Investigating Functional Redundancies in the Context of Vehicle Automation – A Trajectory Tracking Perspective*

Torben Stolte¹, Tianyu Liao¹, Matthias Nee¹, Marcus Nolte¹, and Markus Maurer¹

Abstract—Level 3+ automated driving implies highest safety demands for the entire vehicle automation functionality. For the part of trajectory tracking, functional redundancies among all available actuators provide an opportunity to reduce safety requirements for single actuators. Yet, the exploitation of functional redundancies must be well argued if employed in a safety concept as physical limits can be reached. In this paper, we want to examine from a trajectory tracking perspective whether such a concept can be used. For this, we present a model predictive fault-tolerant trajectory tracking approach for over-actuated vehicles featuring wheel individual all-wheel drive, brakes, and steering. Applying this approach exemplarily demonstrates for a selected reference trajectory that degradations such as missing or undesired wheel torques as well as reduced steering dynamics can be compensated. Degradations at the physical actuator limits lead to significant deviations from the reference trajectory while small constant steering angles are partially critical.

I. INTRODUCTION

In automated vehicles according to SAE level 3+ [1], the driver's role as fallback in conventional vehicles is transferred to the technical system (in level 3 until hand-over to the driver). Hence, ensuring safety is of utmost importance. Compared to conventional vehicles, this results in significantly increased safety requirements for all parts of the vehicle automation system which in turn lead to elaborate technical implementations.

On the actuator level, specifically, each actuator must fulfill fail-operational degradation regimes [2] if not otherwise argued. All actuators contribute to both lateral and longitudinal dynamics as partially exploited in conventional vehicles to enhance vehicle agility and safety, e.g. torque vectoring or electronic stability control. Hence, the use of these functional redundancies among the actuators appears promising in order to reduce safety requirements on the actuator level.

From a functional perspective, following Matthaei and Maurer [3], fault-tolerant trajectory tracking is the first reaction to a degradation on operational level. The trajectory tracking keeps the deviation from the reference trajectory in terms of a temporal sequence of reference poses (position plus heading) in defined boundaries. Still on the same level, trajectory generation prevents non-drivable trajectories by re-planning the reference trajectory under consideration of the actuator degradation [4]. On tactical level, the targeted vehicle behavior must adapt to the degradation, for instance by decreasing speed or even stopping the vehicle on a hard shoulder. Last but not least, the planned route can be changed on strategical level, e.g. driving to a garage for repair or avoiding steep or curvy roads.

In the following we focus on the part of fault-tolerant trajectory tracking. Furthermore, we concentrate on an overactuated actuator topology featuring wheel-individual brakes, drives, and steering, i. e. the topology with the highest force potential [5]. Still, utilization of functional redundancies in a safety concept for automated vehicles has not been subject to comprehensive investigation. For the part of trajectory tracking, the suitability is determined by aspects such as the tolerable degradation types, the actuator topology as well as the vehicle's functional range (allowed velocities, lateral accelerations, etc.) and its operational design domain [1]. The operational design domain defines i. a. friction coefficient ranges through the admissible road and weather conditions and the accepted tracking error for each possible operational scenario (c. f. [6] for definition).

Several publications present trajectory tracking approaches for the selected actuator topology demonstrating its benefits from a vehicle dynamics perspective. Most of these approaches target the vehicle's lateral dynamics, e. g. [7]–[11]. One exception is the work of Park and Gerdes [12], [13] who track a trajectory in terms of a temporal sequence of reference poses. Additionally, trajectory tracking approaches, which provide fault-tolerance against actuator degradations, consider selected degradation types of single actuators only [14]–[19], target lateral dynamics or path tracking [14]– [16], [20], or do not demonstrate limitations of their approaches [14]–[21].

In order to investigate the potential as well as limitations of functional redundancies, we implemented a model predictive control (MPC) approach. The approach is able to track a temporal sequence of references poses and can incorporate the effects of various types of actuator degradations. From an architectural perspective, we assume the remaining system parts as non-reactive to actuator degradations for this paper. In Section II, we outline the control scheme which is subsequently evaluated in Section III at the example of a dynamic reference trajectory in presence of various degradations.

II. FAULT-TOLERANT TRAJECTORY TRACKING

In Figure 1, the adaptive model predictive control scheme for fault-tolerant trajectory tracking is embedded in a functional system architecture. As input, a reference vector containing the target vehicle motion is derived from the reference trajectory in the reference value generation block.

^{*}This work is part of the DFG Research Unit Controlling Concurrent Change, funding number FOR 1800.

¹The authors are with the Institute of Control Engineering at Technische Universität Braunschweig, 38106 Braunschweig, Germany. {stolte, nolte, maurer}@ifr.ing.tu-bs.de

^{© 2018} IEEE. Personal use of this material is permitted. Permission from IEEE must be obtained for all other uses, in any current or future media, including reprinting/republishing this material for advertising or promotional purposes, creating new collective works, for resale or redistribution to servers or lists, or reuse of any copyrighted component of this work in other works.

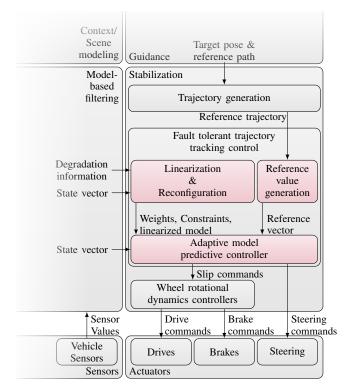


Fig. 1. Control scheme presented in this paper (red) embedded in a functional system architecture according to Matthaei and Maurer [3]

The adaptive model predictive controller generates steering and slip commands in terms of target steering angles and longitudinal slip, respectively, in order to influence the vehicle dynamics. Subsequently, a wheel rotational dynamics controller calculates drive and brake commands as target torques from the target longitudinal slip. The recent vehicle state in terms of state vector and degradation information is determined by means of sensor values which are processed within the model-based filtering block. This process is not within the focus of this paper. Different approaches for degradation detection and isolation are described i. a. in [22]. The state vector serves as input for the model predictive controller as well as as input for the linearization and reconfiguration block which creates a linearized prediction model of the current operating point. Concurrently, the degradation information is used to reconfigure the prediction model as well as the weights and constraints of the optimization.

Assuming a discrete non-linear system without feed-through

$$\mathbf{x}_{k+1} = \mathbf{f} \left(\mathbf{x}_k, \mathbf{u}_k \right)$$
$$\mathbf{y}_k = \mathbf{h} \left(\mathbf{x}_k \right),$$

where \mathbf{x} denotes the state vector, \mathbf{y} the output vector, \mathbf{u} the control vector, k a discrete point of time, as well as \mathbf{f} and \mathbf{h} the transition and output function, the fundamental linear optimization problem can be described as

$$\begin{array}{ll} \min_{\mathbf{x},\mathbf{u}} & J\left(\mathbf{y},\mathbf{u}\right), \\ \mathrm{s.t.} & \Delta \mathbf{x}_0 &= \mathbf{0}, \\ & \Delta \mathbf{u}_k &= \mathbf{u}_k - \mathbf{u}_0, \\ & \Delta \mathbf{x}_{k+1} &= \boldsymbol{A}_0^{\mathrm{lin}} \Delta \mathbf{x}_k + \boldsymbol{B}_0^{\mathrm{lin}} \Delta \mathbf{u}_k + \mathbf{r}_0 \\ & \mathbf{y}_k &= \boldsymbol{C}_0^{\mathrm{lin}} \Delta \mathbf{x}_k + \mathbf{h}_0, \\ & \mathbf{y}_k &\in \mathbb{Y}, \\ & \mathbf{u}_k &\in \mathbb{U} \end{array}$$

with input and output constraints \mathbb{U} and \mathbb{Y} , which are convex sets, the linearized state transition matrix A_0^{lin} , input matrix B_0^{lin} , and output matrix C_0^{lin}

$$\begin{aligned} \boldsymbol{A}_{0}^{\text{lin}} &= \left. \frac{\partial \mathbf{f}}{\partial \mathbf{x}} \right|_{\mathbf{x}_{0},\mathbf{u}_{0}}, \, \boldsymbol{B}_{0}^{\text{lin}} &= \left. \frac{\partial \mathbf{f}}{\partial \mathbf{u}} \right|_{\mathbf{x}_{0},\mathbf{u}_{0}}, \, \boldsymbol{C}_{0}^{\text{lin}} &= \left. \frac{\partial \mathbf{h}}{\partial \mathbf{x}} \right|_{\mathbf{x}_{0},\mathbf{u}_{0}} \\ \Delta \mathbf{x}_{k} &= \mathbf{x}_{k} - \mathbf{x}_{0}, \qquad \Delta \mathbf{u}_{k} &= \mathbf{u}_{k} - \mathbf{u}_{0}, \\ \mathbf{r}_{0} &= \mathbf{f} \left(\mathbf{x}_{0}, \mathbf{u}_{0} \right) - \mathbf{x}_{0}, \qquad \mathbf{h}_{0} &= \mathbf{h} \left(\mathbf{x}_{0}, \mathbf{u}_{0} \right) = \mathbf{y}_{0}, \end{aligned}$$

as well as the cost function $J(\mathbf{y}, \mathbf{u})$

$$J(\mathbf{y}, \mathbf{u}) = \sum_{k=0}^{N_P - 1} \left[\left(\mathbf{y}_{k+1} - \mathbf{y}_{\mathrm{ref}, k+1} \right)^T \boldsymbol{Q}(\mathbf{y}_{k+1} - \mathbf{y}_{\mathrm{ref}, k+1}) + \left(\mathbf{u}_k - \mathbf{u}_{\mathrm{ref}, k} \right)^T \boldsymbol{R}(\mathbf{u}_k - \mathbf{u}_{\mathrm{ref}, k}) \right],$$

with its input and output weight matrices $Q = \text{diag}(\mathbf{w}_y)$ and $\mathbf{R} = \text{diag}(\mathbf{w}_u)$ and the prediction horizon N_P . An index $(\cdot)_{k=0}$ indicates the actual value, an index $(\cdot)_{\text{ref}}$ a reference value. \mathbf{w}_y and \mathbf{w}_u are the weight vectors for the elements of the input and output vectors.

In the following, the fundamental considerations regarding the prediction model are outlined in Subsection II-A. The resulting prediction model is presented in Subsection II-B together with the actuator degradation mapping in Subsection II-C. Table I summarizes the nomenclature used in the model of the vehicle's motion along a trajectory.

A. Prediction Model Requirements

Tracking a trajectory in terms of a temporal sequence of reference poses requires taking several aspects into account which determine the prediction model. First of all, different trajectory implementations are possible. For this paper, we assume a trajectory given in Cartesian coordinates plus heading. From this, a Frenet description of the trajectory is derived, describing the trajectory in distance s along the path, the lateral displacement d, and the yaw angle ψ , c. f. [23]. The longitudinal and lateral vehicle motion – as needed for tracking a trajectory – are part of the prediction model in terms of the variables longitudinal speed v_x^V , side slip angle β , and yaw rate $\dot{\psi}$.

The second aspect to be considered is the stability of the vehicle motion. In conventional, front axle steered vehicles, the side slip angle serves as measure of stability. Vehicle stability control algorithms aim at keeping the side slip angle in defined boundaries. In contrast, all-wheel steering enables high side slip angles while the vehicle is stable [24]. Consequently, the wheels' slip angles α_{ij} are considered as measure for vehicle stability and are contained in the prediction model.

TABLE I

NOMENCLATURE

Superscripts and Subscr	ripts						
$(\cdot)^a, a \in \{\mathcal{O}, \mathcal{V}, \mathcal{W}\}$	Global, vehicle, or wheel coordinate system						
$(\cdot)_b,b\in\{x,y\}$	Translational or rotational quantity along or around x - or y -axis of coordinate system						
$(\cdot)_i, i \in \{\mathrm{f},\mathrm{r}\}$	Front or rear axle						
$(\cdot)_j, j \in \{\mathbf{r}, \mathbf{l}\}$	Right or left side						
Quantities							
m	Vehicle mass						
J_z	Moment of inertia around z-axis in vehi- cle's CG						
$F^a_{b,ij}$	x- and y -components of the forces at the wheels in wheel or vehicle coordinates						
$ \begin{array}{c} F^a_b \\ \vec{F}^W_{ij} \\ M_z \end{array} $	Resulting forces at the vehicle's CG						
$\vec{F}_{ij}^{\mathrm{W}}$	Resulting forces at wheels						
$\stackrel{M_z}{ec v}$	Resulting yaw moment at the vehicle's CG Vehicle speed in CG						
$v_b^{\rm V}, \dot{v}_b^{\rm V}$	Longitudinal and lateral velocity and acceleration of vehicle						
$v^a_{b,ij}$	Longitudinal and lateral velocity of wheels in wheel or vehicle coordinates						
$\psi,\dot\psi,\ddot\psi$	Yaw angle, rate and acceleration in vehi- cle's CG						
$l_{\rm f},l_{ m r}$	Distance between CG and front or rear axle						
$s_{\rm f}, s_{\rm r}$	Track width front and rear						
δ_{ij}, δ_{ij}	Steering angles and rates of wheels						
$\lambda_{ij}, \dot{\lambda}_{ij}$	Longitudinal slips and rates of wheels						
$\alpha_{ij}, \dot{\alpha}_{ij}$	Slip angles and rates of wheels						
β	Side slip angle						
ω_{ij}	Rotational speed of wheels						
r_{ij}	Effective radius of wheels						
$J_{\mathrm{W},ij}$	Moment of inertia of wheels						
s, ś	Traveled distance along path and derivative						
d, d	Lateral deviation from path and derivative						

The third aspect to be considered are the actuators' properties and their effects on vehicle dynamics. Each actuator is subject to limitations which must be respected in the control law. For the steering, these are available steering angles δ_{ij} and available steering dynamics in terms of steering rates $\dot{\delta}_{ij}$. Brake and drives both effect wheel rotational dynamics. Thus, these are mutually integrated into the model by the longitudinal slip λ_{ij} and its dynamics $\dot{\lambda}_{ij}$.

The last aspect respects the potential of braking with the steering actuators in a configuration comparable to a skier's snowplow brake. Instead of braking the wheels, deceleration can be caused through opposing wheel slip angles by turning both wheels of an axle inwards [25], [26]. In order to be able to avoid too excessive snowplow braking, the steering angle deviations $\Delta \delta_{\rm f}$ and $\Delta \delta_{\rm r}$ between left and right wheel are considered in the prediction model, too.

Summing up these considerations, the used output and control vector for the prediction model result in:

$$\mathbf{y} = \begin{bmatrix} s & d & \psi & v_x^{\mathrm{V}} & \beta & \dot{\psi} & \delta_{ij} & \lambda_{ij} & \alpha_{ij} & \Delta \delta_i \end{bmatrix}^T, \\ \mathbf{u} = \begin{bmatrix} \dot{\delta}_{ij} & \dot{\lambda}_{ij} \end{bmatrix}^T.$$

Consequently, the resulting prediction model allows to represent the necessary dynamics for trajectory tracking as well as to incorporate of actuator limitations. The according

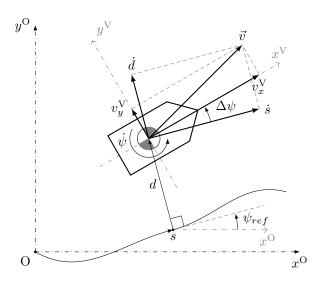


Fig. 2. Trajectory description in a Frenet representation

reference vectors are

$$\mathbf{y}_{\text{ref}} = \begin{bmatrix} s_{\text{ref}} & 0 & \psi_{\text{ref}} & v_{x,\text{ref}}^{\text{V}} & 0 & 0 & 0 & 0 & 0 \end{bmatrix}^{T}, \\ \mathbf{u}_{\text{ref}} = \begin{bmatrix} 0 & 0 \end{bmatrix}^{T}.$$

This reference vector is designed such that the controller tracks the reference distance s_{ref} , the resulting longitudinal speed $v_{x,\text{ref}}$, and the reference yaw angle ψ_{ref} . All other reference variables are set to zero, targeting a behavior that minimizes actuator utilization as well as lateral vehicle dynamics for passenger comfort.

B. Prediction model

The vehicle motion along the path s can be described according to Figure 2 as

$$\dot{s} = v_x^{\mathrm{V}} \cos(\psi - \psi_{\mathrm{ref}}) - v_y^{\mathrm{V}} \sin(\psi - \psi_{\mathrm{ref}}), \dot{d} = v_x^{\mathrm{V}} \sin(\psi - \psi_{\mathrm{ref}}) + v_y^{\mathrm{V}} \cos(\psi - \psi_{\mathrm{ref}}).$$

The dynamics of lateral and longitudinal tracking relates to the vehicles' actual lateral and longitudinal speeds as well as on the actual yaw angle deviation. The dynamics of the yaw angle in terms of the yaw rate $\dot{\psi}$ directly correspond to the vehicles yaw dynamics which are elaborated in the following.

In order to model the influence of independently actuated wheels, a non-linear double track model based on the work of Orend [27] and Falcone *et al.* [28], [29] is employed together with non-linear tires which combine longitudinal and lateral slip. Figure 3 depicts dynamic and kinematic relations in the vehicle model. Roll and pitch movements are neglected in the prediction model.

Considering the force and moment equilibria with $p_{ij} \in \{\frac{s_f}{2}, -\frac{s_f}{2}, \frac{s_r}{2}, -\frac{s_r}{2}\}$ and $q_{ij} \in \{l_f, l_f, -l_r, -l_r\}$ yields:

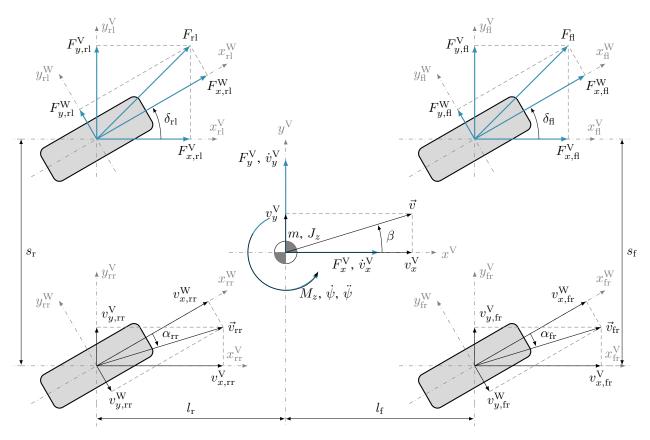


Fig. 3. Double track model

$$\begin{split} \dot{v}_x^{\mathrm{V}} &= v_y^{\mathrm{V}} \dot{\psi} + \frac{1}{m} \sum_{ij} F_{x,ij}^{\mathrm{V}} \\ &= v_y^{\mathrm{V}} \dot{\psi} + \frac{1}{m} \sum_{ij} \left(\cos \delta_{ij} F_{x,ij}^{\mathrm{W}} - \sin \delta_{ij} F_{y,ij}^{\mathrm{W}} \right), \\ \dot{v}_y^{\mathrm{V}} &= -v_x^{\mathrm{V}} \dot{\psi} + \frac{1}{m} \sum_{ij} F_{y,ij}^{\mathrm{V}} \\ &= -v_x^{\mathrm{V}} \dot{\psi} + \frac{1}{m} \sum_{ij} \left(\sin \delta_{ij} F_{x,ij}^{\mathrm{W}} + \cos \delta_{ij} F_{y,ij}^{\mathrm{W}} \right), \\ \ddot{\psi} &= \frac{1}{J_Z} \cdot \sum_{ij} \left[\left(p_{ij} \cos \delta_{ij} + q_{ij} \sin \delta_{ij} \right) F_{x,ij}^{\mathrm{W}} \right] \\ &+ \left(q_{ij} \cos \delta_{ij} - p_{ij} \sin \delta_{ij} \right) F_{y,ij}^{\mathrm{W}} \end{split}$$

Consequently, the vehicle motion dynamics depend on the actual vehicle motion and on the forces acting on the wheels. Transforming the vehicle's velocity to velocities at the wheel centers yields

$$v_{x,ij}^{\mathcal{V}} = v_x^{\mathcal{V}} - p_{ij}\dot{\psi}, \qquad v_{y,ij}^{\mathcal{V}} = v_y^{\mathcal{V}} + q_{ij}\dot{\psi}$$

and further to wheel coordinates

$$\begin{aligned} v_{x,ij}^{\mathrm{W}} &= v_{x,ij}^{\mathrm{V}} \cos \delta_{ij} + v_{y,ij}^{\mathrm{V}} \sin \delta_{ij}, \\ v_{y,ij}^{\mathrm{W}} &= v_{y,ij}^{\mathrm{V}} \cos \delta_{ij} - v_{x,ij}^{\mathrm{V}} \sin \delta_{ij}. \end{aligned}$$

Actuator degradations can lead to states in which physical tire limits are completely exploited, for instance steering degradations at high lateral accelerations, locking wheels due to brake degradations or undesired anti-lock braking interventions. Consequently, modeling the wheel forces $F_{x,ij}^{V}$ and $F_{y,ij}^{V}$ requires the representation of the tire's non-linearities as well as the interaction of lateral and longitudinal tire dynamics. For this, the Pacejka Magic Formula tire model is employed [30, pp. 176] which calculates the longitudinal and lateral tire forces $F_{x,ij}^{W}$ and $F_{y,ij}^{W}$ as a function of the longitudinal slip λ_{ij} and the lateral slip α_{ij} . For these, following definitions are used:

$$\lambda_{ij} = \frac{r_{ij}\omega_{ij} - v_{x,ij}^{\mathrm{W}}}{\max(|v_{x,ij}^{\mathrm{W}}|, |r_{ij}\omega_{ij}|)}, \ \alpha_{ij} = \arctan\frac{v_{y,ij}^{\mathrm{W}}}{|v_{x,ij}^{\mathrm{W}}|}.$$

The longitudinal slip λ_{ij} is negative for deceleration and positive for acceleration. Through utilization of the absolute values in the denominator, the definition is applicable for driving forward as well as reversing.

The same applies to the utilization of the absolute value in the denominator within the definition of the lateral slip α_{ij} . Two velocities of the same speed which are symmetric to the wheels lateral axis yield the same resulting lateral force as illustrated in Figure 4.

In order to reach continuously differentiable functions for λ_{ij} and α_{ij} , the absolute value function is approximated by

$$|x| = x \operatorname{sgn}(x) \approx x \frac{2}{\pi} \arctan(mx) + n$$

where m denotes a parameter to determine the slope of the arctan around 0 and n a small offset used to avoid the singularity at 0. We selected m = 5 and n = 0.1273.

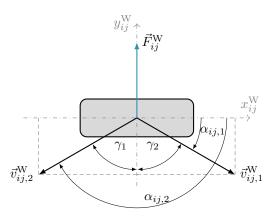


Fig. 4. Two wheel velocity vectors $\vec{v}_{ij,1}^W$, $\vec{v}_{ij,2}^W$ of same speed and the same resulting lateral force \vec{F}_{ij}^W ($\lambda_{ij} = 0, \gamma_1 = \gamma_2$)

The resulting error of this approximation equals n at 0 and converges to values at the order of 10^{-5} for values beyond 0.

Finally, as β is allowed to reach large values in the context of a front and rear steered vehicle, it is defined as

$$\beta = \arctan \frac{v_y^{\rm V}}{v_r^{\rm V}}.$$

C. Degradation mapping

For fault-tolerant trajectory tracking, the control scheme must attune to the specific degradation. Thus, the considered degradation types and the according mapping in the control scheme are outlined in this subsection.

Different kinds of functional degradation can occur on actuator level [31]. Degraded brakes or drives can yield

- D.1 Constant torque at wheel: $M_{\rm W} = \text{const.} \neq 0$
- D.2 Degraded longitudinal slip range, e. g. due to faults in the longitudinal slip control: $\lambda \in [\lambda_{\min, \deg}, \lambda_{\max, \deg}]$,
- D.3 Reduced longitudinal slip dynamic, e.g. caused by reduced maximum torque at a brake or drive actuator: $\dot{\lambda} \in [\dot{\lambda}_{\min, \deg}, \dot{\lambda}_{\max, \deg}],$
- D.4 Zero longitudinal slip, e.g. brake or drive do not provide torque: $\lambda = 0$,
- D.5 Constant longitudinal slip, e.g. anti-lock control is unnecessarily active: $\lambda = \text{const.} \neq 0$, especially $\lambda = \lambda_{\mu, \max}$,
- D.6 Locking or spinning wheel, e.g. brake locks wheel or drive provides maximum torque: $\lambda = 1$, $\lambda = -1$.

For steering following degradation types are possible:

- D.7 Reduced steering angle range:
 - $\delta \in [\delta_{\min, \deg}, \delta_{\max, \deg}],$
- D.8 Reduced steering dynamics: $\delta \in [\delta_{\min, \deg}, \delta_{\max, \deg}]$,
- D.9 Constant steering angle: $\delta = \text{const.}$, especially $\delta = \delta_{\min}$ and $\delta = \delta_{\max}$,
- D.10 Free running steering: Steering behavior is purely influenced by the forces acting at the wheel and determined by the steering kinematics and dynamics (damping etc.).

For fault-tolerant control, the degradations are mapped to the control algorithm in the reconfiguration block in Figure 1. Degradations D.2, D.3, D.7, and D.8 are addressed by adapting the constraints of the allowed value ranges for λ_{ij} , $\dot{\lambda}_{ij}$, δ_{ij} , and $\dot{\delta}_{ij}$ in \mathbb{U} and \mathbb{Y} .

The remaining degradations with respect to the rotational wheel dynamics D.1, D.4, and D.6 are addressed by three measures. The weight $w_{\lambda,ij}$ of the affected actuator is set to zero such that it is not considered in the cost function J. Moreover, the constraints $\lambda_{ij,\max}$ and $\lambda_{ij,\min}$ are voided in order to prevent problems during optimization as physical slip beyond these values can occur due to the degradation. The according entries in the transition and input matrices A_0^{lin} and B_0^{lin} are set to zero, too. By this means, the effect of the degraded actuator is considered during the prediction only by the disturbance \mathbf{r}_0 .

The same principle applies to D.9 by zeroing $w_{\delta,ij}$, voiding $\alpha_{ij,\max}$ and $\alpha_{ij,\min}$, as well as zeroing the matrix elements relevant for the affected steering. Additionally, voiding $\alpha_{ij,\max}$ and $\alpha_{ij,\min}$ on both wheels of the affected axle allows large slip angles which can be expected during a steering degradation. Still, α_{ij} is considered in the cost function J such that the effects of the unconstrained slip angle are minimized with respect to the trajectory tracking.

A special case is degradation D.10: Provided a positive mechanical trail together with longitudinal slip $\lambda_{ij} = 0$, the wheel's motion around its z-axis follows the vehicle's motion. This changes when drive or brake apply a torque. In this case, the wheel turns inwards or outwards respectively depending on the scrub radius and the torques direction, thereby magnifying the degradation's effect on the lateral vehicle dynamics. Consequently, the measures of D.9 and D.4 are combined in order to reach a free running wheel without any intentionally applied forces.

III. EVALUATION

For investigating whether functional redundancies are suitable for ensuring safety on trajectory tracking level, the control algorithm used for trajectory tracking must prove to be capable of handling all degradations accepted by the safety concept. Furthermore, the degradations can occur during driving manifold trajectories which must be derived from the functional range and the operational design domain of the vehicle automation functionality.

In this section, we apply the developed control system in an exemplary *sine-with-dwell*-like maneuver at a speed of ca. 14 m/s such that the tire forces are temporarily close to saturation for degradation-free operation, c. f. Subsection III-A. In Subsection III-B, the control scheme is applied to selected degradations regarding the rotational wheel dynamics caused by brake and drives while Subsection III-C considers steering related degradations.

The control scheme is simulatively evaluated. A double track model with roll and pitch dynamics serves as the vehicle plant with the model parameters demonstrated in Table II. A degradation detection and isolation time $T_{\rm DDI} = 0.2$ s respects the duration of the vehicle's self-diagnosis. The degradation is triggered at t = 1 s and a constant available maximum friction $\mu_{\rm max} = \text{const.}$ is assumed. The MPC is

running at a sampling time $T_S = 50$ ms with a prediction and control horizon $T_P = 1$ s and $T_C = 250$ ms, respectively.

Calzolari *et al.* [32] introduce metrics in order to compare different trajectory tracking control approaches, namely the maximum $\varepsilon_{\{t,n\},max}$, average $\varepsilon_{\{t,n\},avg}$, and final $\varepsilon_{\{t,n\},end}$ tangential and normal deviation from the reference trajectory, as well as the average tire saturation μ_{avg} . Thereby, the authors only regard vehicles with front steering. However, a vehicle featuring front and rear steering basically allows driven trajectories which track the positions accurately while showing a huge yaw angle deviation. Thus, we extend the metrics of Calzolari *et al.* by the maximum $\varepsilon_{\psi,max}$, average $\varepsilon_{\psi,avg}$, and final yaw angle deviation $\varepsilon_{\psi,end}$:

$$\begin{split} \varepsilon_{\psi,\max} &= \max_{t \in [0,T]} |\psi(t) - \psi_{\mathrm{ref}}(t)| \\ \varepsilon_{\psi,\mathrm{avg}} &= \frac{1}{T} \int_0^T |\psi(t) - \psi_{\mathrm{ref}}(t)| dt \\ \varepsilon_{\psi,\mathrm{end}} &= |\psi(T) - \psi_{\mathrm{ref}}(T)| \end{split}$$

Table III summarizes trajectory tracking performance for the different cases outlined in the following. Based on a ride on a major inner city road, tangential deviations $\varepsilon_t > 1$ m, normal deviations $\varepsilon_n > 0.3$ m, and a yaw angle deviation $\varepsilon_{\psi} > 10^{\circ}$ are assumed as not tolerable from a safety perspective. Still, these arbitrary definitions of what is safe must be defined for every individual scenario and, hence, must be further investigated.

A. Degradation-free Operation

Targeting the general suitability of the proposed controller for trajectory tracking, the maneuver is driven without any degradations (1) as depicted in Figure 5. The results indicate a trajectory tracking performance of the same order as other trajectory tracking controllers [32], albeit different trajectories are used. The maximum tangential deviation results from longitudinal speed error at the simulation start. The tangential speed is initialized as $v_{x,0}^V = 12$ m/s while the reference speed is $v_{x,ref,0}^V = 14$ m/s. Consequently, the vehicle accelerates at the beginning and compensates for the resulting position error.

In order to investigate the robustness of the control approach, in (2) the plant's mass m and yaw inertia J_z are increased by 10% each while the CG of the plant is moved 0.20 m to the rear. In this case, no significant changes of the metrics are observable.

TABLE II Vehicle Model Parameter Values and Parameter Ranges for Degradation-free Operation

Parameter	Value		
m J_z	$\begin{array}{ccc} 2200 & \text{kg} \\ 2000 & \text{kg}\text{m}^2 \end{array}$	Parameter	Value Range
l_{f}	1.36 m 1.36 m	$\delta_{ij} \\ \dot{\delta}_{ij}$	[-30°, 30°]
$l_{ m r} \ s_{ m f}$	1.75 m	$M_{\mathrm{W},ij}$	[-120 °/s, 120 °/s] [-2000 N m, 2000 N m]
$s_{r} r_{ij}$	1.75 m 0.28 m	$\lambda_{ij} lpha_{ij}$	[-0.12, 0.12] [-0.2, 0.2]
$J_{ m W} h_{ m CG}$	$\begin{array}{cc} 2 & kg m^2 \\ 0.3 & m \end{array}$		

B. Drive and Brake Degradations

Brake and Drive degradations are considered together since both affect the wheel's rotational dynamics. Different types of degradation with varying parameterization of the degradations were investigated. Table III contains selected results for degradation types D.1, D.4, D.5, and D.6.

When applying a constant torque to one wheel D.1 - such that the resulting longitudinal slip is within the linear tire region – the effects are compensated by the controller (3). In this case, the controller primarily applies a negative torque of the same order to the other wheel of the same side of the vehicle. In consequence, also degradation D.4 representing zero longitudinal slip is easily compensated (4).

Degradation types D.5 and D.6 are more critical, which represent an unnecessarily active anti-lock control (5) or a locking wheel (6), respectively. The results imply that more lateral force potential is left when anti-lock control is active (see Figure 6) compared to a locking wheel. In contrast, the locking wheel yields the most severe position deviation for the trajectory and the used control algorithm. Moreover, the yaw angle deviation is comparably high, too.

C. Steering Degradations

With respect to steering degradations, degradation types D.7, D.8, and D.9 could be investigated as the controlled vehicle model does not yet feature a comprehensive representation of the steering dynamics including kinematics for consideration of a free running steering (D.10).

Degradation types D.7 (7) and D.8 (8) do not show a severe impact on the tracked trajectory. The yaw angle tracking performance is slightly, yet not significantly, decreased compared to the degradation-free operation. In contrast, degradation type D.9 has a higher impact on trajectory tracking. The tracking performance deteriorates for increasing absolute values of $|\delta_{ij}| = \text{const.}$ While the effects manifest in a yaw angle deviation in particular, the effects vary depending on the affected wheel and the turn direction of the steering angle. For $\delta_{ij} = 0 = \text{const.}$ (9), the tracking performance goes beyond the tolerated yaw angle deviation when affecting the front right wheel. In case of $|\delta_{ij}| = 5^\circ = \text{const.}$ (10), the degradation's effects on each front wheel are critical. The observed most severe yaw angle deviation is encountered at $\delta_{fr} = -30^\circ = \text{const.}$ (11) as illustrated in Figure 7.

IV. CONCLUSION AND OUTLOOK

Through the developed fault-tolerant control approach, we are able to investigate the effects of different actuator degradations on tracking a reference trajectory. From a trajectory tracking perspective, the results suggest that functional redundancies can be exploited if certain degradation types are excluded by means of a safety concept. Degradations which lead to an operation of the actuators at their physical limits must be avoided in particular. For drives and brakes, a considerable safe state is to apply zero or a small torque as these can be coped with by the control algorithm. Simultaneously, these degradations must be indicated to the faulttolerant control algorithm. In contrast, a steering actuator

TABLE III

Selected control deviations for a sine-with-dwell-like trajectory without degradation (1), with parameter variation (2), and degradations (3–11). Highlighted values are exceeding the assumed safety boundaries.

#	Description	$arepsilon_{\mathrm{t,max}}$ in m	$rac{arepsilon_{\mathrm{t,avg}}}{\mathrm{in}\ \mathrm{m}}$	$rac{arepsilon_{ m t,end}}{{ m in } { m m}}$	$rac{arepsilon_{n,\max}}{\operatorname{in} m}$	$rac{arepsilon_{\mathrm{n,avg}}}{\operatorname{in} \mathrm{m}}$	$rac{arepsilon_{\mathrm{n,end}}}{\mathrm{in}\ \mathrm{m}}$	$rac{arepsilon_{\psi,\max}}{\operatorname{in}^\circ}$	$arepsilon_{\psi,\mathrm{avg}}$ in °	$rac{arepsilon_{\psi,\mathrm{end}}}{\mathrm{in}}^\circ$	$\mu_{\rm avg}$
(1)	No Degradation	0.34	0.04	0.00	0.05	0.02	0.00	2.07	0.52	0.00	0.40
(2)	No Degradation, misaligned $m, J_z, \& CG$	0.35	0.06	0.00	0.09	0.03	0.00	4.03	1.41	0.00	0.43
(3)	$M_{\rm W,rl} = 500 \mathrm{Nm} = \mathrm{const.}$	0.34	0.04	0.00	0.05	0.02	0.00	2.08	0.49	0.02	0.46
(4)	$M_{\rm W,rr} = 0 = \text{const.}$	0.34	0.04	0.00	0.05	0.02	0.00	2.06	0.50	0.00	0.40
(5)	$\lambda_{\rm fr} = -0.13 = {\rm const.}$	0.91	0.25	0.06	0.33	0.06	0.00	15.80	3.33	0.47	0.76
(6)	$\lambda_{\rm fr} = -1 = {\rm const.}$	5.45	0.73	5.45	2.26	0.48	0.75	27.53	6.88	14.87	0.84
(7)	$\delta_{ m fr} \in [-3^\circ, 3^\circ]$	0.34	0.06	0.00	0.23	0.06	0.00	6.42	2.31	0.07	0.53
(8)	$\dot{\delta}_{\mathrm{fl}} \in [-12^{\circ}/\mathrm{s}, 12^{\circ}/\mathrm{s}]$	0.34	0.04	0.00	0.07	0.02	0.00	4.04	0.99	0.00	0.40
(9)	$\delta_{\rm fr} = 0 = {\rm const.}$	0.43	0.11	0.00	0.74	0.17	0.00	6.67	2.28	0.01	0.67
(10)	$\delta_{\rm fr} = -5^\circ = {\rm const.}$	1.07	0.50	0.12	1.41	0.40	0.00	21.58	6.23	3.57	0.85
(11)	$\delta_{\rm fr} = -30^\circ = {\rm const.}$	16.78	9.01	14.81	4.99	1.56	2.98	43.87	13.51	17.32	0.89

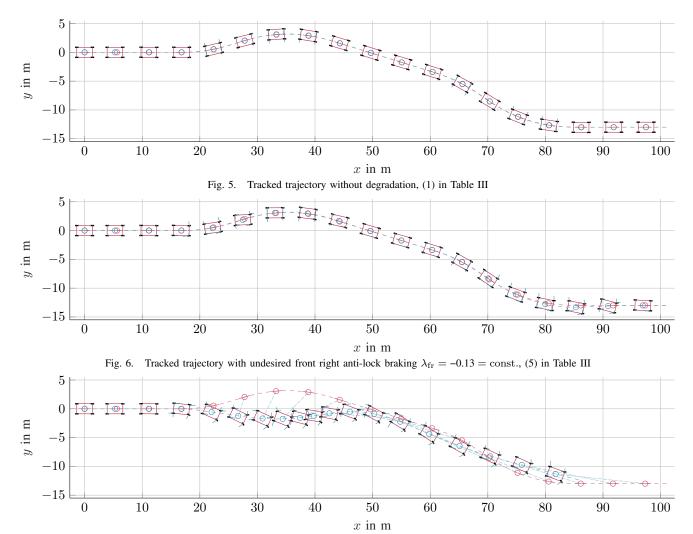


Fig. 7. Tracked trajectory with degraded front right steering angle $\delta_{\rm fr} = -30^\circ = {\rm const.}, (11)$ in Table III

must be designed as fail-operational actuator. Even minor degradations such as a small constant steering angle lead to signification deviations from the reference trajectory.

Still, the results are indications only and require further research before functional redundancies can be exploited. On the one hand, only a single trajectory is investigated. Thus, a set of trajectories must be derived from the automated vehicle's operational ranges and its operational design domain. On the other hand, the investigations are made without noise and with limited model uncertainties. Moreover, superimposed architectural levels could contribute to balance shortcomings on the trajectory tracking level by concurrent adaptation to the degradation. Last but not least, the argumentation is made from a safety engineering's perspective and does not respect other disciplines, e.g. availability engineering or ergonomics. Our future research can be divided in three threads. The first thread consists of improving the simulation capabilities by extending the vehicle model, continuing the presented investigations towards different trajectories, varying degradation detection and isolation times, as well as model and sensor noise. The second thread is connecting fault-tolerant trajectory tracking with additional architectural levels. This is highly relevant for a statement whether functional redundancies can be used. In this regard, combining trajectory tracking with fault-tolerant trajectory generation as proposed by Nolte *et al.* [4] is the first step. The last thread is implementing the control approach into our experimental vehicle MOBILE [33] in order to do real-world experiments.

ACKNOWLEDGMENT

The authors would like to thank Christina Harms for proofreading our work.

REFERENCES

- SAE, "Taxonomy and Definitions for Terms Related to Driving Automation Systems for On-Road Motor Vehicles", Society of Automotive Engineers, Standard J3016, 2016.
- [2] T. Stolte, G. Bagschik, and M. Maurer, "Safety Goals and Functional Safety Requirements for Actuation Systems of Automated Vehicles", in 2016 IEEE 19th International Conference on Intelligent Transportation Systems (ITSC), 2016, pp. 2191–2198.
- [3] R. Matthaei and M. Maurer, "Autonomous driving a top-downapproach", At - Automatisierungstechnik, vol. 63, no. 3, pp. 155– 167, 2015.
- [4] M. Nolte, M. Rose, T. Stolte, and M. Maurer, "Model Predictive Control Based Trajectory Generation for Autonomous Vehicles – An Architectural Approach", in *IEEE INTELLIGENT VEHICLES* SYMPOSIUM (IV), Redondo Beach, CA, USA, 2017.
- [5] M. Jonasson, J. Andreasson, B. Jacobson, and A. S. Trigell, "Global force potential of over-actuated vehicles", *Vehicle System Dynamics*, vol. 48, no. 9, pp. 983–998, 2010.
- [6] T. Stolte, G. Bagschik, A. Reschka, and M. Maurer, "Hazard analysis and risk assessment for an automated unmanned protective vehicle", in *IEEE INTELLIGENT VEHICLES SYMPOSIUM (IV)*, Redondo Beach, CA, USA, 2017, pp. 1848–1855.
- [7] J. Fredriksson, J. Andreasson, and L. Laine, "Wheel force distribution for improved handling in a hybrid electric vehicle using nonlinear control", in 43rd IEEE Conference on Decision and Control (CDC), vol. 4, Nassau, Bahamas, 2004, pp. 4081–4086.
- [8] C. Knobel, A. Pruckner, and T. Bünte, "Optimized Force Allocation: A General Approach to Control and to Investigate the Motion of Over-Actuated Vehicles", *IFAC Proceedings Volumes*, 4th IFAC Symposium on Mechatronic Systems, vol. 39, no. 16, pp. 366–371, 2006.
- [9] E. Ono, Y. Hattori, Y. Muragishi, and K. Koibuchi, "Vehicle dynamics integrated control for four-wheel-distributed steering and four-wheel-distributed traction/braking systems", *Vehicle System Dynamics*, vol. 44, no. 2, pp. 139–151, 2006.
- [10] R. Orend, "Modelling and Control of a Vehicle with Single-Wheel Chassis Actuators", *IFAC Proceedings Volumes*, 16th IFAC World Congress, vol. 38, no. 1, pp. 79–84, 2005.
- [11] —, "Steuerung der ebenen Fahrzeugbewegung mit optimaler Nutzung der Kraftschlusspotentiale aller vier Reifen (Vehicle Dynamics Feedforward Control with Optimal Utilisation of the Adhesion Potentials of all four Tyres)", *At – Automatisierungstechnik*, vol. 53, no. 1, pp. 20–27, 2005.
- [12] H. Park and J. C. Gerdes, "Optimal tire force allocation for trajectory tracking with an over-actuated vehicle", in 2015 IEEE Intelligent Vehicles Symposium (IV), 2015, pp. 1032–1037.
- [13] —, "Analysis of Feasible Tire Force Regions for Optimal Tire Force Allocation with Limited Actuation", *IEEE Intelligent Transportation Systems Magazine*, vol. 9, no. 3, pp. 75–87, 2017.

- [14] A. Hac, D. Doman, and M. Oppenheimer, "Unified Control of Brake- and Steer-by-Wire Systems Using Optimal Control Allocation Methods", SAE International, Warrendale, PA, USA, SAE Technical Paper 2006-01-0924, 2006.
- [15] H. Yang, V. Cocquempot, and B. Jiang, "Hybrid fault tolerant tracking control design for electric vehicles", in *16th Mediterranean Conference on Control and Automation*, 2008, pp. 1210–1215.
- [16] —, "Optimal Fault-Tolerant Path-Tracking Control for 4WS4WD Electric Vehicles", *IEEE Transactions on Intelligent Transportation Systems*, vol. 11, no. 1, pp. 237–243, 2010.
- [17] R. Wang and J. Wang, "Fault-Tolerant Control With Active Fault Diagnosis for Four-Wheel Independently Driven Electric Ground Vehicles", *IEEE Transactions on Vehicular Technology*, vol. 60, no. 9, pp. 4276–4287, 2011.
- [18] —, "Fault-Tolerant Control for Electric Ground Vehicles With Independently-Actuated In-Wheel Motors", *Journal of Dynamic Systems, Measurement, and Control*, vol. 134, no. 2, pp. 021014– 1–021014–10, 2012.
- [19] —, "Passive Actuator Fault-Tolerant Control for a Class of Overactuated Nonlinear Systems and Applications to Electric Vehicles", *IEEE Transactions on Vehicular Technology*, vol. 62, no. 3, pp. 972–985, 2013.
- [20] D. Y. Li, Y. D. Song, D. Huang, and H. N. Chen, "Model-Independent Adaptive Fault-Tolerant Output Tracking Control of 4WS4WD Road Vehicles", *IEEE Transactions on Intelligent Transportation Systems*, vol. 14, no. 1, pp. 169–179, 2013.
- [21] J.-E. Moseberg, "Regelung der horizontalbewegung eines überaktuierten fahrzeugs unter berücksichtigung von realisierungsanforderungen", Dissertation, Universität Erlangen-Nürnberg, Erlangen, Germany, 2016.
- [22] R. Isermann, Fault-Diagnosis Systems: An Introduction from Fault Detection to Fault Tolerance. Berlin Heidelberg: Springer, 2005.
- [23] M. Werling, J. Ziegler, S. Kammel, and S. Thrun, "Optimal trajectory generation for dynamic street scenarios in a Frenét Frame", in *IEEE INTERNATIONAL CONFERENCE on Robotics and Automation (ICRA)*, 2010, pp. 987–993.
- [24] H. E. Russell and J. C. Gerdes, "Low friction emulation of lateral vehicle dynamics using four-wheel steer-by-wire", in *American Control Conference (ACC)*, 2014, pp. 3924–3929.
- [25] P. Reinold, V. Nachtigal, and A. Trächtler, "An Advanced Electric Vehicle for Development and Test of New Vehicle-Dynamics Control Strategies", *IFAC Proceedings Volumes*, 6th IFAC Symposium on Advances in Automotive Control, vol. 43, no. 7, pp. 152–161, 2010.
- [26] B. Jansen, "Brake-by-steer concept Steer-by-wire application with independently actuated wheels used for stopping a vehicle", Master Thesis, Delft University of Technology, Delft, The Netherlands, 2010.
- [27] R. Orend, "Integrierte fahrdynamikregelung mit einzelradaktorik: Ein konzept zur darstellung des fahrdynamischen optimums", Dissertation, Universität Erlangen-Nürnberg, Erlangen, Germany, 2006.
- [28] P. Falcone, F. Borrelli, J. Asgari, H. E. Tseng, and D. Hrovat, "A model predictive control approach for combined braking and steering in autonomous vehicles", in *Mediterranean Conference on Control Automation*, Athens, Greece, 2007, pp. 1–6.
- [29] P. Falcone, M. Tufo, F. Borrelli, J. Asgari, and H. Tsengz, "A linear time varying model predictive control approach to the integrated vehicle dynamics control problem in autonomous systems", in *46th IEEE Conference on Decision and Control*, New Orleans, LA, USA, 2007, pp. 2980–2985.
 [30] H. B. Pacejka, *Tire and Vehicle Dynamics*, 3rd. Oxford:
- [30] H. B. Pacejka, *Tire and Vehicle Dynamics*, 3rd. Oxford: Butterworth-Heinemann, 2012.
- [31] T. Stolte, R. S. Hosse, U. Becker, and M. Maurer, "On Functional Safety of Vehicle Actuation Systems in the Context of Automated Driving", in *Advances in Automotive Control 2016*, Norrköping, Sweden, 2016, pp. 586–591.
- [32] D. Calzolari, B. Schürmann, and M. Althoff, "Comparison of Trajectory Tracking Controllers for Autonomous Vehicles", in *IEEE* 20th International Conference on Intelligent Transportation Systems (ITSC), Yokohama, Japan, 2017.
- [33] P. J. Bergmiller, "Towards Functional Safety in Drive-by-Wire Vehicles", Dissertation, Technische Universität Braunschweig, Braunschweig, Germany, 2015.