



Radar Interference Mitigation for Automated Driving: Exploring Proactive Strategies

Downloaded from: <https://research.chalmers.se>, 2024-05-08 10:16 UTC

Citation for the original published paper (version of record):

Aydogdu, C., Keskin, F., Carvajal, G. et al (2020). Radar Interference Mitigation for Automated Driving: Exploring Proactive Strategies. IEEE Signal Processing Magazine, 37(4): 72-84.
<http://dx.doi.org/10.1109/MSP.2020.2969319>

N.B. When citing this work, cite the original published paper.

© 2020 IEEE. Personal use of this material is permitted. Permission from IEEE must be obtained for all other uses, in any current or future media, including reprinting/republishing this material for advertising or promotional purposes, or reuse of any copyrighted component of this work in other works.

Radar Interference Mitigation for Automated Driving

Canan Aydogdu, Musa Furkan Keskin, Gisela K. Carvajal, Olof Eriksson, Hans Hellsten, Hans Herbertsson, Emil Nilsson, Mats Rydström, Karl Vanäs, Henk Wymeersch

Abstract

Autonomous driving relies on a variety of sensors, especially on radars, which have unique robustness under heavy rain/fog/snow and poor light conditions. With the rapid increase of the amount of radars used on modern vehicles, where most radars operate in the same frequency band, the risk of radar interference becomes a compelling issue. This article analyses automotive radar interference and proposes several new approaches, which combine industrial and academic expertise, toward the path of interference-free autonomous driving.

INTRODUCTION AND MOTIVATION

Radar is becoming the standard equipment in all modern cars, supporting, e.g., cruise control and collision avoidance in most weather conditions whilst providing high-resolution detections on the order of centimeters in the millimeter-wave (mmWave) band. The next generation of Advanced Driver Assistance (ADAS) and Autonomous Drive (AD) vehicles will have a multitude of radars covering multiple safety and comfort applications like crash-avoidance, self-parking, in-cabin monitoring, cooperative driving, collective situational awareness and more. Since automotive radar transmissions are uncoordinated, there is a non-negligible probability of interference among vehicles, as shown in Fig. 1. While current automotive radars are already impacted by interference to some extent, it is today unlikely to get issues noticeable to the customer as the state-of-the-art automotive radars are continuously updated and improved on multiple system levels. However, the mutual interference problem is expected to become more challenging, unless properly handled, as more vehicles are equipped with a larger number of radars providing 360° situational awareness at various distances to enable more advanced future ADAS and AD functionalities. This is evidenced by multiple international studies, such as in the EU MOSARIM project [1] and the

Canan Aydogdu, Musa Furkan Keskin, and Henk Wymeersch are with the Department of Electrical Engineering, Chalmers University of Technology, 41296 Gothenburg, Sweden, Email: canan.aydogdu@chalmers.se, Gisela K. Carvajal is with QAMCOM Research, 41285 Gothenburg, Sweden. Karl Vanäs is with Volvo Car Corporation, 40531, Gothenburg, Sweden. Hans Herbertsson, Olof Eriksson and Mats Rydström are with Veoneer, 44737, Vårgårda, Sweden. Hans Hellsten and Emil Nilsson are with Halmstad University, Sweden. Hans Hellsten is also with SAAB. This research was supported by Vinnova grant 2018-01929.

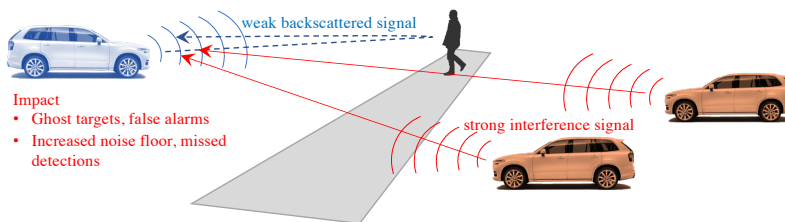


Fig. 1. Interference is generally much stronger than the desired radar signal, due to the one-way propagation. Interference increases with more interfering radars and leads to false alarms and missed detections.

more recent IMIKO RADAR project. All major players in the automotive sensor market, like Volvo and Veoneer, are involved in activities studying the next generation of “interference-free radars”. This includes, for example, enhancing models to see the impact of a larger density of radars, simulating new interference scenarios, investigating different medium access control (MAC) models and methods to coordinate radar transceivers, both decentralized and centralized. At this point, the automotive industry is ready to consider novel designs and approaches, which might impact standardization bodies before new frequency spectrum is made available in the higher RF bands. Signal processing can provide ways to reduce or mitigate interference, both at the raw signal level as well as at the post-detection/target tracking level. The particular properties and requirements of automotive radar impose significant challenges in terms of signal processing. This includes combination of radar and communication waveforms, which brings up further possibilities regarding ultra-reliable low-latency communications (URLLC) in vehicular ad-hoc networks (VANETs). Hence, it is timely to review what has been done, what are reasonable approaches, and what the future holds.

The focus of this article is on frequency modulated continuous wave (FMCW) radar, since it is the most common and robust automotive radar. We provide an analysis of the impact of interference in FMCW both quantitatively and qualitatively, in terms of their probability, severity, and effects. Then, we cover different ways to mitigate interference, ranging from changing FMCW parameters, to new signal structures, and explicit coordination between vehicles. We also study new techniques that are potentially more robust towards interference, including stepped-frequency orthogonal frequency division multiplexing (OFDM). Finally, we describe what we believe will be the long-term evolution of automotive radar and its relation to mobile communication.

AUTOMOTIVE RADAR

History and Future of Automotive Radar

Radar has been used in automotive applications for a long time. Already in 1949, unfortunate car drivers were issued speeding tickets based on speed measurements obtained from the radar speed gun,

recently invented by John L. Barker. However, on-board automotive radar was not made commercially available until 1999, when it was introduced for collision warning and automatic cruise control (ACC). See [2] for an early history of automotive radar with some entertaining vintage photography. Over the years, there has been a strong push to increase the integration level of millimeter wave electronics used for automotive radar and industrial radar sensors. The early discrete hardware designs have been replaced by a few chips in III-V-materials, and now CMOS single chip solutions are available. With CMOS technology comes the ability to fully integrate analog and digital electronics, making very advanced protocols and detection schemes possible at low cost and low power. Consequently, radar is becoming more and more common for supporting various automotive applications. ADAS systems based on radar are today standard equipment in most new vehicles. Vehicles capable of some level of AD are also foreseen to rely, at least to some degree, on radar systems for monitoring vehicle surroundings. The number of radar transceivers operating throughout the traffic environment is foreseen to increase rapidly over the coming years. As the number of radar transceivers in the traffic infrastructure increases, radar interference is also expected to increase. Today most radar transmissions are uncoordinated, meaning that there is no a priori agreement on who is allowed to transmit and when. A number of recent studies have indicated the interference situations which are likely to arise as the automotive radar transceiver market penetration increases [1], [3]. FMCW waveforms can, up to a point, relatively easily be repaired in case it is intermittently corrupted by interference [4], which is why they are still operational.

Future radar systems are expected to occupy frequency bands higher and higher up in frequency. Transceivers operating around 77 GHz are available today, and transceivers operating at carrier frequencies beyond 100 GHz are expected. Frequencies as high as 300 GHz and beyond are being considered for some applications, such as synthetic aperture radar mapping. Operation at such high frequencies bring the obvious benefits of improved miniaturization, but also presents challenges in terms of hardware complexity and signal attenuation. Moreover, interference-free operation will require radar transmission standardization. A standardized transmission scheduling system resembling today's cellular communication system would present a solution to the interference problem, but it is not without challenges, both technical and political.

Basics of FMCW Radar

In a general FMCW radar a frequency sweep, a chirp, is generated by a voltage-controlled oscillator (VCO) controlled by a digital synthesizer. The generated chirp signal is split and sent into two different signal paths: one path is directed to the transmitter antenna (TX), while the other path is directed to the mixer correlator. Before the chirp is sent out on the TX antenna it passes a power amplifier (PA) boosting

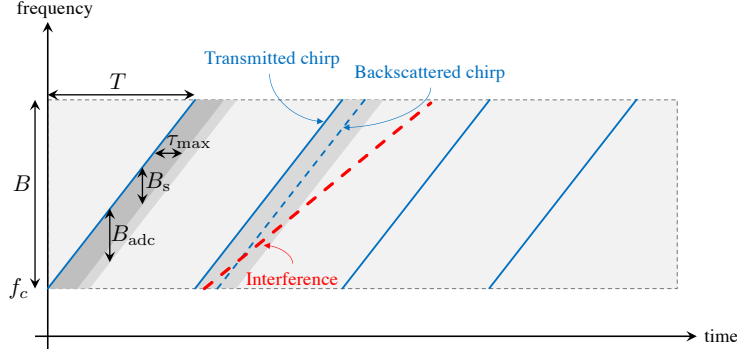


Fig. 2. Four consecutive chirps in time-frequency representation. Several key notations are included. A backscattered signal and an interfering signal is shown at the second chirp.

the transmitted energy. The transmit waveform of an FMCW radar with K consecutive linear frequency modulated (LFM) chirps¹ (or sweeps) can be expressed as [5]

$$s(t) = \sum_{k=0}^{K-1} x(t - kT) \quad (1)$$

where the individual chirps are given by

$$x(t) = e^{j\varphi(t)} \text{rect}_T(t), \quad \varphi(t) = 2\pi(f_c t + 0.5\alpha t^2). \quad (2)$$

Here, $\alpha = B/T$ is the chirp slope, B denotes the sweep bandwidth, T represents the chirp duration, f_c is the carrier frequency, and $\text{rect}_T(t)$ is square pulse of duration T with amplitude 1. The received reflected signal from a target is very weak due to the two-way free space propagation path loss and losses incurred during reflection, and thus needs to be amplified with a low noise amplifier (LNA) to maintain an acceptable signal-to-noise-ratio (SNR). The amplified signal from the target reflection is correlated with the transmitter signal in the mixer correlator, also called dechirping. The low pass filter at the output of the correlating mixer offers some interference rejection. Round-trip delay and Doppler shift caused by the relative velocity of the target shifts the frequency of the received signal compared to the transmitted signal. As a result, the mixer creates a beat signal that will pass through a low-pass filter and be digitized, yielding delay and Doppler estimates after matched filtering. In modern automotive radars, it is also possible to estimate azimuth and elevation of targets using multiple antennas.

FMCW Radar Signal Processing Chain

Suppose there exists a single target of interest acting as a point scatterer, characterized by a complex channel gain γ (including the effects of path loss, antenna gain and radar cross section), an (initial)

¹Here, we assume no idle periods between consecutive chirps. It is also possible to introduce random inter-chirp idle periods to reduce the probability of mutual interference between FMCW radars.

round-trip propagation delay $\tau = 2R/c$ and a normalized relative Doppler shift $\nu = 2v/c$, where R and v denote, respectively, the distance and relative radial velocity between the radar and target, and c is the speed of wave propagation. The received backscattered signal is now processed in three stages.

Stage 1: Dechirping: Under the stop-and-hop assumption [6, Ch. 2.6.2], the k th chirp of the received signal is given by

$$r_k(t) = \gamma x(t + (t + kT)\nu - \tau) + w_k(t) \quad (3)$$

where $0 \leq t \leq T$ denotes the time relative to the beginning of the k th chirp, where $w_k(t)$ is measurement noise. To obtain the *beat signal* at the intermediate frequency (IF), the received signal $r_k(t)$ in (3) is *dechirped* through conjugate mixing with the transmitted signal $x(t)$ in (2)²:

$$y_k(t) = r_k(t)x^*(t) = \gamma e^{j2\pi f_c \nu(t+kT)} e^{-j2\pi \alpha \tau t} \text{rect}_T(t - \tau) + w_k(t)x^*(t). \quad (4)$$

Let τ_{\max} denote the round-trip delay (see Fig. 2) corresponding to a maximum target range of interest (i.e., $\tau_{\max} \geq \tau$), which is related to the *radar bandwidth of interest* B_s as³ $\tau_{\max} = B_s/\alpha$. After low-pass filtering the beat signal in (4) with bandwidth B_s , sampling with a period of T_s for $\tau_{\max} \leq t \leq T$, we rearrange into a slow-time-fast-time data matrix, where the k th row contains the samples of the k th chirp (fast time), while the n th column contains the n th sample of each chirp (slow time). In other words, we have

$$y_{k,n} = \gamma e^{j2\pi(-\alpha\tau + f_c\nu)nT_s} e^{j2\pi f_c \nu kT} + w_{k,n} \quad (5)$$

for $k = 0, \dots, K-1$ and $n = n_{\max}, \dots, N-1$, $n_{\max} = \lfloor \tau_{\max}/T_s \rfloor$, $N = \lfloor T/T_s \rfloor + 1$, and $w_{k,n}$ are independent and identically distributed (i.i.d.) complex Gaussian noise samples with variance σ^2 .

Stage 2: Target Range-Velocity Estimation: To provide an estimate of target range and velocity, two-dimensional (2-D) discrete Fourier transform (DFT) can be applied across slow-time and fast-time dimensions of the beat signal in (5), which yields the FMCW delay-Doppler spectrum evaluated at a given delay-Doppler pair $(\hat{\tau}, \hat{\nu})$:

$$z(\hat{\tau}, \hat{\nu}) = \sum_{k=0}^{K-1} \sum_{n=n_{\max}}^{N-1} y_{k,n} e^{j2\pi \alpha \hat{\tau} n T_s} e^{-j2\pi f_c \hat{\nu} k T}. \quad (6)$$

The periodogram $|z(\hat{\tau}, \hat{\nu})|^2$ corresponding to (6) yields a dominant target peak at $(\hat{\tau}, \hat{\nu}) = (\tau - f_c \nu / \alpha, \nu)$, which can be recovered using, for example, constant false alarm rate (CFAR) detectors [6, Ch. 6]. The peak value of $|z(\hat{\tau}, \hat{\nu})|$ is proportional to the processing gain $G_p = K(N - n_{\max})$. This frequency

²Here, we ignore the terms whose total phase progression over a coherent processing interval (CPI) of K chirps is smaller than $\pi/4$ for typical automotive FMCW settings [6, Ch. 2.6.3].

³The ADC bandwidth $B_{\text{adc}} \geq B_s$ imposes a limit on B_s , and, thus, the maximum detectable range τ_{\max} .

identification method is referred to as the *periodogram spectral estimator* [7, Ch. 2.2.1]. Here, the shift $f_c\nu/\alpha$ in delay stems from *range-Doppler coupling* inherent in the FMCW waveform [6, Ch. 4.6.4]. To compensate for the coupling effect, the Doppler-dependent term $f_c\nu/\alpha$ can be added back to the delay estimate after delay-Doppler retrieval. When there are multiple objects in the radar field of view, (6) will have multiple peaks. In order to distinguish the different objects, each object pair must be separated by a certain minimum gap in delay and Doppler domains, which is determined by the radar *resolution*: the range and velocity resolution of an FMCW radar can be derived from (6) as (assuming $n_{\max} \ll N$) $\Delta R = c/(2B)$ and $\Delta v = \lambda_c/(2KT)$, where λ_c is the carrier wavelength [7, Ch. 2.4]. Therefore, higher sweep bandwidth leads to better range resolution, while longer CPI duration means improved velocity resolution.

Stage 3: Tracking Filter: At the final stage of the signal processing chain, the delay-Doppler detections $\{(\tau_p, \nu_p)\}_{p=0}^{P-1}$ (along with the corresponding azimuth-elevation pairs in the case of multiple antennas [5]) are fed to a data association and tracking filter to provide filtered three-dimensional (3-D) positions and velocities of surrounding objects. Here, P denotes the number of targets seen during one scan.

IS INTERFERENCE REALLY A PROBLEM?

In this section, we provide a theoretical analysis for the impact of interference on the radar signal processing. We start with studying a single link and then extend to a network of vehicles on a multi-lane highway, in order to assess the impact of interference as a function of the vehicle and radar density, as well as the deployment scenario. Our focus will be on direct interference from one radar to another. Indirect interference (i.e., scattered on objects) will be weaker and is ignored for conceptual simplicity.

Single Link Interference

The interfering radar employs the FMCW waveform $s_{\text{int}}(t) = \sum_{k=0}^{K-1} x_{\text{int}}(t - k\tilde{T})$ where $x_{\text{int}}(t) = e^{j2\pi(f_c t + 0.5\tilde{\alpha}t^2)} \text{rect}_{\tilde{T}}(t)$, while the victim radar utilizes the same waveform as specified in (1) and (2). Here, $\tilde{\alpha} = \tilde{B}/\tilde{T}$, \tilde{B} and \tilde{T} denote, respectively, the chirp slope, sweep bandwidth and chirp duration of the interfering radar. The samples (5) then become

$$y_{k,n} = \gamma e^{j2\pi(-\alpha\tau + f_c\nu)nT_s} e^{j2\pi f_c\nu kT} + \gamma_{\text{int}} x_{\text{int},k,n} + w_{k,n}.$$

Interference is generally much stronger than the desired back-scattered signal, as they are governed by the Friis free space propagation equation and the radar equation respectively [8]:

$$|\gamma_{\text{int}}|^2 = P \frac{G_{\text{tx}}\lambda^2}{(4\pi)^2 r^2}, \quad |\gamma|^2 = P \frac{G_{\text{tx}}\sigma\lambda^2}{(4\pi)^3 d^4}, \quad (7)$$

where r is the distance between the interferer and the victim radar, d is the distance between the radar and the target, P is the transmit power, G_{tx} is the combined transmit and receive antenna gain, σ is

the radar cross section of the target. Hence, for similar d and r and typical values of σ , $|\gamma_{\text{int}}|^2 \gg |\gamma|^2$. The nature of the interference depends on the *total interference power* (i.e., the aggregate power of the interference samples), and the *level of coherence* between victim and interfering radar [9].

The total interference power depends on the statistics of the samples $x_{\text{int},k,n}$, which is a function of the radar waveform parameters and signal delays. The samples satisfy $|x_{\text{int},k,n}|^2 \in \{0, 1\}$, depending on whether or not the interference signal at time (k, n) is in the bandwidth of interest of the victim radar. Hence, the overall power of the interference is $\mathbb{E}\{\sum_{k,n} |\gamma_{\text{int}}|^2 |x_{\text{int},k,n}|^2\} = f |\gamma_{\text{int}}|^2 G_p$, where G_p is the radar processing gain and f is the average interference probability⁴.

How this total interference power manifests itself depends on the radar parameters, and interference can be classified as coherent, incoherent, or partially coherent [10]. *Coherent interference* occurs when the interferer uses the same parameters (α, T, B) as the victim radar. In that case, the interfering radar signal leaking into the bandwidth of interest B_s of the victim radar (i.e., $f = 1$) leads to a *ghost target*, a peak in the delay-Doppler spectrum with very high power [11]. Ghost targets lead to false detections, which in turn may cause incorrect behavior of safety systems. *Incoherent interference* occurs when the samples $x_{\text{int},k,n}$ are independent random variables, due to the interferer using very different waveform parameters (e.g., different chirp pattern) so that the total interference power $f |\gamma_{\text{int}}|^2 G_p$ ends up as an increased noise floor. Noise floor increase resulting from interference can lead to more severe degradation in detection performance than an equivalent increase in thermal noise floor due to the side-lobes of the interference spectrum [10]. In between these two extreme cases, a slight mismatch in chirp slope or chirp duration or in the presence of phase noise (*partially coherent interference*) causes the energy of the ghost target peak (which occurs due to coherent interference) to spread over the delay-Doppler domain.

To illustrate how a ghost target is spread out depending on the relative waveform parameters, Fig. 3 shows the fast time FFT output, i.e., the range FFT, corresponding to an interfering radar signal as a function of distance. The larger the difference in the chirp slope, the more the interference is spread out, due to the decrease in coherence. This affects the detection of targets in various ways. Incoherent interference may hinder the detection of low RCS targets (pedestrians, cyclists) over a large fraction of the delay-Doppler domain, whereas a (partially) coherent interference can mask even high RCS targets (vehicles) but in a smaller fraction of the delay-Doppler domain.

In practice, oscillators in FMCW radars do not have an ideal, impulse-like radio-frequency (RF) spec-

⁴ For *incoherent* or *partially coherent interference*, where the interference manifests itself as a noise floor, the overall interference power (or, equivalently, average signal-to-interference-plus-noise ratio (SINR)) is a reasonable performance metric, while for fully *coherent interference*, percentiles are more meaningful.

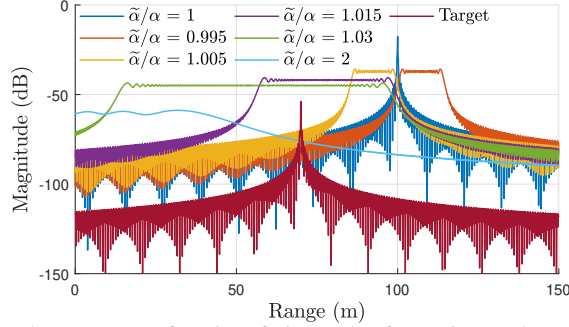


Fig. 3. FMCW range profiles in the presence of an interfering radar for various values of chirp slope ratios, where $\tilde{\alpha}$ and α represent the chirp slopes of the interfering radar and the victim radar, respectively. The victim radar waveform parameters are $f_c = 77$ GHz, $B = 1$ GHz, $T = 20 \mu\text{s}$. The interfering radar has identical chirp duration $\tilde{T} = 20 \mu\text{s}$, but has a varying sweep bandwidth \tilde{B} (thus, $\tilde{\alpha}$). The interference signal has a one-way propagation delay τ_{int} corresponding to a range of $R_{\text{int}} = 100$ m, while the desired target is located at $R = 70$ m. Due to increased noise floor, the target may not be detected depending on its range and the chirp slope mismatch between the victim and interfering radars.

trum due to phase and frequency instabilities [12], [13]. In Fig. 4, we demonstrate the effect of oscillator *phase noise* on the averaged range response⁵ of a victim FMCW radar when the oscillators of both the victim and interfering radars are subject to phase noise processes with parameters $L_p = -70$ dBc/Hz (pedestal height) at $W_p = 200$ kHz (pedestal width) [13]. As observed from the figure, the oscillator phase noise induces spectral smearing of target and interference profiles, thereby causing loss of details in the spectrum, which deteriorates detection performance and leads to masking of weak targets.

Network Interference

The above interference analysis can be extended to a complete network, for instance on a multi-lane road, by employing a stochastic geometry approach [8]. As shown in Fig. 5, consider a victim radar surrounded by L lanes of traffic, with lane separation R , each modeled as a one-dimensional Poisson point process (PPP) $\Phi(\mathbf{x})$ with intensity $1/\Delta$ (so Δ is the expected distance between vehicles and \mathbf{x} is a vehicle location along a road) [3]. Radars (here one per side of the vehicle) are incoherent and can have different chirp durations, but otherwise share the same bandwidth B , duty cycle $u \in [0, 1]$ (i.e., the fraction of time the radar is transmitting), and field of view.⁶ The expected value of the interference

⁵Range spectra are derived by computing the range FFTs of signal and interference powers averaged over the randomness of phase noise, which is modeled as a zero-mean wide sense stationary (WSS) random process under the assumption of white frequency modulated (FM) phase noise in the oscillator [14, Sec. V].

⁶We recall that for antennas with narrow field of view (FOV), the antenna gain is $G \approx 4\pi/(\phi\theta)$, where ϕ is the beam-width in the elevation domain and θ the beam-width in the azimuth domain. This means that a radar with 1 degree elevation beam-width and 30 degrees azimuth beam-width will have a gain of approximately 31.3 dBi.

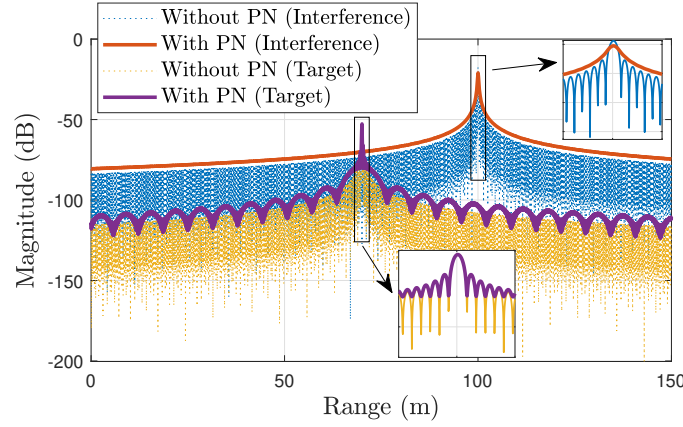


Fig. 4. Range profiles of a victim FMCW radar in the presence of an interfering radar with identical chirp parameters (coherent interference), where both radars' oscillators have phase noise (PN) processes (the profiles without PN are also shown for comparison). The same parameters as in Fig. 3 are used with $\tilde{\alpha}/\alpha = 1$. Perfect range decorrelation of the interfering signal with the victim radar signal (due to independent phase noise processes at the victim and interfering radars) makes the spectral smearing effect more pronounced in the interference profile than in the target profile [15].

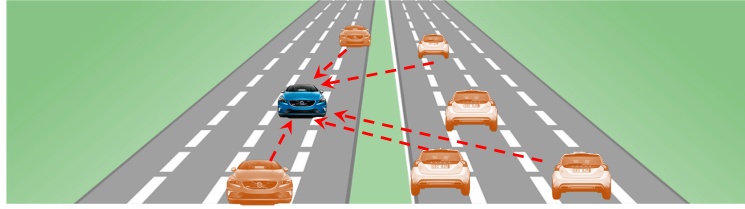


Fig. 5. Example of network interference in a six-lane highway. Interference from interfering radars is aggregated and depends on the properties of the individual radars as well as the placement of vehicles on the road.

probability f is easily found to be⁷ $f = u\alpha\tau_{\max}/B$. Hence, the aggregate interference seen by the victim radar due to interference from lane $\ell \in \mathbb{Z}$ (indexed with reference to the victim radar) is

$$I_p(\ell) = \sum_{\mathbf{x} \in \Phi(\mathbf{x}) \cap \mathbf{x} \in \text{FOV}} P f \frac{G_{\text{trx}} \lambda^2}{(4\pi)^2 r^2(\mathbf{x})}, \quad (8)$$

where $r(\mathbf{x}) = \sqrt{\ell^2 R^2 + x^2}$, where x is the 1-dimensional position along the road, ranging from $\frac{\ell R}{\tan \theta_p/2}$ to $+\infty$. Here, θ_p is the minimum of the forward and backward field of view. Hence (with slight abuse of notation), the interference averaged over the locations of the interferers is

$$\mathbb{E}\{I_p(\ell)\} = P \frac{G_{\text{trx}} \lambda^2}{(4\pi)^2} \frac{f}{\Delta} \int_{\frac{\ell R}{\tan \theta_p/2}}^{+\infty} \frac{1}{\ell^2 R^2 + x^2} dx = P \frac{G_{\text{trx}} \lambda^2}{(4\pi)^2} \frac{f}{\Delta} \frac{1}{\ell R} \frac{\theta_p}{2}, \quad (9)$$

⁷Here we made use of the following asymptotic results. When $\tilde{\alpha} = \alpha$ then the probability of interference is uB_s/B and the interference lasts an entire chirp duration. When $\tilde{\alpha} \ll \alpha$, then the probability of interference is u and the duration is $\tilde{\alpha}\tau_{\max}/(\alpha - \tilde{\alpha})$. When $\tilde{\alpha} \gg \alpha$, then there are $\tilde{\alpha}/\alpha$ simultaneous interferers, each lasting for a duration $\alpha\tau_{\max}/(\tilde{\alpha} - \alpha)$.

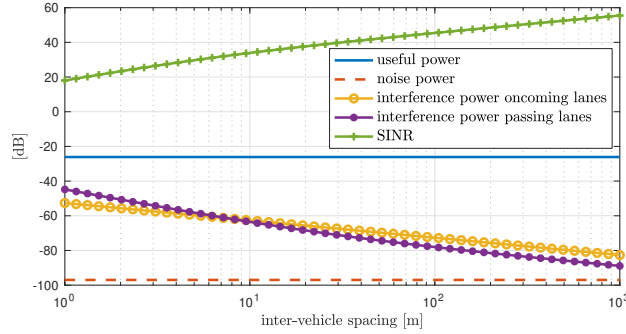


Fig. 6. Incoherent network interference in a 6-lane highway as a function of the average vehicle spacing. The distance to the target is 150 m, 10 μ s chirp time, $\sigma = 10 \text{ m}^2$, 10 dBm transmit power, 1 GHz bandwidth, $T = 30 \text{ } \mu$ s, 150 m maximum range, 50 MHz ADC bandwidth, 10 dBm transmit power (same for front-end and back-end), 30 degree FOV in forward direction, 90 degree in backward direction, 20 % duty cycle, 100 μ s frame duration.

while for $\ell = 0$, $r(\mathbf{x}) = x$, where we need a certain safety margin to avoid singularities, we set x from Δ to $+\infty$, leading to $I_p(\ell = 0) = P \frac{G_{\text{tx}} \lambda^2}{(4\pi)^2} f \frac{1}{\Delta^2}$. An example of network interference of a six-lane highway is shown in Fig. 6, as a function of the average inter-vehicle spacing Δ for a vehicle target 150 meters away with RCS of 10 m^2 . The analytical result shows the impact of interference of nearby vehicles, leading to orders of magnitude reduction of the SINR. For small Δ , interference is larger from passing lanes, while for large Δ , oncoming traffic dominates. We also observe that even though interference power can be large, the factor f reduces its impact significantly. In the example $f \approx 0.01$, leading to 20 dB reduction in interference. In this example, the target can be detected in spite of the incoherent network interference, while a pedestrian target with smaller RCS (such as $0.1 - 1 \text{ m}^2$) further away than 50 m would be hard to detect.

Intermediate Conclusion

From the above analyses, we found that interference can manifest itself in different ways, and can increase both missed detections and false alarms. Due to the nature of the FMCW signals, there is a natural robustness to interference. Both the total received interference power and the mutual coherence between victim and interfering radar play an important role. As a rule of thumb, the signal-to-interference ratio (SIR) for a target at distance d due to power transferred by an interferer at distance r to a victim radar can be determined as follows. The useful signal power (the peak of the periodogram) and the interference power are

$$S = |\gamma|^2 G_p^2, \quad I \leq f |\gamma_{\text{int}}|^2 G_p G_I, \quad (10)$$

where $G_I \in [1, G_p]$ depending on the level of coherence of the interference⁸ (i.e., $G_I = 1$ for incoherent interference, $G_I = G_p$ for coherent interference). Hence,

$$\text{SIR} \geq \frac{|\gamma|^2 G_p^2}{f |\gamma_{\text{int}}|^2 G_p G_I} = \frac{\sigma r^2}{(4\pi)d^4} \frac{G_p B}{u \alpha B_s G_I}. \quad (11)$$

The first factor is out of the designer's control, while the second factor can be optimized (via the duty cycle (small u), chirp slope (small B_s/B), radar FOV (thereby reducing f), effective processing gain (increase G_p/G_I)) to make sure that the SIR is much large than 1. Our results indicate that incoherent interference leads to a significant increase in the noise floor (tens of dBs), so it can reduce the ability to detect weak targets. Nevertheless, for nearby targets or targets with a high RCS, the SIR margin is sufficient to allow reliable detection. When interference is partially coherent this margin drops significantly.

INTERFERENCE MITIGATION STRATEGIES

The impact of interference includes ghost targets and increases in noise floor. Both are detrimental to radar operations. Approaches to deal with interference can be grouped as either *reactive*, which aim to reduce the impact of interference after it has occurred, or *proactive*, which aims to avoid or reduce interference by design. We will describe various reactive strategies as well as three such proactive strategies: quasi-orthogonal FMCW waveforms; low-rate data communication between radar transmitters; an OFDM radar approach. All these approaches lead to high interference suppression, with limited impact on radar performance. In addition, the OFDM radar approach can enable high-rate communication links between vehicles.

Standard (Reactive) Approaches

Extensive studies were conducted in the context of the EU MOSARIM project, where a broad range of time-domain or frequency-domain signal processing techniques were proposed to mitigate FMCW and pulsed radar interference. These techniques are capable of deleting instantaneous interference that exists for a limited time or bandlimited interference that pollutes a specific portion of the whole radar band; while no solution is offered for the worst case recurring or wideband interference [1]. The current attitude toward interference mitigation in the industry focuses on various techniques, including pulse to pulse processing and removing polluted pulses, sniffing and avoiding used frequencies, using frequency diversity, using narrow main beams or side-lobe null steering [3]. These techniques are generally reactive

⁸Level of coherence can be characterized through signal-to-interference mitigation gain, which is a function of FMCW waveform parameters of victim and interfering radars [10], [16].

strategies, which focus on getting rid of interference after it occurred, making it infeasible for highly-dynamic VANETs which require ultra-low latencies. Other reactive strategies exploit sparsity of useful signal and interference components in different transform domains, namely, the DFT and short-time Fourier transform (STFT) domains, respectively, to extract the desired signal component [17] or solve a sparse recovery problem to reconstruct the intervals in the range spectrum spoiled by interference [18], which belongs to a general class of time-domain excision approaches [19]. Such strategies can retain the desired target response while eliminating the interference, however, at the cost of losing information and introducing artifacts [19]. Besides these reactive strategies, there exist also cognitive approaches that utilize idle time-frequency resources for FMCW transmission via slope and bandwidth adaptation [20]. Interference avoidance techniques can also be more invasive, such as notifying the driver, disabling the sensor feature, shifting function to another sensor, reducing CFAR detection sensitivity [3]. However, these avoidance mechanisms either decrease the radar detection performance or disable the radar completely.

Quasi-Orthogonal Waveforms

Concept: From the interference analysis, we established that the interference is proportional to $f = u\alpha\tau_{\max}/B$, where u is the radar duty cycle, α is the chirp slope, τ_{\max} is the maximum target round-trip time, and B is the radar bandwidth. Hence, by decreasing the chirp slope, or, equivalently, increasing the chirp duration, interference can be mitigated. We consider a class of signals with linear chirps with the same chirp rate, a fixed frame rate and a fixed duty cycle. A chirp $x(t)$ from (2) and a delayed chirp $x(t - \Delta\tau)$, repeated with period T , have power leakage/coupling

$$C(\Delta\tau) = \left| \frac{1}{T} \int_0^T e^{j[\varphi(t) - \varphi(t - \Delta\tau)]} dt \right|^2 \leq \frac{1}{\pi^2 B^2 (\Delta\tau)^2} \quad (12)$$

for $\Delta\tau \neq 0$. Since $B\Delta\tau/T$ is the instantaneous frequency difference between the chirps, the coupling is the same as two sinusoids with frequency difference $B\Delta\tau/T$. Hence, we say that these waveforms are *quasi-orthogonal*. As $\Delta\tau$ was arbitrary, this property is maintained under random starting and arrival times of FMCW waveforms. From (12), it is possible to derive the number of signals N that cause acceptable interference, i.e., smaller than the power backscattered from a typical target. Suppose the chirp duration T is divided into N segments of duration $\Delta\tau$, so $\Delta\tau = T/N$, then, using (7):

$$P \frac{G\sigma\lambda^2}{(4\pi)^3 d^4} \geq PC(\Delta\tau) \frac{G\lambda^2}{(4\pi)^2 r^2} = P \frac{N^2}{(\pi BT)^2} \frac{G\lambda^2}{(4\pi)^2 r^2} \Rightarrow N \leq TB \frac{\sqrt{\sigma}}{r}$$

if r and d take on similar values. For $r = 500$ m, $B = 1$ GHz, $\sigma = 0.1$ m², using one long chirp of duration $T = 10$ ms leads to over 6,000 quasi-orthogonal waveforms (compared to 12 for a conventional chirp with $T = 20$ μ s). The challenges of retrieving velocity and range data as well as physically realizing such a radar is now briefly described.

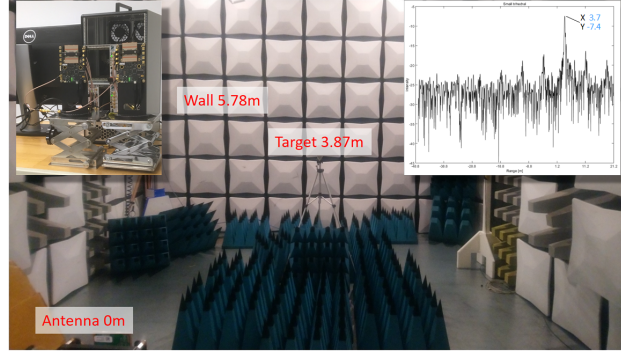


Fig. 7. Radar test setup in anechoic chamber with a trihedral target seen from the radar position. Upper left inset shows experimental radar demonstrator, upper right inset shows a typical acquired range profile.

Signal Processing: While in (5) speed and range appear in an ambiguous combination in a single chirp, this expression is only an approximate representation of Doppler shift, as we neglected several constants and small terms, which are negligible for small T . For long chirps, these neglected values should be considered, so that the range speed ambiguity can be resolved within a single chirp. Formally,

$$y(t) = r(t)x^*(t) = \tilde{\gamma} e^{j2\pi f_c \nu t} e^{-j2\pi \alpha \tau t} \text{rect}_T(t - \tau) e^{j\varphi_0} e^{j2\pi t^2 \nu \alpha} + w(t)x^*(t) \quad (13)$$

where $r(t) = r_0(t)$ with $r_k(t)$ being defined in (3), $\tilde{\gamma}$ is a real quantity denoting the target reflectivity, and $\varphi_0 = \pi \alpha \tau (\tau - 2f_c/\alpha)$ is an absolute phase. The Fourier transform $Y(f)$ of $y(t)$ will have a maximum at $f^* = f_c \nu - \alpha \tau$, with

$$Y(f^*) = \tilde{\gamma} e^{j\varphi_0} \int_0^T e^{j2\pi t^2 \nu \alpha} dt. \quad (14)$$

Hence, finding the maximum of $|Y(f)|^2$ yields an estimate of $f_c \nu - \alpha \tau$, which allows us to write $\varphi_0 = \pi \frac{f_c \nu - f^*}{\alpha} (f_c(\nu - 2) - f^*)$. We can then invert the expression (14) to solve for $\nu = 2v/c$. The solution has to be found numerically, making use of the fact that the target reflectivity $\tilde{\gamma}$ is real and positive and that the complex angle of the integral increases monotonically with velocity within a significant velocity span.

Comparing the outlined approach to that of the slow/fast time FMCW radar case above, note the principal difference that presently velocity is determined by measuring complex amplitude. For pulse-Doppler radar, velocity is found by locating the target peak in the Doppler spectrum. The present approach assumes that just one target is present for any beat frequency whereas pulse-Doppler radar may handle several targets within the same range/Doppler resolution cell. On the other hand the attained beat frequency resolution is refined in proportion to the prolonged sweep. In effect both methods exhibit the same low probability that two separate targets should be superimposed the same resolution bin. The single slow sweep method for obtaining nearly orthogonal waveforms contains a further challenge compared to

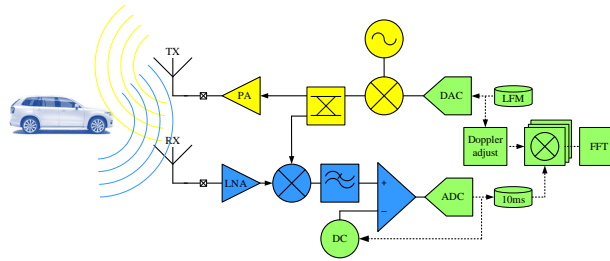


Fig. 8. Simplified scheme of a single slow sweep FMCW radar allowing large numbers of orthogonal signals. The LFM waveform is obtained digitally at baseband and is upconverted in the analog domain. This upconverted signal is mixed with the receive signal yielding downconversion to a signal with bandwidth essentially set by 50 MHz. The dominant power in the downconverted signal will come from transmit signal which however appears as a DC component. This is removed by a DC canceller stage after which the signal is digitized. The canceller operates on the principle of minimizing at ADC output at some rate much slower than the sweep time and has the vital function of avoiding ADC saturation. In the digital domain further mixing with Doppler offsets may be required to cover a very wide range of target speeds.

pulse-Doppler radar, apart from the novel signal processing required. Indeed the steep ramps of pulse-Doppler FMCW frequency offsets the target response as compared to the transmit signal. Leakage between transmitter and receiver will manifest itself at the mixer output as a high amplitude low frequency peak. In a typical FMCW radar, this unwanted response is removed by a configurable analogue electronic filter. However, implementation of analogue high pass filters with very low cut-off frequencies on chip level is not feasible. Presently, the radar is based on subtraction of leakage, appearing as DC component, with a feedback loop rather than filtering with respect to range and Doppler frequency offsets. The conceived radar scheme in Fig. 8 indicates that (14) can be slightly modified by digitally modifying the signal phase by some offset, thereby changing the unambiguous speed range for (14). To effectively cover a sufficiently large velocity span, two or three such velocity channels should be processed in parallel. The overall processing burden still remains fully reasonable.

Implications: The freedom of multiple orthogonal radar channels can be brought into practice in different ways. The considered case with a very large number of channels allows for the convenient method of simply not requiring any common scheduling of the channels adopted (apart from the several radars which may be located in the same vehicle in which case channel coordination is simple to achieve). The number of vehicles in such proximity to each other that an interference conflict is imminent will be much smaller than the number of available channels. Just selecting the radar channels randomly, chances are good that there will be no interference. In the case of interference, the individual vehicle will then randomly pick another channel and with high probability the conflict thereby is resolved.

Coordinated Transmission via Wireless Communication

Another way to mitigate interference is coordination of automotive radars through communications so that radars are assigned disjoint frequency-time-space resources, making use of the facts that (i) radars receive over a small fraction B_s/B of the available bandwidth; (ii) radars are only active a fraction u of the time; (iii) radar signals are blocked –mostly by other vehicles– and limited by the field of view. The assignment requires coordination for allocation of frequency-time resources through distributed network communication. Such communication can be achieved either via a dedicated technology, such as 802.11p or cellular V2X (C-V2X) communication. Alternatively, one can exploit the similarity of the radar circuitry to standard communication hardware, and upgrade automotive radars to joint radar communication units (RCU), which use the same hardware for both radar and communications and are composed of data link and physical layers. The radar and communication functionality are time-multiplexed, where communication occurs over a fixed and dedicated communication bandwidth (with bandwidth limited by the ADC), which is free of radar transmissions. The time-multiplexing is possible because of the idle period. Hence, when $u \approx 1$, RCUs cannot be used and 802.11p or C-V2X are more appropriate. Nevertheless, we will consider here the RCU approach, as it is readily modified when using another dedicated communication technology. As is typical in VANETs, communication is unacknowledged with a distributed MAC based carrier sense multiple access (CSMA). The goal of the communication is to assign radars to time slots, so that different radars remain quasi-orthogonal. In contrast to the long chirps described previously, we consider standard short chirps, thus limiting the number of transmissions per chirp period. The frequency-time resources are shared as illustrated in Fig. 9 for three RCUs r_i , r_j and r_k . The basic principle is as follows. Each vehicle initially assigns starting times to the automotive RCUs mounted on this vehicle through a central processor. These are broadcast to neighbouring vehicles during a communication slot. All RCUs on a vehicle broadcast short control communication packets at the same time over the communication band. The broadcast communication packet includes information about the starting times used by all RCUs on that vehicle. Other RCUs or vehicles, which receive this information, store this information in a database and allocate themselves non-overlapping starting times based on the stored information. A priority index is used to prioritize the dissemination of the resource allocation of a larger group of vehicles in order to avoid fluctuations in the distributed VANET.

A practical implementation requires synchronization among radars, which can be achieved through GPS or via a dedicated synchronization protocol. With reasonable synchronization requirements (around 1–2 μ s error), [21] demonstrated significant reductions in radar interference within a few tens of ms.

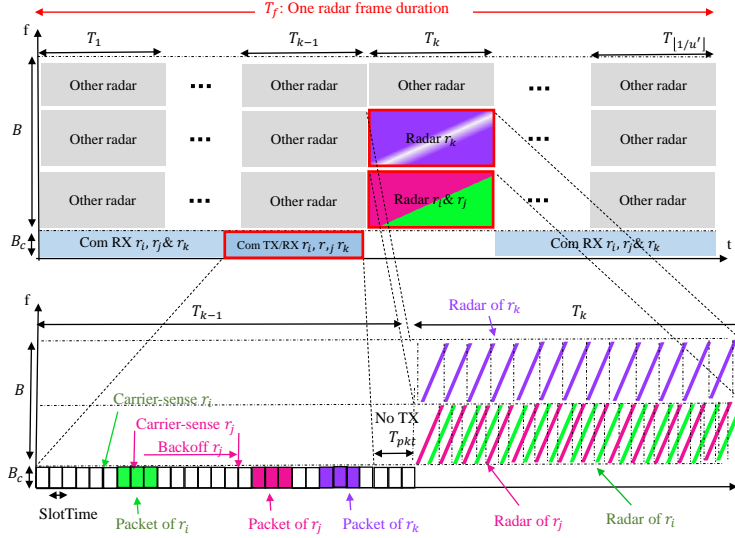


Fig. 9. An example showing the sharing of frequency-time resources by three radar communication units r_i , r_j and r_k . The whole bandwidth is divided into a communication channel of bandwidth B_c and sweep bandwidth B , where various types of automotive radars might use portions of B . One radar frame T_f is divided into time slots T_k , $1 \leq k \leq \lfloor 1/u' \rfloor$, where $u' = (N+1)T/T_f$ is the modified radar duty cycle. The radar frame is divided into time slots, where radar transmission/reception takes place in T_k , communication transmission is done prior to radar at T_{k-1} and reception at anytime except T_k . Each RCU broadcasts its packet over the communication channel through CSMA, which includes the starting time and frequency band information of its radar transmission. In this example interference is resolved because r_i and r_j are allocated to quasi-orthogonal time slots, whereas r_k is allocated to a different frequency band. Any conflicts in frequency-time resource sharing that occur in one frame T_f are resolved in the following frames.

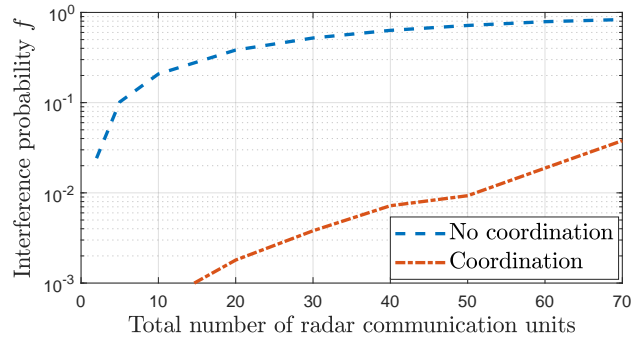


Fig. 10. Radar interference probability f after one frame time (20ms) with coordinated transmission for varying number of radars for 10,000 Monte-Carlo simulations, $B = 1$ GHz, $B_s = 50$ MHz, $T = 20\mu s$, $f_c = 79$ GHz, $K = 99$.

Fig. 10 shows the interference probability (i.e., the expected value of f) as a function of the number of interfering radars, with and without coordination. The potential of such protocols to adapt radar signals according to changing traffic conditions via communications offers intelligent radar sensing strategies, such as cooperative localization, disabling unnecessary sensing, etc.

Joint Radar and Communication

A third, more forward looking alternative is to exploit the fact that radar and communication systems operate in similar frequencies, and develop a system that can perform the dual role of radar and communication [22], coined RadCom. Both pilot and data from the transmitted signal can be exploited for radar functions when processing the backscattered communication signal. A prominent candidate for this is OFDM, which is the de facto waveform for all cellular and wifi-based standards, due to its flexibility and robustness to wireless propagation effects. OFDM has also been studied extensively as a radar waveform⁹ [24]–[28], but is limited by the ADC bandwidth, which is generally orders of magnitude smaller than the radar bandwidth, which in turn limits radar resolution. A way around this problem is the use of *Stepped-Frequency OFDM*, which involves consecutive OFDM frames, each transmitted with a different carrier frequency [29], [30]. The main rationale behind the use of stepped-frequency OFDM as a RadCom waveform is to surpass the range resolution limitation of conventional OFDM radar (which is imposed by ADC bandwidth) via frequency hopping across individual OFDM frames with low baseband bandwidth [30], while maintaining standard wideband OFDM as a special case. Fig. 11(a) illustrates an exemplary time-frequency plot of a stepped-frequency OFDM waveform. To avoid interference, different vehicles are assigned orthogonal resources, as shown for 3 vehicles. Hence, the stepped-frequency OFDM can exploit high resolution offered by the *large total bandwidth* $MN\Delta f$ by joint processing of M individual OFDM frames on different carriers while simultaneously requiring a low-rate ADC to sample *small baseband bandwidth* ($N\Delta f$) OFDM blocks. For each carrier L OFDM symbols of duration T_{sym} are sent, constituting a frame. The choice of N , M , L , Δf , and the hopping pattern provides flexibility in the RadCom waveform, and enables us to provide radar performance similar to an equivalent wideband OFDM radar, but with low-rate, low-cost ADCs [30].

Signal Processing and Resource Allocation: Under standard assumptions (cyclic prefix longer than τ [26], [28] and small Doppler approximation [24]), the received symbol on the n th subcarrier for the ℓ th symbol of the m th frame can be written as (considering the same radar environment with a single target as specified in (3)) [30]

$$y_{m,\ell,n} = \gamma x_{m,\ell,n} e^{-j2\pi(f_m+n\Delta f)\tau} e^{j2\pi f_0(mL+\ell+1)T_{\text{sym}}\nu} + w_{m,\ell,n} \quad (15)$$

where $x_{m,\ell,n}$ denotes the complex data or pilot symbol, γ is the complex channel gain and $w_{m,\ell,n}$ is the additive noise term with variance σ^2 . Delay estimation can be performed by matched filtering the

⁹Under the assumption of high FMCW chirp slope, OFDM and FMCW radars with identical waveform parameters exhibit similar performance in terms of accuracy and resolution [23]. OFDM provides the additional capability of communications at the expense of increased hardware complexity due to OFDM modulator/demodulator operations [23].

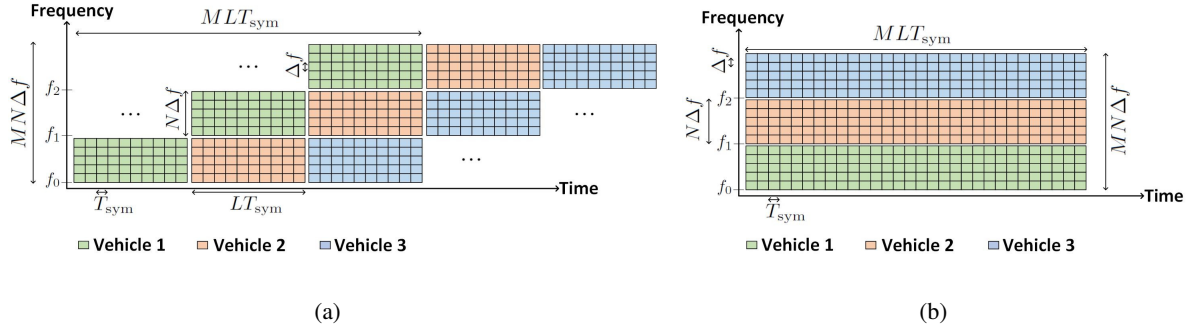


Fig. 11. Time-frequency resource coordination in a joint radar communications vehicular network for (a) stepped-frequency OFDM and (b) narrowband OFDM.

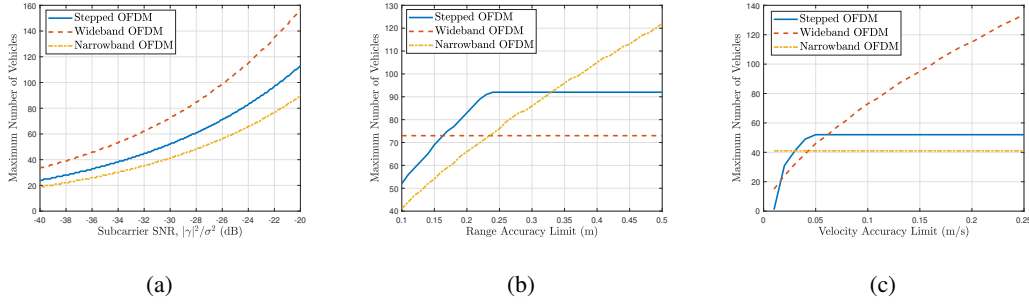


Fig. 12. Maximum number of vehicles that can be accommodated within a time-frequency resource defined by $B_{\text{tot}} = 1$ GHz and $T_{\text{tot}} = 30$ ms for the three different OFDM waveforms, where $f_0 = 77$ GHz, $\Delta f = 500$ KHz, $T_{\text{cp}} = 400$ ns. Stepped OFDM and narrowband OFDM schemes require an ADC with 50 MHz rate, whereas wideband OFDM requires 1 GHz-rate ADC. (a) With respect to subcarrier SNR, where range and velocity accuracy limits are 0.1 m and 0.1 m/s, respectively. (b) With respect to range accuracy limit, where subcarrier SNR is -30 dB and velocity accuracy limit is 0.1 m/s. (c) With respect to velocity accuracy limit, where subcarrier SNR is -30 dB and range accuracy limit is 0.1 m.

data cube $y_{m,\ell,n}$ across frame-frequency dimensions (m and n directions), while processing along frame-time dimensions (m and ℓ directions) can provide an estimate of Doppler. Frequency hopping across consecutive OFDM frames introduces *delay-Doppler coupling*, which can be overcome by incorporating phase correction terms in the DFT implementation of matched filtering [30].

Time-frequency resource allocation scheme coordinated by a central unit (e.g., a 5G base station) helps to alleviate mutual interference among radars on different vehicles, similar to conventional OFDM radar networks [26, Ch. 4]. Resources can be assigned to maximize the number of vehicles that can be fit into a given time-frequency block such that each vehicle meets preset radar accuracy requirements¹⁰. Fig. 12 shows exemplary results for the three different OFDM schemes (stepped-frequency, narrowband, and wideband, where in the latter case each vehicle uses the total bandwidth (and thus requires an ADC with 1 GHz sampling rate) for a duration LT_{sym} and then remains silent for a duration $(M - 1)LT_{\text{sym}}$). As

¹⁰To characterize radar accuracy, we employ the Cramér-Rao bound (CRB) [26] on variances of unbiased estimates of delay and Doppler parameters using the signal model in (15).

seen from the figures, the stepped-frequency OFDM radar can support more vehicles in a given spectral resource than the conventional narrowband OFDM radar with the same hardware requirements since the former offers the flexibility to trade off a decrease in Doppler accuracy for an improvement in ranging accuracy (frequency hopping increases ranging accuracy and reduces Doppler accuracy). In Fig. 12(b), as wideband OFDM is essentially limited by the velocity accuracy constraint, relaxing the range accuracy constraint does not further improve its performance (similarly, for narrowband OFDM in Fig. 12(c)).

As a final remark, we note that the stepped OFDM provides a design trade-off between the narrowband and wideband OFDM schemes, retaining the improved resolution and accuracy properties of the wideband OFDM with much reduced hardware requirements as in the case of narrowband OFDM.

OUTLOOK AND CHALLENGES

In this section, we consider the main research and development challenges for the coming years. For communication-based interference mitigation strategies, the coexistence between radar and communication signals is an important challenge. For joint radar and communication signals, there is a potential of a revolution of cellular-type signals (e.g., 5G NR) to be reused for radar purposes [22], opening exciting synergies and avoiding the need for dedicated RF hardware all-together. The extended frequency bands made available for 5G are interesting by themselves due to the possible improvement in radar resolution, which, together with the already standardized orthogonal signaling, establishes an exciting area for automotive sensing. The main challenge is to find solutions that will enable radar and communication functionalities with such a low information latency that vehicle safety is not compromised in any traffic scenario. These solutions should include techniques for a fair distribution of the available time and frequency space for all users. It must also secure a low data loss for both radar and communication which, of course, is the aim of minimizing the possibility of interference.

For the generation and detection of slow chirps, new hardware architectures will be needed. It will push a migration from analog towards digital electronics and signal processing, which will pave the way for technologies such as imaging radar. The other modulation waveforms proposed in this paper will also require hardware that differs from the current radar designs. The analog to digital, and vice versa, conversion will be close to the RF front end making more complex digitally generated and filtered waveforms possible. To push this development forward, we will implement a demonstrator platform, complete with millimeter wave front ends, high speed digital signal generation and signal acquisition, and independent generation of arbitrary interference. The outlined methods in this paper will be tested and evaluated on the demonstrator platform in a realistic environment. The intention is to use this demonstrator (see Fig. 7) to verify the theoretical analysis regarding interference probability and SINR for different types of modulation and verify the speed measurement method for the slow ramp modulation.

Further development would include the integration of critical electronic components in CMOS technology, to ensure that a complete solution is feasible to implement in commercial scale. Advanced CMOS technologies can also facilitate the implementation of alternative waveforms on automotive radars, such as phase modulated continuous wave (PMCW). Compared to the widely used FMCW radar, the PMCW waveform has the major disadvantage of requiring very high-rate ADCs to sample wideband code sequences. On the other hand, it possesses several advantages making it attractive for future deployments, including improved robustness to interference via proper code design, not requiring a highly linear frequency ramp synthesizer, and inherent applicability to MIMO radar configurations through code orthogonality across multiple antennas. From the perspective of radar interference mitigation and radar communications convergence, we expect that the main focus of the automotive industry in the coming years will be on the cost and integration of both analog and digital functions on the same silicon chip to reduce the likelihood of hardware failure.

Vehicle radars can also be expected to operate in higher frequency bands, 100–300 GHz, to enable more bandwidth, cost reduction and miniaturization of the hardware. It is possible to influence the regulators to include some level of standardization in automotive radars, which is needed for mitigation of interference among different automobile brands [3], before new frequency spectrum is made available in the higher RF bands. Hence, it is timely to conduct research and discuss the development challenges about automotive radar interference before it becomes a problem.

REFERENCES

- [1] I. M. Kunert, “Project final report, MOSARIM: More safety for all by radar interference mitigation,” 2012. [Online]. Available: <http://cordis.europa.eu/docs/projects/cnect/1/248231/080/deliverables/001-D611finalreportfinal.pdf>
- [2] H. Meinel and J. Dickmann, “Automotive radar: From its origin to future directions,” *Microwave Journal*, vol. vol.56, pp. 24–40, 09 2013.
- [3] W. Buller, B. Wilson, J. Garbarino, J. Kelly, N. Subotic, B. Thelen, and B. Belzowski, “Radar congestion study,” (Report No. DOT HS 812 632). Washington, DC: National Highway Traffic Safety Administration, Tech. Rep., Sep. 2018.
- [4] J. Moss and A. Lefevre, “Radar interference suppression,” 2019-05-29 (pub), patent Application EP 3 489 710.
- [5] S. M. Patole, M. Torlak, D. Wang, and M. Ali, “Automotive radars: A review of signal processing techniques,” *IEEE Signal Processing Magazine*, vol. 34, no. 2, pp. 22–35, 2017.
- [6] M. A. Richards, *Fundamentals of Radar Signal Processing*. Tata McGraw-Hill Education, 2005.
- [7] P. Stoica, R. L. Moses *et al.*, *Spectral analysis of signals*. Pearson Prentice Hall Upper Saddle River, NJ, 2005.
- [8] A. Al-Hourani, R. J. Evans, S. Kandeepan, B. Moran, and H. Eltom, “Stochastic geometry methods for modeling automotive radar interference,” *IEEE Transactions on Intelligent Transportation Systems*, vol. 19, no. 2, pp. 333–344, 2017.
- [9] M. Goppelt, H.-L. Blöcher, and W. Menzel, “Automotive radar—investigation of mutual interference mechanisms,” *Advances in Radio Science*, vol. 8, no. B. 3, pp. 55–60, 2010.
- [10] G. Kim, J. Mun, and J. Lee, “A peer-to-peer interference analysis for automotive chirp sequence radars,” *IEEE Transactions on Vehicular Technology*, vol. 67, no. 9, pp. 8110–8117, Sep. 2018.

- [11] M. Goppelt, H. Blöcher, and W. Menzel, "Analytical investigation of mutual interference between automotive FMCW radar sensors," in *2011 German Microwave Conference*, March 2011, pp. 1–4.
- [12] M. Gerstmair, A. Melzer, A. Onic, and M. Huemer, "On the safe road toward autonomous driving: Phase noise monitoring in radar sensors for functional safety compliance," *IEEE Signal Processing Magazine*, vol. 36, no. 5, pp. 60–70, Sep. 2019.
- [13] K. Siddiq, M. K. Hobden, S. R. Pennock, and R. J. Watson, "Phase noise in FMCW radar systems," *IEEE Transactions on Aerospace and Electronic Systems*, vol. 55, no. 1, pp. 70–81, Feb 2019.
- [14] A. Chorti and M. Brookes, "A spectral model for RF oscillators with power-law phase noise," *IEEE Transactions on Circuits and Systems I: Regular Papers*, vol. 53, no. 9, pp. 1989–1999, Sep. 2006.
- [15] M. C. Budge and M. P. Burt, "Range correlation effects in radars," in *The Record of the 1993 IEEE National Radar Conference*, April 1993, pp. 212–216.
- [16] T. Schipper, M. Harter, T. Mahler, O. Kern, and T. Zwick, "Discussion of the operating range of frequency modulated radars in the presence of interference," *International Journal of Microwave and Wireless Technologies*, vol. 6, no. 3-4, p. 371–378, 2014.
- [17] F. Uysal, "Synchronous and asynchronous radar interference mitigation," *IEEE Access*, vol. 7, pp. 5846–5852, 2019.
- [18] J. Bechter, F. Roos, M. Rahman, and C. Waldschmidt, "Automotive radar interference mitigation using a sparse sampling approach," in *2017 European Radar Conference (EURAD)*, Oct 2017, pp. 90–93.
- [19] S. Alland, W. Stark, M. Ali, and M. Hegde, "Interference in automotive radar systems: Characteristics, mitigation techniques, and current and future research," *IEEE Signal Processing Magazine*, vol. 36, no. 5, pp. 45–59, Sep. 2019.
- [20] Z. Slavik and K. V. Mishra, "Cognitive interference mitigation in automotive radars," in *2019 IEEE Radar Conference (RadarConf)*, April 2019, pp. 1–6.
- [21] C. Aydogdu, M. F. Keskin, N. Garcia, H. Wymeersch, and D. W. Bliss, "RadChat: Spectrum sharing for automotive radar interference mitigation," *IEEE Transactions on Intelligent Transportation Systems*, accepted for publication, 2019.
- [22] F. Liu, C. Masouros, A. Petropulu, H. Griffiths, and L. Hanzo, "Joint radar and communication design: Applications, state-of-the-art, and the road ahead," Jun 2019. [Online]. Available: <https://arxiv.org/abs/1906.00789>
- [23] J. Fink and F. K. Jondral, "Comparison of OFDM radar and chirp sequence radar," in *2015 16th International Radar Symposium (IRS)*. IEEE, 2015, pp. 315–320.
- [24] C. R. Berger, B. Demissie, J. Heckenbach, P. Willett, and S. Zhou, "Signal processing for passive radar using OFDM waveforms," *IEEE Journal of Selected Topics in Signal Processing*, vol. 4, no. 1, pp. 226–238, 2010.
- [25] C. Sturm and W. Wiesbeck, "Waveform design and signal processing aspects for fusion of wireless communications and radar sensing," *Proceedings of the IEEE*, vol. 99, no. 7, pp. 1236–1259, July 2011.
- [26] M. Braun, "OFDM radar algorithms in mobile communication networks," *Karlsruher Institutes für Technologie*, 2014.
- [27] G. Hakobyan and B. Yang, "High-performance automotive radar: A review of signal processing algorithms and modulation schemes," *IEEE Signal Processing Magazine*, vol. 36, no. 5, pp. 32–44, Sep. 2019.
- [28] K. V. Mishra, M. R. Bhavani Shankar, V. Koivunen, B. Ottersten, and S. A. Vorobyov, "Toward millimeter-wave joint radar communications: A signal processing perspective," *IEEE Signal Processing Magazine*, vol. 36, no. 5, pp. 100–114, Sep. 2019.
- [29] G. Lellouch, A. K. Mishra, and M. Inggs, "Stepped OFDM radar technique to resolve range and doppler simultaneously," *IEEE Transactions on Aerospace and Electronic Systems*, vol. 51, no. 2, pp. 937–950, April 2015.
- [30] B. Schweizer, C. Knill, D. Schindler, and C. Waldschmidt, "Stepped-carrier OFDM-radar processing scheme to retrieve high-resolution range-velocity profile at low sampling rate," *IEEE Transactions on Microwave Theory and Techniques*, vol. 66, no. 3, pp. 1610–1618, March 2018.

Canan Aydogdu is a Marie Skłodowska-Curie Fellow at Chalmers, working on cross-layer multi-hop sensing system for the future energy-efficient self-driving car networks. Formerly, she was an associate professor at Izmir Institute of Technology, Turkey. She received the Ph.D. degree from Bilkent University, Turkey, in 2011.

Musa Furkan Keskin is a postdoctoral researcher at Chalmers University of Technology. He obtained the B.S., M.S., and Ph.D degrees from the Department of Electrical and Electronics Engineering, Bilkent University, Ankara, Turkey, in 2010, 2012, and 2018, respectively. His current research interests include intelligent transportation systems, radar signal processing and radar communications coexistence.

Henk Wymeersch is a professor of Communication Systems at Chalmers. He received the Ph.D. degree in 2005 from Ghent University Belgium and was a postdoctoral researcher 2005-2009 at MIT. His current research focuses on algorithm design and analysis for transportation systems.

Gisela K. Carvajal currently works on simulation and calibration of radar systems at Qamcom. Previous experience includes algorithm development for retrieval of ocean surface parameters with satellite remote sensing data, image processing and scattering analysis. She received her Ph.D. degree at Chalmers in 2013.

Karl Vanäs works as a technical expert in radar systems at Volvo Cars. He has 20 years of experience from working with radars both within the automotive industry and also from the defense industry. The last 10 years he has worked with the various radar projects at Volvo Cars. He has a MSc degree in Electrical Engineering from Chalmers University of Technology.

Olof Eriksson is a research specialist at Veoneer Sweden AB where he works on advanced electromagnetic sensor technologies, including radar systems.

Hans Herbertsson is a research project leader at Veoneer Sweden AB where he leads concept development activities with focus on electromagnetic sensor technologies. Prior to this role he has been managing microwave development activities in telecom as a product owner and product manager at Ericsson AB.

Mats Rydström received his PhD in Electrical Engineering from Chalmers University of Technology in 2008, where he worked on wireless positioning systems and signal processing for wireless communications. He is currently engaged at Veoneer Sweden AB, where he works on topics related to signal processing for future radar systems in automotive applications.

Emil Nilsson has a PhD in Electrical Engineering from Chalmers, and is currently at the School of Information Technology, Halmstad University Sweden. He also holds a position at Raytelligence AB as microwave and radar expert. Before the current positions he worked as an RFIC designer at ARM. He is currently working on cohabitant radar technologies and vital sign sensors.

Hans Hellsten has a PhD in Theoretical Physics from University of Stockholm. Before becoming a senior radar expert with Saab Surveillance, he was director of research at the Swedish Defense Research Agency FOI. Currently he shares the Saab position with an adjunct professorship at Halmstad University. Amongst other achievements he has wide range of publications ranging from books to a large number of patents. Besides radar system design his expertise lies in electromagnetic modelling and signal processing.