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HIGH QUALITY RECONSTRUCTION OF DYNAMIC OBJECTS USING 2D-3D CAMERA FUSION

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ABSTRACT

In this paper, we propose a complete pipeline for high quality reconstruction of dynamic objects using 2D-3D camera setup attached to a moving vehicle. Starting from the segmented motion trajectories of individual objects, we compute their precise motion parameters, register multiple sparse point clouds to increase the density, and develop a smooth and textured surface from the dense (but scattered) point cloud. The success of our method relies on the proposed optimization framework for accurate motion estimation between two sparse point clouds. Our formulation for fusing *closest-point* and *consensus* based motion estimations, respectively in the absence and presence of motion trajectories, is the key to obtain such accuracy. Several experiments performed on both synthetic and real (KITTI) datasets show that the proposed framework is very robust and accurate.

Index Terms— 3D Reconstruction, 2D-3D Fusion, Point Cloud Registration, RANSAC, ICP

1. INTRODUCTION

Scene reconstruction and modelling are two major tasks of 3D Computer Vision. The reconstruction offers us the exact observation of the 3-dimensional world, whereas, modelling allows us to perceive it accurately. Both of these tasks have always been active areas of research due to their wide range of potential applications, such as scene representation, understanding, and robot navigation [1].

For a moving 2D-3D camera setup, the 3D reconstruction of the scene can be obtained by registering a sequence of point clouds with the help of Visual Odometry (VO) measurements [2,3]. However, the VO-based registration is valid only for the static scene parts. Therefore, such reconstruction suffers from several visual artefacts due to the dynamic parts. In this regard, recent work by *Jiang et al.* [4–6] categorizes the scene into static and dynamic parts before performing VO. Their method focuses on improving VO measurements, and the attempted dynamic object reconstruction is rather preliminary and naive. In this work, we focus on the high quality reconstruction of dynamic objects, making them dense, coherent, and complete, see Fig. 1 for instance.

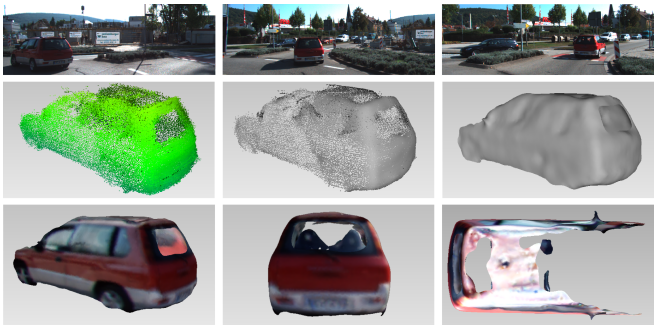


Fig. 1: Moving Car Reconstruction from a Mobile Platform: Top are selected frames of a moving car. Middle show the registered sparse point cloud, the smoothed point cloud, and the reconstructed mesh of the point cloud, respectively. Bottom show the fine reconstruction in different views.

The experimental setup of our work consists of calibrated 2D (Point Grey Flea 2 Colour Camera) and 3D (Velodyne LiDAR HDL-64E) cameras attached to a moving vehicle. Given multiple sparse and partial point clouds of a rigidly moving object, observed from different view ports, we aim to obtain its high quality reconstruction by exploiting both 2D and 3D observation. This paper harnesses the achievements of [4] on detecting dynamic objects. In [4], dynamic objects are reconstructed by registering the sparse point clouds with the help of Random Sample Consensus (RANSAC) on 3D-3D correspondences for this problem. Final results of [4] are noisy, multi-layered and very often incomplete. We argue that such reconstruction is not particularly suitable for the sparse point clouds, since there exists no precise 3D-3D correspondence.

The main contributions of this paper are two-folded: (1) A complete pipeline for high quality 3D reconstruction of dynamic objects using 2D-3D camera setup attached to a moving vehicle has been proposed; (2) Our formulation leverages from the success of *closest-point* and *consensus* based methods, while complementing each other in their unfavourable conditions. The proposed optimization framework is robust as well as accurate.

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2. LITERATURE REVIEW

Recent studies can be categorized as: Iterative Closest Point (ICP) -based point cloud alignment [7–14], RANSAC-based [2,4,15,16] point cloud registration, and volumetric representation -based point cloud fusion [17–19]. ICP-based methods are robust and accurate in general. Yet, it can easily fail when point cloud's geometric structure is low, which yields to an ill-posed problem. RANSAC-based approaches are robust and efficient but require sufficient number of precise 3D-3D matching pairs. Volumetric representation -based algorithms utilize the Signed Distance Function to describe the object surface using RGB-D camera. Volumetric representation methods work nicely for dense point cloud registration of large scene, while they suffer over-smoothing problems.

3. ROBUST POINT CLOUDS REGISTRATION

To register a sequence of sparse point clouds in a common coordinate frame, we formulate an optimization problem supported by their noisy motion trajectories. An accurate registration is the key for obtaining high quality textured surface reconstruction of the dynamic objects.

3.1. Liniarized Rigid Motion Formulation

Given a set of correspondences between two 3D point clouds, the exact solution for rigid motion parameters, *i.e.* R and t, can be obtained in a linear manner. Let $\mathsf{X} = [x, y, z]^\mathsf{T}$ and $\mathsf{Y} = [x', y', z']^\mathsf{T}$ be two corresponding 3D points under rigid transformation, denoted as $\mathsf{X} = \mathsf{RY} + \mathsf{t}$. In which, R is the 3×3 rotation matrix and t is the 3×1 translation matrix. By employing the Gibbs representation [20] and the Cayley transform [21], the 3D registration problem can be formulated as a linear system [4]:

$$\begin{bmatrix} x - x' \\ y - y' \\ z - z' \end{bmatrix} = \begin{bmatrix} 0 & z + z' & -(y + y') & 1 & 0 & 0 \\ -(z + z') & 0 & (x + x') & 0 & 1 & 0 \\ y + y' & -(x + x') & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} g_x \\ g_y \\ g_z \\ \tilde{t}_x \\ \tilde{t}_y \\ \tilde{t}_z \end{bmatrix}. \tag{1}$$

where $[g_x, g_y, g_z]^\mathsf{T}$ are the three rotation elements of Gibbs rotation representation. $[\tilde{t}_x, \tilde{t}_y, \tilde{t}_z]^\mathsf{T} = (\mathsf{I}_3 + \mathsf{G})\mathsf{t}$, in which I_3 is the 3×3 identity matrix and G is the skew-symmetric form of Gibbs rotation angles. Since each matching pair provides 2 independent equations, solving the 6 unknown Eq. (1) requires minimum 3 pairs of correspondences. Moreover, a Random Sample Consensus (RANSAC) framework is adopted for the robustness toward outliers. In the presence of inaccurate correspondences, obtained from noisy motion trajectories, the quality of RANSAC registration is usually not very satisfactory. Therefore, this is further refined by minimizing the dual-weighted closet-point energy.

3.2. Robust Closest-Point Energy Minimization

When two overlapping point clouds of the same rigid object are given, the transformation between them is generally obtained by minimizing the energy derived from the closest-points distance. In most of the cases, this energy is minimized using an iterative method – also known as Iterative Closest Point (ICP) algorithm [10, 11]. In every step, the ICP algorithm considers closest points across two point clouds, say reference and model, to be the corresponding ones. Let $\mathbf{X} = \{\mathsf{X}_1, ..., \mathsf{X}_n\}$ be the reference point cloud, and $\mathbf{Y} = \{\mathsf{Y}_1, ..., \mathsf{Y}_m\}$ be the new model, the robust method of ICP iteratively minimizes the following energy:

$$\mathcal{E}_I(\hat{\mathsf{T}}) = \min_{\mathsf{T}} \sum_{i=1}^{n} \rho(\min_{j \in \{1,\cdots,m\}} \|\mathsf{X}_i - \mathsf{T}\mathsf{Y}_j\|_2), \tag{2}$$

where $\hat{\mathsf{T}}$ is the desired transformation matrix that relates two point clouds. Note that the energy term $\mathcal{E}_I$ includes a robust cost function to handle noisy and partial data. Our choice of robust cost, say $\rho(x)$, is the Tukey's biweight function [22]:

$$\rho(x) = \begin{cases} (\tau^2/6)(1 - [1 - (x/\tau)^2]^3) & \text{if } |x| \leq \tau \\ (\tau^2/6) & \text{if } |x| > \tau \end{cases}, \tag{3}$$

and the weight of each corresponding pair is defined by:

$$w(x) = \frac{1}{x}\frac{\mathrm{d}\rho(x)}{\mathrm{d}x} = \begin{cases} [1 - (x/\tau)^2]^2 & \text{if } |x| \leq \tau \\ 0 & \text{if } |x| > \tau \end{cases}, \tag{4}$$

where τ is the inlier threshold, such that outliers ($|x| > \tau$) are assigned zero weights.

3.3. Modified Closest-Point Energy Minimization

While consensus-based registration method requires a subset of accurate correspondences, closest-point-based method requires rich structure of the point clouds. This prohibits us to make a choice of one method over another. Therefore, we propose to minimize a combined energy function – one from consensus, say $\mathcal{E}_R$, and the other from closest-point, say $\mathcal{E}_I$. We minimize the energy function in an iterative manner, hence use the terminology Dual-Weighted Iterative Closest Point (DW-ICP) for this method.

First, we define an energy function that measures the quality of the inlier set obtained form 3-point RANSAC. Note that due to the sparsity and noisy points, the inlier set obtained from RANSAC is not precise. Let $\{\mathsf{X}_i \leftrightarrow \mathsf{Y}_i\}, i = 1, \ldots, k$ be the inlier set, the energy $\mathcal{E}_R$ for matching consensus can be expressed as:

$$\mathcal{E}_R(\hat{\mathsf{T}}) = \min_{\mathsf{T}} \sum_{i=1}^{k} \tilde{\rho}(\|\mathsf{X}_i - \mathsf{T}\mathsf{Y}_i\|_2), \tag{5}$$

where $k \leq m, n$, and $\tilde{\rho}(\cdot)$ is the Huber's weight function:

$$\tilde{\rho}(x) = \begin{cases} (x^2/2) & \text{if } |x| \leq \tilde{\tau} \\ \tilde{\tau}[|x| - (\tilde{\tau}/2)] & \text{if } |x| > \tilde{\tau} \end{cases}, \tag{6}$$

$$\tilde{w}(x) = \frac{1}{x}\frac{\mathrm{d}\tilde{\rho}(x)}{\mathrm{d}x} = \begin{cases} 1 & \text{if } |x| \leq \tilde{\tau} \\ (\tilde{\tau}/|x|) & \text{if } |x| > \tilde{\tau} \end{cases}, \tag{7}$$

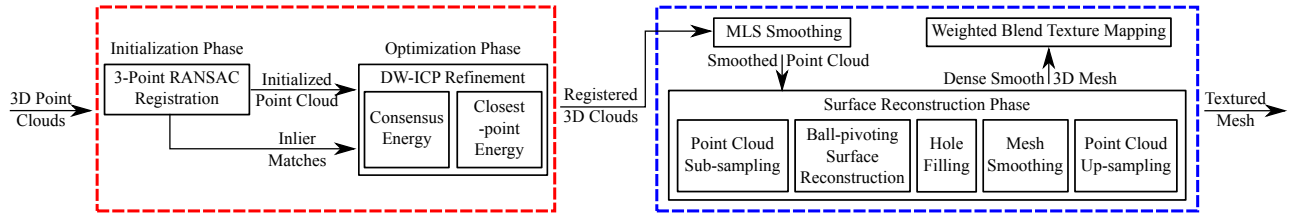


Fig. 2: Framework for High Quality Rigid Object Reconstruction: the Point Clouds Registration and Mesh Reconstruction.

where $\tilde{\tau}$ is the threshold for inlier matches. The Huber loss function is selected under the assumption that the provided inlier set is noisy with no severe outlier that needs to be completely discarded. In the spirit of Eq. (2) and Eq. (5), we formulate our combined energy function as follows:

$$\mathcal{E}(\hat{\mathsf{T}}) = \min_{\hat{\mathsf{T}}} \left\{ \alpha \sqrt{\frac{1}{n}\sum_{i=1}^{n} \rho(\min_{j\in\{1,\cdots,m\}} \|\mathsf{X}_i - \mathsf{T}\mathsf{Y}_j\|_2)} + (1-\alpha)\sqrt{\frac{1}{k}\sum_{i=1}^{k} \tilde{\rho}(\|\mathsf{X}_i - \mathsf{T}\mathsf{Y}_i\|_2)} \right\}, \tag{8}$$

where α is the regularization term to control the influence of the $\mathcal{E}_I$ and $\mathcal{E}_R$ energy terms. Rather than optimizing the closest-point energy $\mathcal{E}_I$ or matching consensus energy $\mathcal{E}_R$ independently, the DW-ICP aims to iteratively and simultaneously optimize the joint energy $\mathcal{E}$ of Eq. (8).

4. 3D RECONSTRUCTION FRAMEWORK

A complete pipeline for high quality 3D reconstruction of rigidly moving objects, using 2D-3D camera setup attached to a moving vehicle, is shown in Fig. 2. There are two major steps involved, namely the Point Clouds Registration and Smooth Mesh Reconstruction.

4.1. Point Cloud Registration

Our method takes the 3D motion trajectories of a sequence of segmented point clouds obtained from [4] as input. First, we use the 3-Point RANSAC registration to roughly register the point clouds as initialization. Afterwards, the DW-ICP is applied to refine the registration. Note that (also refer to Eq. (8)) the DW-ICP iteratively minimizes a combined energy term, one from consensus $\mathcal{E}_R$ and other from closest-point $\mathcal{E}_I$, during the optimization process. On one hand, $\mathcal{E}_I$ minimizes the overall registration error of the whole 3D point clouds. On the other hand, $\mathcal{E}_R$ minimizes the registration error of the inliers obtained form RANSAC. These two terms are usually complementary to each other, which is the key to the success of the proposed optimization framework.

On top of traditional ICP, there are two main advantages of DW-ICP: (a) Feature matching constraint promises a proper registration regardless the poor geometry structure of the point clouds. (b) Robust estimation framework is preserved such that the algorithm is generic and robust to outliers during a long term registration.

4.2. Mesh Reconstruction

To reconstruct a photo-realistic high quality 3D model, a full pipeline is presented in Fig. 2 (blue box). There are three major steps involved, namely Moving Least Square (MLS) [23] point cloud smoothing, 3D Mesh Reconstruction, and Weighted Blend Texture Mapping [24].

Point Cloud Smoothing Due to the measurement noise of the laser scanner and imperfect registrations, a long sequenced registered point cloud consists of outliers and multi-layer effects. Surface reconstructed from such point cloud suffers from many visual artefacts, such as spiky mesh and holes. Thus, a MLS algorithm, which smooths an unorganized point could using a polynomial fitting, is applied.

Surface Reconstruction Prior to the surface reconstruction, a sub-sampling processing according to the points' poisson-disk distribution [25] is applied. This avoids the repetition of redundant points (overlapped points) due to the multiple observations of the same scene. Later, a Ball Pivoting Triangulation algorithm [26] is used to establish the neighbour-points relationships, followed by a dilation operation for hole filling. Next, a Taubin Surface Smoothing method is adopted to smooth the reconstructed surface while preserving the sharp edges. Finally, a Least Square Subdivision approach [27] is performed to up-sample followed by re-meshing the point cloud to produce high quality meshes.

Texture Mapping We make use of 2D images acquired by the 2D-3D camera setup for texture mapping. During this process, photographic alignment between 3D mesh and images are required. Since the 2D-3D camera setup is already calibrated, and the motion of the camera is known, all the images are aligned with respect to the mesh reconstructed frame. The camera poses (between the camera and the reconstructed mesh) are estimated by computing the inverse of the transformation matrices (obtained from registration) and using the camera calibration parameters. Furthermore, the blurring during the texture fusion from multiple images is reduced by using a Weighted Blending algorithm.

5. EXPERIMENTS

For the evaluation, experiments were conducted on both synthetic and real (KITTI [1]) datasets. We generated three sets of synthetic data to quantify the robustness and accuracy of the proposed algorithms. Qualitative results of the proposed framework is presented using real data. In all of our ex-

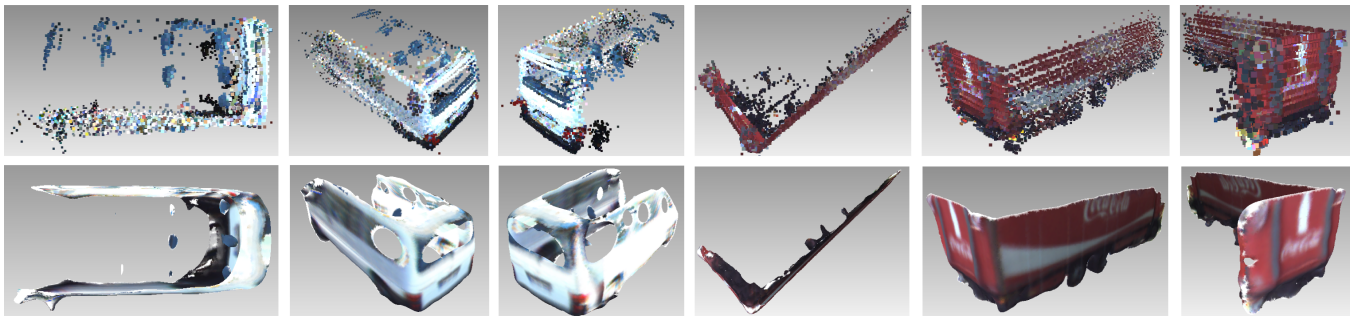


Fig. 3: Reconstructed Van and Cola Truck: top are registered point clouds using [4]; bottom are our high quality meshes.

periments, the algorithm parameters were set as: $\alpha = 0.8$, $\tau = 0.08m$, $\tilde{\tau} = 0.03m$. The stopping conditions of the DW-ICP optimization are: rotation tolerance $\epsilon_{\mathsf{R}} = 10e\text{-}6$, translation tolerance $\epsilon_{\mathsf{T}} = 10e\text{-}6$, and maximum DW-ICP iteration as 100. All the experiments are conducted in a computer with Intel Quad Core i7-2640M, 2.80GHz, 8GB Memory.

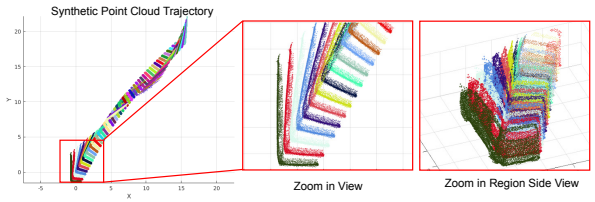


Fig. 4: Synthetic Trajectory of Van Object.

Synthetic Datasets: The synthetic datasets were generated for three objects from KITTI dataset, namely Van, Red Car, and Cola Truck. An example of synthetic trajectory and visible parts are shown in Fig. 4. Note that some frames in the trajectory consist of different views (sides or back views), resembling the partial overlapping and poor 3D geometric structure problems. To evaluate the robustness of the algorithm, different levels of Gaussian noise were added to the model. We applied 10 different levels of noise, from 0.005 to 0.050 in meters. The maximum noise level is chosen as 2.5 times higher than the expected accuracy (0.02m) of the Velodyne laser scanner.

Figure 5 shows the performances of 4 different algorithms, namely 3-Point RANSAC [4], 3-Point RANSAC + ICP refinement [10], 3-Point RANSAC + Robust-ICP [13] and 3-Point RANSAC + DW-ICP. The overall performance of the algorithms are (top-down) ranked as: DW-ICP, Robust-ICP, RANSAC+ICP and RANSAC. The Robust-ICP (using M-Estimator) has significantly better performance against that of traditional ICP. Most importantly, the proposed DW-ICP constantly outperforms the other approaches, regardless of rotation and translation.

Real Datasets: Table 1 depicts the dataset information, where the 3D Error (averaged Leave-One-Out Error) metric is used to quantify the registration performance. The registration error of our method is consistently lower than [4],

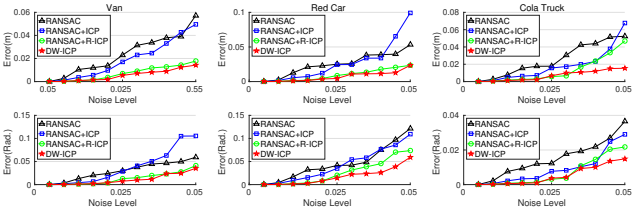


Fig. 5: Synthetic Data Quantification: top and bottom are averaged translation and rotation errors on Van, Red Car, and Cola Truck dataset, respectively.

although we have slightly more computation time due to the DW-ICP refinement process. Moreover, the high quality reconstructions of Fig. 1 and Fig. 3 are obtained using the proposed framework of Fig. 2. Note that the objects are reconstructed from long-term and faraway observations (see column *Dist.* of Table 1), under the situations that both target objects and camera system are moving in high speeds. The framework effectively overcomes the accumulation errors during the registration process and products very satisfactory results. Figure 3 demonstrates that significantly better results of our method are achieved comparing to [4].

Object	# Frame	Sides	Dist. (m)	3-Point RANSAC [4]		Ours	
				Error (m)	Time (s)	Error (m)	Time (s)
Van	44	3	16.5	0.0150	3.1	**0.0131**	4.6
Red Car	60	3	10.8	0.0084	2.8	**0.0080**	4.3
Cola Truck	48	2	30.0	0.0234	3.7	**0.0229**	4.1

Table 1: Dataset Information: *Col. Sides* is number of object sides (left, right, back, and front) being captured. *Col. Dist.* is the averaged distance from the camera to the object. *Col. 3-Point RANSAC [4]* and *Col. Ours* show their respective averaged 3D error and computation time.

6. CONCLUSION

We have proposed an effective optimization method, which combines the idea of *consensus* and *closest-point* in a common framework, to register highly sparse 3D point clouds from long term observations. Furthermore, We present a complete pipeline for high quality 3D mesh reconstruction. Results obtained from several experiments on both synthetic and real data were very satisfactory.

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