(1-p_{\mathrm{T}}\right) \ell_{\mathrm{C}}+\mathrm{E}[D]}, & h_{\mathrm{T}} \geq h_{\mathrm{T}}^{\star} \cap w_{\mathrm{S}} \leq 2 r_{\mathrm{P}}+\frac{\left(h_{\mathrm{P}}-h_{\mathrm{U}}\right)\left(8 w_{\mathrm{L}}+3 w_{\mathrm{S}}\right)}{2\left(h_{\mathrm{A}}-h_{\mathrm{U}}\right)} \\ 1-\frac{\left(\ell_{\mathrm{C}}-p_{\mathrm{T}} \ell_{\mathrm{C}}+\mathrm{E}[D]\right)\left(1-F_{L}(z)\right)}{p_{\mathrm{T}} \ell_{\mathrm{T}}+\left(1-p_{\mathrm{T}}\right) \ell_{\mathrm{C}}+\mathrm{E}[D]}, & h_{\mathrm{T}} \geq h_{\mathrm{T}}^{\star} \cap w_{\mathrm{S}}>2 r_{\mathrm{P}}+\frac{\left(h_{\mathrm{P}}-h_{\mathrm{U}}\right)\left(8 w_{\mathrm{L}}+3 w_{\mathrm{S}}\right)}{2\left(h_{\mathrm{A}}-h_{\mathrm{U}}\right)}\end{cases}
$$

where $F_{L}(x)$ is the CDF of the RV characterizing the distance between the neighboring humans on the same path.

The link can also be blocked by the pedestrians on the other path when the following two conditions apply simultaneously. First, $\ell_{\mathrm{B}}$ has to be large enough so that this path crosses the blockage zone rectangle. Second, there should be at least one cylinder base center within the $2 z$-long segment of the path crossing the blockage zone rectangle (see Fig. 27).

The first condition can be written as $w_{\mathrm{S}} / 2 \leq s_{\mathrm{B}}$, where $w_{\mathrm{H}}=2 w_{\mathrm{L}}+3 w_{\mathrm{S}} / 4$. For the second condition, we apply the result from [14]. Finally, the sought blockage probability is

$$
p_{\mathrm{B}, \mathrm{H}_{2}}= \begin{cases}\frac{2 z-\int_{0}^{2 z} F_{L}(x) d x}{\mathrm{E}[L]}, & w_{\mathrm{S}} \leq 2 r_{\mathrm{P}}+2 w_{\mathrm{H}} \frac{h_{\mathrm{P}}-h_{\mathrm{U}}}{h_{\mathrm{A}}-h_{\mathrm{U}}}  \tag{4}\\ 0, & w_{\mathrm{S}}>2 r_{\mathrm{P}}+2 w_{\mathrm{H}} \frac{h_{\mathrm{P}}-h_{\mathrm{U}}}{h_{\mathrm{A}}-h_{\mathrm{U}}}\end{cases}
$$

Finally, because the events of blockage for the two paths are independent of each other, we arrive at the following expression for the human-body blockage probability

$$
p_{\mathrm{B}, \mathrm{H}}= \begin{cases}F_{L}(z)+\frac{\left(1-F_{L}(z)\right)\left(2 z-\int_{0}^{2 z} F_{L}(x) d x\right)}{\mathrm{E}[L]}, & w_{\mathrm{S}} \leq w_{\mathrm{U}}  \tag{5}\\ F_{L}(z), & w_{\mathrm{S}} \leq w_{\mathrm{U}}\end{cases}
$$

where $z=r_{\mathrm{P}} \sqrt{\left(8 w_{\mathrm{L}}+3 w_{\mathrm{S}}\right)^{2}+16 x_{0}^{2}} /\left(8 w_{\mathrm{L}}+3 w_{\mathrm{S}}\right)$ and $w_{\mathrm{U}}=2 r_{\mathrm{P}}+w_{\mathrm{H}}\left(h_{\mathrm{P}}-h_{\mathrm{U}}\right) /\left(h_{\mathrm{A}}-h_{\mathrm{U}}\right)$.

## B. Vehicle-Body Blockage Modeling

In the considered scenario, a link between UE and AP can also be occluded by large vehicles, termed buses. Based on the scenario geometry in Fig. 33 the following holds for the minimal bus height that results in blockage, $h_{\mathrm{T}}^{\star}$

$$
\begin{equation*}
\frac{h_{\mathrm{T}}^{\star}-h_{\mathrm{U}}}{h_{\mathrm{A}}-h_{\mathrm{U}}}=\frac{\sqrt{x_{\mathrm{B}}^{2}+w^{2}}}{\sqrt{x_{0}^{2}+w_{\mathrm{H}}^{2}}} \tag{8}
\end{equation*}
$$

where $x_{\mathrm{B}}$ is the shift of the blocking vehicle from the UE, $x_{\mathrm{B}}=x_{0} w / w_{\mathrm{H}}$. Substituting $x_{\mathrm{B}}$ into (88, we make an important observation that $h_{\mathrm{T}}^{\star}$ does not depend on $x_{0}$, i.e.,

$$
\begin{equation*}
h_{\mathrm{T}}^{\star}=h_{\mathrm{U}}+\frac{3 w_{\mathrm{S}}+2 w_{\mathrm{L}}-2 w_{\mathrm{T}}}{8 w_{\mathrm{L}}+3 w_{\mathrm{S}}}\left(h_{\mathrm{A}}-h_{\mathrm{U}}\right) . \tag{9}
\end{equation*}
$$



Fig. 2. Human-body blockage modeling.


Fig. 3. Minimal height of a bus resulting in vehicle-body blockage.
We now estimate the fraction of time when the UE-AP link is blocked by a bus. Since the number of cars between the two buses on the same lane follows the geometrical distribution with parameter $p_{\mathrm{T}}$, the mean number of cars between the two buses, $\mathrm{E}\left[N_{\mathrm{C}}\right]$, can be estimated as $\mathrm{E}\left[N_{\mathrm{C}}\right]=\left(1-p_{\mathrm{T}}\right) / p_{\mathrm{T}}$. This implies that the random distance between the two buses, $d_{\mathrm{B}}$, comprises of $N_{\mathrm{C}}$ cars and $N_{\mathrm{C}}+1$ inter-vehicle intervals:
$\mathrm{E}\left[D_{\mathrm{B}}\right]=\mathrm{E}\left[N_{\mathrm{C}} \ell_{\mathrm{C}}+\left(N_{\mathrm{C}}+1\right) d\right]=\frac{\mathrm{E}[D]+\ell_{\mathrm{C}}\left(1-p_{\mathrm{T}}\right)}{p_{\mathrm{T}}}$.
Recalling that the deployment of vehicles follows the renewal process with generally distributed intervals, the vehiclebody blockage probability, $p_{\mathrm{B}, \mathrm{v}}$, can be established as [15]

$$
p_{\mathrm{B}, \mathrm{~V}}= \begin{cases}0, & h_{\mathrm{T}}<h_{\mathrm{T}}^{\star},  \tag{11}\\ \frac{\ell_{\mathrm{T}}}{\ell_{\mathrm{T}}+\mathrm{E}\left[D_{\mathrm{B}}\right]}, & h_{\mathrm{T}} \geq h_{\mathrm{T}}^{\star} .\end{cases}
$$

## C. Mean Spectral Efficiency

We now estimate the mean SE of the link between the UE and the AP. First, since the blockage events caused by humans and those caused by vehicles are independent, we derive the total blockage probability for the UE-AP link, $p_{\mathrm{B}}$, as in (2). Further, we determine the conditional SNR values in case of LoS (non-blocked) and nLoS (blocked) signal path between the UE and the AP, $S_{\mathrm{L}}$ and $S_{\mathrm{N}}$, respectively. Following (1),

$$
\begin{align*}
& S_{\mathrm{L}}=10^{\frac{P_{\mathrm{U}}+G_{\mathrm{A}}+G_{\mathrm{U}}-N_{0}(B)-32.4-20 \log _{10} f_{\mathrm{c}}-21.0 \log _{10}\left(K_{\mathrm{U}}\right)}{10}} \\
& S_{\mathrm{N}}=10^{\frac{P_{\mathrm{U}}+G_{\mathrm{A}}+G_{\mathrm{U}}-N_{0}(B)-32.4-20 \log _{10} f_{\mathrm{c}}-31.9 \log _{10}\left(K_{\mathrm{U}}\right)}{10}} \tag{12}
\end{align*}
$$

where $K_{\mathrm{U}}=\sqrt{x_{0}^{2}+\left[2 w_{\mathrm{L}}+3 w_{\mathrm{S}} / 4\right]^{2}+\left(h_{\mathrm{A}}-h_{\mathrm{U}}\right)^{2}}$.
We obtain the mean SE for the UE located at a separation distance of $x_{0}$ from the AP, $C\left(x_{0}\right)$, as

$$
\begin{equation*}
C\left(x_{0}\right)=p_{\mathrm{B}} \log _{2}\left(1+S_{\mathrm{N}}\right)+\left(1-p_{\mathrm{B}}\right) \log _{2}\left(1+S_{\mathrm{L}}\right) \tag{13}
\end{equation*}
$$

Finally, the mean SE for an arbitrary UE, $\mathrm{E}[C]$, is derived as

$$
\begin{equation*}
\mathrm{E}[C]=\frac{2}{d_{\mathrm{I}}} \int_{0}^{d_{\mathrm{I}} / 2} C\left(x_{0}\right) d x_{0} \tag{14}
\end{equation*}
$$

$$
\begin{align*}
& p_{\mathrm{B}}^{*}=\left\{\begin{array}{l}
F_{D_{\mathrm{B}}}\left(\ell_{\mathrm{B}, \mathrm{C}}-\frac{\ell_{\mathrm{C}}}{2}\right), \quad h_{\mathrm{T}}<h_{\mathrm{T}}^{*}, \\
1-\left(1-\frac{p_{\mathrm{T}} \ell_{\mathrm{T}}}{p_{\mathrm{T}} \ell_{\mathrm{T}}+\left(1-p_{\mathrm{T}}\right) \ell_{\mathrm{C}}+\mathrm{E}[D]}\right)\left(1-F_{D_{\mathrm{B}}}\left(\ell_{\mathrm{B}, \mathrm{C}}-\frac{\ell_{\mathrm{C}}}{2}\right)\right), \quad h_{\mathrm{T}} \geq h_{\mathrm{T}}^{*},
\end{array}\right.  \tag{6}\\
& C_{2}^{\dagger}\left(x_{0}, x_{\mathrm{S}}\right)=\frac{1}{1 / C^{\star}\left(x_{\mathrm{S}}\right)+1 / C^{*}\left(x_{1}\right)}=p_{\mathrm{C}}\left(\frac{p_{\mathrm{B}}^{\star} p_{\mathrm{B}}^{*}}{1 / \log _{2}\left(1+S_{\mathrm{N}}^{\star}\right)+1 / \log _{2}\left(1+S_{\mathrm{N}}^{*}\right)}+\frac{\left(1-p_{\mathrm{B}}^{\star}\right) p_{\mathrm{B}}^{*}}{1 / \log _{2}\left(1+S_{\mathrm{L}}^{\star}\right)+1 / \log _{2}\left(1+S_{\mathrm{N}}^{*}\right)}\right. \\
&\left.+\frac{p_{\mathrm{B}}^{\star}\left(1-p_{\mathrm{B}}^{*}\right)}{1 / \log _{2}\left(1+S_{\mathrm{N}}^{\star}\right)+1 / \log _{2}\left(1+S_{\mathrm{L}}^{*}\right)}+\frac{\left(1-p_{\mathrm{B}}^{\star}\right)\left(1-p_{\mathrm{B}}^{*}\right)}{1 / \log _{2}\left(1+S_{\mathrm{L}}^{\star}\right)+1 / \log _{2}\left(1+S_{\mathrm{L}}^{*}\right)}\right) . \tag{7}
\end{align*}
$$

## IV. Analysis of Relaying Models

## A. UE-COW Link Analysis

We now derive the mean SE for the relay link between the UE and the COW vehicle. We start by calculating the probability $p_{\mathrm{C}}$ that there is at least a single COW within the interval $\left[x_{0}-x_{\mathrm{R}}, x_{0}+x_{\mathrm{R}}\right]$, where $x_{\mathrm{R}}=\sqrt{R^{2}-\left(3 w_{\mathrm{S}} / 4+w_{\mathrm{L}} / 2\right)^{2}}$ is the maximum separation between the UE and the COW, so that the UE is under the COW coverage, $R$.

Recalling that only $p_{\mathrm{R}}$ of cars act as COWs, we produce the mean distance between the neighboring COWs as $\mathrm{E}\left[L_{\mathrm{R}}\right]=$ $\left[\ell_{\mathrm{C}}\left(1-p_{\mathrm{T}}\right)+\mathrm{E}[D]+p_{\mathrm{T}} \ell_{\mathrm{T}}\right] /\left[p_{\mathrm{R}}\left(1-p_{\mathrm{T}}\right)\right]$.

Applying the approach from subsection III-B we obtain

$$
\begin{equation*}
p_{\mathrm{C}}=\left(2 x_{\mathrm{R}}-\int_{0}^{2 x_{\mathrm{R}}} F_{L_{\mathrm{R}}}(x) d x\right) / \mathrm{E}\left[L_{\mathrm{R}}\right] \tag{15}
\end{equation*}
$$

Since we consider only the COWs deployed on the side lanes, the UE-COW link is not affected by vehicle-body blockage. Further, as the antenna array at the COW is assumed to be deployed on the rooftop of a car, the height of the COW, $h_{\mathrm{C}}$, is considered to be lower than that of the UE, $h_{\mathrm{U}}$. Therefore, the blockage zone rectangle (see subsection III-A and Fig. 2) is always crossed by both human paths. Consequently, if there is a COW vehicle within the range of $R$ around the UE, the blockage probability for the UE-COW link, $p_{\mathrm{B}}^{\star}$, can be directly obtained from (5) as

$$
\begin{equation*}
p_{\mathrm{B}}^{\star}=F_{L}\left(z_{1}\right)+\frac{1-F_{L}\left(z_{1}\right)}{\mathrm{E}[L]}\left(2 z_{1}-\int_{0}^{2 z_{1}} F_{L}(x) d x\right), \tag{16}
\end{equation*}
$$

where $z_{1}=r_{\mathrm{P}} \sqrt{\left(2 w_{\mathrm{L}}+3 w_{\mathrm{S}}\right)^{2}+16 x_{s}^{2}} /\left(2 w_{\mathrm{L}}+3 w_{\mathrm{S}}\right), x_{\mathrm{S}}$ is a random separation distance between the COW and the UE (see Fig. 11: $x_{\mathrm{S}} \in\left[-x_{\mathrm{R}}, x_{\mathrm{R}}\right]$.

Finally, the mean SE of the UE-COW link, $C^{\star}\left(x_{\mathrm{S}}\right)$ - if there is at least a single COW in range and the UE selects a random COW out of those available - can be computed as

$$
\begin{equation*}
C^{\star}\left(x_{\mathrm{S}}\right)=p_{\mathrm{B}}^{\star} \log _{2}\left(1+S_{\mathrm{N}}^{\star}\right)+\left(1-p_{\mathrm{B}}^{\star}\right) \log _{2}\left(1+S_{\mathrm{L}}^{\star}\right), \tag{17}
\end{equation*}
$$

where the values $S_{\mathrm{L}}^{\star}$ and $S_{\mathrm{N}}^{\star}$ are obtained similarly to 12 .


Fig. 4. Minimal height of a bus leading to blockage of COW-AP link.

## B. COW-AP Link Analysis

Here, we obtain the mean SE of the link between the AP and the COW separated by $x_{1}$ from the AP. This link is only affected by vehicle-body blockage from two sources: (i) buses on the same lane and (ii) buses on the central lane.

For the latter case, the analysis is similar to that in subsection III-B. Particularly, the blockage probability for the buses on the neighboring lane, $p_{\mathrm{B}, \mathrm{N}}^{*}$, can be written as

$$
p_{\mathrm{B}, \mathrm{~N}}^{*}= \begin{cases}0, & h_{\mathrm{T}}<h_{\mathrm{T}}^{*},  \tag{18}\\ \frac{\ell_{\mathrm{T}}}{\ell_{\mathrm{T}}+\mathrm{E}\left[D_{\mathrm{B}}\right]}, & h_{\mathrm{T}} \geq h_{\mathrm{T}}^{*},\end{cases}
$$

where $h_{\mathrm{T}}^{*}=h_{\mathrm{C}}+\left(2 w_{\mathrm{L}}-w_{\mathrm{T}}\right)\left(h_{\mathrm{A}}-h_{\mathrm{C}}\right) / 3 w_{\mathrm{L}}$ is the minimal height of a bus on the central lane yielding blockage.

Blockage of the COW-AP link by a bus on the same lane may occur if there is at least a single bus in the blockage zone of length $\ell_{\mathrm{B}, \mathrm{C}}$, see Fig. 4 For the given bus height and width, the blockage zone length, $\ell_{\mathrm{B}, \mathrm{C}}$, has to be small enough to result in a blockage situation in both horizontal and vertical planes: $\ell_{\mathrm{B}, \mathrm{C}}=x_{1} \min \left\{\left(h_{\mathrm{T}}-h_{\mathrm{C}}\right) /\left(h_{\mathrm{A}}-h_{\mathrm{C}}\right), w_{\mathrm{T}} / 3 w_{\mathrm{L}}\right\}$, where $x_{1}=x_{0}+x_{\mathrm{s}}$.

The distance from an arbitrary COW vehicle to the nearest bus on the same lane is given by $d_{\mathrm{B}}=N_{\mathrm{C}} \ell_{\mathrm{C}}+\sum_{i=1}^{N_{\mathrm{C}}+1} d$, where $N_{\mathrm{C}}$ is a geometrically-distributed RV characterizing the number of cars between the COW and the nearest bus. The blockage probability by a bus on the same lane, $p_{\mathrm{B}, \mathrm{S}}^{*}$, is equal to the probability that $d_{\mathrm{B}}$ does not exceed $\ell_{\mathrm{B}, \mathrm{C}}-\ell_{\mathrm{C}} / 2$

$$
\begin{equation*}
p_{\mathrm{B}, \mathrm{~S}}^{*}=\operatorname{Pr}\left\{d_{\mathrm{B}} \leq \ell_{\mathrm{B}, \mathrm{C}}-\ell_{\mathrm{C}} / 2\right\}=F_{D_{\mathrm{B}}}\left(\ell_{\mathrm{B}, \mathrm{C}}-\ell_{\mathrm{C}} / 2\right), \tag{19}
\end{equation*}
$$

where $F_{D_{\mathrm{B}}}$ is the CDF of the RV $D_{\mathrm{B}}$ that can be computed numerically using non-linear RV transformation techniques [16].
Observing that blockages by buses on the same and the neighboring lanes are independent events, joint blockage probability for the COW-AP link, $p_{\mathrm{B}}^{*}$, is given in (6) as a combination of 18 and 19 . Finally, the mean SE for the COW-AP link where COW is separated from the AP by $x_{1}$ is

$$
\begin{equation*}
C^{*}\left(x_{1}\right)=p_{\mathrm{B}}^{*} \log _{2}\left(1+S_{\mathrm{N}}^{*}\right)+\left(1-p_{\mathrm{B}}^{*}\right) \log _{2}\left(1+S_{\mathrm{L}}^{*}\right) \tag{20}
\end{equation*}
$$

The corresponding SNR values for the COW-AP link in LoS and nLoS cases, $S_{\mathrm{L}}^{*}$ and $S_{\mathrm{N}}^{*}$, are calculated similarly to (12).

## C. Joint UE-COW-AP Connection Analysis

In this subsection, we derive the mean SE for the relayaided UE-COW-AP connection for both relaying strategies considered by our study as detailed in subsection II-C

According to the Aggressive strategy, the performance of the joint UE-COW-AP connection is limited exclusively by the mean SE of the COW-AP link. Therefore, the mean SE
of the joint UE-COW-AP connection, $C_{1}^{\dagger}\left(x_{0}, x_{s}\right)$, is equal to $C^{*}\left(x_{1}\right)$. Its probability mass function (pmf), $f_{C_{1}^{\dagger}}(x)$, is thus

$$
f_{C_{1}^{\dagger}}(x)= \begin{cases}p_{\mathrm{C}} p_{\mathrm{B}}^{*}, & x=\log _{2}\left(1+S_{\mathrm{N}}^{*}\right)  \tag{21}\\ p_{\mathrm{C}}\left(1-p_{\mathrm{B}}^{*}\right), & x=\log _{2}\left(1+S_{\mathrm{L}}^{*}\right) \\ 1-p_{\mathrm{C}}, & x=0\end{cases}
$$

With the Conservative strategy, the radio resources allocated for UE-COW links do not overlap with those available for COW-AP and UE-AP links. Therefore, if the relay link UECOW exists, the mean SE for the UE-COW-AP connection, $C_{2}^{\dagger}\left(x_{0}, x_{\mathrm{S}}\right)$, is obtained as in 7.

We now derive the mean SE when a smart UE selects the best available connection out of UE-AP and opportunistic UE-COW-AP. For this purpose, we first produce the pmf for the SE of the infrastructure UE-AP link (Baseline strategy) where the UE is separated from the AP by $x_{0}, f_{C}(x)$. Recalling (13),

$$
f_{C}(x)= \begin{cases}1-p_{\mathrm{B}}, & x=\log _{2}\left(1+S_{\mathrm{L}}\right)  \tag{22}\\ p_{\mathrm{B}}, & x=\log _{2}\left(1+S_{\mathrm{N}}\right)\end{cases}
$$

Finally, we calculate the mean SE for the best connection with Aggressive and Conservative strategies $\left(C_{1}\left(x_{0}, x_{\mathrm{S}}\right)\right.$ and $C_{2}\left(x_{0}, x_{\mathrm{S}}\right)$, respectively) as the maximum of two RVs representing the SE of infrastructure UE-AP and relay UE-COWAP connections. Accordingly, the mean SE for an arbitrary UE is derived by numerical integration as

$$
\begin{align*}
& \mathrm{E}\left[C_{1}\right]=\frac{1}{d_{\mathrm{I}} x_{\mathrm{R}}} \int_{0}^{d_{\mathrm{I}} / 2} \int_{x_{0}-x_{\mathrm{R}}}^{x_{0}+x_{\mathrm{R}}}\left(C_{1}\left(x_{0}, x_{\mathrm{S}}\right) d x_{\mathrm{S}}\right) d x_{0} \\
& \mathrm{E}\left[C_{2}\right]=\frac{1}{d_{\mathrm{I}} x_{\mathrm{R}}} \int_{0}^{d_{\mathrm{I}} / 2} \int_{x_{0}-x_{\mathrm{R}}}^{x_{0}+x_{\mathrm{R}}}\left(C_{2}\left(x_{0}, x_{\mathrm{S}}\right) d x_{\mathrm{S}}\right) d x_{0} \tag{23}
\end{align*}
$$

## V. Numerical Results

In this section, the obtained results are elaborated numerically. We model a street segment with mmWave APs operating at 28 GHz with 1 GHz of bandwidth and deployed 300 m apart from each other. Following the 3GPP considerations, the heights of APs and UEs are set to 10 m and 1.5 m , respectively [9]. The UE transmit power is 23 dBm and the antenna gains are given as $G_{\mathrm{A}}=27 \mathrm{~dB}$ and $G_{\mathrm{U}}=15 \mathrm{~dB}$ [17]. The radius of a human body is set to 0.3 m , while its height is 1.75 m . We assume $5 \%$ of large vehicles, i.e., $p_{\mathrm{T}}=0.05$ [18].

1) The effect of human density: We start with Fig. 5] introducing the mean UE SE as a function of the density of human-body blockers on the sidewalks. We first observe that the mean SE decreases with the growing density of humanbody blockers. For the Baseline strategy, the mean SE decreases from 12 bits $/ \mathrm{s} / \mathrm{Hz}$ for 0.1 humans $/ \mathrm{m}^{2}$ to 8 bits $/ \mathrm{s} / \mathrm{Hz}$ for 1.0 humans $/ \mathrm{m}^{2}$. Then, we notice that the gain of the considered relaying strategies grows for a higher density of blockers. In other words, more "challenging" environments unlock better gains. The SE with Aggressive strategy is notably higher than that in Conservative case, especially at higher densities of blockers: $17 \mathrm{bits} / \mathrm{s} / \mathrm{Hz}$ vs. $9 \mathrm{bits} / \mathrm{s} / \mathrm{Hz}$ for 1.0 human $/ \mathrm{m}^{2}$.

In Fig. 5, we also assess the accuracy of our derivations and the assumptions made by the system model. For this purpose,


Fig. 5. Mean SE decreases with the growing density of human-body blockers. A close match between the analytical and simulation-based results is observed.


Fig. 6. High density of vehicles has a negative impact on the SE with Baseline strategy and a complex effect on the performance of relay-aided strategies.
we relax three major analytical assumptions in our simulation framework: (i) the pedestrians are not placed on the paths, but rather are uniformly distributed over the sidewalks; (ii) vehicles are not centered on their lanes, but are randomly shifted within a lane, which models realistic city traffic; and (iii) any of the vehicle's sides can block the mmWave signal, not only the one facing the communicating node. Fig. 5 demonstrates a close match between the analytical and simulation-based results, even when the listed assumptions are relaxed. Similar correspondence between analysis and simulations is observed for other input parameters. Therefore, we rely solely on our analytical results in subsequent figures.
2) The effect of vehicle density: We proceed with Fig. 6 that evaluates the mean UE SE as a function of the density of vehicles in the street. In this figure, we first note that only the Baseline scheme is always negatively affected by the growing density of vehicles. In contrast, the dependency is non-monotonic for relay-aided strategies. Particularly, the mean SE decreases at high vehicle densities as a result of vehicle-body blockage. The decrease in the mean SE at lower densities of vehicles is caused by the absence of vehicular relays. We can conclude that the highest gain of relaying is observed in deployments with the medium density of vehicles: over $9 \mathrm{bits} / \mathrm{s} / \mathrm{Hz}$ with Conservative strategy and $18 \mathrm{bits} / \mathrm{s} / \mathrm{Hz}$ with Aggressive strategy for $3-5$ vehicles per 100 m .
3) The effect of COW coverage range: We then analyze the impact of the COW coverage range on the mean UE SE in


Fig. 7. Mean SE increases with COW coverage range and ceases to grow when the range becomes large enough so that $p_{\mathrm{C}} \rightarrow 1$.


Fig. 8. Mean SE increases by $8 \%-120 \%$ as $p_{\mathrm{R}}$ grows. Even small fractions of COWs lead to notable performance gains with Aggressive strategy.

Fig. 7 Here, we first observe that the mean SE increases with the growing relay coverage range. Second, we notice that the SE ceases to grow when the range becomes large enough to almost guarantee a COW in the UE proximity. The value of COW range after which the mean SE stagnates heavily depends on the fraction of vehicles involved in relaying. Finally, we conclude that the Aggressive strategy notably outperforms the Conservative scheme: the mean SE for the former with only $10 \%$ of COW vehicles is higher than the corresponding value for the latter when all $100 \%$ of vehicles act as COWs.
4) The effect of COW fraction: Finally, we assess the overall increase in UE SE brought by COW relays in Fig. 8 . Accordingly, the relative increase in the SE with respect to the Baseline strategy is presented as a function of the fraction of COW vehicles involved in relaying. Based on the obtained results, Conservative relays offer from $8 \%$ ( 0.1 vehicles act as COWs) to $12 \%$ (all vehicles act as COWs) increase in the mean UE SE. In the same conditions, Aggressive relays offer from $70 \%$ to $120 \%$ improvement. The gains with both strategies increase rapidly until $20 \%$ of vehicles are involved in relaying, whereas they cease growing after $40 \%$ of COW vehicles in the street. Therefore, there is no benefit in engaging more than $40 \%$ of vehicles in relaying. In contrast, the use of small fractions of COWs leads to notable performance gains.

## VI. Conclusions

In this paper, we proposed a performance analysis framework for the mmWave vehicular relaying in urban street
layouts. We demonstrated that the performance gains brought by smart mmWave-based relaying are the most significant in vehicular deployments featured by dense human crowds on sidewalks and moderately-dense vehicular traffic. We also showed that even a small density of mmWave vehicular relays can lead to notable performance improvements provided that intelligent UEs can continuously select the best connectivity options out of those offered by static mmWave APs and mmWave vehicular relays.

The developed framework and the presented results can further aid in identifying the setups where the use of mmWave vehicular relaying is especially beneficial, towards the adoption of mmWave-based mobile relays as part of 5G+ networks and their standardization in NR Rel. 17 and beyond.

## AcKnowledgement

This work was supported by the Academy of Finland (projects WiFiUS, PRISMA, and RADIANT). R. Heath was funded in part by the National Science Foundation under Grant No. ECCS-1711702 and by Honda R\&D Americas.

## REFERENCES

[1] T. Bai and R. W. Heath, "Coverage and rate analysis for millimeter-wave cellular networks," IEEE Trans. on Wireless Commun., vol. 14, no. 2, pp. 1100-1114, Feb 2015.
[2] M. R. Akdeniz et al., "Millimeter wave channel modeling and cellular capacity evaluation," IEEE J. on Sel. Areas in Commun., vol. 32, no. 6, pp. 1164-1179, June 2014.
[3] K. Haneda et al., "5G 3GPP-like channel models for outdoor urban microcellular and macrocellular environments," in Proc. of IEEE VTCSpring, May 2016.
[4] T. Bai and R. W. Heath, "Coverage in dense millimeter wave cellular networks," in Proc. of Asilomar Conference on Signals, Systems and Computers, November 2013.
[5] S. Biswas, S. Vuppala, J. Xue, and T. Ratnarajah, "On the performance of relay aided millimeter wave networks," IEEE J. of Sel. Topics in Signal Proc., vol. 10, no. 3, pp. 576-588, April 2016.
[6] H. Ding, D. B. da Costa, J. Coon, and Y. Chen, "Relay when blocked: A hop-by-hop mmWave cooperative transmission protocol," IEEE Communications Letters, vol. 22, no. 9, pp. 1894-1897, September 2018.
[7] 3GPP, "Study on integrated access and backhaul (Release 15)," 3GPP TR 38.874 V16.0.0, January 2019.
[8] 3GPP, "List of work items," https://www.3gpp.org/DynaReport/WIList.htm, July 2019, [Online: Accessed 16-August-2019].
[9] 3GPP, "Study on channel model for frequencies from 0.5 to 100 GHz (Release 14)," 3GPP TR 38.901 V15.0.0, June 2018.
[10] M. Gapeyenko et al., "An analytical representation of the 3GPP 3D channel model parameters for mmWave bands," in Proc. of the 2nd ACM Workshop on Millimeter Wave Networks and Sensing Systems (mmNets'18) in conjunction with ACM MobiCom, October 2018.
[11] V. Petrov et al., "Interference and SINR in millimeter wave and terahertz communication systems with blocking and directional antennas," IEEE Trans. on Wireless Commun., vol. 16, no. 3, pp. 791-808, March 2017.
[12] M. Giordani, M. Mezzavilla, S. Rangan, and M. Zorzi, "An efficient uplink multi-connectivity scheme for 5G millimeter-wave control plane applications," IEEE Trans. on Wireless Commun., vol. 17, no. 10, pp. 6806-6821, October 2018.
[13] V. Petrov et al., "Dynamic multi-connectivity performance in ultradense urban mmWave deployments," IEEE J. on Sel. Areas in Commun., vol. 35, no. 9, pp. 2038-2055, September 2017.
[14] D. R. Cox, Renewal theory. Methuen and Co ltd., 1970.
[15] J. F. C. Kingman, Poisson processes. Wiley Online Library, 1993.
[16] S. M. Ross, Introduction to probability models. Academic press, 2014.
[17] Y. Huo, X. Dong, and W. Xu, "5G cellular User Equipment: From theory to practical hardware design," IEEE Access, vol. 5, July 2017.
[18] M. Hallenbeck and B. Smith, "Vehicle volume distributions by classification," Washington State Transportation Center Report, July 1997.


[^0]:    ${ }^{1}$ A part of this work has been completed during the research visit of Vitaly Petrov to The University of Texas at Austin, USA in Fall 2018.

