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Sequential Blind Source Extraction For Quasi-Periodic Signals With Time-Varying Period

Thato Tsalaile*, *Member, IEEE*, Reza Sameni, *Student Member, IEEE*, Saeid Sanei, *Senior Member, IEEE*, Christian Jutten, *Fellow, IEEE*, and Jonathon Chambers, *Senior Member, IEEE*

Abstract—A novel second-order-statistics-based sequential blind extraction algorithm for blind extraction of quasi-periodic signals, with time-varying period, is introduced in this paper. Source extraction is performed by sequentially converging to a solution that effectively diagonalizes autocorrelation matrices at lags corresponding to the time-varying period, which thereby explicitly exploits a key statistical nonstationary characteristic of the desired source. The algorithm is shown to have fast convergence and yields significant improvement in signal-to-interference ratio as compared to when the algorithm assumes a fixed period. The algorithm is further evaluated on the problem of separation of a heart sound signal from real-world lung sound recordings. Separation results confirm the utility of the introduced approach, and listening tests are employed to further corroborate the results.

Index Terms—Blind source extraction (BSE), quasi-periodic, second-order statistics, statistical nonstationarity, time-varying period.

I. INTRODUCTION

BLIND SOURCE extraction (BSE) has received much research attention because of its potential utility in a wide range of applications including many in biomedical signal processing. The problem arises when linear, instantaneous mixtures or observations, generated as a set of signals are mixed by traversing an unknown medium, essentially without delay, need to be processed to estimate or recover a number or all of the original sources. One of the important and challenging issues in BSE is how to extract specific sources of interest. This requires the proper use of prior information about the sources or the mixing operation in forcing the algorithm to extract the sources of interest rather than any arbitrary sources. The objective of blind source separation (BSS), on the other hand, is to simultaneously recover or estimate all the original sources from their mixtures. Compared with BSS, BSE provides more flexibility and has

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some potential advantages over BSS, in terms of computational complexity and extraction of only the sources of interest.

Over the last decade or so, several approaches have been developed for the solution of both BSS and BSE problems, which are based on either second-order or higher order statistics of the data. Typically, the higher order techniques consist of two steps: a whitening step for exploiting the second-order statistics and a rotation step for exploiting the higher order statistics. They require few assumptions apart from the statistical independence of the sources, and therefore, have generally been the preferred approach to the solution of BSE and BSS. Higher-order-statisticsbased solutions include [1]-[4]. Second-order statistics methods, on the other hand, have the advantage of requiring shorter data records due to their reduced sensitivity to small sample estimation errors, and do not limit the number of Gaussian sources that can be separated to one (see, for instance, [5]–[8]). As opposed to higher-order methods, second-order methods operate in a semiblind context, since their derivation usually requires that certain additional assumptions are made on the nature of the original signals, such as statistical nonstationarity of the sources, presence of temporal structure in stationary signals, or cyclostationarity [5]-[8]. Such information is usually available in certain biomedical applications, for instance, in physiological signals such as the ECG, and should be exploited.

Several algebraic-block-based methods exist that exploit the temporal correlations of the source signals, and perhaps the best known is the second-order blind identification (SOBI) algorithm [9]. Consistent with the operation of batch algorithms, the original SOBI algorithm entails prewhitening the data, followed by the (approximate) joint diagonalization of a set of covariance matrices at different time lags, thus potentially allowing separation of sources based on their temporal structure. However, in the SOBI algorithm, the time lags at which the covariance matrices are jointly diagonalized are fixed and are not matched to the extraction of a quasi-periodic signal with timevarying period. Furthermore, computational complexity of this algorithm is generally substantially greater than sequential algorithms due to the need to diagonalize a number of sample covariance matrices, and therefore, will not be considered further in this paper. Related algorithms that are essentially based on a similar principle can be found in [10] and [11].

Recently, a sequential algorithm was developed for a class of periodic signals in [12]. In that work, however, the signals, although periodic, have a constant or fixed period. In this paper, we exploit the combination of the sequential blind source extraction (BSE) algorithm using second-order statistics based on the approximate joint diagonalization (AJD) of autocorrelation

matrices [13] and the time-varying lag (period) calculation procedure recently proposed in [20], and thus, introduce a novel sequential blind source extraction algorithm for the extraction of quasi-periodic signals with time-varying period. This paper is motivated by the observation that the majority of physiological signal measurements (for example, ECG) exhibit some degree of periodicity and statistical nonstationarity. The nonstationarity manifests itself as variations in period as a function of time. This makes the assumption of a fixed period (as in [12]) invalid for the ECG signal, and perhaps many other biomedical signals. To the best of our knowledge, a sequential BSE algorithm that is matched to such variations in the signal period has not been discussed previously. Moreover, using a time-varying period can help with the extraction of a specific desired source.

To this end, a time-varying period τ_t , which is estimated for each new cycle-to-cycle interval of the quasi-periodic source to be extracted, is incorporated in the sequential blind extraction algorithm. Source extraction is performed by sequentially converging to a solution that effectively diagonalizes the autocorrelation matrices at lags τ_t corresponding to the different periods.

The rest of the paper is organized as follows. Problem formulation, in the context of BSE using second-order statistics is presented in Section II. In Section III, we present and incorporate the concept of time-varying period in the problem formulated in Section II. We present the simulation results in Section IV. In Section V, we present results of applying the new algorithm to extraction of a heart sound signal (HSS) from real-world lung sound recordings. A summary and concluding remarks are given in Section VI.

II. PROBLEM FORMULATION

We consider the real-valued signal generating model

$$\mathbf{x}(t) = \mathbf{A}\mathbf{s}(t) + \mathbf{n}(t) \tag{1}$$

where $\mathbf{s}(t) = [s_1(t), s_2(t), \dots, s_N(t)]^T$ is a column vector of N mutually uncorrelated zero-mean unknown source signals, $\mathbf{A} = [\mathbf{a}_1, \mathbf{a}_2, \dots, \mathbf{a}_N]$ is an $N \times N$ invertible unknown mixing matrix, $\mathbf{x}(t) = [x_1(t), x_2(t), \dots, x_N(t)]^T$ is a column vector of N observed sensor signals, $\mathbf{n}(t) = [n_1(t), n_2(t), \dots, n_N(t)]^T$ denotes a column vector of additive white Gaussian zero-mean measurement noise, \mathbf{a}_i is the ith column of \mathbf{A} , and $[\cdot]^T$ and t, respectively, denote the vector transpose and the discrete time index. In the discussion that follows, we proceed with the noiseless model of (1) by dropping the noise term $\mathbf{n}(t)$, but we show the effect of the noise on the algorithm in the simulation section (Section IV).

Based on the assumption that the sources are spatially uncorrelated and wide sense stationary, the time-lagged autocorrelation matrix \mathbf{R}_k can be defined as

$$\mathbf{R}_k = E[\mathbf{x}(t)\mathbf{x}^T(t - \tau_k)], \qquad k = 1, 2, 3, \dots, K$$
 (2)

where K is the index of the maximum time lag, i.e., τ_K and $E[\cdot]$ denotes the statistical expectation operator.

The vector $\mathbf{x}(t)$ in (1) (ignoring the noise term) is a linear combination of the columns of matrix \mathbf{A} , i.e., \mathbf{a}_i s. Therefore, the

most intuitive way to extract the ith source is to project $\mathbf{x}(t)$ onto the space in \mathbb{R}^N orthogonal to, denoted by \bot , all of the columns of \mathbf{A} except \mathbf{a}_i , i.e., $\{\mathbf{a}_1,\ldots,\mathbf{a}_{i-1},\mathbf{a}_{i+1},\ldots,\mathbf{a}_N\}$. Henceforth, by defining a vector $\mathbf{q}\bot\{\mathbf{a}_1,\ldots,\mathbf{a}_{i-1},\mathbf{a}_{i+1},\ldots,\mathbf{a}_N\}$ and setting $\mathbf{t}\equiv\mathbf{a}_i$, together with adopting oblique projector notation [14], gives

$$y(t)\mathbf{t} = \mathbf{E}_{\mathbf{t}|\mathbf{q}^{\perp}}\mathbf{x}(t) \tag{3}$$

where y(t) is an estimate of one source, \mathbf{q}^{\perp} is a subspace in \mathbb{R}^N orthogonal to \mathbf{q} , i.e., the space spanned by $\{\mathbf{a}_1,\ldots,\mathbf{a}_{i-1},\mathbf{a}_{i+1},\ldots,\mathbf{a}_N\}$, and $\mathbf{E}_{\mathbf{t}|\mathbf{q}^{\perp}}=(\mathbf{t}\mathbf{q}^T)/(\mathbf{q}^T\mathbf{t})$ is the oblique projection of \mathbf{t} onto the space \mathbf{q}^{\perp} . By omitting the scalar $1/(\mathbf{q}^T\mathbf{t})$ and dropping \mathbf{t} from both sides of (3) results in

$$y(t) = \mathbf{q}^T \mathbf{x}(t). \tag{4}$$

In BSE based on second-order statistics, both vectors ${\bf t}$ and ${\bf q}$ are unknown. In order to extract one source, we adopt the same approach and assumptions as in [13, Sec. III], i.e., the following cost function is exploited to find these vectors

$$[\hat{\mathbf{t}}, \hat{\mathbf{q}}, \hat{\mathbf{d}}] = \arg\min_{\mathbf{t}, \mathbf{q}, \mathbf{d}} J(\mathbf{t}, \mathbf{q}, \mathbf{d})$$
 (5)

where $J(\mathbf{t}, \mathbf{q}, \mathbf{d}) = \sum_{k=1}^{K} ||\mathbf{R}_k \mathbf{q} - d_k \mathbf{t}||^2, \mathbf{d} = [d_1, d_2, \dots, d_K]^T$ is the column vector of unknown scalars, and $\|\cdot\|$ denotes the Euclidean norm. The cost function in (5) utilizes the fact that for BSE, $\mathbf{R}_k \mathbf{q}$ should be collinear with \mathbf{t} , incorporating the coefficients d_k that provide t with proper scaling. The trivial answer for (5) is its immediate global minimum point when t = q = d = 0. This solution has been avoided by imposing the condition $\|\mathbf{t}\| = \|\mathbf{d}\| = 1$. Minimization of the cost function (5) with respect to $\hat{\mathbf{q}}$ leads to the identification of vector \mathbf{q} in (4) that can therefore be used to extract one of the sources. It is, however, worth noting that the actual extracting vector is given by $\mathbf{q}/(\mathbf{q}^T\mathbf{t})$ due to earlier omission of the scaling factor $1/(\mathbf{q}^T \mathbf{t})$ in order to arrive at (4). The convergence of (5) is rather difficult to prove analytically in the time domain due to the product term $d_k \mathbf{t}$ in (5). The formal analytical proof of the convergence is a subject of future research.

A. Signal Extraction Algorithm

By employing the sequential approximate digitalization algorithm (SDA) proposed in [13], the cost function (5) is minimized by adjusting its parameters alternatively as follows.

Stage 1: Freeze both ${\bf t}$ and ${\bf d}$ and adjust ${\bf q}$. Taking the gradient of J with respect to ${\bf q}$ leads to analytical solution for ${\bf q}$ as $\partial J/\partial {\bf q}=2\sum_{k=1}^K {\bf R}_k({\bf R}_k{\bf q}-d_k{\bf t})=0$ to yield a new value of ${\bf q}$:

$$\mathbf{q} \leftarrow \mathbf{H} \left(\sum_{k=1}^{K} d_k \mathbf{R}_k \right) \mathbf{t} \tag{6}$$

where $\mathbf{H} = [\sum_{k=1}^K \mathbf{R}_k^2]^{-1}$ and $e \leftarrow f$ denotes replacing e by f.

Stage 2: Freeze both \mathbf{t} and \mathbf{q} and adjust \mathbf{d} . Utilizing the property that $\|\mathbf{d}\| = 1$ and considering the Lagrangian

function

$$J_{\lambda_d} = J + \lambda_d \left(\sum_{k=1}^K d_k^2 - 1 \right) \tag{7}$$

where λ_d is the Lagrange multiplier, to obtain a new value of \mathbf{d}

$$\mathbf{d} \leftarrow \frac{\mathbf{u}}{\|\mathbf{u}\|}, \quad \mathbf{u} = \left[\mathbf{r}_1^T \mathbf{t}, \mathbf{r}_2^T \mathbf{t}, \dots, \mathbf{r}_K^T \mathbf{t}\right]^T$$
 (8)

where $\mathbf{r}_k = \mathbf{R}_k \mathbf{q}$.

Stage 3: Freeze both ${\bf q}$ and ${\bf d}$ and adjust ${\bf t}$. Using $\|{\bf t}\|=1$ and exploiting the Lagrangian function

$$J_{\lambda_t} = J + \lambda_t (\mathbf{t}^T \mathbf{t} - 1) \tag{9}$$

to obtain the adjustment for t

$$\mathbf{t} \leftarrow \frac{\mathbf{v}}{\|\mathbf{v}\|}, \qquad \mathbf{v} = \sum_{k=1}^{K} d_k \mathbf{r}_k.$$
 (10)

These three stages are repeated until the cost function (5) converges, and one source can be extracted according to (4). For the later presented results on ECG signals, five iterations are typically sufficient and no problem with ill-convergence has been experienced. This, however, depends on the dimensions of the subspace that is being extracted [18]. After extracting one source, a deflation procedure is employed to remove it from the mixture as follows [15]:

$$\mathbf{x}_{i+1}(t) = \mathbf{Z}^T \mathbf{x}_i(t), \qquad \mathbf{x}_1(t) = \mathbf{x}(t) \tag{11}$$

where $\mathbf{x}(t)$ is the original observation signal defined in (1), and

$$\mathbf{Z} = \mathbf{I} - \frac{\mathbf{R}_{0(i)} \mathbf{w} \mathbf{w}^T}{\sigma_y^2}$$
 (12)

where $\mathbf{R}_{0(i)} = E[\mathbf{x}_i(t)\mathbf{x}_i^T(t)]$, \mathbf{I} is the $N \times N$ identity matrix, and $\sigma_y^2 = E[y^2]$.

The autocorrelation matrix is then updated as

$$\mathbf{R}_{0(i+1)} = \mathbf{Z}^T \mathbf{R}_{0(i)} \mathbf{Z} \tag{13}$$

before another source can be extracted following the same procedure, using (6)–(13). An alternative way to obtain a deflation matrix is to design a matrix $\mathbf{Z} = [\mathbf{z}_1, \mathbf{z}_2, \dots, \mathbf{z}_{N-1}]$ whose columns \mathbf{z}_i span the subspace orthogonal to the estimated source direction \mathbf{t} , i.e., $\mathbf{z}_i \perp \mathbf{t}$ for $1 \leq i \leq N-1$. This latter approach can speed up the algorithm in the case of slow convergence.

This extraction algorithm is computationally simple when compared with one stage of other algorithms, such as those proposed in [16] that extract the sources one by one using fourth-order cumulants. It is, however, worth noting that the iterative extraction algorithm for estimating one source at a time in our study, in fact, replaces the joint diagonalization procedure in the SOBI algorithm [9], whereby the computation is simplified since full eigen-decomposition is not required. Nonetheless, performing the iterative procedure in our method is very similar to the procedure that is carried out within techniques that calculate the first (or the first few) eigenvalues [21]. In the next section, we extend this algorithm to the extraction of periodic signals with time-varying period.

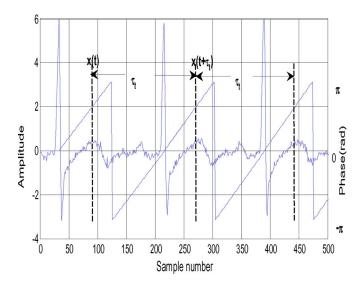


Fig. 1. Demonstration of phase allocation procedure first proposed in [20] for computing τ_t . The sawtooth signal depicts the phase signature $\theta(t)$ ranging from $-\pi$ to π . The peaks positions are assigned to $\theta(t)=0$. For each period of the signal, half of the signal samples are assigned to $\theta(t)$, ranging from $-\pi$ to 0, and the other half is assigned to $\theta(t)$, ranging from 0 to π . Typically, a sample at time instant t is compared with the sample at $t+\tau_t$. τ_t is recalculated on a cycle-by-cycle basis.

III. SEQUENTIAL EXTRACTION ALGORITHM FOR QUASI-PERIODIC SIGNALS WITH TIME-VARYING PERIOD

Successful minimization of the cost function (5) in concert with (4) leads to the extraction of any one source. It is not possible to extract the source of interest (SoI) unless some additional information is known *a priori*. The SoI in our case is a quasiperiodic signal of varying period duration. If the fundamental period, or its approximation, of the SoI is fixed and known, then the algorithm can be made to focus only on this specific source. This is based on the fact that if the fundamental period is, say, τ samples, then its autocorrelation matrix will have the same value at time lags corresponding to integer multiples of τ . Hence, the autocorrelation matrices \mathbf{R}_k s, as computed in (2), can jointly be diagonalized at time lags $\tau, \ldots, K\tau$ along with the constraint $d_1 = d_2 = \cdots = d_K$.

However, if the SoI has a period that varies from period to period (see, for instance, Fig. 5), then to jointly diagonalize the \mathbf{R}_k s at time lags $\tau, \ldots, K\tau$ and applying the extraction algorithm would invariably result in erroneous results. Therefore, a method has to be developed that effectively matches the variations in the period of the SoI.

A. Proposed Method

The method, recently proposed in [20] for multichannel ECG decomposition, entails detecting the peaks of the quasi-periodic signal that are assumed to define the period of the SoI, as is the case in ECG signals, and allowing a linear phase signature $\theta(t)$, to span the range from $-\pi$ to π , between the peaks. The phase signature is then allocated to each sample of the signal, with the positions of the R-peaks being fixed at $\theta(t)=0$, as shown in Fig. 1. It follows that the samples corresponding to a certain specific phase angle are compared along the signal. For

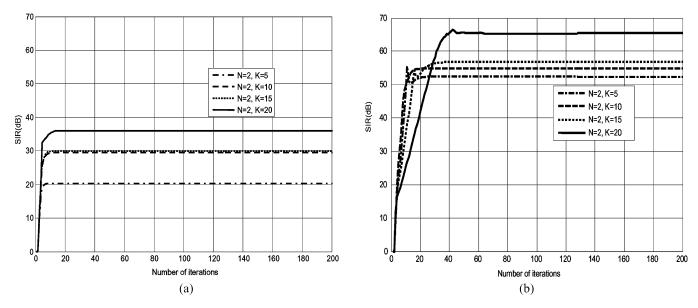


Fig. 2. SIR(dB) versus the number of iterations for both fixed and time-varying extraction algorithms for the case of noise-free BSE, averaged over 250 independent runs when extracting the first source signal. N represents the number of signals while K represents the number of autocorrelation matrices used. SIR performance improves as the number of matrices increases. The SIR performance of the time-varying period algorithm almost doubles that of the fixed period algorithm. (a) SIR(dB) for extraction algorithm using fixed period algorithm. (b) SIR(dB) for extraction algorithm using time-varying period, notice the range on the SIR axis.

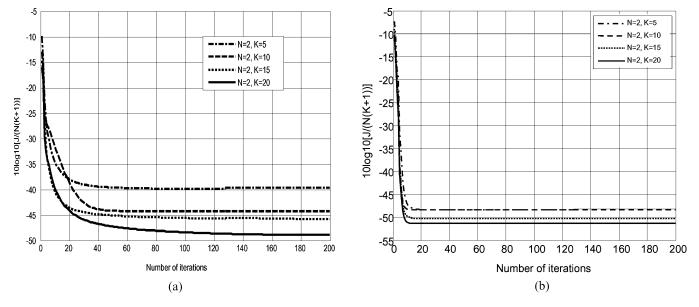


Fig. 3. $J(\mathbf{t}, \mathbf{q}, \mathbf{d})/N(K+1)$ (dB) versus number of iterations for both fixed and time-varying extraction algorithms for the case of noise-free BSE, averaged over 250 independent runs when extracting the first source signal. N represents the number of signals while K represents the number of autocorrelation matrices used. The proposed algorithm converges faster than the fixed-period algorithm. (a) $J(\mathbf{t}, \mathbf{q}, \mathbf{d})/N(K+1)$ (dB) for extraction algorithm using the fixed period algorithm. (b) $J(\mathbf{t}, \mathbf{q}, \mathbf{d})/N(K+1)$ (dB) for extraction algorithm using the time-varying period algorithm.

example, in Fig. 1, for the phase angle of 2 rad, the samples at time instant t and $t + \tau_t$ are compared accordingly. Therefore, in the sequential algorithm explained in Section II, we can redefine the following key equations.

1) The autocorrelation matrix in (2)

$$\tilde{\mathbf{R}}_{\tau_t} = E_t[\mathbf{x}(t)\mathbf{x}^T(t - \tau_t)] \tag{14}$$

where $E_t[\cdot]$ denotes averaging over t, and

$$\tau_t = \min\{\tau | \theta(t+\tau) = \theta(t), \tau > 0\}. \tag{15}$$

2) The cost function in (5) is again exploited

$$[\hat{\mathbf{t}}, \hat{\mathbf{q}}, \hat{\mathbf{d}}] = \arg\min_{\mathbf{t}, \mathbf{q}, \mathbf{d}} J(\mathbf{t}, \mathbf{q}, \mathbf{d})$$
(16)

where $J(\mathbf{t}, \mathbf{q}, \mathbf{d}) = \sum_{p=1}^{K} \|\tilde{\mathbf{R}}_{p\tau_t} \mathbf{q} - d_p \mathbf{t}\|^2$, where the $\tilde{\mathbf{R}}_{p\tau_t}$ terms are also calculated as time averages.

Therefore, the autocorrelation matrix and the cost function now take into account the variable period τ_t , which is calculated from $\theta(t)$ from cycle-to-cycle of the signal. This leads to a new algorithm for extracting SoI with a variable period duration.

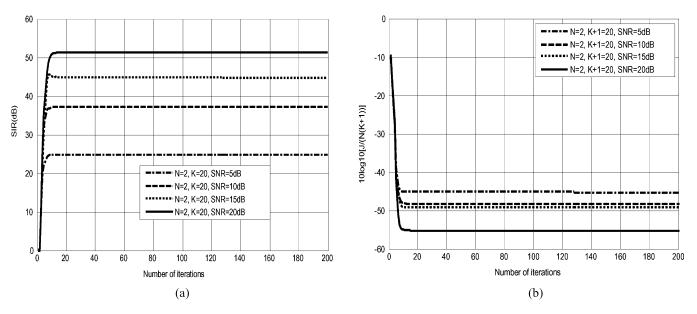


Fig. 4. $J(\mathbf{t}, \mathbf{q}, \mathbf{d})/N(K+1)$ (dB) and SIR(dB) versus number of iterations using time-varying extraction algorithm for the case of noisy BSE, averaged over 250 independent runs when extracting the first source signal. N represents the number of signals while K represents the number of autocorrelation matrices used. (a) SIR(dB) for the extraction algorithm using time-varying period algorithm for different SNRs on observations. Note the degradation in SIR(dB) performance as a function of SNR(dB). (b) $J(\mathbf{t}, \mathbf{q}, \mathbf{d})/N(K+1)$ (dB) for the extraction algorithm using the time-varying period algorithm for different SNRs on observations, note that the degradation in convergence performance as a function of reduction in SNR(dB).

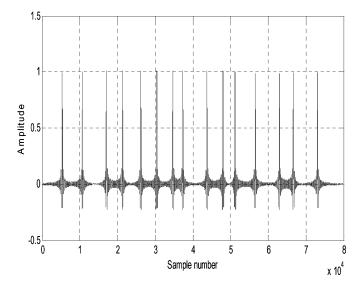


Fig. 5. Synthetic periodic signal designed to have considerable period variations. This signal acts as an SoI after mixing it with WGN.

The main difference in the algorithm of Section II and the one proposed in this paper is the way in which the time-lagged autocorrelation matrix $\tilde{\mathbf{R}}$ is computed, which, in turn, leads to the redefinition of the cost function (5).

In this algorithm, the autocorrelation matrices are calculated at varying time lags τ_t rather than at fixed time lags. Thus, after performing peak detection, and calculating the $\theta(t)$ and the time-varying τ_t , each autocorrelation matrix is calculated by computing correlations between sample points t and their dual samples $t+\tau_t$ across the entire signal length, and then, averaging over the number of correlation and phase angle points. The

resulting $\tilde{\mathbf{R}}s$ are used in the sequential algorithm of Section II to extract the SoI from multichannel mixtures.

IV. SIMULATION RESULTS

Computer simulations were carried out to illustrate the performance of the proposed method, and were compared to the one proposed recently in [17], which is based on a fixed period of the SoI.

A. Signal-to-Interference Ratio and the Cost Function

The performance of the algorithm was evaluated by the following.

1) The peak signal-to-interference ratio (SIR) in decibels is given by

SIR(dB) =
$$10 \log_{10} \frac{\max(|v_i|^2)}{\sum_{i=1}^{N} |v_i|^2 - \max(|v_i|^2)}$$
 (17)

where $[v_1, v_2, ..., v_N] = \mathbf{q}^T \mathbf{A}$ is the global transform vector, and (17) is evaluated by first calculating the average of SIR in a linear scale, and then, converting to decibels. For completeness, we note that from (1) and (4)

$$y(t) = \mathbf{q}^T \mathbf{A} \mathbf{s}(t) = v_1 s_1(t) + v_2 s_2(t) + \dots + v_N s_N(t)$$
(18)

2) The cost function in decibels given by $J(\mathbf{t}, \mathbf{q}, \mathbf{d})/N(K + 1)$.

In the simulation, blind extraction of the ECG signal obtained from DaISY database (available at: http://homes.esat.kuleuven.be/smc/daisy/) was considered. The 2500-sample-long clean ECG signal, sampled at 500 Hz, was concatenated to form a 7500-sample-long signal. It is worth noting that no discontinuity problems were experienced when

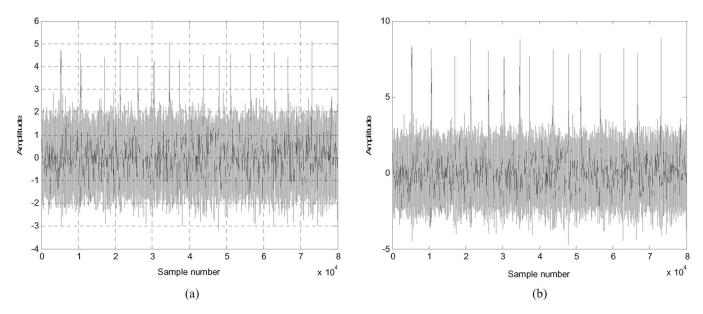


Fig. 6. Mixtures of synthetic periodic signal with time-varying period and WGN, generated by a mixing matrix **A** with elements drawn from a standardized Gaussian distribution. The synthetic periodic signal is designed to have significant period variations. The aim is to extract the synthetic periodic signal (Fig. 5). (a) Mixture 1 of synthetic signal with time-varying period and WGN. (b) Mixture 2 of synthetic signal with time-varying period and WGN.

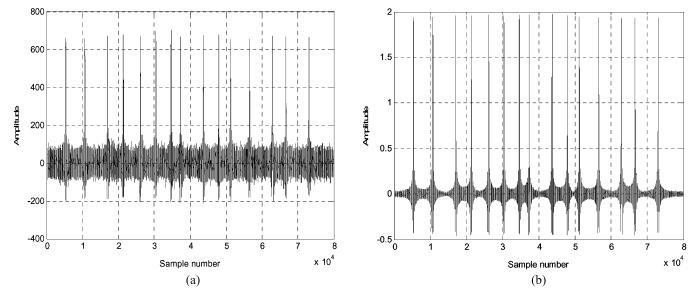


Fig. 7. Extracted synthetic signals using algorithms with the fixed and time-varying period. Clearly, the algorithm employing time-varying period much better reconstructs the synthetic signal and we can see the variations in the signal period. The algorithm using the fixed period locks onto the noise component and results in a poorly reconstructed signal. (a) Extracted synthetic signal using the algorithm with fixed period. (b) Extracted signal using the algorithm with time-varying period.

concatenating the signal. The ECG signal was mixed with white Gaussian noise (WGN) by a mixing matrix $\bf A$ with elements drawn from a standardized Gaussian distribution. Fig. 2(a) and (b) shows the SIR(dB) versus the number of iterations averaged over 250 independent runs when extracting the SoI, assuming a fixed and time-varying period, respectively. Fig. 3(a) and (b) represents the corresponding cost function performance in decibels for both cases. N and K, shown in the figures, represent the number of original signals and the number of autocorrelation matrices used, respectively. Thus, the performance criteria were evaluated for N=2 and K set to 5, 10, 15, and 20 accordingly.

It is seen from Fig. 3(a) and (b) that the proposed algorithm converges faster than the fixed-period algorithm, with convergence improving with the number of matrices used. The SIR performance also improves as the number of matrices is increased. As seen from Fig. 2(b), there is a marked increase in the SIR performance for the proposed algorithm. In fact, the SIR performance of the proposed algorithm almost doubles that of the algorithm using a fixed period. For instance, from Fig. 2(a) and (b), the maximum SIR when assuming fixed and time-varying period, and using 20 matrices is 33 and 65 dB, respectively. This underlines the motivation for our study, since by exploiting the

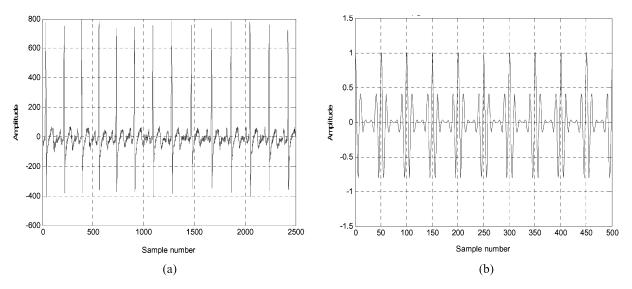


Fig. 8. ECG and a zoomed-in portion of a synthetic pure periodic signal whose repetition frequency is not a multiple of that of the ECG. These signals are combined by a mixing matrix **A** with elements drawn from standardized Gaussian distribution. The aim was to extract the ECG signal that has a time-variant period. (a) ECG signal that is to be extracted after mixing it with a synthetic pure periodic signal. The signal has slight variations in period durations. (b) Synthetic pure periodic signal that is mixed with the ECG signal. It is designed to be nonharmonically related to the ECG signal.

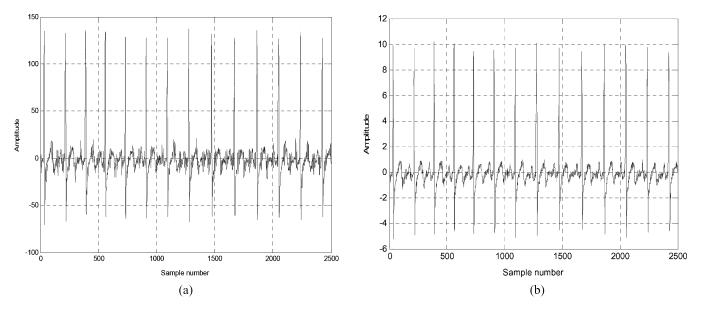


Fig. 9. Extracted ECG signals using algorithms with fixed and time-varying period. The algorithm employing time-varying period reconstructs the ECG signal perfectly. Although the algorithm using the fixed period reconstructs the ECG, it is also affected by the noise component. (a) Extracted ECG using the algorithm employing fixed period. (b) Extracted ECG using the algorithm employing time-varying period.

nonstationarity of the source, captured in the varying period, we are achieving improved SIR performance for the same fast convergence performance.

The performance of our algorithm was also investigated using different SNRs on mixture signals for the case of the noisy model given by (1). Fig. 4(a) and (b) shows SIR(dB) and convergence performance as a function of SNR(dB), respectively. It is seen from the figures that the performance degrades as more independent noise is added to the mixtures, i.e., as SNR(dB) reduces. It is however seen from Figs. 2(a) and 4(a) that our algorithm, when applied to the noisy BSE, still outperforms (at

least at SNR of 10 dB) the one using a fixed period in terms of SIR(dB), when applied to noise-free BSE.

B. Extraction of Synthetic Variable Period Signal

This simulation considers the extraction of a synthetic, deterministic signal, with time-varying period (Fig. 5). The signal is mixed with WGN in the same manner as before. Both algorithms are run to extract the periodic signal. Fig. 6(a) and (b) shows the mixtures while Fig. 7(a) and (b) shows the extracted periodic signal using algorithms employing the fixed and the

time-varying periods, respectively. As seen from the latter figures, when a fixed period is used in the algorithm, the algorithm not only recovers the signal, but also heavily locks onto the noise component, by running the proposed algorithm, which incorporates the time-varying period, accurate reconstruction is achieved, as confirmed by Fig. 7(b).

C. Separation of Two Periodic Signals

Another investigation was performed considering the separation of two nonharmonically related periodic signals, i.e., the ECG signal having varying period duration [see Fig. 8(a)], mixed with a synthetic purely periodic signal shown in Fig. 8(b). The SoI in this case is the ECG signal. The recovered ECG signals are shown in Fig. 9(a) and (b) for algorithms employing fixed and time-varying periods, respectively. As seen in Fig. 9(b), the proposed algorithm recovers the ECG completely. This shows that the algorithm works, not only for a periodic signal contaminated with WGN, but also for separating periodic signals. This can be likened to biomedical applications, such as the extraction of the HSS from lung sound recordings, where both the HSS and lung sound signal (LSS) have distinct periodicity but are generally not harmonically related. Another example is the extraction of fetal ECG signals from maternal abdominal sensors that are highly contaminated with the maternal ECG [20].

V. APPLICATION OF THE PROPOSED ALGORITHM TO SEPARATION OF THE HEART BEAT SOUND SIGNAL FROM REAL LUNG SOUND RECORDINGS

In this section, we demonstrate the applicability of the proposed algorithm to the extraction of the HSS from real recorded lung sound recordings. The dataset comprises two synchronized recordings obtained from channel (1), front left chest (heart location), and channel (2), front right chest, by digital stethoscopes sampled at 44100 Hz with 16-bit resolution. It is worth noting that, in order to use the algorithm, a clean reference signal with clear distinct peaks is required such that the peaks could automatically be detected using the readily available peak detection algorithm. The clean reference signal in our case would be the ECG signal that is synchronized with the two channel recordings. However, since this ECG was not available, we reverted to using "manual" peak detection where data from channel (1) was prefiltered prior to using our judgement about the occurrence of the peaks in the data. Using the resulting peak locations, we calculated both the $\theta(t)$ and the τ_t , which are necessary to compute the Rs for two channel data. The algorithm was run with the two raw recordings as mixture signals. The two recordings are shown in Fig. 10(a) and (b). The recovered HSSs for when both the fixed and time-varying algorithms are used are shown in Fig. 10(c) and (d), respectively. The HSS recovered from using the time-varying algorithm has clear distinct peaks depicting a better estimate of the actual HSS. Using the fixed-period algorithm results in a noisy reconstructed HSS. These results have been further corroborated by listening tests. In the listening tests, five subjects of normal hearing ability were asked to listen to both the recovered HSSs and to comment on their intelligibil-

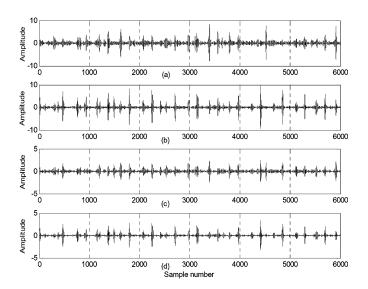


Fig. 10. Extraction of HSS from lung sound recordings. (a) and (b) Lung sound recordings (also called mixtures since each contain both heart and lung sound signals). The aim is to extract the HSS from the recordings. (c) and (d) Resulting extracted HSS for algorithms employing fixed and time-varying period, respectively,the definition of the signal in (d) is much improved.

ity. All subjects observed that although it was evident that the recovered signals were HSSs, the one recovered when using the fixed period was less intelligible due to the presence of noise.

VI. SUMMARY AND CONCLUSION

The performance of the BSE algorithm depends on a priori knowledge of the source signal. Knowledge of the period of the SoI helps to extract the source signal of interest from the mixtures. In this paper, a novel sequential algorithm using secondorder statistics for the BSE of quasi-periodic source signals, which exploits the temporal, time-varying, quasi-periodicity of the source signals, was introduced. The algorithm was based on partial approximate joint diagonalization of autocorrelation matrices at time-varying lag τ_t , which is recalculated on a cycle-bycycle basis. The algorithm is suitable for multichannel decomposition of periodic signals with or without a time-varying period. Simulation results suggest that if the SoI has a time-varying period, then using an algorithm employing a fixed period results in erroneous results. Results from other investigations show that the algorithm is suitable for removing a HSS from lung sound recordings where the periodic variation in the heart beat has been extracted manually. However, with the availability of a suitably clean ECG signal, which would be synchronous with the underlying heart sound within the phonocardiogram signals, significant improvements might be possible and the heart beat period extraction could then be automated. Furthermore, due to the multidimensional nature of the ECG, the results for multichannel recordings may be improved by using more ECG reference signals [19] which could thereby better exploit the subcomponents of the ECG recording, i.e., the P, QRS, and the T-waves.

The cost function in (5), proposed in [13], has some limitations. First, its convergence is rather difficult to prove analytically in the time domain. Second, there are some questions regarding its exact formulation and constraints imposed on the

associated vector norms. This, together with increasing the number of channels for lung sound recordings and exploring other algorithms based on cost functions that do not exhibit the aforementioned shortcomings, forms part of our future work. In conclusion, this paper is nonetheless a step forward in overcoming the time-varying periodic characteristic of many nonstationary biomedical measurements such as the HSSs, thereby allowing separation using information about a signal's periodicity.

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