

# Performance Analysis and Power Allocation for Cooperative ISAC Networks

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**Abstract**—To mitigate the overlapping of the radar and communication frequency bands caused by large-scale devices access, we propose a novel integrated sensing and communication (ISAC) system, where a micro base station (MiBS) simultaneously carries out both target sensing and cooperative communication. Concretely, the MiBS, acting as the sensing equipment, can also serve as a full-duplex decode-and-forward relay to assist end-to-end communication. Moreover, non-orthogonal downlink transmission (NO-DLT) is adopted between the macro base station and the Internet-of-Things devices, so that the spectrum utilization can be further improved. To facilitate the performance evaluation, both the exact and asymptotic outage probabilities, the ergodic rates associated communication, and the probability of successful sensing detection are characterized. Subsequently, a pair of problems of maximizing the receive signal-to-interference-plus-noise ratio of the sensing signal and maximizing the sum rate of communication are formulated that are solved by the classic Lagrangian method while exploiting the associated function monotonicity. Our simulation results demonstrate that: 1) The proposed ISAC NO-DLT system improves both the communication and sensing performance under the same power consumption as non-cooperative NO-DLT; 2) The proposed power allocation (PA) schemes are superior to the random PA scheme.

**Index Terms**—Integrated sensing and communication, cooperative communication, non-orthogonal downlink transmission, full-duplex.

## I. INTRODUCTION

### A. Background

**T**RIGGERED by the roll-out of the Internet-of-Things (IoT), a large number of devices are connected to the mobile communication networks, resulting in escalating spectrum demand in support of superior user experience [1]–[3]. In order to alleviate the potential spectrum congestion, diverse methods

have been proposed, among which the sensing-communication coexistence (SCC) [4] and the integrated sensing and communication (ISAC) [5] techniques are appealing, exhibiting promising system performance. As for the SCC scheme, the communication and sensing (C&S) devices operate independently of each other in the same frequency band, hence resulting in interfering C&S signals. By contrast, for the ISAC scheme, the C&S devices operate by cooperating or sharing a physical site in support of the C&S functions [6].

With the global introduction of the fifth-generation (5G) new radio (NR), reliability, delay, and user experience have reached unprecedented levels. Recently, looking forward to the future multi-functional network application scenarios of smart cities, smart transportation, smart environments, and smart healthcare, purely relying on mobile communications for data transmission has been shown insufficient to cater for these demanding requirements [7]. These emerging needs have fueled the fusion of C&S paving the way for the completing concept of ISAC [8]. Indeed, heterogeneous wireless applications are omni-present and the IoT has been widely used in various domains, which jointly pave the way for the implementation of ISAC [9]. For instance, the authors of [10] proposed an ISAC system, which is capable of reducing the delay of information sharing among vehicles and of improving the data rate, while guaranteeing the safety of autonomous driving. Furthermore, in [11], an ISAC system of unmanned aerial vehicle (UAV) based on beam sharing was studied, in which UAVs could accomplish the functions of C&S. The above mentioned papers have shown that ISAC has the potential of further improving the sensing function of wireless communication networks to new levels.

In practice, the success of ISAC requires the implementation of massive end-to-end data transmission. However, it is challenging to realize information transmission with limited spectral resources. To address this issue, non-orthogonal downlink transmission (NO-DLT) is capable of delivering significant improvements in delay, energy efficiency, and throughput in contrast to the conventional orthogonal downlink transmission (O-DLT). Specifically, O-DLT can only serve a single user by exploiting the time/frequency/code domain orthogonally, while NO-DLT can simultaneously provide a balanced service for multiple devices while guaranteeing the required quality-of-service (QoS) of the devices [12]–[14]. The principle of NO-DLT is to allow controlled multiple access interference, while relying on successive interference cancellation (SIC) to decode the desired signals at the receiver [15]. For in-

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stance, in [16], a traffic offloading scheme of a device-to-device (D2D) network was investigated by using NO-DLT and the resources were optimized for ensuring that the system capacity was maximized. Furthermore, the multi-constraint optimization algorithm was proposed in [17] for maximizing the throughput in wireless-cached NO-DLT UAV systems. The aforementioned contributions demonstrate that NO-DLT yields significant performance gains over O-DLT in various communication scenarios, serving as a promising candidate in support of future mobile communication systems.

In order to further enhance the system's robustness and to extend the coverage area, cooperative relaying has been introduced into NO-DLT systems in [18]. For example, the authors employed a large intelligent reflecting surface as a relay to assist the end-to-end transmission of the NO-DLT system in [19], while the pairwise error probability expressions of the users were derived for quantifying the system performance attained. Furthermore, in [20], the outage probabilities (OPs) and the ergodic sum rate (ESR) of users were analyzed both in cooperative and non-cooperative NO-DLT scenarios, which demonstrated that cooperative NO-DLT is indeed capable of enhancing the overall system performance. In addition, a novel cooperative NO-DLT system was explored in [21], where the near user acted as a relay in support of a far user to communicate with the source and the closed-form expressions of the associated power allocation (PA) were obtained to maximize the sum rate at a low computational complexity.

In contrast to the half-duplex (HD) relaying schemes adopted in [18]–[21], which requires two orthogonal time slots for two-way signal transmission, full-duplex (FD) relaying requires only a single time slot to accomplish this task that potentially doubles the system's spectral efficiency. Nevertheless, the inherent loop self-interference (LSI) is unavoidable in FD systems. To address this issue, the authors of [22] adopted the natural isolation, the time-domain elimination, and the spatial suppression techniques for substantially reducing the LSI, hence facilitating the practical implementation of FD systems. Furthermore, the authors of [23] studied a FD NO-DLT vehicle-to-everything system and demonstrated that FD systems are capable of improving the latency, despite the negative impacts of LSI. Moreover, in a FD NO-DLT system supporting multiple downlink and uplink users [24], the authors further confirmed that the FD mode succeeds in improving the system's throughput and enable a fairer resource allocation than the conventional HD mode.

### B. Motivation and Contribution

The authors of [6], [10], [11], [19]–[24] have respectively laid the theoretical foundations of C&S and of cooperative relaying systems. In this context, there are several attempts in the literature for investigating ISAC and SCC systems. To elaborate the authors of [25], assumed that a radar can simultaneously perform target tracking and cooperative communication. In particular, the bounds of radar and communication as well as the optimal Fisher information were discussed to evaluate the system performance attained. Furthermore, the performance bounds of ISAC system's were developed in [26].

However, the detailed features of relay were not provided in [25] and [26]. As a further advance, single-carrier and multi-carrier SCC systems were devised in [27] and [28], respectively, and sophisticated PA schemes were proposed for maximizing the communication sum rate or receive signal-to-interference-plus-noise ratio (SINR) of radar. However, [25]–[28] were based on the conventional O-DLT philosophy without determining their optimal spectrum sharing.

As a remedy, the authors of [29] conceived a cognitive OFDM-NO-DLT ISAC system, in which the cognitive source was capable of sensing the state of the primary user for opportunistically accessing the primary network's frequency band. In particular, a PA algorithm was designed for maximizing the system capacity under the premise of a specific maximum tolerable interference caused by the cognitive source. In the cognitive Industrial IoT system of [30], multiple sensing stations worked together and transmitted the sensing information to the data center by relying on non-orthogonal communication for improving the data transmission efficiency. Another NO-DLT ISAC framework was proposed in [31], in which the transmit and receive beamformers were designed for minimizing the computational error and maximizing weighted the sum rate. Indeed, [29]–[31] provided embryonic recipes for the development of NO-DLT ISAC systems, but no cooperative ISAC schemes were considered. From a practical point of view, the integration of ISAC and NO-DLT arrangements are capable of improving the spectrum efficiency, enhance the communication reliability, and ensure resource allocation fairness. As for the cooperative ISAC systems of [25], [26], [32], and [33], the introduction of FD NO-DLT is capable of reducing the time duration of communication, thus reserving more time for sensing and further improving the exploitation of the limited resources [34]–[36]. Therefore, the performance analysis and PA schemes of FD NO-DLT ISAC networks is of pivotal significance. Against the above background, we consider a FD NO-DLT ISAC system, where a micro base station (MiBS) is capable of simultaneously realizing the functions of cooperative relaying and target sensing. A bold and definitive comparison of our contributions to the prior art is presented in Table I. Concretely, the contributions of this paper are summarized as follows:

- For the proposed FD NO-DLT ISAC system, both the exact and asymptotic lower bound expressions of the OP of IoT devices are derived along with the diversity orders attained in the high signal-to-noise ratio (SNR) regime. Furthermore, the ESR of the system considered is also investigated. To shed light on the results obtained, we further approximate the expression of the ESR. The results indicate that on the basis of realizing the extra sensing function, the ESR of the proposed FD NO-DLT ISAC system is better than that of the traditional non-cooperative NO-DLT system, despite requiring no additional power.
- The probability of successful detection (PoD) and probability of false alarm (PoFA) of the MiBS are derived for characterizing the sensing performance of the FD NO-DLT ISAC system. Also, the distance between the MiBS

TABLE I: Boldly and explicitly contrasting on contribution to the start-of-the-art

Paper	[4], [27], [28]	[6]	[25], [26], [32]	[29], [30]	[31]	[33]	[34]	[35]	Proposed
SCC	✓	✓							
ISAC		✓	✓	✓	✓	✓	✓	✓	✓
NO-DLT				✓	✓			✓	✓
FD							✓		✓
Cooperative			✓			✓			✓
Beamforming		✓			✓			✓	
PA	✓			✓					✓
PoD						✓	✓		✓
OP									✓
ESR									✓

and the target and the radial velocity of the target are analyzed. The results obtained show that the proposed NO-DLT ISAC system outperforms its O-DLT counterpart and the sensing capability is mainly determined by the transmit power of the macro base station (MaBS).

- To further improve the performance of the system considered, we formulate a pair of PA problems: *i*) A sensing-centric design (SCD), for maximizing the receive SINR of the sensing signal at the MiBS, while the IoT devices satisfy the minimum required SINR constraint; *ii*) A communication-centric design (CCD), for maximizing the sum rate of the IoT devices, while the MiBS meets the minimum SINR requirement. Finally, we analytically derive the closed-form expressions of the PA coefficients.

### C. Organization and Notations

The remainder of this paper is organized as follows. Section II discusses the system model of the FD NO-DLT ISAC system. In Section III, the performance of the system considered is evaluated by deriving the exact and asymptotic OPs and the corresponding diversity orders. The ESR of the IoT devices is derived in Section IV, while Section V analyzes the sensing performance of the system. Two PA problems are formulated in Section VI. Finally, the numerical results are provided to demonstrate the correctness of our theoretical analysis in Section VII, before concluding in Section VIII.

*Notation:*  $\mathbb{E}[\cdot]$  represents the expectation operation,  $\mathcal{CN}(\mu, \sigma^2)$  denotes a complex-valued Gaussian random variable with mean  $\mu$  and variance  $\sigma^2$ ,  $\triangleq$  denotes the definition operation,  $\text{Ei}(\cdot)$  is the exponential integral function,  $\mathbb{C}$  represents the set of complex numbers,  $f_X(\cdot)$  and  $F_X(\cdot)$  are the probability density function (PDF) and cumulative distribution function (CDF) of the random variable  $X$ , respectively.

## II. SYSTEM MODEL

We consider the cooperative FD NO-DLT ISAC network of Fig. 1(a), where a MaBS,  $S$ , is in charge of communication with two IoT devices<sup>1</sup>, while a MiBS,  $R$ , is responsible for sensing the surrounding targets and for facilitating cooperative communication between the MaBS and the IoT devices located

<sup>1</sup>Although only two IoT devices are considered in this paper, the network can be readily extended to multiple IoT devices. A feasible method is to reaggregate the IoT devices into different clusters, where the devices use NO-DLT within each cluster, while the O-DLT philosophy is adopted by the different clusters [37].

at different distances from the MaBS, namely the far IoT device  $D_f$  and the near IoT device  $D_n$ . Specifically, in order to improve the communication performance of the system, the MiBS can also act as a FD decode-and-forward (DF) relay to assist the end-to-end communication while sensing a target  $T^2$ . In order to reduce both the power consumption and the hardware resources, we assume furthermore that the MiBS is equipped with two antennas, one for transmitting and the other for receiving signals, respectively. The MaBS and IoT devices are single-antenna devices. For the convenience of the presentation, the channel coefficients of the links  $S \rightarrow R$ ,  $S \rightarrow D_f$ ,  $S \rightarrow D_n$ ,  $R \rightarrow T$ ,  $T \rightarrow R$ ,  $R \rightarrow D_f$ , and  $R \rightarrow D_n$  of Fig. 1 are denoted by  $h_i \in \mathbb{C}$ ,  $i \in \{SR, SD_f, SD_n, RT, TR, RD_f, RD_n\}$ , respectively. We also assumed that all the links are subject to Rayleigh fading, i.e. the channel gains  $\rho_i = |h_i|^2$  all obey an exponential distribution, capturing both the path-loss and small-scale fading.<sup>3</sup> Next, we will discuss the signal transmission process of the FD NO-DLT ISAC system.

As for the direct links, during the  $t$ -th time slot,  $S$  intends to send the signal  $y_c = \sqrt{a_n P_{\text{com}}} x_n(t) + \sqrt{a_f P_{\text{com}}} x_f(t)$  to  $D_f$  and  $D_n$  concurrently, where  $P_{\text{com}}$  denotes the total transmit power of  $S$ ,  $x_f \in \mathbb{C}$  and  $x_n \in \mathbb{C}$  are the desired signals of  $D_f$  and  $D_n$ , respectively, with  $\mathbb{E}[|x_f|^2] = \mathbb{E}[|x_n|^2] = 1$ ,  $a_f$  and  $a_n$  represent the PA coefficients of  $S$ , so that  $a_n + a_f = 1$  and  $a_f > a_n$  [39], [40]. Thus, the signals received at  $D_f$  and  $D_n$  can be expressed as

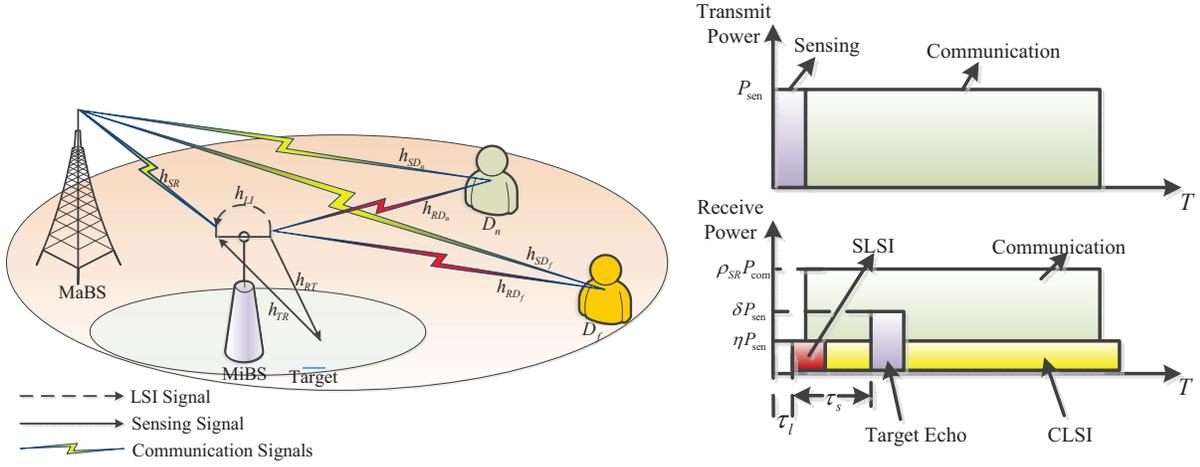
$$y_{i_1} = h_{i_1} \left( \sqrt{a_n P_{\text{com}}} x_n(t) + \sqrt{a_f P_{\text{com}}} x_f(t) \right) + n_{i_1}, \quad (1)$$

where  $i_1 \in \{SD_f, SD_n\}$ ,  $n_{i_1} \sim \mathcal{CN}(0, N_0)$  is the additive white Gaussian noise (AWGN) and  $N_0$  is the noise power.

As for the cooperative links, the MiBS transmits  $y_r = \sqrt{P_{\text{sen}}} x_r(t - \tau_r)$  for sensing the target, then it receives the signals from  $S$  and the target echo, where  $P_{\text{sen}}$  is the power budget of  $R$ ,  $x_r \in \mathbb{C}$  denotes the transmit signal of the MiBS with  $\mathbb{E}[|x_r|^2] = 1$ , and  $\tau_r$  is the sensing signal duration. Fig. 1(b) shows the transmit and receive power at the MiBS

<sup>2</sup>We should point out that the essence of the multi-target system is based on the aggregate of multiple single-target echo signal, which will be set aside for our future work.

<sup>3</sup>Explicitly, the PDF and CDF of  $\rho_i$  are, respectively, given by  $f_{\rho_i}(x) = \exp(-x/\beta_i)/\beta_i$  and  $F_{\rho_i}(x) = 1 - \exp(-x/\beta_i)$ , where  $\beta_i = h/\sqrt{1 + d_i^\alpha}$  denotes the channel's variance,  $h \sim \mathcal{CN}(0, \Omega)$  is the complex channel coefficient,  $\alpha$  denotes the path loss exponent, and  $d_i$  is the distance between the nodes [38].



(a): An illustration of cooperative FD NO-DLT ISAC network.

(b): A diagram of the transmit and receive power at the MiBS.

Fig. 1: The cooperative FD NO-DLT ISAC system model.

during the  $t$ -th time slot. The signals received at the MiBS can be divided into five parts: 1) The communication signal transmitted from the MaBS; 2) The target echo reflected by the target; 3) The communication LSI (CLSI) transmitting the communication signal; 4) The sensing LSI (SLSI) transmitting the sensing signal; and 5) The AWGN. Therefore, the signal received at  $R$  can be expressed as<sup>4</sup>

$$y_{SR} = h_{SR}y_c + h_{RR}\sqrt{\delta P_{\text{sen}}x_r(t - \tau_l - \tau_s)} + h_{LI}\sqrt{\eta P_{\text{sen}}}[x_{LI}^c(t - \tau_l) + x_{LI}^r(t - \tau_l)] + n_{SR}, \quad (2)$$

where  $n_{SR} \sim \mathcal{CN}(0, N_0)$  is the AWGN at  $R$ ,  $x_{LI}^c \in \mathbb{C}$  and  $x_{LI}^r \in \mathbb{C}$  represent the CLSI and SLSI at  $R$  by transmitting the C&S signals associated with  $\mathbb{E}[|x_{LI}^c|^2] = \mathbb{E}[|x_{LI}^r|^2] = 1$ , respectively. Furthermore,  $h_{LI} \in \mathbb{C}$  is the coefficient of the LSI channel at  $R$  and  $\eta \in [0, 1]$  denotes the LSI cancellation capability. Specifically,  $\eta = 0$  indicates that the LSI is perfectly cancelled, while  $\eta = 1$  represents that no interference cancellation is employed between the transmit and receive antennas. Furthermore,  $\tau_l$  and  $\tau_s$  represent the time delay of the LSI and the target echo, respectively. Additionally,  $h_{RR} \in \mathbb{C}$  is the new channel coefficient which captures the joint impact of  $h_{RT} \in \mathbb{C}$  and  $h_{TR} \in \mathbb{C}$  as well as  $\delta \in [0, 1]$  denotes the reflection factor of the target [41]. In the sequel, we introduce the CDF and PDF of  $\rho_{RR}$ , respectively.

**Lemma 1.** *Upon assuming that the target is moving slowly, the channel environment experienced by the signals of  $R \rightarrow T$  and  $T \rightarrow R$  remains approximately time-invariant, i.e.,  $\rho_{RT} =$*

$\rho_{TR}$ . Then the CDF and PDF of  $\rho_{RR}$  are expressed as

$$F_{\rho_{RR}}(x) = 1 - e^{-\frac{\sqrt{x}}{\beta_{RR}}}, \quad (3)$$

$$f_{\rho_{RR}}(x) = \frac{1}{2\beta_{RR}\sqrt{x}} e^{-\frac{\sqrt{x}}{\beta_{RR}}}. \quad (4)$$

*Proof.* By using the CDF of  $\rho_i$ , we have

$$\begin{aligned} F_{\rho_{RR}}(x) &= \Pr(\rho_{RR} = \rho_{RT}\rho_{TR} \leq x) \\ &= \int_0^{\sqrt{x}} f_{\rho_{RT}}(t)dt = \int_0^{\sqrt{x}} f_{\rho_{TR}}(t)dt \\ &= 1 - e^{-\frac{\sqrt{x}}{\beta_{RT}}} = 1 - e^{-\frac{\sqrt{x}}{\beta_{TR}}}. \end{aligned} \quad (5)$$

Using the basic variable substitution, (3) can be obtained. Then, taking the derivative of  $F_{\rho_{RR}}(x)$  with respect to  $x$ , (4) can be obtained.  $\square$

After receiving the signals, the MiBS, serving as a FD DF relay for communication, decodes and forwards the receive signals to  $D_f$  and  $D_n$ . The signals received by the IoT devices can be expressed as<sup>5</sup>

$$y_{i_2} = h_{i_2} \left( \sqrt{b_n P_{\text{sen}}} x_n(t - \tau_c) + \sqrt{b_f P_{\text{sen}}} x_f(t - \tau_c) \right) + n_{i_2}, \quad (6)$$

where  $i_2 \in \{RD_f, RD_n\}$ ,  $b_f$  and  $b_n$  denote the PA coefficients of the MiBS associated with  $b_f + b_n = 1$  and  $b_f > b_n$ <sup>6</sup> [39],  $n_{i_2} \sim \mathcal{CN}(0, N_0)$  denotes the AWGN.

The receive SINRs of the communication signals can be divided into direct and cooperative links as well.

<sup>5</sup>It should be emphasized that if  $R$  can decode the communication signals successfully, then it will forward them to the IoT devices. Otherwise  $R$  remains silent and the cooperative links will be in a state of outage.

<sup>6</sup>As stated in [37], [39], [42]–[44], we assume that the IoT devices which are far/near from the MaBS, are far/near from the MiBS as well. In practice, an easily overlooked scenario exists, where the IoT devices are far/near from the MaBS, while near/far from the MiBS. In this case, the PA coefficients of the MiBS satisfy  $b_f < b_n$  and  $b_f + b_n = 1$ . The expressions of the SINRs, OP, and ESR also have to be changed according to the NO-DLT protocol.

<sup>4</sup>The secondary reflection from the target received by the MiBS due to the illumination of the MaBS is ignored in the data transmission, because the direct-path communication interference arriving from the MaBS is more serious than the secondary reflection [28].

### A. Direct Links

As for the direct links, the MaBS communicates with the IoT devices directly. According to the NO-DLT protocol,  $x_f$  is first decoded at  $D_n$ , and then  $x_n$  is decoded by the application of SIC. Thus, the SINRs of  $D_n$  associated with decoding  $x_f$  and  $x_n$  are respectively expressed as

$$\gamma_{SD_n}^{D_f} = \frac{a_f \rho_{SD_n} \gamma_c}{a_n \rho_{SD_n} \gamma_c + 1}, \quad (7)$$

$$\gamma_{SD_n}^{D_n} = a_n \rho_{SD_n} \gamma_c, \quad (8)$$

where we have  $\gamma_c = P_{\text{com}}/N_0$ .

The receive SINR of  $D_f$  decoding its own signal over the direct link can be expressed as

$$\gamma_{SD_f}^{D_f} = \frac{a_f \rho_{SD_f} \gamma_c}{a_n \rho_{SD_f} \gamma_c + 1}. \quad (9)$$

### B. Cooperative Links

As for the cooperative links,  $R$  decodes the IoT devices' desired signals in turn by employing SIC and treats the echo, CLSI, and SLSI as interferences imposed on the communication signals. Thus, the receive SINRs of  $x_f$  and  $x_n$  at  $R$  can be respectively expressed as

$$\gamma_{SR}^{D_f} = \frac{a_f \rho_{SR} \gamma_c}{a_n \rho_{SR} \gamma_c + \rho_{RR} \delta \gamma_r + 2\eta \rho_{LI} \gamma_r + 1}, \quad (10)$$

$$\gamma_{SR}^{D_n} = \frac{a_n \rho_{SR} \gamma_c}{\rho_{RR} \delta \gamma_r + 2\eta \rho_{LI} \gamma_r + 1}, \quad (11)$$

where we have  $\gamma_r = P_{\text{sen}}/N_0$ .

If  $x_f$  is decoded successfully at  $R$ , i.e., the receive SINR of  $x_f$  exceeds the outage threshold,  $x_f$  will be sent to  $D_f$ . Then, the receive SINR of  $x_f$  at  $D_f$  can be expressed as

$$\gamma_{RD_f}^{D_f} = \frac{b_f \rho_{RD_f} \gamma_r}{b_n \rho_{RD_f} \gamma_r + 1}. \quad (12)$$

Similarly, if both  $x_f$  and  $x_n$  are decoded successfully at  $R$ , the signals will be sent to the  $D_n$ . At  $D_n$ , the high-power signal  $x_f$  will be decoded first and then it will be remodulated and subtracted from  $D_n$  to cancel its effect until  $x_n$  is detected. Therefore, the receive SINRs of  $x_f$  and  $x_n$  at  $D_n$  are respectively expressed as

$$\gamma_{RD_n}^{D_f} = \frac{b_f \rho_{RD_n} \gamma_r}{b_n \rho_{RD_n} \gamma_r + 1}, \quad (13)$$

$$\gamma_{RD_n}^{D_n} = b_n \rho_{RD_n} \gamma_r. \quad (14)$$

In the following, the communication performance of the system considered is evaluated by investigating both the exact and asymptotic OPs, diversity orders, and the ESR of the IoT devices. As a further development, the PoFA and PoD of the MiBS are respectively derived for characterizing the sensing performance. For the sake of convenience, the significant performance analysis identifiers are summarized in Table II.

TABLE II: Summary of the notations

Identifier	Description	Identifier	Description
$P_{\text{out}}^{D_f}$	OP of $D_f$	$P_{\text{out}}^{D_n}$	OP of $D_n$
$P_{\text{out}}^{D_f, \infty}$	Asy. OP of $D_f$	$P_{\text{out}}^{D_n, \infty}$	Asy. OP of $D_n$
$D_f^D$	Diversity order of $D_f$	$D_n^D$	Diversity order of $D_n$
$R_{\text{ave}}^f$	ER of $D_f$	$R_{\text{ave}}^n$	ER of $D_n$
$R_{\text{ave}}^{ap, f}$	Asy. ER of $D_f$	$R_{\text{ave}}^{ap, n}$	Asy. ER of $D_f$
$R_{\text{ave}}^{\text{sum}}$	ESR	$R_{\text{ave}}^{ap, \text{sum}}$	Asy. ESR
$P_{\text{fa}}$	PoFA	$P_{\text{d}}$	PoD

## III. OP ANALYSIS

The OP is an important performance metric of a system, which is related to the average SINRs of the links and the channel fading parameters. Therefore, in this section, we derive the exact OP lower bound of the IoT devices. In order to glean deeper insights concerning the OP, both the asymptotic OPs as well as the diversity orders are analyzed for further characterizing the performance of the proposed FD NO-DLT ISAC system.

### A. Exact OP

An outage event is encountered at  $D_f$ , when one of the following two events occurs. Case *i*) Neither  $R$  nor  $D_f$  can successfully decode  $x_f$  from the  $S \rightarrow R$  and  $S \rightarrow D_f$  links; Case *ii*)  $R$  decodes and forwards  $x_f$  to  $D_f$ , while  $D_f$  fails to decode the desired signal from the  $R \rightarrow D_f$  and  $S \rightarrow D_f$  links. Thus, the OP of  $D_f$  is expressed as<sup>7</sup>

$$P_{\text{out}}^{D_f} = \underbrace{\Pr \left( \max \left( \gamma_{SR}^{D_f}, \gamma_{SD_f}^{D_f} \right) < \gamma_{\text{th}_f} \right)}_{I_1} + \underbrace{\Pr \left( \gamma_{SR}^{D_f} \geq \gamma_{\text{th}_f}, \max \left( \gamma_{RD_f}^{D_f}, \gamma_{SD_f}^{D_f} \right) < \gamma_{\text{th}_f} \right)}_{I_2}, \quad (15)$$

where  $\gamma_{\text{th}_f}$  denotes the SNR threshold of  $x_f$ , while  $I_1$  refers to Case *i* and  $I_2$  refers to Case *ii*. The exact OP expression of  $D_f$  for the FD NO-DLT ISAC system considered is given in the following theorem.

**Theorem 1.** *The exact OP of  $D_f$  device is expressed as*

$$P_{\text{out}}^{D_f} = \left( 1 - e^{-\frac{\theta_1}{\beta_{SD_f}}} \right) \left\{ 1 - \frac{\beta_{SR}}{2\beta_{RR}(\beta_{SR} + 2\eta\beta_{LI}\gamma_r\theta_1)} \sqrt{\frac{\pi\beta_{SR}}{\delta\gamma_r\theta_1}} \right. \\ \left. \times e^{\frac{\beta_{SR}}{4\beta_{RR}^2\delta\gamma_r\theta_1} - \frac{\theta_1}{\beta_{SR}} - \frac{\varphi_1}{\beta_{RD_f}}} \left[ 1 - \text{erfc} \left( \frac{1}{2\beta_{RR}} \sqrt{\frac{\beta_{SR}}{\delta\gamma_r\theta_1}} \right) \right] \right\}, \quad (16)$$

where  $\theta_1 = \gamma_{\text{th}_f} / (a_f \gamma_c - a_n \gamma_c \gamma_{\text{th}_f})$  with  $a_f > a_n \gamma_{\text{th}_f}$ ,  $\varphi_1 = \gamma_{\text{th}_f} / (b_f \gamma_r - b_n \gamma_r \gamma_{\text{th}_f})$  with  $b_f > b_n \gamma_{\text{th}_f}$ , otherwise  $P_{\text{out}}^{D_f} = 1$  and  $\text{erfc}(\cdot)$  denotes the complementary error function which is expressed as

$$\text{erfc}(z) = \frac{2}{\sqrt{\pi}} \int_z^\infty e^{-t^2} dt. \quad (17)$$

<sup>7</sup>The selection combining (SC) scheme is adopted to calculate the OPs of the IoT devices, since it has low implementation cost and does not reduce the diversity gain. Our analysis may also be reality extended to the maximal ratio combining (MRC) scheme, which will be set aside for our future work.

$$\begin{aligned}
P_{\text{out}}^{D_n} = & \underbrace{\Pr \left( \min \left( \frac{\gamma_{SR}^{D_f}, \gamma_{SR}^{D_n}}{\gamma_{\text{th}_f}, \gamma_{\text{th}_n}} \right) < 1, \min \left( \frac{\gamma_{SD_n}^{D_f}, \gamma_{SD_n}^{D_n}}{\gamma_{\text{th}_f}, \gamma_{\text{th}_n}} \right) < 1 \right)}_{I_3} \\
& + \underbrace{\Pr \left( \min \left( \frac{\gamma_{SR}^{D_f}, \gamma_{SR}^{D_n}}{\gamma_{\text{th}_f}, \gamma_{\text{th}_n}} \right) \geq 1, \min \left( \frac{\gamma_{RD_n}^{D_f}, \gamma_{RD_n}^{D_n}}{\gamma_{\text{th}_f}, \gamma_{\text{th}_n}} \right) < 1, \min \left( \frac{\gamma_{SD_n}^{D_f}, \gamma_{SD_n}^{D_n}}{\gamma_{\text{th}_f}, \gamma_{\text{th}_n}} \right) < 1 \right)}_{I_4}. \tag{18}
\end{aligned}$$

*Proof.* See Appendix A.  $\square$

Similarly, an outage event occurs at  $D_n$  when: Case *iii*) Either  $x_f$  or  $x_n$  cannot be decoded successfully from the  $S \rightarrow D_n$  and  $S \rightarrow R$  links; Case *iv*)  $R$  decodes and forwards  $x_f$  and  $x_n$  to  $D_n$ , while  $D_n$  fails to decode either of them from the  $S \rightarrow D_n$  and  $R \rightarrow D_n$  links. Thus, the OP of  $D_n$  is expressed as (18), shown at the top of the next page, where  $\gamma_{\text{th}_n}$  denotes the SNR threshold of  $x_n$ ,  $I_3$  refers to Case *iii*) and  $I_4$  refers to Case *iv*). The exact OP expression of  $D_n$  for the FD NO-DLT ISAC considered system is given in the following theorem.

**Theorem 2.** *The exact OP of  $D_n$  device is expressed as*

$$\begin{aligned}
P_{\text{out}}^{D_n} = & \left( 1 - e^{-\frac{\theta}{\beta_{SD_n}}} \right) \left\{ 1 - \frac{\beta_{SR}}{2\beta_{RR}(\beta_{SR} + 2\eta\beta_{LI}\gamma_r\theta)} \sqrt{\frac{\pi\beta_{SR}}{\delta\gamma_r\theta}} \right. \\
& \times \left. e^{\frac{\beta_{SR}}{4\beta_{RR}^2\delta\gamma_r\theta} - \frac{\theta}{\beta_{SR}} - \frac{\varphi}{\beta_{RD_n}}} \left[ 1 - \text{erfc} \left( \frac{1}{2\beta_{RR}} \sqrt{\frac{\beta_{SR}}{\delta\gamma_r\theta}} \right) \right] \right\}, \tag{19}
\end{aligned}$$

where  $\theta \triangleq \max(\theta_1, \theta_2)$ ,  $\theta_2 = \gamma_{\text{th}_n}/(a_n\gamma_c)$ ,  $\varphi \triangleq \max(\varphi_1, \varphi_2)$ ,  $\varphi_2 = \gamma_{\text{th}_n}/(b_n\gamma_r)$ .

*Proof.* Similar to Appendix A, substituting (7), (8), and (10)-(14) into (18), and then using the PDFs and CDFs of  $\rho_i$ , (19) can be obtained through a series of mathematical manipulations.  $\square$

**Remark 1.** *We can observe from Theorem 1 and Theorem 2 that the OP of  $D_f$  depends on the decoding capability of  $x_f$  at  $R$  and  $D_f$ , while the OP of  $D_n$  is related to the decoding capability of both  $x_f$  and  $x_n$  at  $R$  and  $D_f$ . More particularly, when considering the direct links, the OPs of the far and near IoT devices are limited by the channel fading, which are respectively given by  $P_{\text{out}}^{D_f} = 1 - \exp(-\theta_1/\beta_{SD_f})$  and  $P_{\text{out}}^{D_n} = 1 - \exp(-\theta/\beta_{SD_n})$ . When considering the cooperative links, the CLSI, SLSI, and echo have a significant impact on the OPs of the IoT devices.*

### B. Diversity Order

To obtain further insights concerning on the FD NO-DLT ISAC system, the diversity orders of the IoT devices in the high-SNR regime are analyzed in this subsection. The diversity order is defined as [45]

$$D_O = - \lim_{\Upsilon \rightarrow \infty} \frac{\log(P_{\text{out}}^\infty)}{\log \Upsilon}, \tag{20}$$

where  $\Upsilon \in \{\gamma_c, \gamma_r\}$  and  $P_{\text{out}}^\infty$  is the asymptotic OP of the IoT devices in the high-SNR regime.

The asymptotic OPs of  $D_f$  and  $D_n$  in the high-SNR regime are summarized in the following corollaries.

**Corollary 1.** *The asymptotic OP of  $D_f$  is expressed as*

$$\begin{aligned}
P_{\text{out}}^{D_f, \infty} \approx & \frac{\theta_1}{\beta_{SD_f}} \left\{ 1 - \left( 1 - \frac{\varphi_1}{\beta_{RD_f}} \right) \frac{\beta_{SR}}{2\beta_{RR}(\beta_{SR} + 2\eta\beta_{LI}\theta_1^*)} \right. \\
& \times \left. \sqrt{\frac{\pi\beta_{SR}}{\delta\theta_1^*}} e^{\frac{\beta_{SR}}{4\beta_{RR}^2\delta\theta_1^*}} \left[ 1 - \text{erfc} \left( \frac{1}{2\beta_{RR}} \sqrt{\frac{\beta_{SR}}{\delta\theta_1^*}} \right) \right] \right\}, \tag{21}
\end{aligned}$$

where we have  $\theta_1^* = \gamma_{\text{th}_f}/(a_f - a_n\gamma_{\text{th}_f})$ .

*Proof.* See Appendix B.  $\square$

By substituting (21) into (20), we can show that the diversity order of  $D_f$  in the high-SNR regime is  $D_O^f = 1$ .

**Corollary 2.** *The asymptotic OP of  $D_n$  is expressed as*

$$\begin{aligned}
P_{\text{out}}^{D_n, \infty} \approx & \frac{\theta}{\beta_{SD_n}} \left\{ 1 - \left( 1 - \frac{\varphi}{\beta_{RD_n}} \right) \frac{\beta_{SR}}{2\beta_{RR}(\beta_{SR} + 2\eta\beta_{LI}\theta^*)} \right. \\
& \times \left. \sqrt{\frac{\pi\beta_{SR}}{\delta\theta^*}} e^{\frac{\beta_{SR}}{4\beta_{RR}^2\delta\theta^*}} \left[ 1 - \text{erfc} \left( \frac{1}{2\beta_{RR}} \sqrt{\frac{\beta_{SR}}{\delta\theta^*}} \right) \right] \right\}, \tag{22}
\end{aligned}$$

where we have  $\theta^* \triangleq \max(\theta_1^*, \theta_2^*)$  and  $\theta_2^* = \gamma_{\text{th}_n}/a_n$ .

*Proof.* Similar to Appendix upon, substituting (7), (8) and (10)-(14) into (18), with the PDF and CDF of  $\rho_i$ , (22) can be obtained after some mathematical manipulations.  $\square$

By substituting (22) into (20), the diversity order of  $D_n$  in the high-SNR regime is  $D_O^n = 1$ .

**Remark 2.** *We can observe from (21) and (22), that the OPs of cooperative links are constant in the high-SNR regime due to the existence of the CLSI, SLSI and echo, which further leads to having a zero diversity order for the cooperative links. In this case, the diversity orders of the IoT devices are provided by those of the direct links. Specifically, for the direct links, the asymptotic OPs of the far and near IoT devices are respectively given by  $P_{\text{out}}^{D_f, \infty} \approx \theta_1/\beta_{SD_f}$  and  $P_{\text{out}}^{D_n, \infty} \approx \theta/\beta_{SD_n}$ , while the corresponding diversity orders are  $D_O^f = D_O^n = 1$ .*

$$R_{\text{ave}}^f = \int_0^\infty \frac{g_c^{\frac{3}{2}}(w_1) e^{\frac{\beta_{SR} g_c(w_1)}{4\beta_{RR}^2 \delta \gamma_r} - \frac{1}{\beta_{SR} g_c(w_1)} - \frac{1}{\beta_{RD_f} g_r(w_1)} - \frac{1}{\beta_{RD_n} g_r(w_1)}} \left[ 1 - \operatorname{erfc} \left( \frac{1}{2\beta_{RR}} \sqrt{\frac{g_c(w_1) \beta_{SR}}{\delta \gamma_r}} \right) \right]}{(1+w_1)(\beta_{SR} g_c(w_1) + 2\eta \beta_{LI} \gamma_r)} dw_1$$

$$\times \frac{\beta_{SR}}{2\beta_{RR} \ln 2} \sqrt{\frac{\pi \beta_{SR}}{\delta \gamma_r}} + \frac{1}{\ln 2} \int_0^\infty \frac{1}{1+w_2} e^{-\frac{1}{\beta_{SD_f} g_c(w_2)} - \frac{1}{\beta_{SD_n} g_c(w_2)}} dw_2. \quad (27)$$

$$R_{\text{ave}}^n = \int_0^\infty \frac{\frac{q_c^{\frac{3}{2}}(w_3)}{(\beta_{SR} q_c(w_3) + 2\eta \beta_{LI} \gamma_r)} e^{\frac{\beta_{SR} q_c(w_3)}{4\beta_{RR}^2 \delta \gamma_r} - \frac{1}{\beta_{SR} q_c(w_3)} - \frac{1}{\beta_{RD_n} q_r(w_3)}} \left[ 1 - \operatorname{erfc} \left( \frac{1}{2\beta_{RR}} \sqrt{\frac{q_c(w_3) \beta_{SR}}{\delta \gamma_r}} \right) \right]}{1+w_3} dw_3$$

$$\times \frac{\beta_{SR}}{2\beta_{RR} \ln 2} \sqrt{\frac{\pi \beta_{SR}}{\delta \gamma_r}} - \frac{1}{\ln 2} e^{\frac{1}{\beta_{SD_n} a_n \gamma_c}} \operatorname{Ei} \left( -\frac{1}{\beta_{SD_n} a_n \gamma_c} \right). \quad (28)$$

#### IV. ESR ANALYSIS

The ESR represents the sum rate of the IoT devices per unit time, which characterize the fading performance of the system from a different perspective than the OP. Thus, in this section, the ESR of the IoT devices is explored for the FD NO-DLT ISAC system considered.

The achievable rates of  $x_f$  and  $x_n$  are respectively expressed as [39]

$$R_f = \underbrace{\log_2 \left( 1 + \min \left( \gamma_{SR}^{D_f}, \gamma_{RD_f}^{D_f}, \gamma_{RD_n}^{D_f} \right) \right)}_{R_f^1}$$

$$+ \underbrace{\log_2 \left( 1 + \min \left( \gamma_{SD_f}^{D_f}, \gamma_{SD_n}^{D_f} \right) \right)}_{R_f^2}, \quad (23)$$

$$R_n = \underbrace{\log_2 \left( 1 + \min \left( \gamma_{SR}^{D_n}, \gamma_{RD_n}^{D_n} \right) \right)}_{R_n^1} + \underbrace{\log_2 \left( 1 + \gamma_{SD_n}^{D_n} \right)}_{R_n^2}. \quad (24)$$

Then, the ergodic rates (ERs) of  $D_f$  and  $D_n$  are respectively given by

$$R_{\text{ave}}^f = R_{\text{ave}}^{f,1} + R_{\text{ave}}^{f,2} = \mathbb{E} [R_f^1] + \mathbb{E} [R_f^2], \quad (25)$$

$$R_{\text{ave}}^n = R_{\text{ave}}^{n,1} + R_{\text{ave}}^{n,2} = \mathbb{E} [R_n^1] + \mathbb{E} [R_n^2]. \quad (26)$$

**Theorem 3.** *The ER of the far IoT device is expressed as (27), shown at the top of the next page, where  $g_c(w) = (a_f \gamma_c - a_n \gamma_c w)/w$  and  $g_r(w) = (b_f \gamma_r - b_n \gamma_r w)/w$ .*

*The ER of the near IoT device is expressed as (28), shown at the top of the next page, where  $q_c(w) = a_n \gamma_c/w$  and  $q_r(w) = b_n \gamma_r/w$ .*

*Proof.* See Appendix C.  $\square$

Thus, the ESR of the IoT devices is expressed as

$$R_{\text{ave}}^{\text{sum}} = R_{\text{ave}}^f + R_{\text{ave}}^n. \quad (29)$$

From (27) and (28), we can observe that it is challenging to obtain the exact ESR of the IoT devices, if not impossible. As a compromise, we analyze the ESR by adopting some approximations. The approximate ERs of  $D_f$  and  $D_n$  are given in the following corollary.

**Corollary 3.** *The approximated ER of the far IoT device is expressed as (30), shown at the top of the next page.*

*The approximate ER of the near IoT device is formulated as (31), shown at the top of the next page.*

Based on (30) and (31), the ESR of the IoT devices can be approximated as

$$R_{\text{ave}}^{\text{ap,sum}} \approx R_{\text{ave}}^{\text{ap,f}} + R_{\text{ave}}^{\text{ap,n}}. \quad (32)$$

*Proof.* See Appendix D.  $\square$

**Remark 3.** *From Theorem 3 and Corollary 3, we can observe that the sensing signal has a negative impact on the ESR of the IoT devices. For the cooperative links, the ERs of  $D_f$  and  $D_n$  respectively tend to be  $\log_2 [1 + a_f \beta_{SR} / (a_n \beta_{SR} + 2\beta_{RR}^2 \delta + 2\eta \beta_{LI})]$  and  $\log_2 [1 + a_n \beta_{SR} / (2\beta_{RR}^2 \delta + 2\eta \beta_{LI})]$  in the high-SNR regime. For the non-cooperative scheme, the sum rate reduces to  $R_{\text{sum}} = R_f^2 + R_n^2$ . Moreover, it is noteworthy that if the MiBS operates in the HD mode, the rates of the IoT devices can be increased due to the absence of CLSI.*

#### V. POD ANALYSIS

As for sensing, the fundamental task is to find the target and make the correct identification, which is the premise of target parameter estimation. Generally, the receive echo is a mixture of the desired signal, interference, and noise. The presence/absence of the target can be determined by the power of the receive signals. Assuming that  $H_0$  represents the null hypothesis and  $H_1$  includes echoes, interference and AWGN, they can be defined as

$$H_0: y_{SR} = h_{SR} y_c + h_{LI} \sqrt{\eta P_{\text{sen}}} (x_{LI}^c + x_{LI}^r) + n_{SR},$$

$$H_1: y_{SR} = h_{SR} y_c + h_{RR} \sqrt{\delta} y_r + h_{LI} \sqrt{\eta P_{\text{sen}}} (x_{LI}^c + x_{LI}^r) + n_{SR}, \quad (33)$$

where  $y_c$  and  $y_r$  denote the signals transmitted by the MaBS and the MiBS, respectively. Indeed, PoFA and PoD are adopted for characterizing the sensing performance. Specifically, if the receive power of the MiBS exceeds the preset threshold under  $H_0$ , the MiBS concludes that a target is present and hence makes the wrong inference. By contrast, the target can be

$$R_{\text{ave}}^{ap,f} \approx \frac{1}{\ln 2} \left\{ \ln \left[ 1 + \min \left( \frac{a_f \beta_{SD_f} \gamma_c}{a_n \beta_{SD_f} \gamma_c + 1}, \frac{a_f \beta_{SD_n} \gamma_c}{a_n \beta_{SD_n} \gamma_c + 1} \right) \right] \right. \\ \left. + \ln \left[ 1 + \min \left( \frac{a_f \beta_{SR} \gamma_c}{a_n \beta_{SR} \gamma_c + 2\beta_{RR}^2 \delta \gamma_r + 2\eta \beta_{LI} \gamma_r + 1}, \frac{b_f \beta_{RD_f} \gamma_r}{b_n \beta_{RD_f} \gamma_r + 1}, \frac{b_f \beta_{RD_n} \gamma_r}{b_n \beta_{RD_n} \gamma_r + 1} \right) \right] \right\}. \quad (30)$$

$$R_{\text{ave}}^{ap,n} \approx \frac{1}{\ln 2} \left\{ \ln(1 + a_n \beta_{SD_n} \gamma_c) + \ln \left[ 1 + \min \left( \frac{a_n \beta_{SR} \gamma_c}{2\beta_{RR}^2 \delta \gamma_r + 2\eta \beta_{LI} \gamma_r + 1}, b_n \beta_{RD_n} \gamma_r \right) \right] \right\}. \quad (31)$$

sensed successfully. Hence, it can be inferred from (33) that the receive power of the MiBS is a non-central Chi-square distributed random variable having a degree-of-freedom (DoF) of four under  $H_0$  and five under  $H_1$  [46]. Therefore, according to  $H_0$ , the false-alarm probability of the MiBS is expressed as [47]

$$P_{\text{fa}} = Q_2 \left( \sqrt{\frac{2(\rho_{SR} P_{\text{com}} + 2\eta \rho_{LI} P_{\text{sen}})}{N_0}}, \sqrt{\frac{2\zeta}{N_0}} \right), \quad (34)$$

where  $\zeta$  denotes the sensing threshold and  $Q(\cdot, \cdot)$  represents the Marcum Q-function [48]. The PoD of the MiBS according to  $H_1$  can be expressed as [33]

$$P_{\text{d}} = Q_{\frac{5}{2}} \left( \sqrt{\frac{2(\rho_{SR} P_{\text{com}} + \eta \rho_{LI} P_{\text{sen}} + \rho_{RR} \delta P_{\text{sen}})}{N_0}}, \sqrt{\frac{2\zeta}{N_0}} \right). \quad (35)$$

In the following, we adopt the receive signal of the MiBS for inferring the presence/absence of the target. According to (2), the power received at the MiBS can be expressed as

$$\mathbb{E} \left[ |y_{SR}|^2 \right] = \rho_{SR} P_{\text{com}} + \rho_{RR} \delta P_{\text{sen}} + 2\eta \rho_{LI} P_{\text{sen}} + N_0. \quad (36)$$

Naturally,  $\mathbb{E} \left[ |y_{SR}|^2 \right]$ ,  $\rho_{SR}$ ,  $P_{\text{com}}$ ,  $P_{\text{sen}}$ , and  $N_0$  are known for the MiBS. Then the information related to the target can be expressed as

$$\rho_{RR} \delta = \frac{\mathbb{E} \left[ |y_{SR}|^2 \right] - 2\eta \rho_{LI} P_{\text{sen}} - \rho_{SR} P_{\text{com}} - N_0}{P_{\text{sen}}}. \quad (37)$$

Apart from the target detection, the measurements of target parameters are also significant. In this context, the distance between the target and the MiBS as well as the velocity of the target are analyzed according to the echo at the receiver.

According to the time difference between transmitting the sensing signal and receiving the target echo, the distance between the MiBS and target may be expressed as [49]

$$d_{RT} = \frac{c}{2} (\tau_l + \tau_s), \quad (38)$$

where  $c$  is the speed of light, and  $(\tau_l + \tau_s)$  denotes the time delay of the target.

As a further step, the radial velocity of the target can be written as [49]

$$v_T = \frac{c}{2f_s} |f_e - f_s|, \quad (39)$$

where  $|f_e - f_s|$  denotes Doppler frequency, while  $f_s$  and  $f_e$  respectively represent the frequency of the transmitted signal and the received echo, which can be observed from the MiBS.

**Remark 4.** It can be observed from (34) that for a given PoFA, there exists a unique detection threshold corresponding to it, and then the PoD can be obtained. In addition, we reiterate that if the target is outside the range of sensing, the result obtained through (37) may be generated by the randomness of noise, thus further signal processing is essential to determine whether the target exists.

**Remark 5.** It should be noted that as the basis of target detection, it is essential to derive the PoD expression for characterizing the sensing performance of the ISAC system considered. In contrast to the cognitive radio networks, in the ISAC systems, the target to be detected is non-cooperative, which is challenging for the MiBS. Therefore, in the following, we design a PA scheme for maximizing the received SINR of the sensing signal, so that the PoD can be further increased.

## VI. POWER ALLOCATION SCHEMES

Having accurate PA is essential to enhance the system performance and the resource utilization. Therefore, in this section, a pair of PA designs are proposed for the FD NO-DLT ISAC system considered, namely, SCD and CCD. Specifically, SCD aims for maximizing the receive SINR of the sensing signal at the MiBS under the IoT devices' QoS constraints. By contrast, CCD aims for maximizing the IoT devices' sum rate under the constraints of minimum SINR requirements. It is worth stating that both SCD and CCD are of practical interest [27], [28]. According to (34) and (35), it can be observed that increasing the SINR of the sensing signal improves the receive echo power and enhances the sensing performance. This means that for SCD, increasing the receive SINR of sensing signal improves the PoD and guarantees the decoding requirements for the cooperative links. Moreover, the proportion of the sensing signal is fixed at a prescribed PoD, which indicates that for CCD, the sum rate is improved, while meeting the sensing performance target. Indeed, these PA problems are meaningful for ISAC systems in practical scenarios from a range of different perspectives. To this end, the receive SINR of  $x_r$  at the MiBS, which according to (2) can be expressed as

$$\gamma_{SR}^R = \frac{\delta \rho_{RR} \gamma_r}{\rho_{SR} \gamma_c + 2\eta \rho_{LI} \gamma_r + 1}. \quad (40)$$

### A. SCD Scheme

On the basis of (40), the SCD scheme can be optimized as

$$\underset{P_{\text{com}}, P_{\text{sen}}, a_n, b_n}{\text{maximize}} \quad \gamma_{SR}^R \quad (41)$$

$$\text{s.t.} \quad \min \left( \gamma_{SR}^{D_f}, \gamma_{RD_f}^{D_f}, \gamma_{RD_n}^{D_f} \right) \geq \gamma_{\text{th}_f}, \quad (41a)$$

$$\min \left( \gamma_{SR}^{D_n}, \gamma_{RD_n}^{D_n} \right) \geq \gamma_{\text{th}_n}, \quad (41b)$$

$$0 \leq P_{\text{com}} \leq P_{\text{max}}, \quad 0 \leq P_{\text{sen}} \leq P_{\text{max}}, \quad (41c)$$

$$a_n + a_f = 1, \quad 0 < a_n < a_f < 1,$$

$$b_n + b_f = 1, \quad 0 < b_n < b_f < 1, \quad (41d)$$

where (41a) and (41b) indicate that  $x_f$  and  $x_n$  respectively can be decoded successfully from the cooperative links, (41c) characterizes the power budget of the MaBS and MiBS, and (41d) guarantees the enforceability of NO-DLT.

Substituting (10)-(12) into (41a) and (41b), the PA problem can be rewritten as

$$\underset{P_{\text{com}}, P_{\text{sen}}, a_n, b_n}{\text{maximize}} \quad \gamma_{SR}^R \quad (42)$$

$$\text{s.t.} \quad P_{\text{com}} \geq (\delta\rho_{RR} + 2\eta\rho_{LI})\theta'P_{\text{sen}} + N_0\theta', \quad (42a)$$

$$P_{\text{sen}} \geq C_1, \quad (41c), \quad (41d), \quad (42b)$$

where  $\theta' = \theta^*/\rho_{SR}$ ,  $C_1 \triangleq \max(C_{11}, C_{12}, C_{13})$ ,  $C_{11} = \varphi_1^*/\rho_{RD_f}$ ,  $C_{12} = \varphi_1^*/\rho_{RD_n}$ ,  $C_{13} = N_0\gamma_{\text{th}_n}/b_n\rho_{RD_n}$ , and  $\varphi_1^* = N_0\gamma_{\text{th}_f}/(b_f - b_n\gamma_{\text{th}_f})$ , while  $\theta_1^*$  and  $\theta^*$  can be obtained from Corollary 1 and Corollary 2, respectively.

Observe from (42) that the PA coefficients are coupled, thus it is difficult to obtain them simultaneously. In the following, we apply the popular alternating optimization (AO) technique and the expressions of  $P_{\text{sen}}$ ,  $P_{\text{com}}$ ,  $a_n$ , and  $b_n$  are derived iteratively.

Substituting (40) into (42), we can observe that  $\gamma_{SR}^R$  is a convex function, since as  $\partial^2\gamma_{SR}^R/\partial P_{\text{sen}}^2 < 0$ . Therefore, the Lagrangian function of (42) can be expressed as

$$\begin{aligned} L_1(P_{\text{sen}}, \lambda_{11}, \lambda_{12}, \lambda_{13}) &= \frac{\delta\rho_{RR}P_{\text{sen}}}{\rho_{SR}P_{\text{com}} + 2\eta\rho_{LI}P_{\text{sen}} + 1} \\ &+ \lambda_{11}[P_{\text{com}} - (\delta\rho_{RR} + 2\eta\rho_{LI})\theta'P_{\text{sen}} - N_0\theta'] \\ &+ \lambda_{12}(P_{\text{sen}} - C_1) + \lambda_{13}(P_{\text{max}} - P_{\text{sen}}), \end{aligned} \quad (43)$$

where  $\lambda_{11}$ ,  $\lambda_{12}$ , and  $\lambda_{13}$  are the non-negative Lagrange multipliers with respect to the constraints (42a), (42b), and (41c), respectively. Examining the Karush-Kuhn-Tucker (KKT) condition for  $L(\cdot)$  yields

$$\begin{aligned} \frac{\partial L_1}{\partial P_{\text{sen}}} &= \frac{\delta\rho_{RR}(\rho_{SR}P_{\text{com}} + 1)}{(\rho_{SR}P_{\text{com}} + 2\eta\rho_{LI}P_{\text{sen}} + 1)^2} \\ &- \lambda_{11}(\delta\rho_{RR} + 2\eta\rho_{LI})\theta' + \lambda_{12} - \lambda_{13} = 0. \end{aligned} \quad (44)$$

After some mathematical manipulations, the PA coefficient  $P_{\text{sen}}^*$  with the fixed multipliers is expressed as (45), shown at the top of the next page, where  $(\Delta)^+ \triangleq \max(0, \Delta)$ .

Next, we optimize  $P_{\text{com}}$  at fixed  $P_{\text{sen}}$ ,  $a_n$ , and  $b_n$ , where the objective function in (42) is monotonically decreasing with

respect to  $P_{\text{com}}$ . Herewith, according to (41c), (42a), and (45), the PA coefficient  $P_{\text{com}}^*$  is expressed as

$$P_{\text{com}}^* = \min[(\delta\rho_{RR} + 2\eta\rho_{LI})\theta'P_{\text{sen}} + N_0\theta', P_{\text{max}}]. \quad (46)$$

The problem can be solved by employing the subgradient method, and the subgradient at  $(\lambda_{11}, \lambda_{12}, \lambda_{13})$  is written as

$$\mathbf{d} = [d_{11}, d_{12}, d_{13}], \quad (47)$$

where  $d_{11} = P_{\text{com}}^* - (\delta\rho_{RR} + 2\eta\rho_{LI})\theta'P_{\text{sen}}^* - N_0\theta'$ ,  $d_{12} = P_{\text{sen}}^* - C_1$ , and  $d_{13} = P_{\text{max}} - P_{\text{sen}}^*$ .

Finally, let us turn our attention to the PA coefficients of  $a_n$  and  $b_n$  at fixed  $P_{\text{com}}$  and  $P_{\text{sen}}$ . Observe from (42) that  $\gamma_{SR}^R$  is independent of  $a_n$  and  $b_n$ , while  $P_{\text{com}}^*$  and  $P_{\text{sen}}^*$  are related to  $a_n$  and  $b_n$  upon combining with (40), (45), and (46), we can observe that  $\gamma_{SR}^R$  is decreasing with respect to  $\theta^*$ . By exploiting this property, the PA problem can be reformulated to find the minimum  $\theta^*$ . Observe from Corollary 1 and Corollary 2 that  $\theta_1^*$  is monotonically increasing, while  $\theta_2^*$  is decreasing with respect to  $a_n$ . Therefore,  $\theta^*$  can be expressed as

$$\theta^* = \begin{cases} \theta_2^*, & \text{if } a_n \in (0, a_n^\dagger] \\ \theta_1^*, & \text{if } a_n \in [a_n^\dagger, 0.5) \end{cases}, \quad (48)$$

where  $a_n^\dagger = \gamma_{\text{th}_n}/(\gamma_{\text{th}_f} + \gamma_{\text{th}_n} + \gamma_{\text{th}_f}\gamma_{\text{th}_n})$ . According to the characteristics of  $\theta_1^*$  and  $\theta_2^*$ ,  $\theta^*$  can be minimized if and only if  $a_n = a_n^\dagger$ .

Furthermore, we can obtain  $b_n^\dagger = \rho_{RD_f}\gamma_{\text{th}_n}/(\rho_{RD_f}\gamma_{\text{th}_n} + \rho_{RD_n}\gamma_{\text{th}_f} + \rho_{RD_f}\gamma_{\text{th}_n}\gamma_{\text{th}_f})$  by using the same method. Therefore,  $a_n^*$  and  $b_n^*$  are expressed as

$$a_n^* = \min(a_n^\dagger, 0.5 - \sigma), \quad (49)$$

$$b_n^* = \min(b_n^\dagger, 0.5 - \sigma), \quad (50)$$

where  $\sigma > 0$  and  $\sigma \rightarrow 0$ .

The alternating optimization algorithm of the SCD scheme is summarized in Algorithm 1, which iteratively determines the PA coefficients.

**Remark 6.** For the SCD scheme, the computational complexity of the algorithm is on the order of  $O[(K_1 + 2)K_2]$ , where  $K_1$  is the number of iterations required for finding the optimal Lagrangian,  $K_2$  is the number of iterations in the main loop.

### B. CCD Scheme

Now, we switch our focus to the CCD scheme. Based on (23) and (24), the CCD scheme can be optimized as follows:

$$\underset{P_{\text{com}}, P_{\text{sen}}, a_n, b_n}{\text{maximize}} \quad R_{\text{sum}} \quad (51)$$

$$\text{s.t.} \quad \min \left( \gamma_{SR}^{D_f}, \gamma_{RD_f}^{D_f}, \gamma_{RD_n}^{D_f}, \gamma_{SD_f}^{D_f}, \gamma_{SD_n}^{D_f} \right) \geq \gamma_{\text{th}_f}, \quad (51a)$$

$$\min \left( \gamma_{SR}^{D_n}, \gamma_{RD_n}^{D_n}, \gamma_{SD_n}^{D_n} \right) \geq \gamma_{\text{th}_n}, \quad (51b)$$

$$\gamma_{SR}^R \geq \kappa, \quad (41c), \quad (41d), \quad (51c)$$

where (51a) and (51b) indicate that the communication signals can be decoded successfully from the cooperative links, (51c) is the receive SINR of  $x_r$  constraint at the MiBS,  $\kappa$  denotes

$$P_{\text{sen}}^* = \left( \frac{1}{2\eta\rho_{LI}} \left[ \sqrt{\frac{\delta\rho_{RR}(\rho_{SR}P_{\text{com}} + 1)}{\lambda_{11}(\delta\rho_{RR} + 2\eta\rho_{LI})\theta' - \lambda_{12} + \lambda_{13}}} - (\rho_{SR}P_{\text{com}} + 1) \right] \right)^+. \quad (45)$$

$$R_{\text{sum}} = \frac{1}{\ln 2} [\min(\ln(l_1) - \ln(f_1), -\ln(b_n)) + \ln(f_2) + \ln(f_3) - \ln(a_n) - 2\ln(N_0)], \quad (52)$$

---

**Algorithm 1: Alternate Optimization Algorithm**


---

**input :** The maximum number of iterations  $L$ ,  $\ell = 1$ , and  $\lambda > 0$ .

**output:** the optimal PA coefficients  $P_{\text{sen}}^\ell$ ,  $P_{\text{com}}^\ell$ ,  $a_n^\ell$ , and  $b_n^\ell$ .

- 1 Initialize  $P_{\text{sen}}^1$ ,  $P_{\text{com}}^1$ ,  $a_n^1$ , and  $b_n^1$  according to (39c) and (39d).
  - 2 **repeat**
  - 3      $\ell = \ell + 1$
  - 4     Fixed  $a_n = a_n^{\ell-1}$ ,  $b_n = b_n^{\ell-1}$ ,  $P_{\text{com}} = P_{\text{com}}^{\ell-1}$ ,  $\lambda_{11} \geq 0$ ,  $\lambda_{12} \geq 0$ , and  $\lambda_{13} \geq 0$ .
  - 5     **repeat**
  - 6         Set  $t = 1$ .
  - 7         Derive the optimal  $\lambda_{11}^*$ ,  $\lambda_{12}^*$ , and  $\lambda_{13}^*$  until convergence using the subgradient-based method.
  - 8         Solve (43) for given  $\lambda_{11}^*$ ,  $\lambda_{12}^*$ , and  $\lambda_{13}^*$  and denote the solution as  $P_{\text{sen}}^{t+1}$ .
  - 9         Update  $t = t + 1$ .
  - 10     **until** The objective value of (43) reaches convergence;
  - 11     Update  $P_{\text{sen}}^\ell = P_{\text{sen}}^t$ .
  - 12     Fixed  $P_{\text{sen}} = P_{\text{sen}}^\ell$ , update  $P_{\text{com}}^\ell$  according to (44).
  - 13     Fixed  $P_{\text{sen}} = P_{\text{sen}}^\ell$  and  $P_{\text{com}} = P_{\text{com}}^\ell$ , update  $a_n^\ell$  and  $b_n^\ell$  according to (46) and (47).
  - 14     Update  $\ell = \ell + 1$ .
  - 15 **until**  $\gamma_{SR}^R(\ell) - \gamma_{SR}^R(\ell - 1) \leq \lambda$  or  $\ell = L$ ;
- 

the lower bound of the receive SINR and  $R_{\text{sum}}$  can be further expressed as (52), shown at the top of the next page<sup>8</sup>, where  $l_1 = \rho_{SR} + \rho_{RR}\delta + 2\eta\rho_{LI}$ ,  $f_1 = a_n\rho_{SR} + \rho_{RR}\delta + 2\eta\rho_{LI}$ ,  $f_2 = a_n\rho_{RD_n}P_{\text{sen}} + N_0$  and  $f_3 = a_n\rho_{SD_n}P_{\text{com}} + N_0$ .

Substituting (7)-(12) and (40) into (51a)-(51c), after some mathematical manipulations, (51) can be rewritten as

$$\underset{P_{\text{com}}, P_{\text{sen}}, a_n, b_n}{\text{maximize}} \quad R_{\text{sum}} \quad (53)$$

$$\text{s.t. } a_n\rho_{SR}P_{\text{com}} - l_2\gamma_{\text{th}_n}P_{\text{sen}} - N_0\gamma_{\text{th}_n} \geq 0, \quad (53a)$$

$$l_3P_{\text{com}} - l_2\gamma_{\text{th}_f}P_{\text{sen}} - N_0\gamma_{\text{th}_f} \geq 0, \quad (53b)$$

$$l_4P_{\text{sen}} - \kappa\rho_{SR}P_{\text{com}} - \kappa N_0 \geq 0, \quad (53c)$$

$$C_2 \leq P_{\text{com}} \leq P_{\text{max}}, C_3 \leq P_{\text{sen}} \leq P_{\text{max}}, \quad (41d), \quad (53d)$$

<sup>8</sup>It should be noted that due to the intractability of the sum rate, it is extremely difficult to obtain the exact PA factors, thus we focus on the approximate sum rate in the high-SNR regimes as in [37] and [50].

where  $l_2 = \rho_{RR}\delta + 2\eta\rho_{LI}$ ,  $l_3 = a_f\rho_{SR} - a_n\rho_{SR}\gamma_{\text{th}_f}$ ,  $l_4 = \delta\rho_{RR} - 2\eta\kappa\rho_{LI}$ ,  $C_2 = \max(C_{21}, C_{22}, C_{23})$  with  $C_{21} = N_0\gamma_{\text{th}_f}/(a_f\rho_{SD_f} - a_n\rho_{SD_f}\gamma_{\text{th}_f})$ ,  $C_{22} = N_0\gamma_{\text{th}_f}/(a_f\rho_{SD_n} - a_n\rho_{SD_n}\gamma_{\text{th}_f})$ , and  $C_{23} = N_0\gamma_{\text{th}_n}/(a_n\rho_{SD_n})$ ,  $C_3 = \max(C_{31}, C_{32}, C_{33})$  with  $C_{31} = N_0\gamma_{\text{th}_f}/(b_f\rho_{RD_f} - b_n\rho_{RD_f}\gamma_{\text{th}_f})$ ,  $C_{32} = N_0\gamma_{\text{th}_n}/(b_f\rho_{RD_n} - b_n\rho_{RD_n}\gamma_{\text{th}_n})$ , and  $C_{33} = N_0\gamma_{\text{th}_n}/(b_n\rho_{RD_n})$ .

Similar to (42), it is hard to simultaneously optimize  $P_{\text{com}}$ ,  $P_{\text{sen}}$ ,  $a_n$ , and  $b_n$ , therefore we adopt AO to derive the PA coefficients as well. By introducing the slack variable  $V$  and according to (52), we can rewrite (53) as (54), shown at the top of the next page.

Since (54) is a convex problem, the Lagrangian function can be expressed as (55), shown at the top of the next page.

It is easy to obtain that  $\lambda_{21} + \lambda_{22} = 1$  and the KKT conditions are expressed as

$$\frac{\partial L}{\partial P_{\text{com}}} = \frac{\lambda_{21}a_n\rho_{SD_n}}{f_3} - \lambda_{23}\kappa\rho_{SR} + \lambda_{24}l_3 + \lambda_{25}a_n\rho_{SR} - \lambda_{26} + \lambda_{28} = 0, \quad (56)$$

$$\frac{\partial L}{\partial P_{\text{sen}}} = \frac{(\lambda_{21} + \lambda_{22})a_n\rho_{RD_n}}{f_2} + \lambda_{23}l_4 - \lambda_{24}l_2\gamma_{\text{th}_f} - \lambda_{25}l_2\gamma_{\text{th}_n} - \lambda_{27} + \lambda_{29} = 0. \quad (57)$$

Based on (56) and (57), the PA coefficients  $P_{\text{com}}^*$  and  $P_{\text{sen}}^*$  are respectively expressed as

$$P_{\text{com}}^* = \left[ \frac{\lambda_{21}}{\lambda_{23}\kappa\rho_{SR} - \lambda_{24}l_3 - \lambda_{25}a_n\rho_{SR} + \lambda_{26} - \lambda_{28}} - \frac{N_0}{a_n\rho_{SD_n}} \right]^+, \quad (58)$$

$$P_{\text{sen}}^* = \left[ \frac{\lambda_{21} + \lambda_{22}}{\lambda_{24}l_2\gamma_{\text{th}_f} - \lambda_{23}l_4 + \lambda_{25}l_2\gamma_{\text{th}_n} + \lambda_{27} - \lambda_{29}} - \frac{N_0}{a_n\rho_{SD_n}} \right]^+. \quad (59)$$

Similarly, the problem can be solved by adopting the subgradient method, and the subgradient at  $(\lambda_{21}, \lambda_{23}, \lambda_{24}, \lambda_{25}, \lambda_{26}, \lambda_{27}, \lambda_{28}, \lambda_{29})$  is written as

$$\mathbf{d} = [d_{21}, d_{23}, d_{24}, d_{25}, d_{26}, d_{27}, d_{28}, d_{29}], \quad (60)$$

where we have  $d_{21} = \ln(l_1) - \ln(f_1) + \ln(b_n)$ ,  $d_{23} = l_4P_{\text{sen}}^* - \kappa\rho_{SR}P_{\text{com}}^* - \kappa N_0$ ,  $d_{24} = l_3P_{\text{com}}^* - l_2\gamma_{\text{th}_f}P_{\text{sen}}^* - N_0\gamma_{\text{th}_f}$ ,  $d_{25} = a_n\rho_{SR}P_{\text{com}}^* - l_2\gamma_{\text{th}_n}P_{\text{sen}}^* - N_0\gamma_{\text{th}_n}$ ,  $d_{26} = P_{\text{max}} - P_{\text{com}}^*$ ,  $d_{27} = P_{\text{max}} - P_{\text{sen}}^*$ ,  $d_{28} = P_{\text{com}}^* - C_2$ , and  $d_{29} = P_{\text{sen}}^* - C_3$ .

$$\underset{P_{\text{com}}, P_{\text{sen}}, V}{\text{maximize}} \quad V \quad (54)$$

$$\text{s.t. } V \leq \ln(l_1) - \ln(f_1) + \ln(f_2) + \ln(f_3) - \ln(a_n) - 2 \ln(N_0), \quad (54a)$$

$$V \leq -\ln(b_n) + \ln(f_2) + \ln(f_3) - \ln(a_n) - 2 \ln(N_0), \quad (53a) - (53d). \quad (54b)$$

$$\begin{aligned} L(P_{\text{com}}, P_{\text{sen}}, V, \lambda_{21}, \lambda_{22}, \lambda_{23}, \lambda_{24}, \lambda_{25}, \lambda_{26}, \lambda_{27}, \lambda_{28}, \lambda_{29}) &= V + \lambda_{21} (\ln(l_1) - \ln(f_1) + \ln(f_2) + \ln(f_3) \\ &- \ln(a_n) - 2 \ln(N_0) - V) + \lambda_{22} (-\ln(b_n) + \ln(f_2) + \ln(f_3) - \ln(a_n) - 2 \ln(N_0) - V) \\ &+ \lambda_{23} (l_4 P_{\text{sen}} - \kappa \rho_{SR} P_{\text{com}} - \kappa N_0) + \lambda_{24} (l_3 P_{\text{com}} - l_2 \gamma_{\text{th}_f} P_{\text{sen}} - N_0 \gamma_{\text{th}_f}) + \lambda_{25} (a_n \rho_{SR} P_{\text{com}} - l_2 \gamma_{\text{th}_n} P_{\text{sen}} \\ &- N_0 \gamma_{\text{th}_f}) + \lambda_{26} (P_{\text{max}} - P_{\text{com}}) + \lambda_{27} (P_{\text{max}} - P_{\text{sen}}) + \lambda_{28} (P_{\text{com}} - C_2) + \lambda_{29} (P_{\text{sen}} - C_3). \end{aligned} \quad (55)$$

$$R_{\text{sum}} = \begin{cases} \frac{1}{\ln 2} [\ln(l_1) - \ln(f_1) + \ln(f_2) + \ln(f_3) - \ln(a_n) - 2 \ln(N_0)], & \text{if } \ln(l_1) - \ln(f_1) \leq \ln(b_n^{-1}) \\ \frac{1}{\ln 2} [-\ln(b_n) + \ln(f_2) + \ln(f_3) - \ln(a_n) - 2 \ln(N_0)], & \text{if } \ln(l_1) - \ln(f_1) > \ln(b_n^{-1}) \end{cases}. \quad (64)$$

Next, we optimize  $a_n$  and  $b_n$  at a fixed  $P_{\text{com}}$  and  $P_{\text{sen}}$ . Substituting (7)-(12) into (53a) and (53b), after some mathematical manipulations, the PA problem can be written as

$$\underset{a_n, b_n}{\text{maximize}} \quad R_{\text{sum}} \quad (61)$$

$$\text{s.t. } C_4 \leq a_n \leq C_5, C_6 \leq b_n \leq C_7, \quad (41d), \quad (61a)$$

where  $C_4 = \max(C_{41}, C_{42})$ ,  $C_{41} = (l_2 P_{\text{sen}} \gamma_{\text{th}_n} + N_0 \gamma_{\text{th}_n}) / (\rho_{SR} P_{\text{com}})$ ,  $C_{42} = N_0 \gamma_{\text{th}_n} / (\rho_{SD_n} P_{\text{com}})$ ,  $C_5 = \min(C_{51}, C_{52}, C_{53})$ ,  $C_{51} = (P_{\text{com}} \rho_{SR} - l_2 P_{\text{sen}} \gamma_{\text{th}_f} - N_0 \gamma_{\text{th}_f}) / [P_{\text{com}} \rho_{SR} (1 + \gamma_{\text{th}_f})]$ ,  $C_{52} = g_1(\rho_{SD_f})$ ,  $C_{53} = g_1(\rho_{SD_n})$ ,  $C_6 = N_0 \gamma_{\text{th}_n} / (\rho_{RD_n} P_{\text{sen}})$ ,  $C_7 = \min(C_{71}, C_{72})$ ,  $C_{71} = g_2(\rho_{RD_f})$ , and  $C_{72} = g_2(\rho_{RD_n})$ . Then,  $g_1(\rho)$  and  $g_2(\rho)$  are respectively given by

$$g_1(\rho) = \frac{P_{\text{com}} \rho - N_0 \gamma_{\text{th}_f}}{P_{\text{com}} \rho (1 + \gamma_{\text{th}_f})}, \quad (62)$$

$$g_2(\rho) = \frac{P_{\text{sen}} \rho - N_0 \gamma_{\text{th}_f}}{P_{\text{sen}} \rho (1 + \gamma_{\text{th}_f})}. \quad (63)$$

For the sake of further analysis,  $R_{\text{sum}}$  is divided into two cases as (64), shown at the top of the next page.

From (64), it can be inferred that the first-order derivative of  $R_{\text{sum}}$  with respect of  $a_n$  in the high-SNR regime always satisfies  $\partial R_{\text{sum}} / \partial a_n > 0$ . Furthermore, if  $\ln(l_1) - \ln(f_1) \leq \ln(b_n^{-1})$ , we can observe that  $\partial R_{\text{sum}} / \partial b_n = 0$ , and we can further observe that  $\partial R_{\text{sum}} / \partial b_n < 0$ , if  $\ln(l_1) - \ln(f_1) > \ln(b_n^{-1})$ . Thus,  $R_{\text{sum}}$  can be maximized if and only if  $b_n$  satisfies  $\ln(l_1) - \ln(f_1) = \ln(b_n^{-1})$ . Therefore, the PA coefficients  $a_n^*$  and  $b_n^*$  are respectively given by

$$a_n^* = 0.5 - \sigma, \quad (65)$$

$$b_n^* = \frac{a_n^* \rho_{SR} + \rho_{RR} \delta + 2\eta \rho_{LI}}{\rho_{SR} + \rho_{RR} \delta + 2\eta \rho_{LI}}. \quad (66)$$

The alternating optimization algorithm of the CCD scheme is summarized in Algorithm 2, which iteratively determines the PA coefficients.

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#### Algorithm 2: Alternate Optimization Algorithm

---

**input :** The maximum number of iterations  $\Psi$ ,  $\psi = 1$ , and  $\dagger > 0$ .  
**output:** the optimal PA coefficients  $P_{\text{sen}}^\psi$ ,  $P_{\text{com}}^\psi$ ,  $a_n^\psi$ , and  $b_n^\psi$ .

- 1 Initialize  $P_{\text{sen}}^1$ ,  $P_{\text{com}}^1$ ,  $a_n^1$ , and  $b_n^1$  according to (39d) and (50d).
- 2 **repeat**
- 3      $\psi = \psi + 1$
- 4     Fixed  $a_n = a_n^{\psi-1}$ ,  $b_n = b_n^{\psi-1}$ ,  $0 \leq \lambda_{21} \leq 1$ ,  $\lambda_{23} \geq 0$ ,  $\lambda_{24} \geq 0$ ,  $\lambda_{25} \geq 0$ ,  $\lambda_{26} \geq 0$ ,  $\lambda_{27} \geq 0$ ,  $\lambda_{28} \geq 0$ , and  $\lambda_{29} \geq 0$ .
- 5     **repeat**
- 6         Set  $q = 1$ .
- 7         Derive the optimal  $\lambda_{21}^*$ ,  $\lambda_{23}^*$ ,  $\lambda_{24}^*$ ,  $\lambda_{25}^*$ ,  $\lambda_{26}^*$ ,  $\lambda_{27}^*$ ,  $\lambda_{28}^*$ , and  $\lambda_{29}^*$  until convergence using the subgradient-based method.
- 8         Solve (55) for given  $\lambda_{21}^*$ ,  $\lambda_{23}^*$ ,  $\lambda_{24}^*$ ,  $\lambda_{25}^*$ ,  $\lambda_{26}^*$ ,  $\lambda_{28}^*$  and denote the solution as  $P_{\text{com}}^{q+1}$ .
- 9         Solve (56) for given  $\lambda_{21}^*$ ,  $\lambda_{23}^*$ ,  $\lambda_{24}^*$ ,  $\lambda_{25}^*$ ,  $\lambda_{27}^*$ ,  $\lambda_{29}^*$  and denote the solution as  $P_{\text{sen}}^{q+1}$ .
- 10         Update  $q = q + 1$ .
- 11     **until** The objective value of (55) and (56) reaches convergence;
- 12     Update  $P_{\text{com}}^\psi = P_{\text{com}}^q$  and  $P_{\text{sen}}^\psi = P_{\text{sen}}^q$ .
- 13     Fixed  $P_{\text{com}}^\psi = P_{\text{com}}^q$  and  $P_{\text{sen}}^\psi = P_{\text{sen}}^q$ , update  $a_n^\psi$  and  $b_n^\psi$  according to (61) and (62).
- 14     Update  $\psi = \psi + 1$ .
- 15 **until**  $R_{\text{sum}}(\psi) - R_{\text{sum}}(\psi - 1) \leq \dagger$  or  $\psi = \Psi$ ;

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**Remark 7.** For the CCD scheme, the computational complexity of the algorithm is  $O[(K_3 + 1) K_4]$ , where  $K_3$  denotes the

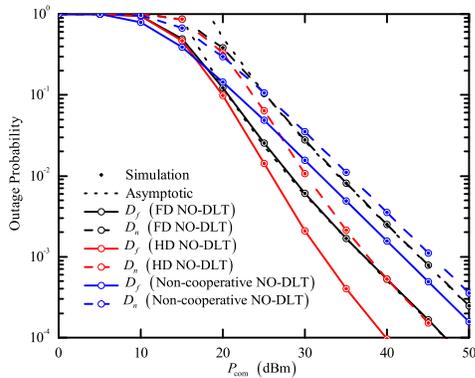


Fig. 2: OPs of the IoT devices vs. the transmit power of  $S$ .

number of iterations to find the optimal Lagrangian and  $K_4$  is the number of iterations in the main loop.

## VII. NUMERICAL RESULTS

In this section, some numerical results are provided for supporting the theoretical analysis presented in Section III-Section VI by using Monte-Carlo computer simulations. Hereinafter, unless otherwise mentioned, the simulation parameters are as follows:  $a_f = b_f = 0.7$ ,  $a_n = b_n = 0.3$ ,  $\gamma_{th_f} = 1$ ,  $\gamma_{th_n} = 2$ ,  $\delta = 0.2$ ,  $N_0 = 1$ ,  $\Omega = 5$ ,  $\alpha = 2$ ,  $\eta = 0.01$ ,  $d_{LI} = 0.5$  m,  $d_{SR} = 100$  m,  $d_{RD_f} = 200$  m,  $d_{RD_n} = 150$  m,  $d_{SD_n} = 200$  m,  $d_{SD_f} = 250$  m,  $d_{RT} = d_{TR} = 75$  m [38]–[40].

Fig. 2 presents the OPs of  $D_n$  and  $D_f$  versus the transmit power of  $S$  with  $P_{com} = P_{sen}$ . For comparison, the OP of the traditional non-cooperative NO-DLT and cooperative HD NO-DLT schemes are presented as well at the same power consumption. It can be seen from Fig. 2 that the Monte Carlo simulation perfectly matches the analytical results and the convergence between the curves in the high-SNR regime verifies the accuracy of the results derived in (16), (19), (21), and (22). We can also observe from Fig. 2 that the OPs of the IoT devices for the proposed FD NO-DLT ISAC scheme are lower than the traditional non-cooperative NO-DLT at the same energy consumption. This is due to the fact that cooperative NO-DLT transmissions are capable of significantly improving the frequency band exploitation. Furthermore, we notice that the OP of the proposed FD NO-DLT scheme is worse than that of HD NO-DLT, mainly due to the additional CLSI.

Fig. 3 demonstrates the ERs of  $D_n$  and  $D_f$  versus the transmit power of  $S$  with  $P_{com} = P_{sen}$ . We reiterate that the total power consumption of the three schemes is identical to ensure a fair comparison. It can be observed from Fig. 3 that the ER of  $D_n$  keeps on increasing, while for  $D_f$ , the ER tends to be saturate eventually. In fact, the ER of the far IoT device is numerically expressed as  $\log_2(1 + a_f/a_n) + \log_2[1 + a_f\beta_{SR}/(a_n\beta_{SR} + 2\beta_{RR}^2\delta + 2\eta\beta_{LI})]$  for the FD NO-DLT,  $\log_2(1 + a_f/a_n) + 0.5\log_2[1 + a_f\beta_{SR}/(a_n\beta_{SR} + 2\beta_{RR}^2\delta + 2\eta\beta_{LI})]$  for the HD NO-DLT, and  $\log_2(1 + a_f/a_n)$  for the non-cooperative

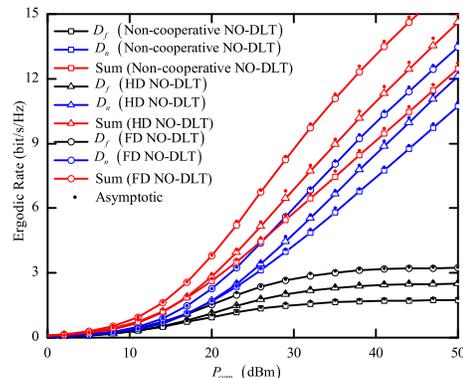


Fig. 3: ERs of the IoT devices vs. the transmit power of  $S$ .

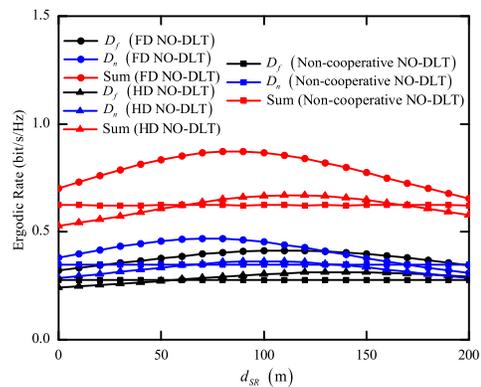


Fig. 4: ERs of the IoT devices vs. the relay location.

NO-DLT in the high SNR regime. Moreover, it can be seen that the ER of the near IoT device would eventually govern the ESR in the high-SNR regime.

Fig. 4 illustrates the ERs of  $D_n$  and  $D_f$  versus the relay location for the FD, HD, and non-cooperative schemes. Since the near IoT device makes a significant contribution to the ESR, for tangibly characterizing the system performance, we assume that  $S$ ,  $R$ , and  $D_n$  are positioned along a straight line, and  $R$  is located between  $S$  and  $D_n$ . We set  $P_{com} = P_{sen} = 20$  dBm,  $d_{SD_n} = 200$  m,  $d_{SD_f} = 250$  m, the angle between  $S \rightarrow D_f$  and  $S \rightarrow D_n$  is set to  $\phi = 30^\circ$ , thus the distance between  $R$  and  $D_f$  is  $d_{RD_f} = \sqrt{d_{SR}^2 + d_{SD_f}^2 - 2d_{SR}d_{SD_f}\cos\phi}$ . Observe from Fig. 4 that for the cooperative NO-DLT schemes, the ESR of the IoT devices improves first and then degrades upon increasing  $d_{SR}$ . The reason for this phenomenon can be attributed to the fact that the increase of  $d_{SR}$  improves the channel gains between the relay and the IoT devices. However, at a shorter  $d_{RD_n}$ , the path loss between the MaBS and the relay increases, thus degrading the data transmission. Additionally, it can also be seen that if  $R$  and  $D_n$  are particularly close to each other, the ERs of  $D_n$  for the FD and HD NO-DLT become inferior to that of non-cooperative NO-DLT, since the cooperative NO-DLT schemes have to share a

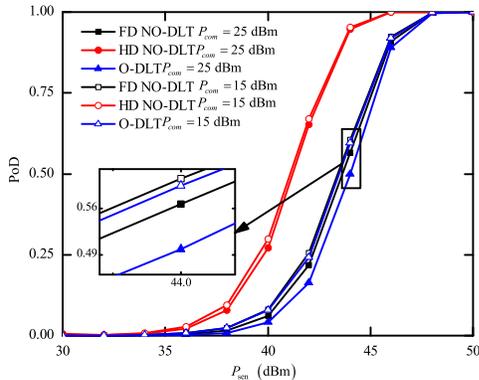


Fig. 5: PoD vs. the transmit power of the MiBS.

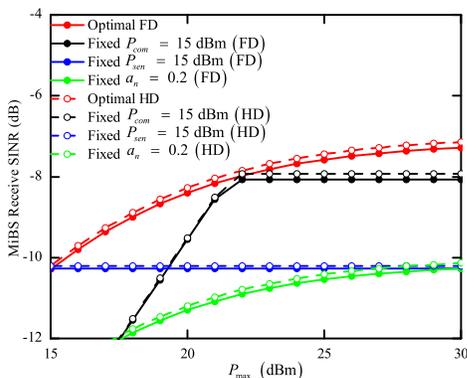


Fig. 6: Receive SINR of  $x_r$  vs. the maximum power budget of the MaBS and MiBS.

portion of the total power for target sensing.

Fig. 5 shows the PoD of the MiBS versus the transmit power of  $R$  at  $P_{fa} = 10^{-5}$ . Intuitively, the PoD can be improved by increasing the transmit power of  $R$ . It can be observed that the PoD of the proposed NO-DLT ISAC system is superior to that of the traditional O-DLT, since NO-DLT can serve multiple IoT devices at the same time, whereas O-DLT requires repeated communication signal transmission, which further increases the interference during sensing. We can further see from Fig. 5 that the sensing behavior can be improved by reducing  $P_{com}$ , which is due to the fact that the signal transmitted by the MaBS is regarded as interference. Furthermore, due to the existence of supererogatory CLSI, the sensing performance of FD NO-DLT scheme lags behind that of HD NO-DLT at the same parameter settings, which is consistent with the result of (35).

Fig. 6 plots the receive SINR of  $x_r$  at the MiBS versus the power budget of the MaBS and the MiBS  $P_{max}$  for both the FD and HD modes. For comparison, we plot the curves of the proposed PA scheme and three other random power allocation (RPA) baseline schemes, i.e., 1) Jointly optimizing  $P_{sen}$ ,  $a_n$ , and  $b_n$  at fixed  $P_{com} = 15$  dBm; 2) Jointly optimizing  $P_{com}$ ,

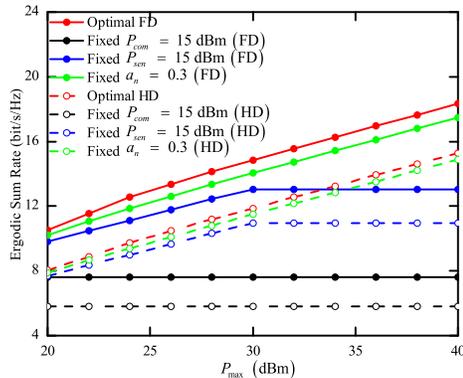


Fig. 7: Sum rate vs. the maximum power budget of the MaBS and MiBS.

$a_n$ , and  $b_n$  at fixed  $P_{sen} = 15$  dBm; 3) Jointly optimizing  $P_{com}$  and  $P_{sen}$  at fixed  $a_n = b_n = 0.2$ . For a fixed  $P_{com}$ , the receive SINR of  $x_r$  first increases with  $P_{max}$  and then gradually saturating with a diminishing small return for an exceedingly large  $P_{max}$ . This is because the increase of  $P_{max}$  also increases  $P_{sen}$  and further improves the receive SINR of  $x_r$ . However, if the critical communication decoding capability is reached, no additional sensing power is allocated so as to cater for the lowest signals decoding of communication, and the receive SINR of  $x_r$  remains unchanged. For a fixed  $P_{sen}$ , the sensing performance is degraded as  $P_{com}$  increases, once the required decoding requirements are achieved, the receive SINR of  $x_r$  saturates. For the fixed  $a_n$  and  $b_n$ , limited by the decoding requirements, the receive SINR of  $x_r$  observed for the RPA scheme lags behind that of the proposed PA scheme. Additionally, it can be observed from Fig. 6 that due to the existence of CLSI, the receive SINR of the FD mode becomes lower than that of the HD mode.

Fig. 7 shows the advantages of the proposed PA scheme over other RPA baseline schemes in terms of the sum rate attained in both the FD and HD modes. As seen from Fig. 7, the proposed PA scheme is superior to the schemes of the fixed  $P_{com}$ ,  $P_{sen}$  or  $a_n$ . For a fixed  $P_{com}$ , due to associated the sensing constraint and the requirements of communication signals decoding, the sum rate remains constant. Furthermore, for a given  $P_{sen}$ , the sum rate increases with  $P_{max}$ . This phenomenon continues until the communication scheme reaches its peak power at a fixed sensing demand. For the fixed  $a_n$  and  $b_n$ , restricted by the characteristics of the objective function and the decoding of communication signals, the sum rate becomes inferior to that of the proposed PA scheme. Finally, as expected, the sum rate of the FD NO-DLT system considered is reduced by the CLSI compared to that of the HD mode.

## VIII. CONCLUSION

In this paper, we studied a FD NO-DLT ISAC system, in which the MiBS supports simultaneous target sensing and cooperative relaying. We characterized the performance of C&S by deriving both the exact and asymptotic OPs, the diversity

$$\begin{aligned}
I_1 &= \Pr \left( \frac{a_f \rho_{SR} \gamma_c}{a_n \rho_{SR} \gamma_c + \rho_{RR} \delta \gamma_r + 2\eta \rho_{LI} \gamma_r + 1} < \gamma_{\text{th}_f} \right) \Pr \left( \frac{a_f \rho_{SD_f} \gamma_c}{a_n \rho_{SD_f} \gamma_c + 1} < \gamma_{\text{th}_f} \right) \\
&= \Pr (\rho_{SR} < \rho_{RR} \delta \gamma_r \theta_1 + 2\eta \rho_{LI} \gamma_r \theta_1 + \theta_1) \Pr (\rho_{SD_f} < \theta_1) \\
&= \underbrace{\int_0^\infty \int_0^\infty \int_0^{\theta_1(x\delta\gamma_r + 2y\gamma_r + 1)} f_{\rho_{SR}}(x) f_{\rho_{LI}}(y) f_{\rho_{RR}}(z) dx dy dz}_{I_{1,I}} \underbrace{\int_0^{\theta_1} f_{\rho_{SD_f}}(w) dw}_{I_{1,II}}. \tag{A.1}
\end{aligned}$$

orders, the approximate ESR expressions for communication, the PoFA and PoD as well as the velocity and distance between the MiBS and target for sensing. To further characterize the performance of the system considered, both the SCD and CCD, PA problems were solved. Then, the maximization problems of the sensing signal's receive SINR at the MiBS and the IoT devices' sum rate were determined by using the Lagrangian method. The simulation results demonstrated that the FD NO-DLT system outperformed its traditional non-cooperative counterpart in terms of its OP at a constant total power, while it was inferior to the HD NO-DLT system. In terms of the ESR, the location of the MiBS had a substantial influence on it and the FD NO-DLT revealed its benefits. Furthermore, the sensing performance of the proposed FD NO-DLT ISAC system is improved over that of the traditional O-DLT scheme as well. Finally, we confirmed that the proposed PA scheme is superior to the RPA schemes.

#### APPENDIX A: PROOF OF THEOREM 1

Upon substituting (9) and (10) into (15),  $I_1$  can be rewritten as (A.1), shown at the top of the next page.

By using PDFs and CDFs of  $\rho_i$ ,  $I_{1,I}$  can be expressed as

$$\begin{aligned}
I_{1,I} &= 1 - \frac{\beta_{SR}}{2\beta_{RR}(\beta_{SR} + 2\eta\beta_{LI}\gamma_r\theta_1)} e^{-\frac{\theta_1}{\beta_{SR}}} \\
&\quad \times \underbrace{\int_0^\infty \frac{1}{\sqrt{x}} e^{-\frac{\sqrt{x}}{\beta_{RR}} - \frac{x\delta\gamma_r\theta_1}{\beta_{SR}}} dx}_{I_{1,I}^\Delta}. \tag{A.2}
\end{aligned}$$

By defining  $t \triangleq \sqrt{x}$  and using [51, Eq. (3.322.2)],  $I_{1,I}^\Delta$  can be further expressed as

$$\begin{aligned}
I_{1,I}^\Delta &= 2 \int_0^\infty e^{-\frac{t}{\beta_{RR}} - \frac{\delta\gamma_r\theta_1 t^2}{\beta_{SR}}} dt \\
&= \sqrt{\frac{\pi\beta_{SR}}{\delta\gamma_r\theta_1}} e^{\frac{\beta_{SR}}{4\beta_{RR}^2\delta\gamma_r\theta_1}} \left[ 1 - \operatorname{erfc} \left( \frac{1}{2\beta_{RR}} \sqrt{\frac{\beta_{SR}}{\delta\gamma_r\theta_1}} \right) \right]. \tag{A.3}
\end{aligned}$$

Substituting the PDF of  $\rho_i$  into the second part of (A.1), after some straightforward mathematical manipulations,  $I_1$  can be finally expressed as

$$\begin{aligned}
I_1 &= \left( 1 - e^{-\frac{\theta_1}{\beta_{SD_f}}} \right) \left\{ 1 - \frac{\beta_{SR}}{2\beta_{RR}(\beta_{SR} + 2\eta\beta_{LI}\gamma_r\theta_1)} e^{\frac{\beta_{SR}}{4\beta_{RR}^2\delta\gamma_r\theta_1} - \frac{\theta_1}{\beta_{SR}}} \right. \\
&\quad \left. \times \sqrt{\frac{\pi\beta_{SR}}{\delta\gamma_r\theta_1}} \left[ 1 - \operatorname{erfc} \left( \frac{1}{2\beta_{RR}} \sqrt{\frac{\beta_{SR}}{\delta\gamma_r\theta_1}} \right) \right] \right\}. \tag{A.4}
\end{aligned}$$

Upon substituting (9), (10), and (12) into (15), and similar to  $I_1$ , after some mathematical manipulations,  $I_2$  can be expressed as

$$\begin{aligned}
I_2 &= \left( 1 - e^{-\frac{\theta_1}{\beta_{SD_f}}} \right) \left( 1 - e^{-\frac{\varphi_1}{\beta_{RD_f}}} \right) \frac{\beta_{SR}}{2\beta_{RR}(\beta_{SR} + 2\eta\beta_{LI}\gamma_r\theta_1)} \\
&\quad \times e^{\frac{\beta_{SR}}{4\beta_{RR}^2\delta\gamma_r\theta_1} - \frac{\theta_1}{\beta_{SR}}} \sqrt{\frac{\pi\beta_{SR}}{\delta\gamma_r\theta_1}} \left[ 1 - \operatorname{erfc} \left( \frac{1}{2\beta_{RR}} \sqrt{\frac{\beta_{SR}}{\delta\gamma_r\theta_1}} \right) \right]. \tag{A.5}
\end{aligned}$$

Substituting (A.4) and (A.5) into (15), after some straightforward mathematical manipulations, (16) can be obtained.

#### APPENDIX B: PROOF OF COROLLARY 1

In the high-SNR regime of  $\gamma_c, \gamma_r \rightarrow \infty$ , we can obtain

$$\lim_{\gamma_c \rightarrow \infty} \theta_1 = \lim_{\gamma_c \rightarrow \infty} \frac{\gamma_{\text{th}_f}}{a_f \gamma_c - a_n \gamma_c \gamma_{\text{th}_f}} \approx 0, \tag{B.1}$$

$$\lim_{\gamma_r \rightarrow \infty} \varphi_1 = \lim_{\gamma_r \rightarrow \infty} \frac{\gamma_{\text{th}_f}}{a_f \gamma_r - a_n \gamma_r \gamma_{\text{th}_f}} \approx 0, \tag{B.2}$$

$$\lim_{\gamma_c, \gamma_r \rightarrow \infty} \gamma_r \theta_1 = \lim_{\gamma_r \rightarrow \infty} \frac{\gamma_r \gamma_{\text{th}_f}}{a_f \gamma_c - a_n \gamma_c \gamma_{\text{th}_f}} \approx \theta_1^*. \tag{B.3}$$

Upon substituting (B.3) into (A.1),  $I_{1,I}$  can be expressed as in the high-SNR regime

$$I_{1,I}^\infty = \int_0^\infty \int_0^\infty \int_0^{x\delta\theta_1^* + 2y\theta_1^*} f_{\rho_{RR}}(x) f_{\rho_{LI}}(y) f_{\rho_{SR}}(z) dx dy dz. \tag{B.4}$$

Similar to (A.2), after some mathematical manipulations, we can obtain the expression of  $I_{1,I}^\infty$ .

When  $x \rightarrow 0$ , the approximation  $1 - e^{-x} \approx x$  holds and substituting (B.1) into (A.1),  $I_{1,II}$  in the high SNR regime is expressed as  $I_{1,II}^\infty = \theta_1 / \beta_{SD_f}$ .

Likewise, we can obtain  $I_2^\infty$  by using the same method. Substituting  $I_1^\infty$  and  $I_2^\infty$  into (15), (21) can be obtained.

#### APPENDIX C: PROOF OF THEOREM 3

Upon defining  $W_1 \triangleq \min(\gamma_{SR}^{D_f}, \gamma_{RD_f}^{D_f}, \gamma_{RD_n}^{D_f})$  and  $W_2 \triangleq$

$\min(\gamma_{SD_f}^{D_f}, \gamma_{SD_n}^{D_f})$ , the achievable rate of  $D_f$  can be rewritten

$$R_f = \underbrace{\log_2(1 + W_1)}_{R_f^1} + \underbrace{\log_2(1 + W_2)}_{R_f^2}. \tag{C.1}$$

$$R_{\text{ave}}^{ap,f1} \approx \frac{1}{\ln 2} \ln \left[ 1 + \min \left( \frac{a_f \mathbb{E}[\rho_{RD_f}] \gamma_r}{a_n \mathbb{E}[\rho_{RD_f}] \gamma_r + 1}, \frac{a_f \mathbb{E}[\rho_{RD_n}] \gamma_r}{a_n \mathbb{E}[\rho_{RD_n}] \gamma_r + 1}, \frac{a_f \mathbb{E}[\rho_{SR}] \gamma_c}{a_n \mathbb{E}[\rho_{SR}] \gamma_c + \mathbb{E}[\rho_{RR}] \delta \gamma_r + 2\eta \mathbb{E}[\rho_{LI}] \gamma_r + 1} \right) \right]. \quad (\text{D.3})$$

Substituting (10), (12), and (13) into  $W_1$ , with the aid of probability theory, the CDF of  $W_1$  can be expressed as

$$\begin{aligned} F_{W_1}(w_1) &= 1 - \Pr \left( \rho_{SR} \geq \frac{\delta \gamma_r \rho_{RR}}{g_c(w_1)} + \frac{2\eta \gamma_r \rho_{LI}}{g_c(w_1)} + \frac{1}{g_c(w_1)} \right. \\ &\quad \left. \rho_{RD_f} \geq g_r(w_1), \rho_{RD_n} \geq g_r(w_1) \right) \\ &= 1 - \frac{\beta_{SR} g_c(w_1)}{2\beta_{RR}(\beta_{SR} g_c(w_1) + 2\beta_{LI} \gamma_r)} \sqrt{\frac{\pi \beta_{SR} g_c(w_1)}{\delta \gamma_r}} \\ &\quad \times e^{\frac{\beta_{SR} g_c(w_1)}{4\beta_{RR}^2 \delta \gamma_r} - \frac{1}{\beta_{SR} g_c(w_1)} - \frac{1}{\beta_{RD_f} g_r(w_1)} - \frac{1}{\beta_{RD_n} g_r(w_1)}} \\ &\quad \times \left[ 1 - \operatorname{erfc} \left( \frac{1}{2\beta_{RR}} \sqrt{\frac{g_c(w_1) \beta_{SR}}{\delta \gamma_r}} \right) \right]. \quad (\text{C.2}) \end{aligned}$$

Next, we can further observe that

$$\begin{aligned} R_{\text{ave}}^{f,1} &= \int_0^\infty \log_2(1+w_1) f_{W_1}(w_1) dw_1 \\ &= \frac{1}{\ln 2} \int_0^\infty \frac{1 - F_{W_1}(w_1)}{1+w_1} dw_1. \quad (\text{C.3}) \end{aligned}$$

Substituting (C.2) into (C.3), we can obtain the expression of  $R_{\text{ave}}^{f,1}$ . The same procedure can be adopted for the proof of  $R_{\text{ave}}^{f,2}$ . Then, we can obtain (27) after some mathematical manipulations.

Likewise, we can derive  $R_{\text{ave}}^{n,1}$  following the same approach as in (C.2).

For  $R_{\text{ave}}^{n,2}$ , denoting  $U \triangleq \gamma_{SD_n}^{D_n}$  first, the CDF of  $U$  can be written as

$$F_U(u) = \Pr(a_n \rho_{SD_n} \gamma_c \leq u) = 1 - e^{-\frac{u}{\beta_{SD_n} a_n \gamma_c}}. \quad (\text{C.4})$$

Similar to (C.3), and with the aid of [51, Eq. (3.352.4)], the exact expression of  $R_{\text{ave}}^{n,2}$  can be formulated as

$$R_{\text{ave}}^{n,2} = -\frac{1}{\ln 2} e^{\frac{1}{\beta_{SD_n} a_n \gamma_c}} \operatorname{Ei} \left( -\frac{1}{\beta_{SD_n} a_n \gamma_c} \right). \quad (\text{C.5})$$

After some straightforward mathematical manipulations, (28) can be obtained.

#### APPENDIX D: PROOF OF COROLLARY 3

Substituting (10), (12), and (13) into (23), and using the inequality [39]

$$\mathbb{E} \left[ \log_2 \left( 1 + \frac{x}{y} \right) \right] \approx \log_2 \left( 1 + \frac{\mathbb{E}[x]}{\mathbb{E}[y]} \right), \quad (\text{D.1})$$

$R_{\text{ave}}^{f,1}$  can be approximated as (D.3), shown at the top of the next page, where  $\mathbb{E}[\rho_{SR}]$  is expressed as

$$\mathbb{E}[\rho_{SR}] = \int_0^\infty x f_{\rho_{SR}}(x) dx = \beta_{SR}. \quad (\text{D.2})$$

Then, we can obtain  $\mathbb{E}[\rho_{RD_f}]$ ,  $\mathbb{E}[\rho_{RD_n}]$ ,  $\mathbb{E}[\rho_{RR}]$ , and  $\mathbb{E}[\rho_{LI}]$  with the same method.  $R_{\text{ave}}^{ap,f1}$  can be obtained after some mathematical manipulations.

Similarly,  $R_{\text{ave}}^{ap,f2}$ ,  $R_{\text{ave}}^{ap,n1}$ , and  $R_{\text{ave}}^{ap,n2}$  can be derived. Then, the approximate ESR of the IoT devices can be obtained.

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