Adaptive Beam Tracking based on Recurrent Neural Networks for mmWave Channels

Saeid K.Dehkordi

Dept. of Information Theory Technische Universität Berlin Berlin, Germany s.khalilidehkordi@tu-berlin.de Mari Kobayashi
Institute for Communications Engineering
Technische Universität München
Munich, Germany

Munich, Germany mari.kobayashi@tum.de Giuseppe Caire

Dept. of Information Theory

Technische Universität Berlin

Berlin, Germany

caire@tu-berlin.de

Abstract—The performance of millimeter wave (mmWave) communications critically depends on the accuracy of beamforming both at base station (BS) and user terminals (UEs) due to high isotropic path-loss and channel attenuation. In high mobility environments, accurate beam alignment becomes even more challenging as the angles of the BS and each UE must be tracked reliably and continuously. In this work, focusing on the beamforming at the BS, we propose an adaptive method based on Recurrent Neural Networks (RNN) that tracks and predicts the Angle of Departure (AoD) of a given UE. Moreover, we propose a modified frame structure to reduce beam alignment overhead and hence increase the communication rate. Our numerical experiments in a highly non-linear mobility scenario show that our proposed method is able to track the AoD accurately and achieve higher communication rate compared to more traditional methods such as the particle filter.

Index Terms—mm Wave Adaptive Beam Tracking, Beam Tracking with Neural Networks

I. INTRODUCTION

Millimeter wave (mmWave) communication systems, operating in frequency bands of 30-300 GHz, are considered as a promising technology for 5G and beyond cellular systems to achieve a high data rate thanks to wide frequency bands [1]. Due to the large isotropic path loss, large antenna arrays are typically deployed at base station (BS) and/or user terminals (UEs) in order to form narrow beams between BS-UE pairs. The classical beam sweeping mechanism is highly inefficient as its complexity increases substantially with the number of antenna arrays and its practical implementation using quantized phases may limit its accuracy. Therefore, a number of low-complexity schemes for initial beam alignment have been proposed in the literature (see e.g. a compressed sensing approach in [2] and references therein). However, the existing schemes cannot be adapted directly to the high-mobility scenario, where the displacement of UEs may significantly increase the probability of beam misalignment. In such a scenario, the angle of each UE shall be estimated continuously through beam tracking methods (e.g. [3]-[6] and references therein). For example, [4]-[6] proposed variants of Kalman filter (KF) to address this problem. Since their restricted channel model together with high complexity makes these

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methods [4], [5] impractical in high mobility environments, [6] considered the use of particle filtering (PF) in a time-varying channel and demonstrated an improved performance by modeling the non-linearities of the channel compared to other KF variants. Further, [7] attempted to overcome the computational burden.

In this work, by focusing on the beamforming at the BS, we propose a beam tracking approach based on Recurrent Neural Networks (RNN) that can be applied to any arbitrary UE mobility pattern. The proposed method takes advantage of the temporal correlations within measurement data and learns the amount of *adjustment* required for the beam direction from the sequence of measurements by approaching the problem as a classification task. Based on the proposed scheme, we define a modified frame structure with variable length which can be adapted to reduce overhead. The numerical examples in a highly non uniform linear motion scenario using the Quadriga channel generator demonstrate that our proposed scheme can track the AoD accurately and achieve higher communication rate compared to the PF.

Finally, we remark that a number of recent works extensively adapted machine/deep learning for beamforming design over the mmWave channels (see e.g. [8], [9], [11]-[13]). In [11], a convolutional neural network (NN) is proposed for an optimal beamformer design. A deep learning framework was proposed for beam selection by using the channel state information (CSI) in [12], while [14] demonstrates an autoencoder/decoder architecture for robust angle estimation. Although [8], [9] also addressed beam tracking using machine learning tools, the proposed method differs from these approaches. In [8], only fully connected layers, unable to capture time correlations of input data, are considered. The work of [9] aims to infer the correct beam index by predicting (i.e. regression problem) the channel vector under the assumption of a linear motion path. More recently, the work in [10] applied a Reinforcement Learning principle for UAV beam tracking, where the authors deal with the design of the reward function by introducing thresholds for the reward. These threshold values need to be optimized depending on the operational SNR. In contrast, our model does not require any SNR specific design parameter. While a comparison of the NN based methods is an interesting topic for future work, due to the limited space, we have restricted our comparison with the well assessed and understood PF scheme.

II. SYSTEM MODEL

A. Frame Structure and Signaling Scheme

Fig. 1 illustrates the proposed frame structure consisting of two different types depending on the operating mode: (a) initialization frame and (b) secondary frame. Frame (a) is used at the initialization of the system. During initial beam alignment (BA) phase, a beam alignment takes place where the BS transmits a number of pilots to sweep the beam space. The BS receives feedback (FB) signal from the UE on the previously transmitted pilots on the uplink (UL) channel, in the *UL-FB* phase, as explained in Section II-C. During the *Data* Transmission phase, the data is transmitted in downlink (DL) channel. The final phase refers to Secondary Probing SP phase of variable length dedicated to transmit a reduced number of pilots for further channel probing. Frame (b) of length $T_{F'} < T_F$ comes into operation once a reliable connection between a BS-UE pair is established after the initialization frame (a). During the first phase UL-FB, the BS receives feedback on the previous probing (SP) from UEs. The second and third phases are identical to that of the initialization frame (a).

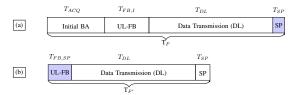


Fig. 1: Frame structures depending on operating mode. Note, the UL-FB slot at the beginning receives feedback from the previous SP.

B. Transmission Scheme and Measurement Equation

Suppose the transmitter (BS), with N_{rx} uniformly and linearly positioned elements, sends pilot symbols to the receiver receiver (UE), with N_{nx} elements over the time-varying MIMO channel at frame k by

$$\mathbf{H}_{k}(t,\tau) = \alpha_{k} \mathbf{a}_{xx}(\varphi_{k}) \mathbf{a}_{xx}^{H}(\theta_{k}) \delta(t - \tau_{k}) e^{j2\pi\nu_{k}t}$$
(1)

where α_k, τ_k, ν_k denotes the attenuation coefficient, the delay, and the Doppler shift, respectively, $\{d_i\}$ is the antenna spacing with $d_1 = 0$, λ is the wavelength, $\mathbf{a}_{rx}(\theta_k)$ is a steering vector at the Tx given by

$$\mathbf{a}_{rx}(\theta_k) = \left[e^{j\frac{2\pi}{\lambda}d_1\cos(\theta_k)}, ..., e^{j\frac{2\pi}{\lambda}d_{N_{TX}}\cos(\theta_k)}\right]^T \tag{2}$$

for the angle-of-departure (AoD) denoted by θ_k , $\mathbf{a}_{\scriptscriptstyle \mathrm{LX}}(\varphi_k)$ is defined similarly for the angle-of-arrival (AoA) denoted by φ_k . Since we consider a LoS path between the UE/BS, we have $\varphi_k = \theta_k$. The model above can be easily extended to multiple paths. The parameters $(\theta_k, \alpha_k, \tau_k, \nu_k)$ remain constant over a frame duration.

We consider the beamforming vector \mathbf{f} and the combining vector \mathbf{c} according to a predefined beam codebook. Namely, by focusing on the beamforming codebook at the BS side,

denoted by $\mathcal{CB} = \{\mathbf{f}_1, \dots, \mathbf{f}_G\}$, where we let $\mathbf{f}_i = \mathbf{f}(\tilde{\theta}_i) = \frac{1}{\sqrt{N_{rx}}}\mathbf{a}_{rx}(\tilde{\theta}_i), i \in \{1, \dots, G\}$ for some angles $\tilde{\theta}_i$. Then, the observed signal at the UE for frame k after the combining vector is given by

$$z_k(t) = \alpha_k \mathbf{c}^H(\tilde{\varphi}) \mathbf{a}_{xx}(\varphi_k) \mathbf{a}_{xx}^H(\theta_k) \mathbf{f}(\tilde{\theta}) x(t - \tau_k) e^{j2\pi\nu_k t} + \eta(t)$$
(3)

where $\eta(t) \sim \mathcal{N}(0, \sigma_n^2)$ is the additive Gaussian noise.

The objective of initial BA is to acquire an accurate AoA estimate $\tilde{\theta} \in \{\tilde{\theta}_1, \dots, \tilde{\theta}_G\}$ so that the corresponding beamforming vector $\mathbf{f}(\tilde{\theta})$ is used for the DL data transmission. We also assume that the codebooks available for UL and DL operation at the BS are identical.

C. Initial Channel State Estimation

In order to focus on tracking the UE's angular location at the BS side, we further assume that the UE is equipped with a single antenna. The UE initially listens to the channel during the initial BA period where the BS sends pilots through T probing directions according to the predefined codebook \mathcal{CB} . By replacing $\mathbf{f}(\tilde{\theta})$ with \mathbf{f}_i for $i=1,\ldots,T$ in (3) followed by suitable sampling every T_{ACQ}/T , we obtain T discrete observations or measurements, denoted by $\mathbf{z}=\{z_{\tilde{\theta}_1}[1],\ldots,z_{\tilde{\theta}_T}[T]\}$, where $z_{\tilde{\theta}_i}[i]$ is the received signal when probing in the direction $\tilde{\theta}_i$ at the i^{th} sampling instant. After this initial BA phase, the UE selects the best beam direction $\tilde{\theta}_m$ corresponding to $\max_{i=1,\ldots,T}(z_{\tilde{\theta}_i}[i])$ and feeds back \mathbf{z} to the BS during UL-FB phase.

III. BEAM TRACKING METHODS

A. Classical Beam Tracking

Beam tracking based on Bayesian statistical inference principles have been extensively investigated in literature [4]-[6]. In this subsection, we provide a brief overview of the PF technique similar to that described in [6]. The filtering problem consists of estimating the internal states in dynamical systems when partial observations are available in the presence of random perturbations. The objective is to compute the posterior distributions of the states of a Markov process, given some noisy and/or partial observations. Based on the system model described in (3) state is sequentially estimated by using the measurement $z_{\tilde{\theta}_m}[k]$ (for brevity z_k) at each time frame. Due to the nonlinear dependency between the state space and the measurements in the problem at hand, the PF is particularly well suited among Kalman filtering methods. By letting $\theta[k], z_k$ denote the state and the observation at frame k obtained from (3) after a suitable sampling¹, we model the transition of the state as $\tilde{\theta}[k] = \tilde{\theta}[k-1] + u_k$ where $u_k \sim \mathcal{N}(0, \sigma_{\tilde{\theta}}^2)$ is the process noise (i.e. perturbation). We can modify [6] by focusing on particles (beams) within a reduced region of interest of the beam space. These regions can be selected adaptively, for instance in the case of static or slow moving users, the space in proximity of the main beam direction of the previous step will have a denser distribution of particles.

¹It is also possible to consider multiple measurements for a given frame.

B. Proposed method with Recurrent Neural Networks

The particle filter discussed previously incurs increased complexity and overhead in the massive MIMO regime and in high mobility channels. In this section we consider a RNN approach for the aforementioned tracking problem by exploiting the time correlation between measurement data. Since the underlying channel parameters such as the AoD, the range, and the Doppler shift in (II-B) evolve in time with some memory, a recurrent NN architecture seems a viable solution for this problem. In recent years, Long Short-Term Memory (LSTM) networks have been used to create large recurrent networks that in turn can be used to address complicated sequence problems in machine learning and achieve state-of-the-art results. The LSTM network, is trained using backpropagation through time and overcomes the vanishing gradient problem in this way. LSTM networks have memory blocks that replace neurons which are connected through layers. A block contains gates that manage the block's state and output, thus developing a memory state for recent sequences. A block operates upon an input sequence and each gate within a block uses the sigmoid activation units to control whether they are triggered or not, making the change of state and addition of information flowing through the block conditional.

The input data sequence of interest are the observed signal values z_k at frame k. These input values referred to as input features, are used to train the network to output estimates of the UE's future AoD under a supervised learning framework. The input features of the NN are generated based on the windowed input method where features corresponding to the previous time steps are inputs to the current step. Due to the fact that the measurements in (3) are equivalent to the beam space representation of the channel at discrete angles, they can be viewed as a pseudo-spectrum. On this basis, we define our input features using a sliding window technique consisting of these values. As the initial feature set, we take the pseudo-spectrum $S \equiv \mathbf{z}$ described in section II-C and define the window length parameter L such that L bins around the current main beam direction $\hat{\theta}_m[k]$ are selected at each time step (total of L' = 2L + 1 bins, as in Fig. 2). These inputs are updated at every measurement frame. With reference to Fig. 1, the updates are made at interval $T_{SP,FB}$ which relates to the secondary probe transmitted during interval T_{SP} of the previous frame. The number of directions to be scanned during the secondary probation can be adaptively selected, leading to a trade-off between overhead and improved channel exploration. If the user has moved out of span of the current window, at the next time instance (this can happen if for example the window length is very small or that the grid points are very fine) the initial BA shall be performed by using the initialization frame (a) and the label generated for the current time frame will be the last element of the label vector (i.e. farthest from current) to minimize the distance to the next user position (note that this will only happen during inference mode). An exemplary graphical representation of this input is depicted in Fig. 3.

The labels generated for the supervised learning task consist of a hot-one-encoded vector with the same dimension as the sliding window such that the vector contains all zeros except at the position which corresponds to the next angular position (i.e. AoD) of the UE. The network outputs a value between '0' and '1' for each position in the window which can be interpreted as the probability of the target AoD in the next instant. The significance of this technique is that the NN output becomes invariant to the value of the AoD itself, rather the predicted value is the amount of correction (in discrete grid points) needed for the next beam. This classificationtype solution is an alternative to works attempting to regress values [9]. It is well known that for limited data inputs and training, classification outperforms regression. It's also worth noting that by defining the problem as a classification task, we directly bypass the problem of dealing with ambiguities within the regressed values (e.g. regressing 370° and 10° for a desired value of 10°).

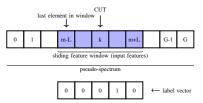


Fig. 2: Schematic of the sliding window and the corresponding label vector. Here the 1 indicates that the UE moves one grid point (discrete angle from grid) in the next time frame.

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 \begin{array}{ll} \text{input} & : \text{measurements } z_k \text{ and } \tilde{\theta}_m[k] \text{ as in (3) for time frames} \\ k \in \{0,1,...,K\} \text{ and sliding window size } 2L+1 \\ \text{output} & : \text{feature set } \mathcal{F}, \text{ label set } \mathcal{L} \\ \text{initialization;} \\ \text{set } \mathcal{W} = \mathcal{S} \text{ and } \mathcal{F}_k = [w_{k-L},....,w_{k+L}] \text{ while } k \leq K-1 \text{ do} \\ \text{insert } z(\tilde{\theta}_m[k]) \text{ at } m^{th} \text{ position of } \mathcal{W} \\ \text{center sliding window of length } 2L+1 \text{ at position } m \\ \text{acquire } \tilde{\theta}_m[k+1] \text{ and calculate } d_{\tilde{\theta}} = \tilde{\theta}_m[k+1] - \tilde{\theta}_m[k] \text{ ;} \\ \text{if } |d_{\tilde{\theta}}| \leq L \text{ then} \\ | \text{ set position } (L+1+d_{\tilde{\theta}}) \text{ of } \mathcal{L}_k \text{ to 1 and the rest 0;} \\ \text{else} \\ | \text{ set position } (L+1+\operatorname{sgn}(d_{\tilde{\theta}})L) \text{ of } \mathcal{L}_k \text{ to 1 and the rest 0;} \\ \text{end} \\ \end{array}
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Algorithm 1: Algorithm for feature and label generation from dataset. m denotes the index of the main beam.

C. Neural Network Architecture

The recurrent network architecture is depicted in Fig. 4 consisting of two LSTM layers followed by a fully connected

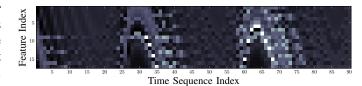


Fig. 3: Graphical representation of the input features for the RNN in a dynamic scenario where the UE has a cyclic motion. The window length parameter L is set to 8 for a total of 90 time frames.

layer before the final classification layer. Here we have used a bi-directional LSTM (biLSTM) layer in order to preserve the information contained within the time series from the future samples. For conciseness we refrain from discussing different recurrent implementations here. An important remark here is that as the final layer of the classifier we have chosen the sigmoid activation function as opposed to a softmax due to the fact that when angular grids of the labels are smaller than the beam width of the array, it is possible that a certain beam can cover multiple grid points.

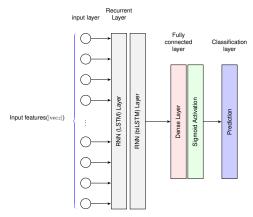


Fig. 4: RNN architecture with the LSTM layer directly fed by the input data. Note that it is also possible to replace the sigmoid activation at the final layer with a softmax layer.

IV. SIMULATIONS AND NUMERICAL RESULTS

In this section we use the Fraunhofer Quadriga [15] channel generator with a mobile UE to train a network to predict the UE's AoD. The parameters generated by Quadriga at each time instance include channel coefficients, delay values and position coordinates (trajectory) among others. In the following we assume a ULA at the BS with $N_{TX} = 64$. Since this ULA is not available in Quadriga, we have self-defined a 64 element ULA to obtain the channel parameters. These values are then used to simultaneously generate multiple realizations of the measurement values for the NN and state variables for the PF along the same trajectory. As can be seen in Fig. 5, the UE trails a trajectory with variable speed along a circular path (start:S) followed by a linear path. The circular path can be a representation of a likely scenario for a BS installed at the corner of an urban round-about. The significant challenge of a circular path is the non-linearity in AoD values with time. The dataset contains 26 realizations of the the same trajectory, where in each case the parameters vary.

Fig. 6 shows the performance of PF compared to the proposed method. The number of particles is set to 100 as in [6] and the other parameters have been accommodated correspondingly to the array size. The *Oracle* defines the real AoD, *GT* denotes the Ground Truth value which is the rounded (within 1 degree) value of the corresponding real value, included in the plots to signify that the network has been trained to predict up to a pre-chosen *gridded* accuracy.

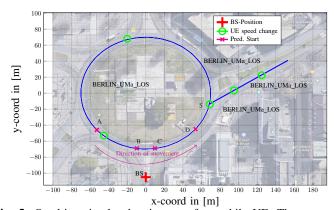


Fig. 5: Quadriga simulated trajectory of a mobile UE. The green markings on the trajectory imply that the linear speed of the UE changes from there onward. The notation BERLIN-UMa-LOS describes the scenario defined by the Quadriga software to generate the coefficients (in this case a LoS environment in Berlin, Germany).

Fig. 6 shows the estimated AoD values associated with the UE along the marked circular section (A-D) of the trajectory from Fig. 5. A few remarks are in order. 1) The section of the path used for inference, has not been seen by the network during training and validation. 2) Note that when the AoD progression becomes highly nonlinear along the path, the PF deviates significantly from the true value. This could be attributed to the channel model considered in [6], which ignores the Doppler induced time-variance of the channel. Additionally, even though the PF outperforms other EKF variants, the particles are not fully able to capture the channel dynamics. For both estimators, at each time index the reported values are the average estimated value (binned avg. for RNN) over 26 independent runs. In Tab. I, MSE of the RNN estimated angles for various window lengths (L') and probe lengths are shown. It is observed that with a larger window (more memory) and larger number of probes, the estimation error decreases.

In Fig. 7, a comparison of the achievable rate between the proposed RNN scheme, the PF from [6] and an Oracle estimator is provided. The reported values correspond to the predictions form Fig. 6. The plotted values at each time index are averaged for 26 runs. It's worth mentioning, the change in the Oracle rate occurs as the result of the UE moving closer to the BS, leading to a higher received signal power. The achievable rate is calculated according to:

$$r(\tilde{\theta}, \theta) = \left(1 - \frac{T_X}{T_{FR}}\right) \cdot \log_2 \left(1 + \frac{P|\mathbf{c}^H(\tilde{\theta})\mathbf{H}(\theta)\mathbf{f}(\tilde{\theta})|^2}{\sigma_{\eta}^2}\right)$$
(4)

where θ and $\tilde{\theta}$ are the actual and estimated AoD of the UE. The channel is defined $\mathbf{H}(\theta) = \alpha \mathbf{a}_{\rm ax}(\theta) \mathbf{a}_{\rm rx}^H(\theta) e^{j2\pi \nu T_s}$, where T_s is the sampling time. T_X and $T_{FR} \in [T_F, T_{F'}]$ denote the intervals in each frame type of Fig. 1 defined as:

$$T_X = \left\{ \begin{array}{ll} T_{\scriptscriptstyle ACQ} + T_{\scriptscriptstyle FB,I} + T_{\scriptscriptstyle SP} & \text{initialization frame} \\ T_{\scriptscriptstyle FD,SP} + T_{\scriptscriptstyle SP} & \text{secondary frame} \end{array} \right.$$

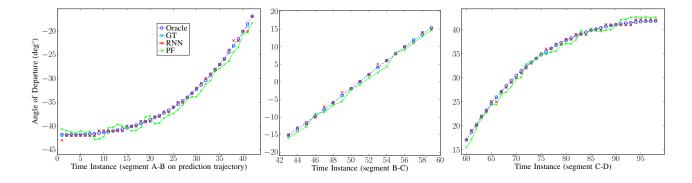


Fig. 6: The performance of PF compared to the proposed method. The overall MSE is reported in Tab.I for other training window lengths and transmitted number of secondary probes. The results are segmented in multiple plots for better visualization

TABLE I: RNN Estimation MSE vs. Window/Probe Length

	# probes $= 1$		# probes = 3	
	L' = 17	L'=29	L' = 17	L'=29
MSE(°)	0.058	0.051	0.048	0.044

Note that the values for the proposed estimator in Fig. 7 are obtained with a combination of T_X , depending on whether any future values move out of the current frame (in Fig. 6 this is not the case, only a secondary T_X is used). However for the Oracle we use the initial T_X since a full BA must takes place for the exact AoD to be discovered. The above results have been obtained with $\sigma_n=1$ and we assume P=1.

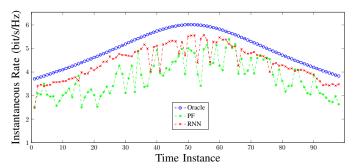


Fig. 7: Comparison of achievable instantaneous rate.

V. CONCLUSION

In this paper, we proposed a RNN based approach for beam tracking at the BS side. This model is trained based on past channel measurements to predict the amount on alignment correction for the next time frame. Furthermore, this model places no restriction on the mobility on the UE. Based on this model, we proposed a frame structure which can adapted be to channel conditions. Our simulations demonstrate that our proposed scheme outperforms PF both in terms of prediction and communication rates, especially at the high mobility scenarios.

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