# MACHINE LEARNING-AIDED PIECE-WISE MODELING TECHNIQUE OF POWER AMPLIFIER FOR DIGITAL PREDISTORTION

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# ABSTRACT

We propose a new power amplifier (PA) behavioral modeling approach, to characterize and compensate for the signal quality degrading effects induced by a PA with a machine learning (ML) aided piece-wise (PW) modeling approach. Instead of using a single pruned Volterra model, we use multiple smallsize pruned Volterra models by classifying the input data into different classes. For that purpose, an ML classifier model is trained by extracting some crucial features from both the input signal statistics and the PA operating point. The simulation results indicate that our approach contributes to an improved performance/complexity trade-off than a single generalized memory polynomial (GMP) model in terms of PA behavior modeling and linearization.

*Index Terms*— Behavioral modeling, computational complexity, decision tree, digital predistortion (DPD), linearization, machine learning (ML), power amplifier (PA).

## 1. INTRODUCTION

As per green communications obligation, a power amplifier (PA) must be operated as close as possible to its saturation point [1]. However, that leads to wanted effects arising from PA non-linear (NL) behavior such as gain compression, inband (IB), and out-of-band (OOB) distortions [2].

Digital predistortion (DPD) is a popular PA linearization technique requiring PA behavior modeling [3]. PA is also a NL dynamic system. The Volterra series is computationally expensive but can capture the behavior of PA and memory. It has been theoretically proved that the k-th order pre-inverse of a Volterra system is identical to its post-inverse [4]. This paved way for the usage of pruned Volterra models with reduced complexity to retain most of the modeling capabilities, such as memory polynomial (MP) [5], generalized MP (GMP) [6] and dynamic deviation reduction (DDR) [7] and etc.

ML techniques for DPD have already gained traction [8– 11]. However, it is difficult to model the PA behavior with a single model for the entire range of output power because of varying behavior at different power levels. Thus, piecewise (PW) polynomial-based models have been shown to be quite effective in modeling and linearizing PAs with strong nonlinear effects [12-15]. In [12], a vector switched model has been proposed where the input data samples are classified by a computationally expensive k-means clustering algorithm based on their envelope. Nevertheless, the basic intent of PW modeling and results shown in [12] are interesting as they paved the way with better hardware-friendly techniques such as [13] and [14]. In [13], a low-computation learning algorithm based on a simple decorrelation rule is used for PW modeling. In [14], authors proposed a PW closed-loop DPD solution using low-complexity gradient-adaptive parameter learning algorithms. Recently, a machine learning (ML)based scheme was proposed in [15] where the input samples are classified by the decision tree classifier using features like current magnitude and past samples. The sub-model coefficients are then extracted.

Our proposed approach involves two stages: ML classification of the input and output baseband signal samples and piecewise digital predistortion (DPD). The novelty of this scheme is to model an accurate and low-complex machine learning (ML)-aided classifier in the first stage involving the input and output baseband signal samples. Here, the boundaries between the classes are calculated as a function of both the input data statistics and PA operating point. In the second stage, the class-wise samples are linearized by tailored GMP models. Supervised ML approaches such as k-nearest neighbors (kNN) and decision trees are non-parametric and do not have an assumption on the distribution of the data. Therefore, the key aspect lies in extracting some essential features from the statistics of the input data samples and also the PA operating point. The simulation results validate this perspective leading to an improved performance/complexity trade-off than a single GMP model in terms of PA behavior modeling and linearization. Albeit, further improvements can be achieved by determining the minimum required number of classes and properly identifying their boundaries.

Rest of the paper is organized as follows. Section 2

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Fig. 1. Wiener-Hammerstein Model of the PA with memory.

presents the simulated PA model and relevant metrics. The proposed scheme is explained in Section 3. The simulation results are given in Section 4 and then the paper is concluded.

# 2. PA MODEL AND PERFORMANCE METRICS

# 2.1. PA Model

Let us denote the orthogonal frequency-division multiplexing (OFDM) modulated discrete-time input and output data vectors for PA as  $\mathbf{x} = [x_0, \dots, x_{N-1}]$  and  $\mathbf{y} = [y_0, \dots, y_{N-1}]$ , where N is the fast Fourier transform (FFT) size. Then, x can be mathematically modeled as a function of x as  $\mathbf{y} = \mathbb{F}_a(|\mathbf{x}|) e^{j(\mathbb{F}_p(|\mathbf{x}|) + \phi_{\mathbf{x}})}$ , where,  $\mathbb{F}_a$  and  $\mathbb{F}_p$  are the classsical amplitude-to-amplitude (AM/AM) and amplitude-tophase (AM/PM) conversion characteristics respectively and  $\phi_{\mathbf{x}} = [\phi_0, \dots, \phi_{N-1}]$  is the phase vector of  $\mathbf{x}$ . A Wiener-Hammerstein structure [16] is used to model the behavior of a memory PA as illustrated in Fig. 1. A modified Rapp model is used as the NL static system [17]. It is preceded by a high pass filter (HPF) and succeeded by a low pass filter (LPF). The designed LPF is an invertible 3-tap finite impulse response filter with the coefficients [0.7692, 0.1538, 0.0769] [18]. The HPF is designed as an inverse of the LPF.

Let  $k \in \mathcal{N}$  be the time index of an input sample  $x_k$  where  $\mathcal{N} = \{0, 1, \dots, N-1\}$  is the set of indices of all time samples in **x**. Then, the mathematical expression of the modified Rapp model's conversion characteristic is

$$y_{k} = \frac{g_{s}|x_{k}|}{\left(1 + \left(\frac{g_{s}|x_{k}|}{v_{sat}}\right)^{2p}\right)^{\frac{1}{2p}}} \cdot e^{j\left(\frac{\alpha|x_{k}|^{q_{1}}}{1 + \left(\frac{|x_{k}|}{\beta}\right)^{q_{2}} + \phi_{k}\right)}$$
(1)

where  $g_s$  is the small signal gain of PA, p is the knee factor,  $v_{sat}$  is the input saturation voltage of PA and  $\alpha$ ,  $\beta$ ,  $q_1$ ,  $q_2$  are the parameters related to AM/PM characteristic. The input back-off (IBO) of a PA, often expressed in dB, is defined as IBO =  $10 \log_{10} \frac{N v_{sat}^2}{||\mathbf{x}||_2^2}$ , where  $||.||_2$  is the Euclidean norm. Likewise, output back-off (OBO) can be defined as the ratio between the mean power of the saturation point of the PA output to the mean power of the output signal.

## 2.2. Performance and Complexity Metrics

Two metrics are widely used to characterize the quality of the transmitted signal in IB and OOB. These two are error vector magnitude (EVM) and adjacent channel leakage ratio (ACLR) [19]. The ACLR is defined in dB as



Fig. 2. Block diagram of the proposed scheme.

ACLR =  $10 \log_{10}(P_{channel}/P_{adj})$ , where  $P_{channel}$  denotes the total power within the assigned channel and  $P_{adj}$  is the maximum power of the two adjacent channels. The EVM is measured for the post-amplified signal by using a measurement receiver and is defined both in % and dB as  $EVM_{\%} = ||\mathbf{Y} - \mathbf{X}||_2/||\mathbf{X}||_2 \times 100$  and  $EVM_{dB} = 20 \log_{10}(||\mathbf{Y} - \mathbf{X}||_2/||\mathbf{X}||_2)$  and, where **X** and **Y** are the corresponding complex samples in the frequency domain after the equalization and demodulation of **y** and **x** respectively.

Computational complexity reduction ratio (CCRR) is used for estimating the proposed scheme's complexity reduction performance over the conventional one. CCRR is defined in % as CCRR =  $\left(1 - \frac{C_{new}}{C_{ref}}\right) \times 100$ , where  $C_{new}$  and  $C_{ref}$ are computational complexities of the proposed scheme and the conventional scheme that are used for comparison. We use F1 score as the ML classifier performance metric [20].

### 3. THE ML-AIDED PW-DPD SCHEME

Our proposed scheme, termed as ML-aided PW-DPD, has two stages and follows the direct learning architecture (DLA). It is presented as a block diagram in Fig. 2. Stage I involves MLbased classification of the input data samples into different sample classes using intuitive and easily interpretable supervised learning algorithms like kNN and decision-tree. The selected classifiers are generic and flexible as they are nonparametric and do not assume any inherent distribution of input samples [20]. Under Stage II, we perform behavior modeling using class-wise tailored GMP models followed by DPD for each of the samples. At the end of Stage II, all the classwise samples are realigned w.r.t. their original time sample indices to construct the predistorted signal z. The mathematical model of GMP is given in [6] and not presented in this paper for the sake of brevity. We denote the GMP model with NL polynomial degree P and memory depth of K for the leading and lagging memories as GMP (P, K) [21].

# 3.1. Stage I: ML-aided classification

Initially, we scale  $\mathbf{x}$  with the IBO coefficient to make Stage I dependent on the PA operating point. In Stage I, the first step is to build essential features for the ML-based classifier of the

input data samples. Each input data sample  $x_k$  in the baseband may be modeled as a complex Gaussian random variable with Rayleigh envelope distribution if N is sufficiently large [22]. The histogram of  $|\mathbf{x}|$  is fitted to a Rayleigh distribution for extracting the estimated statistical parameters such as mean  $\hat{\mu}$  and standard deviation  $\hat{\sigma}$  based on the maximum likelihood estimation. Now, we need to build some important features for the ML classifier training. Therefore, we extract the four essential features from the statistical properties of the input sample  $x_k$ . Those are square of deviation of the sample's amplitude from mean (i.e.  $(|x_k| - \hat{\mu})^2)$ , samples's energy (i.e.  $|x_k|^2$ ), real and imaginary parts of the sample (i.e.  $\operatorname{Re} |x_k|$  and  $\operatorname{Im} |x_k|$ ). We extract the fifth feature from the PA operating point which is the *deviation of the sample's* amplitude from saturation voltage (i.e.  $|x_k| - v_{sat}$ ). These features can be constructed with meager computational complexity.

The ML classifier is trained with these five features and each input sample  $x_k$  is classified into one of the *B* classes.  $\forall i \in B$ , let  $\kappa_{(i)} \in \mathcal{N}$  be the set of indices of the samples that are classified as belonging to the  $i^{th}$  class. Then,  $\forall \{i, j\} \in B$ , we have any two sets  $\kappa_{(i)}$  and  $\kappa_{(j)}$  being mutually disjoint, i.e. we have  $\cup_i \kappa_{(i)} = \mathcal{N}$  and  $\cap_i \kappa_{(i)} = \emptyset$ . Each output sample  $y_k$  will be automatically classified to be the  $i^{th}$  class if  $k \in \kappa_{(i)}$ . In other words, the input and output samples with the same time sample index will belong to the same class but ML classification takes into account only the input sample.

# 3.2. Stage II: PW behaviour modelling and compensation

We denote classified input and output samples belonging to the  $i^{th}$  class as  $\mathbf{x}_{(i)}$  and  $\mathbf{y}_{(i)}$  respectively. These outputs of Stage I are fed as inputs to the  $i^{th}$  Regressor block, Regressor<sub>i</sub> in Stage II for the extraction of DPD coefficients for that class which we denote as  $c_{(i)}$ . All the *B* Regressor blocks use a tailored GMP model to capture the PA behavior over the samples belonging to the respective classes and may be implemented in a parallel fashion. The proposed scheme also allows for any classical pruned Volterra model or any ML-based model to be used as the regressor in Stage II. In the  $i^{th}$  parallel chain, the extracted class-wise DPD coefficients from Regressor<sub>i</sub> are fed into the DPD<sub>i</sub> block to generate the class-wise predistorted samples  $z_{(i)}$ .

Finally, all the class-wise predistorted samples are realigned into a discrete-time series as per their sample index positions for the construction of the predistorted signal zwhich is then sent to the PA. From the DLA perspective, we identify the PW ideal post-distorter for each class by an improved PA behavior modeling and copying it as the PW predistorter. Our scheme involves only one iteration.

# 4. SIMULATION RESULTS

We consider 64 quadrature amplitude modulated OFDM symbols  $M = 10^5$  and FFT size N = 1024 with all active subcarriers and an oversampling factor L = 4. The complemen-

 Table 1. Classwise F1-scores over the test dataset for different ML classifier models.

	kNN F1 score			DT F1 score		
	2 features	4 features	5 features	2 features	4 features	5 features
Class 1	0.05	0.76	0.95	0.05	0.95	1
Class 2	0.31	0.98	0.99	0.31	0.99	1
Class 3	0.42	0.99	0.99	0.41	1	1
Class 4	0.56	0.97	0.98	0.53	1	1
Class 5	0.02	0.91	0.95	0.05	0.98	0.98

tary cumulative distribution function of the sample level peakto-average power ratio of the composite digital waveform, after selected mapping [23], read 8.8 dB and 9 dB when measured at 1% and 0.01% points, respectively. The PA gain is normalized in our analysis (i.e.  $g_s = 1$ ) and  $v_{sat}$  is 1 V. The modified Rapp model parameters are knee factor p = 2.25,  $\alpha = -270$ ,  $\beta = 0.17$ ,  $q_1 = 1.1$  and  $q_2 = 1.1$ . The number of classes in the ML classifier *B* was chosen to be 5. We have used GMP (6,3) for the single GMP model and for the proposed scheme's five classes they were chosen by trial and error method to be GMP (4,3), GMP (3,3), GMP (5,3), GMP (3,3) and GMP (2, 1) respectively.

Our motivation and focus were on the hardware-friendly DPD schemes. It became evident that further improvements can be achieved by determining the minimum required number of the class and properly identifying their boundaries. So, we are of the opinion that it is not fair to compare with the state-of-the-art schemes mentioned in the introduction unless the proposed scheme is fully optimized. Therefore, in this work we do the performance and complexity analysis only with the conventional single GMP model and similar analysis with the aforementioned state-of-the-art schemes shall be included in our future work.

#### 4.1. Performance of ML-based Classification Model

In this subsection, we analyze the performance of ML-based classification using kNN and decision-tree algorithms. The total number of input OFDM signal samples will be MLN. We initially consider a dataset with  $8.192 \times 10^6$  (i.e. just 2% of the total samples) samples and 5 class labels. In the next step, the aforementioned essential feature information is collected over each sample and used for training/testing the classification algorithms. We note that only 10% of the entire dataset is used for training both kNN and decision-tree algorithms. For the kNN classifier, we chose k = 10 and Euclidean distance metric as hyper-parameters.

Table 1 shows the F1 score performances of kNN and decision-tree classifiers over the test dataset for all 5 classes, respectively. We notice that classifier models with less than 5 features have shown sub-optimal performance. For both the training algorithms, we observe that if provided with important features then 10% of signal samples is enough to accurately predict the classes for the remaining 90% of the dataset. This shows that, *statistical feature selection favors less algorithmic complexity (training with 0.2% of MLN samples) with reliable classification accuracies*. Moreover,



Fig. 3. EVM performance at different IBO values.<sup>1</sup>



Fig. 4. AM/AM conversion characteristic at  $6 \, dB \, IBO^1$ 

the decision-tree classifier is observed to show the best performance between both ML classifiers with an average F1score over 5 classes  $\approx 1$ .

#### 4.2. Performance and complexity analysis

We analyse the relative EVM improvement (with arrow text) in IB and the relative ACLR gains in OOB for different IBO (and OBO) values as shown in Fig. 3 and Table. 2, respectively.<sup>1</sup> We observe that the proposed scheme outperforms the conventional approach in IB and also for lower IBO values in OOB. The AM/AM and AM/PM plots have been shown at 6 dB IBO in Figures 4 and 5.<sup>1</sup> The extent of each class along with its boundaries is shown where we can see the relative outperformance of the proposed scheme.



**Fig. 5**. AM/PM conversion characteristic at 6 dB IBO.<sup>1</sup>

Table 2. ACLR Performance in dB at different IBO values.

IBO	OBO	Single GMP model	The proposed scheme	ACLR gain
3	1.52	22.80	24.39	1.59
4	2.18	27.69	30.61	2.92
5	2.91	33.39	34.05	0.66
6	3.69	36.71	36.29	-0.42
7	4.54	38.20	37.89	-0.31
8	5.42	38.75	38.75	0.0
9	6.34	38.79	38.79	0.0

At 6 dB IBO, the single GMP model with GMP(6, 3) requires 48 coefficients and the proposed scheme requires 113 coefficients. For computational complexity analysis, we try to compare the number of complex multiplications and additions. The number of complex multiplications and additions. The number of complex multiplications and additions in a single GMP fitting model is  $2MLN\Lambda$  and  $2MLN(\Lambda-1)$ respectively, where  $\Lambda$  is the number of DPD coefficients.  $\forall i \in$ B, the proposed scheme require  $\sum_i (2\Lambda_i \operatorname{card}(\kappa_i))$  complex multiplications and  $\sum_i (2(\Lambda_i - 1)\operatorname{card}(\kappa_i))$  complex additions, where  $\Lambda_i$  is the number of DPD coefficients for the i<sup>th</sup> class and  $\sum_i \operatorname{card}(\kappa_i) = MLN$ . Compared to the traditional scheme, using CCRR we have estimated 42.44% and 41.56% reduction in complex multiplications and additions for the proposed scheme at 6 dB IBO.

# 5. CONCLUSION

An ML-aided PW DPD scheme has been proposed by classifying the PA input data based on some crucial features related to the input data's statistics and the selected PA operating point. The OFDM signal dataset built over these features also trained less complex ML classifiers. The simulation results indicate this approach to be promising with an improved performance/complexity trade-off than a single GMP model. However, there is scope for further improvement in the performance. Perhaps the class boundaries may be defined as some function of both the input data statistics and PA behavior instead. Exploring other Volterra models and comparison with state-of-the-art schemes will be part of our future work.

<sup>&</sup>lt;sup>1</sup>In the legends of all the plotted figures, 'NL' (in black), 'Single GMP model' (in red) and 'The proposed scheme' (in green) indicate conversion characteristic of the original NL PA output (i.e. no DPD), the linearized PA output by the single GMP model and the proposed PW approach, respectively.

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